Artificial Neural Networks

Prof. Dr. A K M Akhtar Hossain Dept. Of CSE, RU

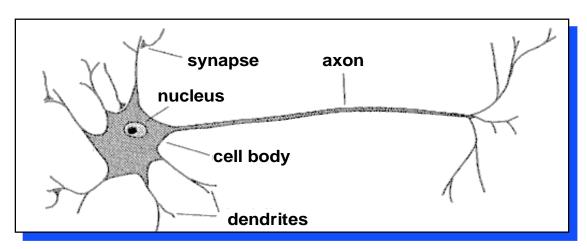
Artificial Neural Network (ANN)

- Artificial neural network (ANN) is a machine learning approach that models human brain and consists of a number of artificial neurons.
- Neuron in ANNs tend to have fewer connections than biological neurons.
- Each neuron in ANN receives a number of inputs.
- An activation function is applied to these inputs which results in activation level of neuron (output value of the neuron).
- ☐ Before we discuss about ANN, we have to know some basic concept about biological neurons and their functions.

Biological inspirations

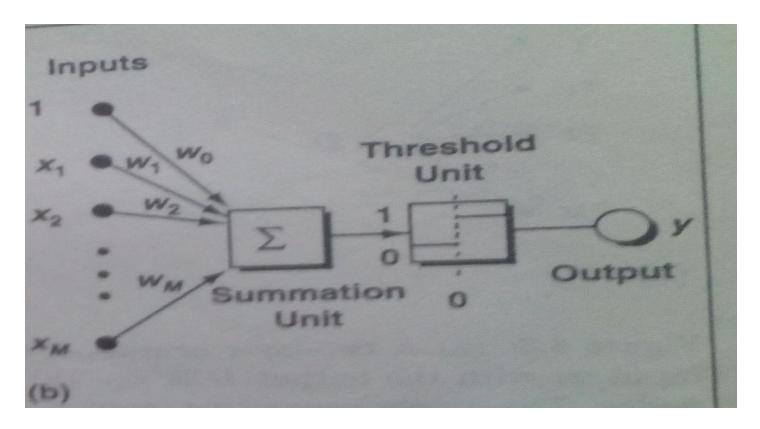
- Some numbers...
 - ❖ The human brain contains about 10¹⁴ nerve cells (neurons)
 - ❖ Each neuron is connected to the others through 10⁴ synapses
- Properties of the brain
 - > It can learn, reorganize itself from experience
 - > It adapts to the environment
 - > It is robust and fault tolerant

Biological Neuron



- A neuron has
 - ☐ A branching input (dendrites which receive input signals.)
 - ☐ A branching output (the axon, which send output signals.)
- The information circulates from the dendrites to the axon via the cell body.
- Dendrites receive input from sensory organs such as the eyes, ears, noses, skin and from axons of other neurons.
- Axons send output to organs such as muscles and to dendrites of other neurons.

- An early attempt to form an abstract mathematical model of a neuron was by McCulloch and Pitts in 1943.
- Their model
 - \triangleright receives a finite number of inputs x_1, x_2, \ldots, x_M
 - Computes the weighted sum, $s = \sum_{i=1}^{M} \omega_i x_i$
 - \triangleright using the weights ω_1 , ω_2 , ω_M



Model of a neuron with a bias weight.

- Thresholds s and outputs 0 or 1 depending on whether the weighted sum is less than or greater than a given threshold value T.
- Node inputs with positive weights are called excitatory.
- Node inputs with negative weights are called inhibitory.

The action of the model neuron is output a if

•
$$\omega_0 x_0 + \omega_1 x_1 + \omega_2 x_2 + \dots + \omega_M x_M > T$$
 (1)

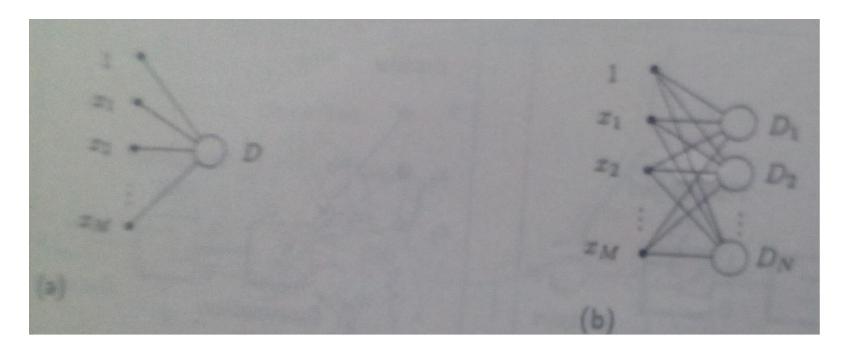
- and 0 otherwise.
- We rewrite Eq.(1) as the sum

$$D = \omega_0 x_0 + \omega_1 x_1 + \dots + \omega_M x_M \quad (2)$$

- Where, $\omega_0 = -T$ and $x_0 = 1$.
- Output 1 if D>0 and Output 0 if D≤0.
- D = Decision Parameter.

- The weight ω_0 in Eq.(1) is called the bias weight.
- The input x_0 in Eq.(1) is called the bias input.

A two layer neural net



• Figure(a). A two-layer neural net with one output. Fig.(b). A two-layer neural net with multiple output.

Neural Networks

- Artificial neural network (ANN) is a machine learning approach that models human brain and consists of a number of artificial neurons.
- Neuron in ANNs tend to have fewer connections than biological neurons.
- Each neuron in ANN receives a number of inputs.
- An activation function is applied to these inputs which results in activation level of neuron (output value of the neuron).
- Knowledge about the learning task is given in the form of examples called training examples.

Contd...

