# dl-completely-inelastic-collision-rnn

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### 0.1 Deep Learning Completely Inelastic Collision Solver

This notebook implements a recurrent neural network to solve for the post collision velocity of a two-mass system where the collision is completely inelastic and the second mass is initially at rest. The model is formulated using a recurrent neural network (RNN) and its input is represented as a text string giving the masses and the initial velocity of the first mass. Exact solutions calculated using conservation of momentum equations are used to train the RNN and evaluate the accuracy of predictions. This notebook is inspired by the addition\_rnn.py example included with Keras.

### 0.1.1 Import useful packaged including TensorFlow 2.0 and Keras.

The notebook utilizes tensorflow  $\geq 2.0$ , which now includes keras, a package of high level wrappers designed to make building and training deep learning models easier.

```
[1]: # import packages
import tensorflow as tf
import tensorflow.keras as keras
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.lines import Line2D

from tensorflow.keras.layers import RNN, LSTM, TimeDistributed, RepeatVector,
□
□Dense, LSTMCell, Dropout
# LSTM doesn't work well since cuDNN is compiled with certain restrictions.
# So, here I will create LSTM layers by wrapping LSTMCell in RNN
from tensorflow.keras.models import Sequential
from tensorflow.keras import optimizers
```

# 0.1.2 Check to see if a Tensorflow is installed with GPU support and if a GPU is available.

```
[2]: if not tf.test.is_gpu_available():
    print('No GPU found. Training will be slower.')
    else:
        print('Default GPU {} found.'.format(tf.test.gpu_device_name()))
```

0.1.3 Define a class to encode and decode between a selection of characters and one-hot integer representations.

```
[3]: class CharacterTable(object):
         """Given a set of characters:
         + Encode them to a one-hot integer representation
         + Decode the one-hot or integer representation to their character output
         + Decode a vector of probabilities to their character output
         def __init__(self, chars):
             """Initialize character table.
             # Arguments
                 chars: Characters that can appear in the input.
             self.chars = sorted(set(chars))
             self.char_indices = dict((c, i) for i, c in enumerate(self.chars))
             self.indices_char = dict((i, c) for i, c in enumerate(self.chars))
         def encode(self, C, num_rows):
             """One-hot encode given string C.
             # Arguments
                 C: string, to be encoded.
                 num_rows: Number of rows in the returned one-hot encoding. This is
                     used to keep the # of rows for each data the same.
             x = np.zeros((num_rows, len(self.chars)))
             for i, c in enumerate(C):
                 x[i, self.char_indices[c]] = 1
             return x
         def decode(self, x, calc_argmax=True):
             """Decode the given vector or 2D array to their character output.
             # Arguments
                 x: A vector or a 2D array of probabilities or one-hot\sqcup
      \hookrightarrow representations;
                      or a vector of character indices (used with \sqcup
      \rightarrow `calc_argmax=False`).
                 calc_argmax: Whether to find the character index with maximum
                     probability, defaults to `True`.
             n n n
             if calc_argmax:
                 x = x.argmax(axis=-1)
             return ''.join(self.indices_char[x] for x in x)
```

```
class colors:
    ok = '\033[92m'
    fail = '\033[91m'
    close = '\033[0m'
```

### 0.1.4 Generate input and output character sequences.

The input is in the form {}w{}v{} where the values in the {}s are randomly drawn one or two character sequences representing, from left to right, the mass of object one, the mass of object two, and the initial velocity of object one. Object two is initially at rest.

