Question: https://leetcode.com/problems/distinct-subsequences/

The idea is the following:

* we will build an array mem where mem[i+1][j+1] means that S[0..j] contains T[0..i] that many times as distinct subsequences. Therefor the result will be mem[T.length()][S.length()].
* we can build this array rows-by-rows:
* the first row must be filled with 1. That's because the empty string is a subsequence of any string but only 1 time. So mem[0][j] = 1 for every j. So with this we not only make our lives easier, but we also return correct value if T is an empty string.
* the first column of every rows except the first must be 0. This is because an empty string cannot contain a non-empty string as a substring -- the very first item of the array: mem[0][0] = 1, because an empty string contains the empty string 1 time.

So the matrix looks like this:

S 0123....j

T +----------+

|1111111111|

0 |0 |

1 |0 |

2 |0 |

. |0 |

. |0 |

i |0 |

From here we can easily fill the whole grid: for each (x, y), we check if S[x] == T[y] we add the previous item and the previous item in the previous row, otherwise we copy the previous item in the same row. The reason is simple:

* if the current character in S doesn't equal to current character T, then we have the same number of distinct subsequences as we had without the new character.
* if the current character in S equal to the current character T, then the distinct number of subsequences: the number we had before ****plus**** the distinct number of subsequences we had with less longer T and less longer S.

An example:  
S: [acdabefbc] and T: [ab]

first we check with a:

\* \*

S = [acdabefbc]

mem[1] = [0111222222]

then we check with ab:

\* \* ]

S = [acdabefbc]

mem[1] = [0111222222]

mem[2] = [0000022244]

And the result is 4, as the distinct subsequences are:

S = [a b ]

S = [a b ]

S = [ ab ]

S = [ a b ]

Code:  
class Solution {

public int numDistinct(String s, String t) {

int dp[][] = new int[t.length()+1][s.length()+1];

for(int j=0; j<=s.length(); j++){

dp[0][j]=1;

}

for(int i=1; i<=t.length(); i++){

for(int j=1; j<=s.length(); j++){

if(s.charAt(j-1)==t.charAt(i-1)){

dp[i][j]=dp[i-1][j-1]+dp[i][j-1];

}

else{

dp[i][j]=dp[i][j-1];

}

}

}

return dp[t.length()][s.length()];

}

}

Github Link :<https://lnkd.in/ecwtJeaz>