- An Artificial Neural Network is specified by:
 - neuron model: the information processing unit of the NN,
 - an architecture: a set of neurons and links connecting neurons.
 Each link has a weight,
 - a learning algorithm: used for training the NN by modifying the weights in order to model a particular learning task correctly on the training examples.
- The aim is to obtain a NN that is trained and generalizes well.
- It should behaves correctly on new instances of the learning task.

Applications off NNs

classification

in marketing: consumer spending pattern classification

In defence: radar and sonar image classification
In agriculture & fishing: fruit and catch grading

In medicine: ultrasound and electrocardiogram image classification, EEGs, medical diagnosis

recognition and identification

In general computing and telecommunications: speech, vision and handwriting recognition In finance: signature verification and bank note verification, voice recognition

assessment

In engineering: product inspection monitoring and control

In defence: target tracking

In security: motion detection, surveillance image analysis and fingerprint matching

forecasting and prediction

In finance: foreign exchange rate and stock market forecasting

In agriculture: crop yield forecasting

In marketing: sales forecasting

In meteorology: weather prediction

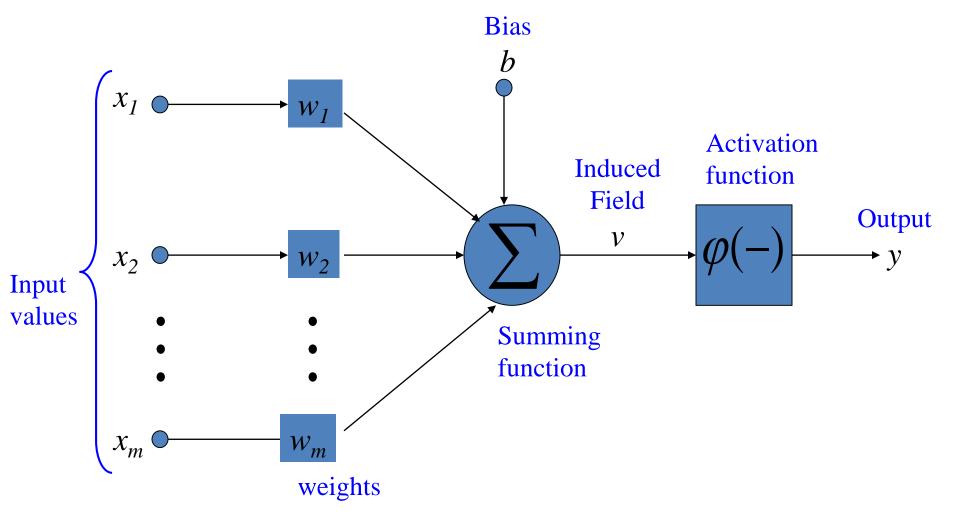
Neuron

- The neuron is the basic information processing unit of a NN. It consists of:
 - 1 A set of links, describing the neuron inputs, with weights W_1 , W_2 , ..., W_m
 - 2 An adder function (linear combiner) for computing the weighted sum of the inputs:

 (real numbers)
 - 3 Activation function or limiting the amplitude of the neuron output. Here 'b' denotes bias.

$$y = \varphi(u + b)$$

The Neuron Diagram



Bias of a Neuron

 The bias b has the effect of applying a transformation to the weighted sum u

$$v = u + b$$

- The bias is an external parameter of the neuron. It can be modeled by adding an extra input.
- v is called induced field of the neuron

$$v = \sum_{j=0}^{m} w_j x_j$$

$$w_0 = b$$

Neuron Models

ullet The choice of activation function arphi determines the neuron model.

Examples:

• step function:

$$\varphi(v) = \begin{cases} a & \text{if } v < c \\ b & \text{if } v > c \end{cases}$$

• ramp function:
$$\varphi(v) = \begin{cases} a & \text{if } v < c \\ b & \text{if } v > d \\ a + ((v-c)(b-a)/(d-c)) & \text{otherwise} \end{cases}$$

sigmoid function with z,x,y parameters

$$\varphi(v) = z + \frac{1}{1 + \exp(-xv + y)}$$

Gaussian function:

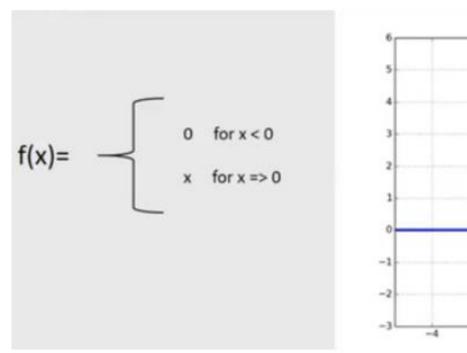
$$\varphi(v) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{1}{2} \left(\frac{v-\mu}{\sigma}\right)^2\right)$$

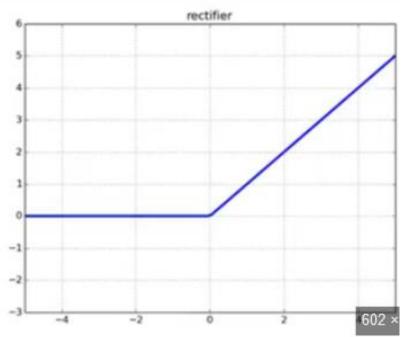
Rectified Linear Unit (ReLU)

ReLU function

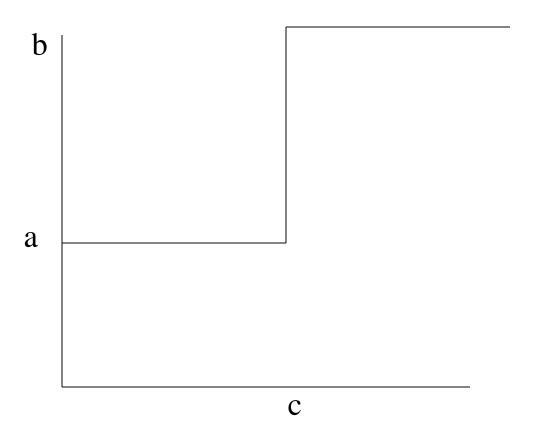
- ReLU formula is : f(x) = max(0,x)
- ReLU is the most often used activation function in neural networks, especially CNNs, and is utilized as the default activation function.
- The rectified linear activation function or ReLU for short is a piecewise linear function that will output the input directly if it is positive, otherwise, it will output zero.