The output is a character string representing the post collision velocity of the system after a head on totally inelastic collision.

```
[4]: # Parameters for the model and dataset.
     num problems = 80000 # number of sequences in the training and validation sets
     digits = 2 # maximum number of digits for mass and velocity in the input
     \rightarrow sequence
     lenans = 4 # number of characters in the answer sequence
     REVERSE=False
     # Maximum length of input is 'int + int' (e.g., '345+678'). Maximum length of
     # int is DIGITS.
     maxlen = digits + 1 + digits + 1 + digits
     # All the numbers, plus sign and space for padding.
     chars = '0123456789mv.'
     ctable = CharacterTable(chars)
     questions = []
     expected = []
     seen = set()
     print('Generating data...')
     while len(questions) < num_problems:</pre>
         f = lambda: int(''.join(np.random.choice(list('123456789')))
                         for i in np.arange(np.random.randint(1, digits + 1))))
         a, b, c = f(), f(), f()
         # Skip any questions we've already seen
         key = tuple(sorted((a, b, c)))
         if key in seen:
             continue
         seen.add(key)
         # Pad the data with spaces such that it is always MAXLEN.
         q = '{m{}v{}'.format(a, b, c)}
         query = q + ' ' * (maxlen - len(q))
         ans = a*c/(a+b)
```

```
if ans < 10:
        r = lenans-2
    elif ans < 100:
        r = lenans-3
    ans = str(round(a*c/(a+b),r))
    # Answers can be of maximum size LENANS.
    ans += '0' * (lenans - len(ans))
    questions.append(query)
    expected.append(ans)
print('Total momentum questions:', len(questions))
print('Vectorization...')
x = np.zeros((len(questions), maxlen, len(chars)), dtype=np.bool)
y = np.zeros((len(questions), lenans, len(chars)), dtype=np.bool)
for i, sentence in enumerate(questions):
    x[i] = ctable.encode(sentence, maxlen)
for i, sentence in enumerate(expected):
    y[i] = ctable.encode(sentence, lenans)
\# Shuffle (x, y) in unison as the later parts of x will almost all be larger
# digits.
indices = np.arange(len(y))
np.random.shuffle(indices)
x = x[indices]
y = y[indices]
# set apart 20% for validation and text data that we never train over.
split_at = len(x) - len(x) // 5
(x_train, x_val) = x[:split_at], x[split_at:]
(y_train, y_val) = y[:split_at], y[split_at:]
split_at = len(x_val) - len(x_val) // 2
(x_val, x_test) = x_val[:split_at], x_val[split_at:]
(y_val, y_test) = y_val[:split_at], y_val[split_at:]
print('Training Data:')
print(x_train.shape)
print(y_train.shape)
print('Validation Data:')
print(x val.shape)
print(y_val.shape)
print('Test Data:')
print(x_test.shape)
print(y_test.shape)
```

```
Generating data...
    Total momentum questions: 80000
    Vectorization...
    Training Data:
    (64000, 8, 14)
    (64000, 4, 14)
    Validation Data:
    (8000, 8, 14)
    (8000, 4, 14)
    Test Data:
    (8000, 8, 14)
    (8000, 4, 14)
[5]: # show an example of the input and output character strings
     ii = np.random.randint(0, 1000)
     print('input:', questions[ii], 'output:', expected[ii])
    input: 1m9v93
                    output: 9.30
[6]: # hyperparameters
     HIDDEN_SIZE = 128
     BATCH_SIZE = 256
     LAYERS = 2
     learning_rate = 0.001
     print('Build model...')
     model = Sequential()
     # "encode" the input sequence using an RNN, producing an output of HIDDEN_SIZE.
     # note: in a situation where your input sequences have a variable length, use,
     → input_shape=(None, num_feature).
     # model.add(LSTM(HIDDEN SIZE, input shape=(MAXLEN, len(chars))))
     model.add(RNN(LSTMCell(HIDDEN_SIZE), input_shape=(maxlen, len(chars))))
     # as the decoder RNN's input, repeatedly provide with the last output of
     # RNN for each time step. Repeat 'lenans' times as that's the maximum length of u
     \rightarrow output.
     model.add(RepeatVector(lenans))
     # the decoder RNN could be multiple layers stacked or a single layer.
     for _ in range(LAYERS):
         # by setting return sequences to True, return not only the last output but
         # all the outputs so far in the form of (num_samples, timesteps,
         # output_dim). This is necessary as TimeDistributed in the below expects
         # the first dimension to be the timesteps.
         # model.add(LSTM(HIDDEN_SIZE, return_sequences=True))
         model.add(RNN(LSTMCell(HIDDEN_SIZE), return_sequences=True))
     # add a dropout layer to prevent overfitting
```

Build model...

Model: "sequential"

Layer (type)	Output Shape	Param #
rnn (RNN)	(None, 128)	73216
repeat_vector (RepeatVector)	(None, 4, 128)	0
rnn_1 (RNN)	(None, 4, 128)	131584
rnn_2 (RNN)	(None, 4, 128)	131584
time_distributed (TimeDistri	(None, 4, 14)	1806
Total params: 338,190 Trainable params: 338,190 Non-trainable params: 0		

## 0.1.5 Train the model and generate example predictions every 3 epochs.

```
for i in range(10):
    ind = np.random.randint(0, len(x_val))
    rowx, rowy = x_test[np.array([ind])], y_test[np.array([ind])]
    preds = model.predict_classes(1.0*rowx, verbose=0) # mult by 1.0 to get_U

data types to jive

q = ctable.decode(rowx[0])
    correct = ctable.decode(rowy[0])
    guess = ctable.decode(preds[0], calc_argmax=False)
    print('Q', q[::-1] if REVERSE else q, end=' ')
    print('A', correct, end=' ')

for ii in np.arange(len(correct)):
    if correct[ii] == guess[ii]:
        print(colors.ok + ' ' + colors.close, end='')
    else:
        print(colors.fail + ' ' + colors.close, end='')

print(' P', guess)
```

```
Iteration 1
Train on 64000 samples, validate on 8000 samples
64000/64000 [============== ] - 6s 91us/sample - loss: 2.0252 -
accuracy: 0.3221 - val_loss: 1.9072 - val_accuracy: 0.3399
accuracy: 0.3581 - val_loss: 1.6968 - val_accuracy: 0.3859
Epoch 3/3
accuracy: 0.3887 - val_loss: 1.5840 - val_accuracy: 0.3912
score: [1.5855826959609984, 0.39]
Q 3m92v97 A 3.06 P 1.30
Q 94m53v88 A 56.3 P 44.6
Q 74m74v4 A 2.00 P 1.38
Q 29m32v31 A 14.7 P 11.3
Q 82m7v32 A 29.5 P 24.8
Q 59m98v4 A 1.50 P 0.33
Q 4m89v74 A 3.18 P 1.38
Q 77m16v75 A 62.1 P 54.6
             P 14.3
Q 81m77v49 A 25.1
Q 41m9v74 A 60.7 P 58.8
```

```
Epoch 1/3
accuracy: 0.4214 - val_loss: 1.4270 - val_accuracy: 0.4591
64000/64000 [============== ] - 2s 39us/sample - loss: 1.4187 -
accuracy: 0.4543 - val_loss: 1.4477 - val_accuracy: 0.4371
accuracy: 0.4751 - val_loss: 1.3870 - val_accuracy: 0.4625
score: [1.38504066324234, 0.46590626]
Q 29m2v13 A 12.2 P 10.8
Q 58m76v27 A 11.7 P 13.8
Q 28m15v41 A 26.7 P 20.8
Q 16m8v61 A 40.7 P 48.0
Q 65m57v31 A 16.5 P 18.8
Q 5m27v97 A 15.2 P 15.8
Q 16m8v22 A 14.7 P 17.8
Q 68m5v56 A 52.2 P 50.8
Q 18m59v42 A 9.82 P 12.8
Q 61m85v66 A 27.6 P 30.8
Iteration 3
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============= ] - 3s 40us/sample - loss: 1.3155 -
accuracy: 0.4893 - val_loss: 1.3143 - val_accuracy: 0.4773
Epoch 2/3
64000/64000 [============== ] - 3s 40us/sample - loss: 1.2835 -
accuracy: 0.5013 - val_loss: 1.2968 - val_accuracy: 0.4835
Epoch 3/3
64000/64000 [=============== ] - 3s 40us/sample - loss: 1.2592 -
accuracy: 0.5097 - val_loss: 1.2515 - val_accuracy: 0.5061
score: [1.25640402507782, 0.5069375]
Q 52m76v4 A 1.62 P 1.80
Q 26m31v82 A 37.4 P 44.2
Q 23m25v14 A 6.71 P 6.80
Q 43m34v8 A 4.47 P 4.20
Q 78m48v1 A 0.62 P 0.62
Q 92m1v15 A 14.8 P 16.8
Q 89m86v44 A 22.4 P 24.2
Q 5m57v6 A 0.48 P 0.42
Q 4m81v7 A 0.33 P 0.42
Q 24m24v23 A 11.5 P 12.2
```

```
Epoch 1/3
64000/64000 [============= ] - 3s 40us/sample - loss: 1.2372 -
accuracy: 0.5167 - val_loss: 1.2266 - val_accuracy: 0.5182
64000/64000 [============== ] - 3s 40us/sample - loss: 1.2172 -
accuracy: 0.5231 - val_loss: 1.2430 - val_accuracy: 0.5013
accuracy: 0.5298 - val_loss: 1.2064 - val_accuracy: 0.5277
score: [1.2089817209243774, 0.526875]
Q 63m58v25 A 13.0 P 12.2
Q 37m58v34 A 13.2 P 13.2
Q 45m75v36 A 13.5 P 13.2
Q 47m91v45 A 15.3 P 14.2
Q 45m4v23 A 21.1 P 21.6
Q 84m54v21 A 12.8 P 12.2
Q 62m42v81 A 48.3 P 49.6
Q 81m41v23 A 15.3 P 14.2
Q 9m57v27 A 3.68 P 3.70
Q 55m68v87 A 38.9 P 35.7
Iteration 5
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 40us/sample - loss: 1.1831 -
accuracy: 0.5356 - val_loss: 1.1539 - val_accuracy: 0.5506
Epoch 2/3
64000/64000 [============== ] - 3s 40us/sample - loss: 1.1664 -
accuracy: 0.5411 - val_loss: 1.1241 - val_accuracy: 0.5673
Epoch 3/3
64000/64000 [============== ] - 3s 40us/sample - loss: 1.1503 -
accuracy: 0.5472 - val_loss: 1.1327 - val_accuracy: 0.5453
score: [1.1363491096496583, 0.54075]
Q 38m85v21 A 6.49 P 6.11
Q 78m59v97 A 55.2 P 56.5
Q 99m5v67 A 63.8 P 61.1
Q 21m31v8 A 3.23 P 3.50
Q 33m87v16 A 4.40 P 4.80
Q 16m71v22 A 4.05 P 4.11
Q 16m8v22 A 14.7 P 13.4
Q 89m3v82 A 79.3 P 78.1
Q 5m85v12 A 0.67 P 0.75
Q 88m24v29 A 22.8 P 21.8
```

```
Epoch 1/3
64000/64000 [============= ] - 3s 41us/sample - loss: 1.1355 -
accuracy: 0.5518 - val_loss: 1.1521 - val_accuracy: 0.5374
64000/64000 [============= ] - 3s 40us/sample - loss: 1.1223 -
accuracy: 0.5569 - val_loss: 1.0885 - val_accuracy: 0.5785
accuracy: 0.5634 - val_loss: 1.1267 - val_accuracy: 0.5455
score: [1.1247176299095154, 0.545625]