ReLU function

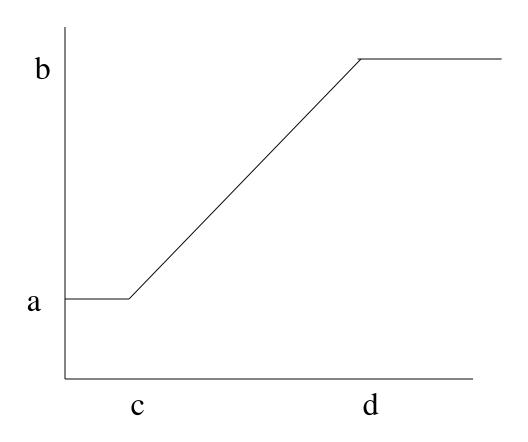




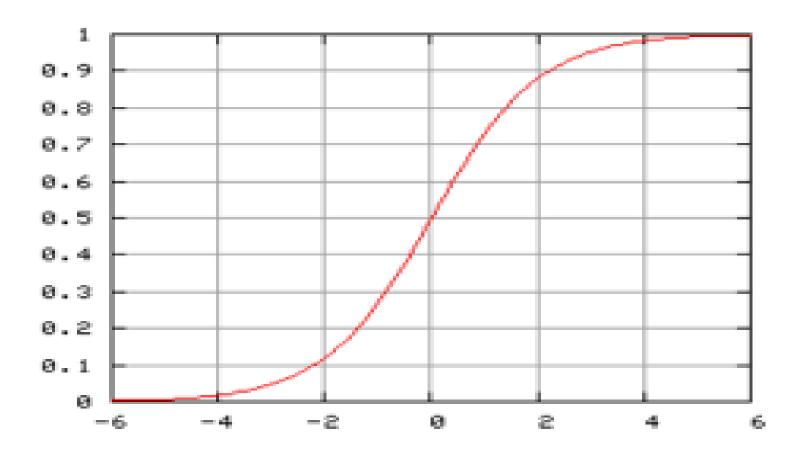
Step Function



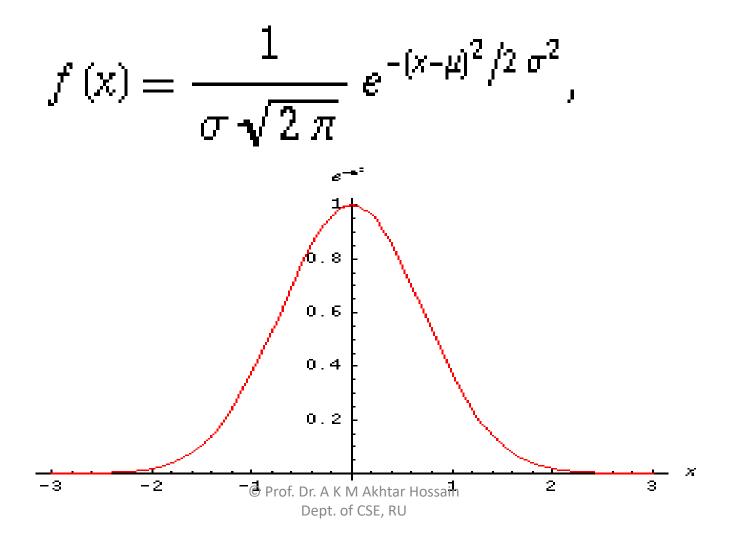
Ramp Function



Sigmoid function



• The Gaussian function is the probability function of the normal distribution. Sometimes also called the frequency curve.



Network Architectures

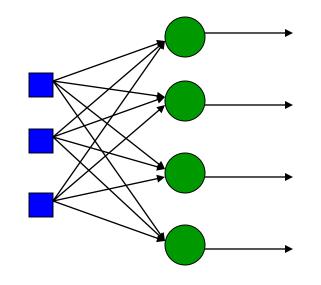
 Three different classes of network architectures

- single-layer feed-forward
- multi-layer feed-forward
- recurrent

 The architecture of a neural network is linked with the learning algorithm used to train

Single Layer Feed-forward

Input layer of source nodes

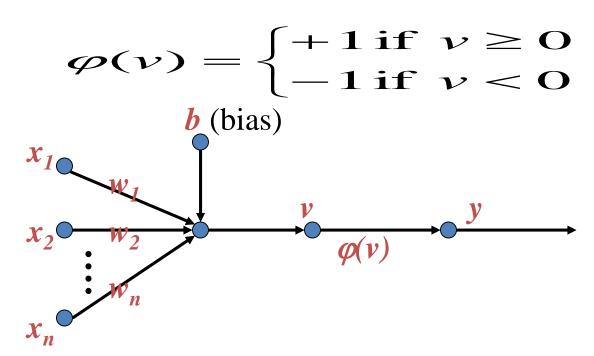


Output layer of neurons

Perceptron: Neuron Model

(Special form of single layer feed forward)

- The perceptron was first proposed by Rosenblatt (1958) is a simple neuron that is used to classify its input into one of two categories.
- A perceptron uses a step function that returns +1 if weighted sum of its input ≥ 0 and -1 otherwise



Learning Algorithms

- Supervised learning Algorithms
- Unsupervised learning Algorithms
- Semi-supervised learning Algorithms
- Reinforcement learning Algorithms

Supervised learning

- The desired response of the neural network in function of particular inputs is well known.
- A "Professor" may provide examples and teach the neural network how to fulfill a certain task.
- In Supervised learning, you train the machine using data which is well "labeled." It means some data is already tagged with the correct answer. It can be compared to learning which takes place in the presence of a supervisor or a teacher.