Q 82m19v44 A 35.7 P 37.3
Q 41m13v78 A 59.2 P 61.0
Q 31m35v31 A 14.6 P 15.3
Q 39m54v21 A 8.81 P 8.10
Q 75m58v85 A 47.9 P 50.3
Q 21m8v18 A 13.0 P 14.8
Q 75m3v92 A 88.5 P 89.0
Q 83m1v13 A 12.8 P 13.8
Q 84m73v32 A 17.1 P 17.3
Q 48m7v58 A 50.6 P 51.8
Iteration 7
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
accuracy: 0.5667 - val_loss: 1.0560 - val_accuracy: 0.5927
Epoch 2/3
64000/64000 [============== ] - 3s 41us/sample - loss: 1.0814 -
accuracy: 0.5710 - val_loss: 1.0823 - val_accuracy: 0.5720
Epoch 3/3
accuracy: 0.5775 - val_loss: 1.0657 - val_accuracy: 0.5742
score: [1.0661763501167298, 0.5701875]
Q 14m39v26 A 6.87 P 6.60
Q 38m58v28 A 11.1 P 11.1
Q 92m97v29 A 14.1 P 13.1
Q 59m36v4 A 2.48 P 2.10
Q 98m76v38 A 21.4 P 20.1
Q 1m11v45 A 3.75 P 3.70
Q 8m23v35 A 9.03 P 7.00
Q 14m89v97 A 13.2 P 13.1
Q 22m54v78 A 22.6 P 22.3
Q 98m88v24 A 12.6 P 12.1
```

```
Epoch 1/3
64000/64000 [============= ] - 2s 38us/sample - loss: 1.0580 -
accuracy: 0.5813 - val_loss: 1.1565 - val_accuracy: 0.5343
64000/64000 [============== ] - 2s 38us/sample - loss: 1.0475 -
accuracy: 0.5848 - val_loss: 1.0371 - val_accuracy: 0.5832
accuracy: 0.5898 - val_loss: 1.0094 - val_accuracy: 0.5998
score: [1.0074513502120972, 0.6014063]
Q 99m23v56 A 45.4 P 44.5
Q 61m2v94 A 91.0 P 91.1
Q 46m97v44 A 14.2 P 13.9
Q 64m89v62 A 25.9 P 25.5
Q 91m1v27 A 26.7 P 26.6
Q 8m18v43 A 13.2 P 12.0
Q 38m2v71 A 67.5 P 68.9
Q 22m8v73 A 53.5 P 54.5
Q 1m51v22 A 0.42 P 0.25
Q 41m34v63 A 34.4 P 33.5
Iteration 9
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 38us/sample - loss: 1.0279 -
accuracy: 0.5941 - val_loss: 1.0148 - val_accuracy: 0.5924
Epoch 2/3
64000/64000 [============= ] - 2s 38us/sample - loss: 1.0197 -
accuracy: 0.5962 - val_loss: 1.0253 - val_accuracy: 0.5934
Epoch 3/3
64000/64000 [=============== ] - 2s 38us/sample - loss: 1.0099 -
accuracy: 0.6014 - val_loss: 1.0736 - val_accuracy: 0.5699
score: [1.0733536467552185, 0.568375]
Q 2m25v31 A 2.30 P 2.90
Q 41m76v58 A 20.3 P 20.8
Q 41m13v78 A 59.2 P 69.9
Q 69m66v62 A 31.7 P 32.9
Q 8m48v61 A 8.71 P 8.00
Q 67m6v62 A 56.9 P 58.1
Q 24m72v15 A 3.75 P 3.12
Q 61m7v13 A 11.7 P 12.4
Q 94m43v89 A 61.1 P 61.9
Q 41m59v11 A 4.51 P 4.12
```

```
Epoch 1/3
64000/64000 [============= ] - 2s 39us/sample - loss: 1.0022 -
accuracy: 0.6037 - val_loss: 0.9463 - val_accuracy: 0.6365
64000/64000 [============== ] - 2s 39us/sample - loss: 0.9947 -
accuracy: 0.6069 - val_loss: 0.9755 - val_accuracy: 0.6210
accuracy: 0.6104 - val_loss: 0.9564 - val_accuracy: 0.6224
score: [0.9550179929733277, 0.6228125]
Q 41m34v63 A 34.4 P 33.5
Q 24m48v81 A 27.0 P 26.6
Q 36m37v7 A 3.45 P 3.60
Q 96m64v86 A 51.6 P 50.6
Q 99m18v29 A 24.5 P 23.6
Q 15m75v73 A 12.2 P 12.6
Q 13m75v62 A 9.16 P 9..2
  Q 7m89v7 \qquad A 0.51 \qquad P 0.42 
Q 91m26v1 A 0.78 P 0.76
Q 49m98v9 A 3.00 P 2.56
Iteration 11
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.9791 -
accuracy: 0.6124 - val_loss: 0.9770 - val_accuracy: 0.6109
Epoch 2/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.9716 -
accuracy: 0.6165 - val_loss: 1.0375 - val_accuracy: 0.5902
Epoch 3/3
accuracy: 0.6185 - val_loss: 0.9217 - val_accuracy: 0.6428
score: [0.9180031900405884, 0.6445625]
Q 48m17v79 A 58.3 P 58.8
Q 84m15v47 A 39.9 P 49.8
Q 13m37v59 A 15.3 P 15.1
Q 61m59v12 A 6.10 P 6.10
Q 68m16v33 A 26.7 P 26.1
Q 58m13v95 A 77.6 P 76.1
Q 39m97v91 A 26.1 P 25.1
Q 9m17v49 A 17.0 P 16.8
Q 77m49v3 A 1.83 P 1.78
Q 56m44v28 A 15.7 P 15.1
```

```
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.9587 -
accuracy: 0.6226 - val_loss: 0.9403 - val_accuracy: 0.6226
64000/64000 [============= ] - 3s 40us/sample - loss: 0.9515 -
accuracy: 0.6248 - val_loss: 1.0730 - val_accuracy: 0.5728
accuracy: 0.6260 - val_loss: 1.0166 - val_accuracy: 0.6011
score: [1.0162253673076629, 0.601375]
Q 86m99v32 A 14.9 P 15.8
Q 89m86v44 A 22.4 P 22.8
Q 35m6v39 A 33.3 P 33.8
Q 85m51v63 A 39.4 P 38.0
Q 46m65v77 A 31.9 P 32.8
Q 83m7v45 A 41.5 P 41.8
Q 41m2v99 A 94.4 P 94.8
Q 26m52v85 A 28.3 P 28.2
Q 16m57v4 A 0.88 P 0.94
Q 73m19v16 A 12.7 P 12.8
Iteration 13
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 40us/sample - loss: 0.9416 -
accuracy: 0.6291 - val_loss: 0.9205 - val_accuracy: 0.6395
Epoch 2/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.9360 -
accuracy: 0.6313 - val_loss: 0.8947 - val_accuracy: 0.6570
Epoch 3/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.9322 -
accuracy: 0.6318 - val_loss: 0.8813 - val_accuracy: 0.6644
score: [0.8812202425003052, 0.66353124]
Q 93m8v11 A 10.1 P 10.1
Q 73m28v2 A 1.45 P 1.43
Q 24m83v43 A 9.64 P 9..0
Q 13m75v56 A 8.27 P 8.90
Q 13m91v78 A 9.75 P 9..1
Q 52m9v1 A 0.85 P 0.80
Q 33m6v64 A 54.2 P 54.0
Q 58m55v63 A 32.3 P 32.0
Q 57m93v74 A 28.1 P 28.0
Q 77m18v43 A 34.9 P 35.0
```

```
Epoch 1/3
64000/64000 [============== ] - 3s 40us/sample - loss: 0.9266 -
accuracy: 0.6358 - val_loss: 0.9004 - val_accuracy: 0.6448
64000/64000 [============= ] - 3s 40us/sample - loss: 0.9201 -
accuracy: 0.6375 - val_loss: 0.9676 - val_accuracy: 0.6114
accuracy: 0.6390 - val_loss: 0.9426 - val_accuracy: 0.6218
score: [0.9460811560153961, 0.61928123]
Q 75m6v58 A 53.7 P 53.2
Q 31m58v62 A 21.6 P 21.2
Q 3m72v15 A 0.60 P 0.62
Q 97m65v73 A 43.7 P 42.2
Q 25m74v55 A 13.9 P 13.2
Q 41m2v99 A 94.4 P 94.0
Q 24m42v92 A 33.5 P 33.2
Q 12m79v69 A 9.10 P 8.22
Q 8m21v72 A 19.9 P 29.2
Q 23m11v85 A 57.5 P 56.2
Iteration 15
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 38us/sample - loss: 0.9127 -
accuracy: 0.6403 - val_loss: 0.9325 - val_accuracy: 0.6245
Epoch 2/3
64000/64000 [=============== ] - 2s 39us/sample - loss: 0.9073 -
accuracy: 0.6424 - val_loss: 0.8621 - val_accuracy: 0.6674
Epoch 3/3
64000/64000 [=============== ] - 2s 38us/sample - loss: 0.9047 -
accuracy: 0.6437 - val_loss: 0.8590 - val_accuracy: 0.6737
score: [0.8556039447784424, 0.6741875]
Q 56m49v91 A 48.5 P 48.0
Q 62m75v51 A 23.1 P 23.6
Q 4m98v18 A 0.71 P 0.72
Q 3m81v14 A 0.50 P 0.53
Q 61m91v2 A 0.80 P 0.86
Q 22m88v1 A 0.20 P 0.22
Q 8m33v85 A 16.6 P 15.2
Q 8m71v15 A 1.52 P 1.53
Q 61m53v6 A 3.21 P 3.10
Q 92m25v38 A 29.9 P 29.6
```

```
Epoch 1/3
accuracy: 0.6468 - val_loss: 0.9359 - val_accuracy: 0.6243
64000/64000 [============= ] - 2s 39us/sample - loss: 0.8949 -
accuracy: 0.6485 - val_loss: 0.8677 - val_accuracy: 0.6587
accuracy: 0.6490 - val_loss: 0.9218 - val_accuracy: 0.6384
score: [0.919591515302658, 0.6401875]
Q 6m91v58 A 3.59 P 3.00
Q 9m9v55 A 27.5 P 27.0
Q 48m56v72 A 33.2 P 32.0
Q 27m32v94 A 43.0 P 42.0
Q 49m74v24 A 9.56 P 9.40
Q 71m37v57 A 37.5 P 37.0
Q 17m57v29 A 6.66 P 6.00
Q 19m62v33 A 7.74 P 7.60
Q 11m45v22 A 4.32 P 4.70
Q 28m91v23 A 5.41 P 5.02
Iteration 17
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.8881 -
accuracy: 0.6504 - val_loss: 0.8694 - val_accuracy: 0.6616
Epoch 2/3
64000/64000 [============= ] - 2s 39us/sample - loss: 0.8826 -
accuracy: 0.6533 - val_loss: 0.8683 - val_accuracy: 0.6633
Epoch 3/3
64000/64000 [=============== ] - 2s 39us/sample - loss: 0.8805 -
accuracy: 0.6540 - val_loss: 0.8797 - val_accuracy: 0.6520
score: [0.879545749425888, 0.6511875]
Q 26m42v64 A 24.5 P 24.5
Q 7m67v5 A 0.47 P 0.48
Q 52m82v24 A 9.31 P 9.60
Q 94m47v36 A 24.0 P 23.8
Q 8m37v43 A 7.64 P 7.50
Q 71m89v99 A 43.9 P 44.5
Q 53m59v28 A 13.2 P 13.5
Q 15m42v2 A 0.53 P 0.40
Q 43m14v25 A 18.9 P 19.5
Q 7m87v98 A 7.30 P 6.50
```

```
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.8775 -
accuracy: 0.6547 - val_loss: 0.8412 - val_accuracy: 0.6785
64000/64000 [============== ] - 3s 40us/sample - loss: 0.8729 -
accuracy: 0.6578 - val_loss: 0.9125 - val_accuracy: 0.6407
accuracy: 0.6592 - val_loss: 0.9355 - val_accuracy: 0.6315
score: [0.9333925821781158, 0.631375]
Q 32m8v9
        A 7.20 P 6.58
Q 29m26v86 A 45.3 P 44.9
Q 6m12v8 A 2.67 P 2.80
Q 96m95v8 A 4.02 P 4.90
Q 35m33v65 A 33.5 P 33.5
Q 98m77v6 A 3.36 P 3.51
Q 53m75v32 A 13.2 P 13.5
Q 35m5v4 A 3.50 P 3.47
Q 72m52v41 A 23.8 P 24.8
Iteration 19
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.8688 -
accuracy: 0.6578 - val_loss: 0.8574 - val_accuracy: 0.6658
Epoch 2/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.8644 -
accuracy: 0.6605 - val_loss: 0.8219 - val_accuracy: 0.6862
Epoch 3/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.8597 -
accuracy: 0.6615 - val_loss: 0.8497 - val_accuracy: 0.6683
score: [0.8487990510463714, 0.66809374]
Q 81m48v35 A 22.0 P 22.8
Q 75m96v11 A 4.82 P 4.88
Q 28m75v33 A 8.97 P 9.10
Q 2m65v67 A 2.00 P 2.08
Q 75m6v29 A 26.9 P 26.8
Q 16m83v99 A 16.0 P 16.8
Q 19m42v23 A 7.16 P 7.80
Q 9m11v32 A 14.4 P 14.0
Q 97m23v61 A 49.3 P 48.8
Q 7m89v94 A 6.85 P 6.88
```