Supervised learning

- In supervised training, both the inputs and the outputs are provided. The network then processes the inputs and compares its resulting outputs against the desired outputs. Errors are then propagated back through the system, causing the system to adjust the weights which control the network.
- Example for Supervised Learning Methods:
 - ☐ Artificial Neural Network
 - ☐ Linear regression for regression problems.
 - Random forest for classification and regression problems.
 - ☐ Support vector machines for classification problems.

Unsupervised learning

- Unsupervised learning is a machine learning technique, where you do not need to supervise the model. Instead, you need to allow the model to work on its own to discover information. It mainly deals with the unlabeled data.
- No need of a professor
 - ☐ The network finds itself the correlations between the data.

Unsupervised learning

• In unsupervised training, the network is provided with inputs but not with desired outputs. The system itself must then decide what features it will use to group the input data. This is often referred to as self-organization or adaption.

Example for Unsupervised Learning Methods:

- K-means clustering.
- KNN (k-nearest neighbors)
- Hierarchal clustering.
- Principle Component Analysis.
- Independent Component Analysis.
- Apriori algorithm.

Semi-Supervised learning

- Semi-Supervised learning is a type of Machine Learning algorithm that represents the intermediate ground between Supervised and Unsupervised learning algorithms.
- It uses the combination of labeled and unlabeled datasets during the training period.

Semi-Supervised learning

- assumptions:
- Continuity / smoothness assumption.
- Cluster assumption.
- Manifold assumption.
- Generative models.
- Low-density separation.
- Laplacian regularization.
- Heuristic approaches.

Reinforcement learning (RL)

- Reinforcement learning (RL) is an area of machine learning concerned with how intelligent agents duty to take actions in an environment in order to maximize the notion of cumulative reward.
- Reinforcement learning is one of three basic machine learning paradigms, alongside supervised learning and unsupervised learning.

Reinforcement learning (RL)

- Reinforcement learning differs from supervised learning in not needing labelled input/output pairs to be presented, and in not needing sub-optimal actions to be explicitly corrected.
- Instead the focus is on finding a balance between exploration of uncharted territory and exploitation of current knowledge.

Reinforcement learning (RL)

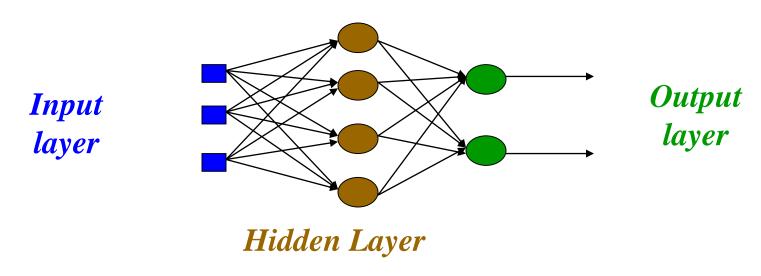
- Associative reinforcement learning
- Deep reinforcement learning
- Adversarial deep reinforcement learning
- Fuzzy reinforcement learning
- Inverse reinforcement learning
- Safe reinforcement learning

Network Architectures

- Different classes of network architectures:
 - Multi-Layer Feed-Forward
 - Backpropagation Neural Network
- The architecture of a neural network is linked with the learning algorithm used to train.

Multi layer feed-forward NN (FFNN)

- FFNN is a more general network architecture, where there are hidden layers between input and output layers.
- Hidden nodes do not directly receive inputs nor send outputs to the external environment.
- FFNNs overcome the limitation of single-layer NN.
- They can handle non-linearly separable learning tasks.



Multi layer feed-forward NN (FFNN)

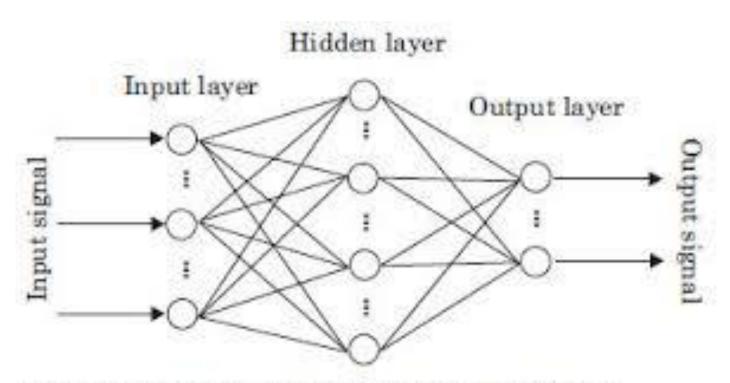


Figure 1. Structured chart of neural network.