-----

Iteration 20

```
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.8561 -
accuracy: 0.6644 - val_loss: 0.9543 - val_accuracy: 0.6270
64000/64000 [============== ] - 3s 40us/sample - loss: 0.8556 -
accuracy: 0.6645 - val_loss: 0.8521 - val_accuracy: 0.6663
accuracy: 0.6655 - val_loss: 0.8926 - val_accuracy: 0.6453
score: [0.8878784575462342, 0.64821875]
Q 57m72v64 A 28.3 P 28.5
Q 34m92v85 A 22.9 P 23.1
Q 85m51v63 A 39.4 P 39.5
Q 26m54v5 A 1.62 P 1.65
Q 92m2v39 A 38.2 P 38.1
Q 9m7v46 A 25.9 P 26.5
Q 65m3v68 A 65.0 P 65.2
Q 76m8v51 A 46.1 P 46.5
Q 74m36v83 A 55.8 P 55.1
Q 36m59v22 A 8.34 P 8.60
Iteration 21
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 38us/sample - loss: 0.8488 -
accuracy: 0.6674 - val_loss: 0.8952 - val_accuracy: 0.6420
Epoch 2/3
64000/64000 [============= ] - 2s 38us/sample - loss: 0.8433 -
accuracy: 0.6698 - val_loss: 0.8314 - val_accuracy: 0.6712
Epoch 3/3
64000/64000 [=============== ] - 2s 38us/sample - loss: 0.8416 -
accuracy: 0.6701 - val_loss: 0.8651 - val_accuracy: 0.6618
score: [0.866441558599472, 0.6590313]
Q 22m54v57 A 16.5 P 16.0
Q 8m35v13 A 2.42 P 2.20
Q 41m48v8 A 3.69 P 3.50
Q 52m74v12 A 4.95 P 4.30
Q 78m46v29 A 18.2 P 18.8
Q 2m89v29 A 0.64 P 0.53
Q 28m41v73 A 29.6 P 29.3
Q 75m3v92 A 88.5 P 88.5
Q 37m81v79 A 24.8 P 24.3
Q 71m14v5 A 4.18 P 4.18
```

```
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.8392 -
accuracy: 0.6709 - val_loss: 0.8508 - val_accuracy: 0.6631
64000/64000 [============== ] - 2s 38us/sample - loss: 0.8361 -
accuracy: 0.6733 - val_loss: 0.8439 - val_accuracy: 0.6679
accuracy: 0.6732 - val_loss: 0.8815 - val_accuracy: 0.6482
score: [0.8830624108314514, 0.6481562]
Q 59m57v24 A 12.2 P 11.0
Q 53m6v8 A 7.19 P 7.25
Q 7m23v17 A 3.97 P 3.00
Q 47m18v98 A 70.9 P 71.0
Q 28m88v8 A 1.93 P 1.80
Q 98m91v18 A 9.33 P 9.10
Q 55m97v86 A 31.1 P 30.3
Q 24m9v17 A 12.4 P 12.1
Q 57m75v51 A 22.0 P 21.1
Q 43m21v7 A 4.70 P 4.10
Iteration 23
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 38us/sample - loss: 0.8305 -
accuracy: 0.6741 - val_loss: 0.8411 - val_accuracy: 0.6668
Epoch 2/3
64000/64000 [============= ] - 2s 39us/sample - loss: 0.8275 -
accuracy: 0.6763 - val_loss: 0.8227 - val_accuracy: 0.6740
Epoch 3/3
64000/64000 [=============== ] - 2s 39us/sample - loss: 0.8267 -
accuracy: 0.6771 - val_loss: 0.8481 - val_accuracy: 0.6644
score: [0.8486135015487671, 0.6670625]
Q 2m53v65 A 2.36 P 2.20
Q 76m84v66 A 31.4 P 31.8
Q 22m13v41 A 25.8 P 25.0
Q 17m3v45 A 38.2 P 38.8
Q 97m94v66 A 33.5 P 33.0
Q 34m38v27 A 12.8 P 12.8
Q 6m8v59 A 25.3 P 24.0
Q 97m44v29 A 20.0 P 20.8
Q 5m95v11 A 0.55 P 0.43
Q 18m38v61 A 19.6 P 18.0
```

```
Epoch 1/3
64000/64000 [============= ] - 2s 39us/sample - loss: 0.8223 -
accuracy: 0.6785 - val_loss: 0.8180 - val_accuracy: 0.6837
64000/64000 [============== ] - 2s 39us/sample - loss: 0.8195 -
accuracy: 0.6793 - val_loss: 0.8330 - val_accuracy: 0.6690
accuracy: 0.6807 - val_loss: 0.7950 - val_accuracy: 0.6927
score: [0.7929418609142304, 0.6969375]
Q 47m67v49 A 20.2 P 20.5
Q 76m8v51 A 46.1 P 46.8
Q 46m69v93 A 37.2 P 37.0
Q 38m51v35 A 14.9 P 15.6
Q 38m18v19 A 12.9 P 12.8
Q 2m22v77 A 6.42 P 6.00
Q 14m22v42 A 16.3 P 16.0
Q 81m66v21 A 11.6 P 11.5
Q 68m6v54 A 49.6 P 59.8
Q 47m9v66 A 55.4 P 55.5
Iteration 25
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.8155 -
accuracy: 0.6811 - val_loss: 0.7967 - val_accuracy: 0.6908
Epoch 2/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.8133 -
accuracy: 0.6815 - val_loss: 0.8581 - val_accuracy: 0.6598
Epoch 3/3
64000/64000 [=============== ] - 3s 39us/sample - loss: 0.8105 -
accuracy: 0.6831 - val_loss: 0.8080 - val_accuracy: 0.6808
score: [0.8066634085178376, 0.68290627]
Q 95m54v58 A 37.0 P 37.5
Q 95m16v35 A 30.0 P 30.8
Q 5m24v63 A 10.9 P 11.5
Q 81m8v16 A 14.6 P 14.6
Q 4m37v53 A 5.17 P 5.00
Q 61m34v52 A 33.4 P 33.5
Q 71m85v51 A 23.2 P 23.5
Q 92m8v78 A 71.8 P 71.5
Q 12m53v9 A 1.66 P 1.55
Q 94m86v39 A 20.4 P 20.5
```

```
Epoch 1/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.8074 -
accuracy: 0.6841 - val_loss: 0.8086 - val_accuracy: 0.6776
64000/64000 [============== ] - 2s 39us/sample - loss: 0.8052 -
accuracy: 0.6858 - val_loss: 0.8475 - val_accuracy: 0.6694
accuracy: 0.6864 - val_loss: 0.8037 - val_accuracy: 0.6816
score: [0.8009607315063476, 0.6852813]
Q 67m44v71 A 42.9 P 43.0
Q 96m37v56 A 40.4 P 40.8
Q 67m32v67 A 45.3 P 45.0
Q 47m98v7 A 2.27 P 2.33
Q 72m2v4 A 3.89 P 3.89
Q 57m23v52 A 37.0 P 37.0
Q 62m94v54 A 21.5 P 21.5
Q 6m76v76 A 5.56 P 5.50
Q 84m98v34 A 15.7 P 16.1
Q 12m96v29 A 3.22 P 3.30
Iteration 27
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.7995 -
accuracy: 0.6881 - val_loss: 0.8097 - val_accuracy: 0.6853
Epoch 2/3
64000/64000 [============= ] - 3s 40us/sample - loss: 0.7986 -
accuracy: 0.6888 - val_loss: 0.8176 - val_accuracy: 0.6776
Epoch 3/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.7955 -
accuracy: 0.6890 - val_loss: 0.8158 - val_accuracy: 0.6735
score: [0.8188097815513611, 0.67175]
Q 26m5v34 A 28.5 P 28.8
Q 62m26v86 A 60.6 P 60.9
Q 23m15v7 A 4.24 P 4.20
Q 98m4v41 A 39.4 P 39.4
Q 5m68v84 A 5.75 P 5.09
Q 37m27v56 A 32.4 P 32.9
Q 83m12v43 A 37.6 P 36.9
Q 24m72v59 A 14.8 P 15.2
Q 67m91v44 A 18.7 P 18.9
Q 53m59v28 A 13.2 P 13.6
```

```
Epoch 1/3
64000/64000 [============== ] - 2s 38us/sample - loss: 0.7933 -
accuracy: 0.6895 - val_loss: 0.8693 - val_accuracy: 0.6583
64000/64000 [============== ] - 2s 38us/sample - loss: 0.7918 -
accuracy: 0.6907 - val_loss: 0.7983 - val_accuracy: 0.6832
accuracy: 0.6927 - val_loss: 0.8026 - val_accuracy: 0.6790
score: [0.8030582339763641, 0.6786875]
Q 25m29v65 A 30.1 P 30.6
Q 66m24v5 A 3.67 P 3.66
Q 51m96v93 A 32.3 P 32.0
Q 68m81v19 A 8.67 P 8.60
Q 7m22v43 A 10.4 P 10.6
Q 25m53v75 A 24.0 P 23.3
Q 35m35v8 A 4.00 P 3.90
Q 58m59v98 A 48.6 P 49.5
Q 37m47v85 A 37.4 P 37.0
Q 62m15v3 A 2.42 P 2.40
Iteration 29
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
accuracy: 0.6931 - val_loss: 0.7769 - val_accuracy: 0.6988
Epoch 2/3
64000/64000 [============= ] - 2s 38us/sample - loss: 0.7840 -
accuracy: 0.6938 - val_loss: 0.8692 - val_accuracy: 0.6630
Epoch 3/3
accuracy: 0.6953 - val_loss: 0.8320 - val_accuracy: 0.6703
score: [0.8350286138057709, 0.66809374]
Q 9m47v78 A 12.5 P 12.8
Q 16m19v1 A 0.46 P 0.46
Q 72m27v99 A 72.0 P 71.6
Q 34m38v27 A 12.8 P 12.8
Q 4m56v28 A 1.87 P 1.90
Q 54m58v39 A 18.8 P 18.5
Q 66m58v31 A 16.5 P 16.6
Q 48m6v2 A 1.78 P 1.75
Q 56m12v71 A 58.5 P 57.6
Q 94m84v61 A 32.2 P 31.0
```

```
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.7793 -
accuracy: 0.6959 - val_loss: 0.7784 - val_accuracy: 0.6968
64000/64000 [============== ] - 3s 39us/sample - loss: 0.7776 -
accuracy: 0.6969 - val_loss: 0.7880 - val_accuracy: 0.6925
accuracy: 0.6982 - val_loss: 0.8171 - val_accuracy: 0.6817
score: [0.8186441586017609, 0.67934376]
Q 84m2v74 A 72.3 P 72.2
Q 47m98v35 A 11.3 P 11.0
Q 28m9v36 A 27.2 P 27.0
Q 3m45v68 A 4.25 P 4.25
Q 7m67v5 A 0.47 P 0.44
Q 18m95v79 A 12.6 P 12.0
Q 53m78v82 A 33.2 P 32.5
Q 41m57v7 A 2.93 P 2.90
Q 2m33v3 A 0.17 P 0.15
Q 13m43v83 A 19.3 P 19.2
Iteration 31
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 3s 40us/sample - loss: 0.7739 -
accuracy: 0.6985 - val_loss: 0.7901 - val_accuracy: 0.6886
Epoch 2/3
64000/64000 [============= ] - 3s 39us/sample - loss: 0.7712 -
accuracy: 0.6992 - val_loss: 0.7590 - val_accuracy: 0.7062
Epoch 3/3
accuracy: 0.6995 - val_loss: 0.7859 - val_accuracy: 0.6930
score: [0.7823098633289337, 0.698]
Q 56m7v86 A 76.4 P 76.1
Q 79m57v92 A 53.4 P 53.3
Q 52m32v25 A 15.5 P 15.5
Q 42m14v87 A 65.2 P 65.5
Q 4m92v28 A 1.17 P 1.15
Q 58m89v35 A 13.8 P 13.8
Q 81m88v63 A 30.2 P 30.3
Q 2m61v3 A 0.10 P 0.09
Q 24m79v78 A 18.2 P 18.5
Q 15m42v2 A 0.53 P 0.50
```

```
Epoch 1/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.7674 -
accuracy: 0.7008 - val_loss: 0.8750 - val_accuracy: 0.6531
64000/64000 [============= ] - 3s 39us/sample - loss: 0.7644 -
accuracy: 0.7033 - val_loss: 0.8079 - val_accuracy: 0.6768
accuracy: 0.7032 - val_loss: 0.7945 - val_accuracy: 0.6870
score: [0.7964618723392487, 0.68703127]
Q 38m9v29 A 23.4 P 23.0
Q 93m5v58 A 55.0 P 55.1
Q 6m81v47 A 3.24 P 3.20
Q 24m12v82 A 54.7 P 55.9
Q 79m68v7 A 3.76 P 3.77
Q 16m83v9 A 1.45 P 1.45
Q 99m45v5 A 3.44 P 3.51
Q 93m36v46 A 33.2 P 33.2
Q 21m8v18 A 13.0 P 12.5
Q 26m38v18 A 7.31 P 7.80
Iteration 33
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.7609 -
accuracy: 0.7042 - val_loss: 0.8159 - val_accuracy: 0.6761
Epoch 2/3
64000/64000 [============== ] - 3s 39us/sample - loss: 0.7588 -
accuracy: 0.7043 - val_loss: 0.7773 - val_accuracy: 0.6978
Epoch 3/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.7567 -
accuracy: 0.7058 - val_loss: 0.8803 - val_accuracy: 0.6568
score: [0.8798099870681763, 0.65578127]
Q 67m23v24 A 17.9 P 17.8
Q 37m61v22 A 8.31 P 8.46
Q 3m83v7 A 0.24 P 0.24
Q 43m69v27 A 10.4 P 10.1
Q 34m79v98 A 29.5 P 29.2
Q 67m87v1 A 0.44 P 0.45
Q 47m44v21 A 10.8 P 10.8
Q 61m8v39 A 34.5 P 35.6
Q 35m33v28 A 14.4 P 14.0
Q 9m26v3 A 0.77 P 0.72
```