FFNN NEURON MODEL

- The classical learning algorithm of FFNN is based on the gradient descent method.
- For this reason the activation function used in FFNN are continuous functions of the weights, differentiable everywhere.
- The activation function for node i may be defined as a simple form of the **sigmoid function** in the following manner: $\varphi(Vi) = \frac{1}{1+\varrho^{(-A*Vi)}}$

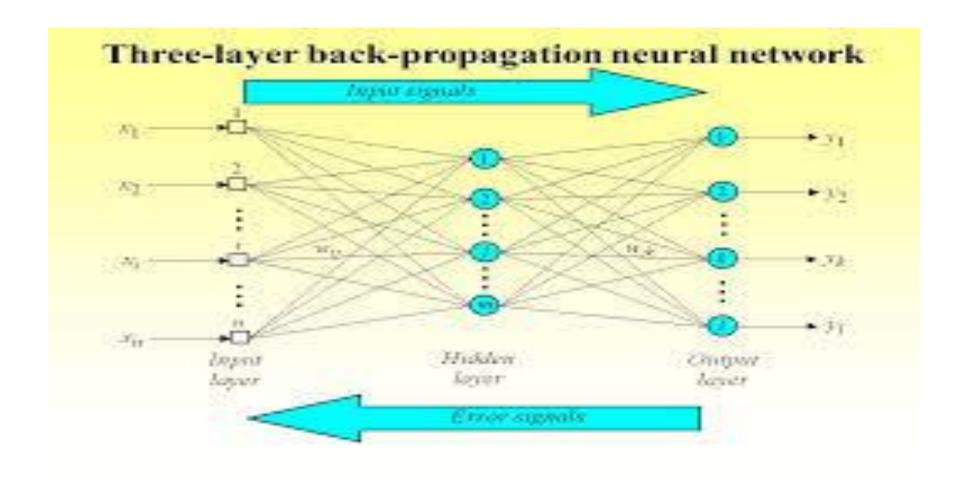
where A > 0, $V_i = \sum W_{ij} * Y_j$, such that W_{ij} is a weight of the link from node i to node j and Y_i is the output of node j.

Backpropagation Neural Network: Training Algorithm:

- The Backpropagation algorithm is a supervised learning method for multilayer feed-forward networks from the field of Artificial Neural Networks.
- The Backpropagation algorithm learns in the same way as single perceptron.
- It searches for weight values that minimize the total error of the network over the set of training examples (training set).
- Backpropagation consists of the repeated application of the following two passes:
 - Forward pass: In this step, the network is activated on one example and the error of (each neuron of) the output layer is computed.
 - Backward pass: in this step the network error is used for updating the weights. The error is propagated backwards from the output layer through the network layer by layer. This is done by recursively computing the local gradient of each neuron. © Prof. Dr. AKM Akhtar Hossain

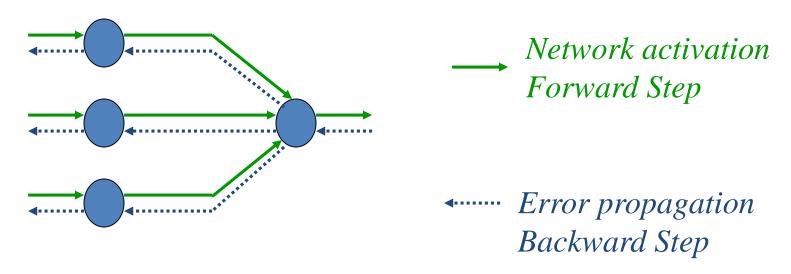
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Backpropagation Neural Network:



Backpropagation

Back-propagation training algorithm



 Backpropagation adjusts the weights of the NN in order to minimize the network total mean squared error.

Contd..

- Consider a network of three layers.
- Let us use i to represent nodes in input layer, j to represent nodes in hidden layer and k represent nodes in output layer.
- w_{ij} refers to weight of connection between a node in input layer and node in hidden layer.
- The following equation is used to derive the output value Yj of node j

$$\mathbf{Y}\mathbf{j} = \frac{1}{1 + e^{-X_j}}$$

where, $X_j = \sum x_i \cdot w_{ij} - \theta_j$, $1 \le i \le n$; n is the number of inputs to node j, and θ_i is threshold for node j

Total Mean Squared Error

• The error of output neuron k after the activation of the network on the n-th training example (x(n), d(n)) is:

$$e_k(n) = d_k(n) - y_k(n)$$

• The network error is the sum of the squared errors of the output neurons:

$$E(n) = \sum e_k^2(n)$$

• The total mean squared error is the average of the network errors of the training examples.

$$E_{\text{AV}} = \frac{1}{N} \sum_{n=1}^{N} E(n)$$

Weight Update Rule

- The Backprop weight update rule is based on the gradient descent method:
 - It takes a step in the direction yielding the maximum decrease of the network error E.
 - This direction is the opposite of the gradient of E.
- Iteration of the Backprop algorithm is usually terminated when the sum of squares of errors of the output values for all training data in an epoch is less than some threshold such as 0.01

$$w_{ij} = w_{ij} + \Delta w_{ij}$$
 $\Delta w_{ij} = -\eta \frac{\partial E}{\partial w_{ii}}$

Backprop learning algorithm (incremental-mode)

```
n=1;
initialize weights randomly;
while (stopping criterion not satisfied or n < max iterations)
    for each example (x,d)
    - run the network with input x and compute the output y
```

- update the weights in backward order starting from those of the output layer:

$$w_{ji} = w_{ji} + \Delta w_{ji}$$

with Δw_{ii} computed using the (generalized) Delta rule end-for

n = n+1;

end-while;

Stopping criterions

Total mean squared error change:

 Back-prop is considered to have converged when the absolute rate of change in the average squared error per epoch is sufficiently small (in the range [0.01, 0.001]).

Generalization based criterion:

- After each epoch, the NN is tested for generalization.
- If the generalization performance is adequate then stop.
- If this stopping criterion is used then the part of the training set used for testing the network generalization will not used for updating the weights.

Backpropagation Neural Network:

- This Algorithm is similar to BackPropagation (BP) algorithm, but the major change is to calculate error rate. Here the Euclidean distance is used to calculate the error rate, which is the difference between the present output and the target output. The proposed algorithm is as follows:
- The learning of BP Algorithm has been accomplished by error Back Propagation Neural Network (Fig.12.7). The weight vectors and are the weighted values between layers and, and respectively.

 In the hidden layer, each PE(Processing Element) or neuron computed the weighted sum according to the equation, which is given by

$$net_{aj} = \sum W_{ij} O_{ai}$$
 (1)

• Where O_{ai} is the input of unit i for pattern number a. The threshold, uh_j of each PE is then added to its weighted sum to obtain the activation $active_i$ of that PE i,e,

•
$$active_j = net_{aj} + uh_j$$
 (2)

Where uh_i is the hidden threshold weight for jth PEs.

 This activation determines whether the output of the respective PE is either 1 or 0 (fires or not) by using a sigmoid function,

$$O_{aj} = \frac{1}{1 + e^{-k_1 * active_j}} \tag{3}$$

• Where k_1 is called the *spread factors*, these O_{aj} are then serve as the input to the output computation. Signal O_{aj} are then fan out to the output layer according to the relation,

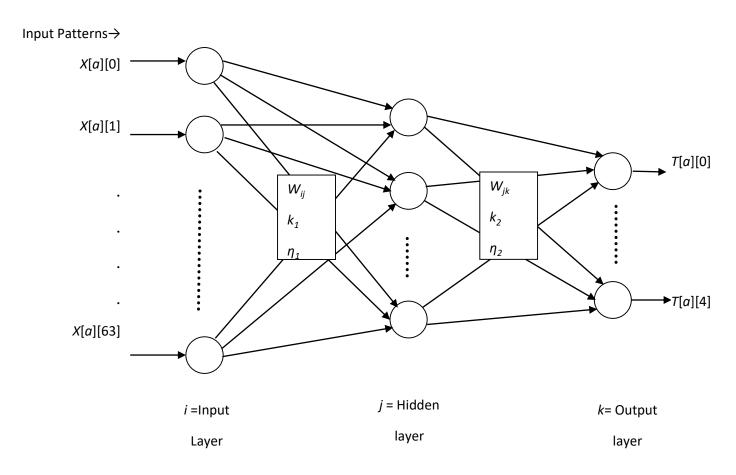


Fig.12.7 BackPropagation Neural Network

$$net_{ak} = \sum W_{jk} O_{aj}$$
 (4)

• and the output threshold weight uo_k for k-th output neuron is added to it to find out the activation $active_{(k)}$

•
$$active_k = net_{ak} + uo_k$$
 (5)

• The actual output O_{ak} is computed using the same sigmoid function,

$$O_{ak} = \frac{1}{1 + e^{-k_2 * active_k}}$$
 (6)

- Here another *spread factor* k_2 has been employed for the output units.
- In the second stage, after completing the feed-forward propagation, an error is computed by comparing the output O_{ak} with the respective target t_{ak} , i.e

$$\delta_{ak} = \sqrt{\sum_{k=0}^{k-1} (t_{ak} - O_{ak})^2}$$
 (7)

 This error is then used to adjust the weight vector using the equation,

$$\Delta W_{jk} = \eta_2 k_2 \delta_{ak} O_{aj} O_{ak} (1 - O_{ak})$$
 (8)

Where,

$$\int (activeo_k) = k_2 O_{ak} (1 - O_{ak})$$

the derivation of sigmoid function and is the *learning factor* of the network.

• The weight vector W_{jk} is then adjusted to $W_{jk} + \Delta W_{jk}$. For the threshold weight of the output PE, similar equation is applied,

$$\Delta u o_k = \eta_2 k_2 \delta_{ak} O_{ak} (1 - O_{ak}) \tag{9}$$

and the new threshold weight equaled

$$uo_k + \Delta uo_k$$

• In the *next step*, this error and the adjusted weight vector W_{jk} are feedback to the hidden layer to adjust the weight vector W_{ij} and threshold weight $uh_{j.}$ In this layer change in weight vector W_{ij} is computed by using equation,

$$\Delta W_{ij} = \eta_1 k_1 O_{ai} O_{aj} (1 - O_{ak}) \sum \delta_{ak} W_{jk}$$
 (10)

• Where, $\int (activeh_j) = k_1 O_{ai} (1 - O_{aj})$ and η_1 is the *learning factor* of the network.

• The weight vector W_{ij} is then adjusted to $W_{ii} + \Delta W_{ii}$.

 For the threshold weights of the hidden PEs, similar equation is applied

•
$$\Delta u h_j = \eta_1 k_1 (1 - O_{aj}) \sum \delta_{ak} W_{jk}$$
 (11)

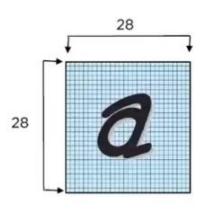
and new threshold weights are calculated

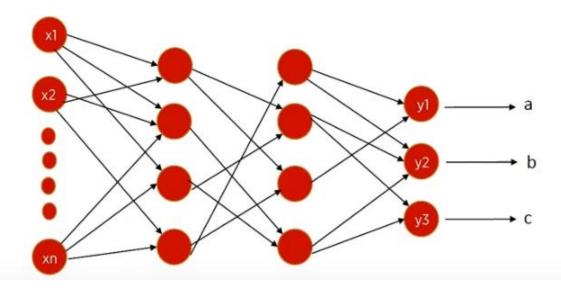
$$uh_i + \Delta uh_i$$

- When the sum-squared error is minimum then we stop the recursion.
- Finally, the weighted and threshold values are stored to test the program.

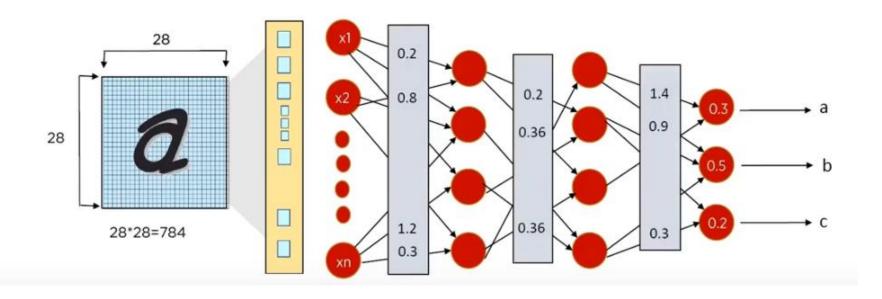
Example for Training

The handwritten alphabets are present as images of 28*28 pixels

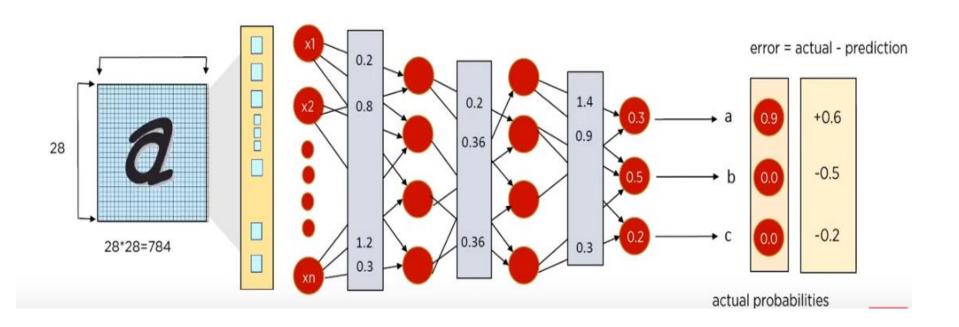




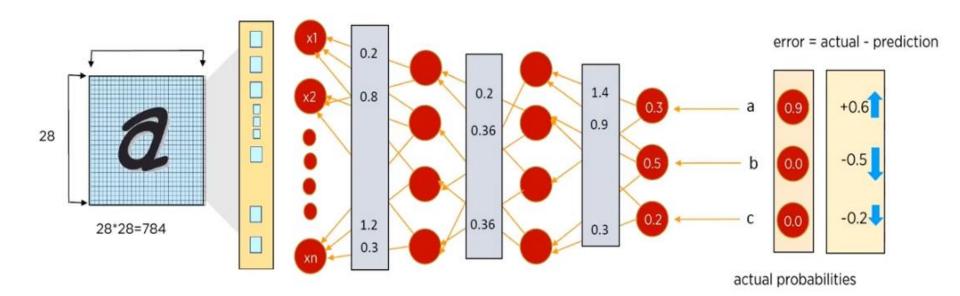
The initial prediction is made using the random weights assigned to each channel



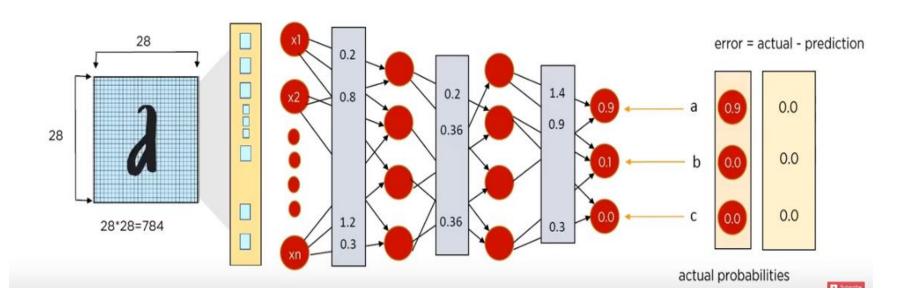
The predicted probabilities are compared against the actual probabilities and the error is calculated



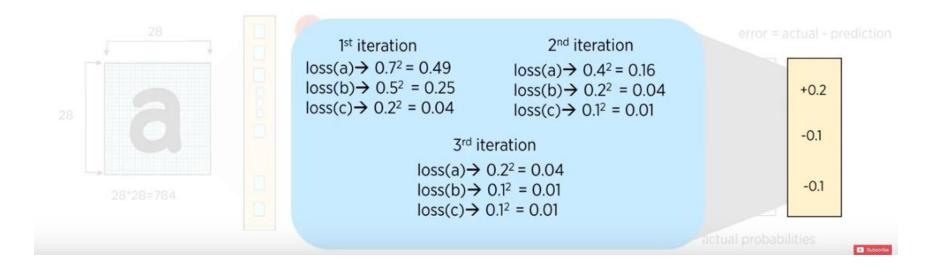
The information is transmitted back through the network



In this manner, we keep training the network with multiple inputs until it is able to predict with high accuracy



Weights through out the network are adjusted in order to reduce the loss in prediction



- RNN works on the principle of saving the output of a particular layer and feeding this back to the input in order to predict the output of the layer.
- The nodes in different layers of the neural network are compressed to form a single layer of recurrent neural networks.

- RNN works on the principle of saving the output of a particular layer and feeding this back to the input in order to predict the output of the layer.
- In below figure shows how toconvert a Feed-Forward Neural Network into a Recurrent Neural Network:

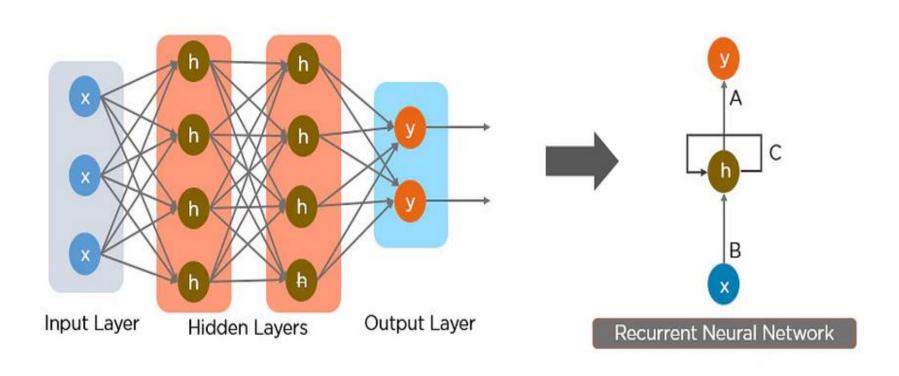
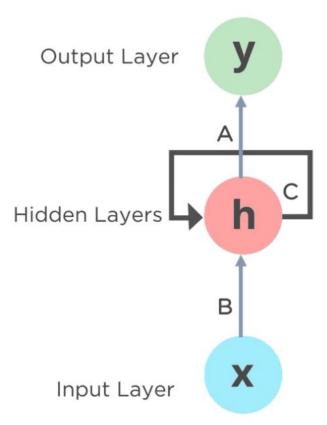


Fig: Simple Recurrent Neural Network

 The nodes in different layers of the neural network are compressed to form a single layer of recurrent neural networks. A, B, and C are the parameters of the network.



A, B and C are the parameters

- Here, "x" is the input layer, "h" is the hidden layer, and "y" is the output layer.
- A, B, and C are the network parameters used to improve the output of the model.
- At any given time t, the current input is a combination of input at x(t) and x(t-1).
- The output at any given time is fetched back to the network to improve on the output.

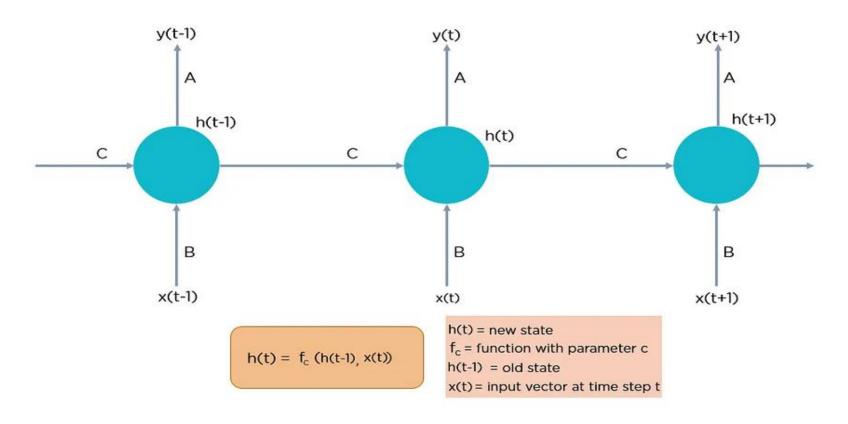


Fig: Fully connected Recurrent Neural Network

Now that you understand what a recurrent neural network is let's look at the different types of recurrent neural networks.

- Why Recurrent Neural Networks?
- RNN were created because there were a few issues in the feed-forward neural network:
 - 1. Cannot handle sequential data
 - 2. Considers only the current input
 - 3. Cannot memorize previous inputs
- The solution to these issues is the RNN.
- An RNN can handle sequential data, accepting the current input data, and previously received inputs.
- RNNs can memorize previous inputs due to their internal memory.

How Does Recurrent Neural Networks Work?

In Recurrent Neural networks, the information cycles through a loop to the middle hidden layer.

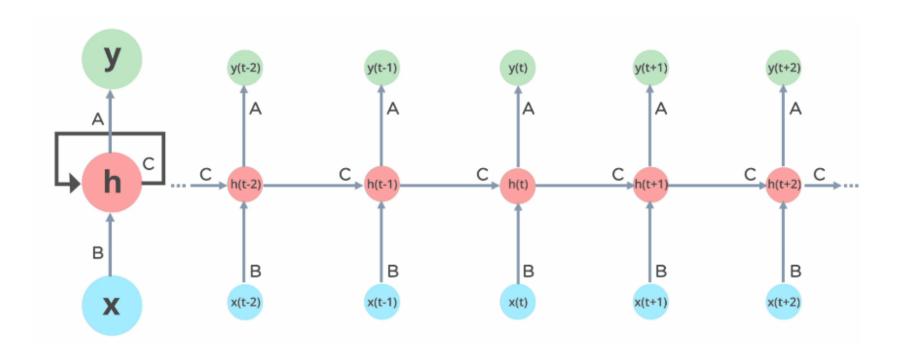


Fig: Working of Recurrent Neural Network

How Does Recurrent Neural Networks Work?

- The input layer 'x' takes in the input to the neural network and processes it and passes it onto the middle layer.
- The middle layer 'h' can consist of multiple hidden layers, each with its own activation functions and weights and biases.
- If you have a neural network where the various parameters of different hidden layers are not affected by the previous layer, ie: the neural network does not have memory, then you can use a recurrent neural network.

How Does Recurrent Neural Networks Work?

- The Recurrent Neural Network will standardize the different activation functions and weights and biases so that each hidden layer has the same parameters.
- Then, instead of creating multiple hidden layers, it will create one and loop over it as many times as required.

References

- https://mattmazur.com/2015/03/17/a-stepby-step-backpropagation-example/
- https://www.youtube.com/watch?v=GJXKOrq
 Zauk
- https://www.youtube.com/watch?v=0e0z28w
 AWfg

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