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Iteration 34

```
Epoch 1/3
64000/64000 [============== ] - 3s 40us/sample - loss: 0.7554 -
accuracy: 0.7063 - val_loss: 0.7768 - val_accuracy: 0.6930
64000/64000 [============= ] - 3s 40us/sample - loss: 0.7540 -
accuracy: 0.7064 - val_loss: 0.7572 - val_accuracy: 0.7030
64000/64000 [============= ] - ETA: Os - loss: 0.7515 -
accuracy: 0.70 - 2s 38us/sample - loss: 0.7521 - accuracy: 0.7061 - val_loss:
0.7697 - val_accuracy: 0.6945
score: [0.7694476416110992, 0.69578123]
Q 31m14v27 A 18.6
                 P 18.5
Q 57m26v17 A 11.7
                  P 11.6
Q 7m25v34 A 7.44 P 7.20
Q 25m6v91 A 73.4 P 74.8
Q 88m35v38 A 27.2 P 27.0
Q 47m2v98 A 94.0 P 94.2
Q 96m7v62 A 57.8 P 58.1
Q 88m7v91 A 84.3 P 84.3
Q 19m57v36 A 9.00 P 8.12
Q 68m17v3 A 2.40 P 2.41
Iteration 35
Train on 64000 samples, validate on 8000 samples
Epoch 1/3
64000/64000 [============== ] - 2s 39us/sample - loss: 0.7482 -
accuracy: 0.7089 - val_loss: 0.7972 - val_accuracy: 0.6853
64000/64000 [============= ] - 2s 38us/sample - loss: 0.7480 -
accuracy: 0.7082 - val_loss: 0.7576 - val_accuracy: 0.7023
64000/64000 [============== ] - 2s 39us/sample - loss: 0.7467 -
accuracy: 0.7091 - val_loss: 0.7545 - val_accuracy: 0.7038
score: [0.7542344851493835, 0.7033125]
Q 98m94v95 A 48.5
                 P 48.0
Q 36m62v35 A 12.9 P 12.6
Q 44m28v8 A 4.89 P 4.70
Q 55m8v53 A 46.3 P 46.5
Q 3m93v4
         A 0.12 P 0.12
Q 9m48v83 A 13.1 P 12.4
Q 65m26v67 A 47.9 P 48.0
Q 92m72v59 A 33.1
                P 32.0
Q 61m56v73 A 38.1
                P 37.0
Q 9m58v42 A 5.64 P 5.40
```

[]: