Tutorial1-RNN Sequence classifier

April 9, 2024

1 Tutorial 1 - RNN Sequence classifier

In this notebook, we will predict the winner of a basketball game based on the scores observed in the first 3 quarters of the game. Each column represents the beginning of a minute during the game. (There are 12 minutes in each quarter. There are 3 quarters in the data, so we have 36 columns as input variables in chronological order.) The values captured in each column represent the score difference observed at that minute (home score minus away score)

The last column W represents whether the home team (1) or the away team (0) won the game. This is the target variable. Our unit of analysis is a single game.

```
[]: # Common imports
import numpy as np
import tensorflow as tf
from tensorflow import keras
import pandas as pd
import matplotlib.pyplot as plt

np.random.seed(1)
tf.random.set_seed(1)
epoch_num = 5 # numer of epochs to train each model
```

1.1 Load and split data

Basketball data consists of each row (observation) representing a single game. The first 36 columns represent the score difference at each minute of the game. The last column represents the winner of the game (1 = home team, 0 = away team). The data is stored in a csv file. We will load the data into a pandas dataframe.

We see that we have 1230 observations (games) and 37 columns (36 minutes of the game + 1 target variable).

```
[]: data.shape
```

```
[]: (1230, 37)
```

```
[]: data.head(5)
```

```
[ ]:
          M1
                                                                   M28
                                                                          M29
                                                                                M30
                                                                                              M32
               M2
                    МЗ
                         M4
                               M5
                                    M6
                                         M7
                                              M8
                                                    M9
                                                         M10
                                                                                       M31
                                                                                                    M33
      0
          -2
               -1
                      1
                           1
                               -1
                                    -3
                                         -1
                                                0
                                                     3
                                                            6
                                                                      9
                                                                            11
                                                                                  10
                                                                                         7
                                                                                                7
                                                                                                       4
      1
           0
                2
                     7
                           6
                               10
                                     8
                                           8
                                                6
                                                     0
                                                            6
                                                                      7
                                                                           11
                                                                                  11
                                                                                        14
                                                                                               14
                                                                                                      15
      2
               -2
           0
                      2
                           0
                                5
                                     4
                                           5
                                                3
                                                     5
                                                            3
                                                                      9
                                                                           11
                                                                                  13
                                                                                        13
                                                                                               12
                                                                                                      17
                                           5
                                                     3
                                                                                   7
      3
                2
                           3
                                4
                                     3
                                                4
                                                            1
                                                                                         7
                                                                                                8
           0
                      0
                                                                     10
                                                                             6
                                                                                                       8
      4
           0
               -2
                    -2
                           0
                                3
                                         -7
                                    -2
                                               -5
                                                    -7
                                                                     10
                                                                            10
                                                                                  15
                                                          -4
                                                                                         13
                                                                                               11
                                                                                                      11
```

```
M34
          M35
                M36
                      W
0
      6
            2
                   1
                       1
1
     13
           13
                 13
                      0
2
     15
           15
                 12
                      1
3
      8
            8
                   8
                      1
4
     11
           13
                 10
                      1
```

[5 rows x 37 columns]

Split each observation into a sequence of 36 observations (minutes) and a single observation (winner). The sequence of 36 observations will be the input (X) to the RNN. The single observation (y) will be the target variable.

```
[]: y = data['W']
X = data.drop('W', axis=1)
```

```
[ ]: y = np.array(y).astype(np.int8)
X = np.array(X).astype(np.int8)
```

Finally, we need to split the data into training and test sets. A random split on this data is OK, as each 'game' (observation) is independent of the others. We will use 70% of the data for training and 30% for testing.

```
[]: from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3)
```

1.2 Create dataframe to store results

We are running 8 models in this notebook. We will store the results in a dataframe for easy comparison.

1.3 MODEL01 - A normal (cross-sectional) NN

This model assumes that the data is NOT a time-series data set. It treats the data as cross-sectional and the columns being independent of each other.

```
[]: print(X_train.shape) # 2d array of shape (n_samples, n_features)
     print(y_train.shape) # 1d array of shape (n_samples,)
    (861, 36)
    (861,)
[]: model = keras.models.Sequential([
         keras.layers.Flatten(input_shape=[36, 1]),
         keras.layers.Dense(72, activation='relu'),
         keras.layers.Dense(1, activation='sigmoid')
     ])
    /Users/timsmith/miniconda3/envs/dsp/lib/python3.11/site-
    packages/keras/src/layers/reshaping/flatten.py:37: UserWarning: Do not pass an
    `input_shape`/`input_dim` argument to a layer. When using Sequential models,
    prefer using an `Input(shape)` object as the first layer in the model instead.
      super().__init__(**kwargs)
    2024-04-09 07:30:26.758631: I metal_plugin/src/device/metal_device.cc:1154]
    Metal device set to: Apple M1 Pro
    2024-04-09 07:30:26.758655: I metal_plugin/src/device/metal_device.cc:296]
    systemMemory: 16.00 GB
    2024-04-09 07:30:26.758662: I metal_plugin/src/device/metal_device.cc:313]
    maxCacheSize: 5.33 GB
    2024-04-09 07:30:26.758680: I
    tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:305]
    Could not identify NUMA node of platform GPU ID 0, defaulting to 0. Your kernel
    may not have been built with NUMA support.
    2024-04-09 07:30:26.758694: I
    tensorflow/core/common_runtime/pluggable_device/pluggable_device_factory.cc:271]
    Created TensorFlow device (/job:localhost/replica:0/task:0/device:GPU:0 with 0
    MB memory) -> physical PluggableDevice (device: 0, name: METAL, pci bus id:
    <undefined>)
[]: model.compile(
         loss="binary_crossentropy", # If multiclass, use_
      →"sparse_categorical_crossentropy" as the loss function
         optimizer=tf.keras.optimizers.Nadam(learning_rate=0.001),
         metrics=['accuracy']
     model.summary()
    Model: "sequential"
     Layer (type)
                                       Output Shape
                                                                      Param #
     flatten (Flatten)
                                        (None, 36)
                                                                            0
```

```
dense (Dense) (None, 72) 2,664
dense_1 (Dense) (None, 1) 73
```

Total params: 2,737 (10.69 KB)

Trainable params: 2,737 (10.69 KB)

Non-trainable params: 0 (0.00 B)

[]: | ### How to interpret the output shape?

- The first layer
 - None is a wild-card representing the number of observations this will be the number of observations in a batch that is fed into the network.
 - 36 is the number of units in the layer, since there will be 36 outputs from this layer 36, the second dimension will have 36
- The second layer
 - None is a wild-card representing the number of observations this will be the number of observations in a batch that is fed into the network. This will be the same at each later, since the batch size is the same during each epoch.
 - 72 is the number of units in the layer, since there will be 72 outputs from these 72 units
- The third layer
 - None is a wild-card, is the number of observations given in the batch.
 - 1 is the number of units in the layer. Since the output is a binary value, there is one unit for the output, and therefore 1 is the number of outputs.

We can write this formulaically as:

```
[]: p = 1  # for NN, one weight per unit input
b = 1  # for NN, one bias per unit

# First hidden layer
i = 36  # 36 inputs from the previous layer (flatten layer)
h = 72  # number of units in this layer

p * (h*i + b*h)
```

[]: 2664

1.3.1 Calculate the number of paramaters for the model

- The first later doesn't have any parameters, because it's just flattening the input
 - 0 inputs to 36 unites, is 0 weights and zero biases

- The second layer has 36 units connecting to 72 units, so 36^{**72} weights. If each weight also has a bias, then we add 72
 - -36*72+72 = 2664
- The third layer has 72 outputs from the previous later to 1 unit, so 72 weights. If each unit in the layer has a bias, then we add 1 since there is only one unit
 - -72+1=73

https://towardsdatascience.com/counting-no-of-parameters-in-deep-learning-models-by-hand-8f1716241889

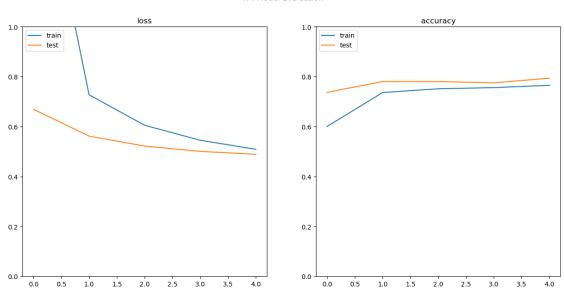
```
[]: import time
     start time = time.time()
     call_back = keras.callbacks.EarlyStopping(patience=5, restore_best_weights=True)
     history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[call_back]
     )
     end_time = time.time()
    Epoch 1/5
    2024-04-09 07:30:27.617055: I
    tensorflow/core/grappler/optimizers/custom_graph_optimizer_registry.cc:117]
    Plugin optimizer for device_type GPU is enabled.
    27/27
                      2s 25ms/step -
    accuracy: 0.5047 - loss: 2.9070 - val_accuracy: 0.7371 - val_loss: 0.6694
    Epoch 2/5
    27/27
                      Os 11ms/step -
    accuracy: 0.7198 - loss: 0.7530 - val accuracy: 0.7805 - val loss: 0.5617
    Epoch 3/5
    27/27
                      Os 11ms/step -
    accuracy: 0.7477 - loss: 0.6374 - val_accuracy: 0.7805 - val_loss: 0.5219
    Epoch 4/5
    27/27
                      Os 11ms/step -
    accuracy: 0.7589 - loss: 0.5625 - val_accuracy: 0.7751 - val_loss: 0.5007
    Epoch 5/5
    27/27
                      Os 12ms/step -
    accuracy: 0.7667 - loss: 0.5233 - val accuracy: 0.7940 - val loss: 0.4889
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('NN Model Evaluation')
     ax1.set_title('loss')
```

```
ax1.set_ylim(0, 1)
ax1.plot(history.history['loss'])
ax1.plot(history.history['val_loss'])
ax1.legend(['train', 'test'], loc='upper left')

ax2.set_title('accuracy')
ax2.set_ylim(0, 1)
ax2.plot(history.history['accuracy'])
ax2.plot(history.history['val_accuracy'])
ax2.legend(['train', 'test'], loc='upper left')

plt.show()
```

NN Model Evaluation



```
[ ]: y_pred = model.predict(X_test)
y_pred[:10]
```

12/12 0s 5ms/step

```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test)  # these predictions are probabilities (0-1)_\( \text{\text}\)  # taken from the sigmoid function

y_pred = (y_pred > 0.5).astype('int8')  # let's turn these into predictions (0_\( \text{\text}\)  # or 1)

print(classification_report(y_test, y_pred, digits=4))
```

12/12	/12 Os 1ms/step				
	precision	recall	f1-score	support	
0	0.7407	0.8383	0.7865	167	
1	0.8500	0.7574	0.8010	202	
accuracy			0.7940	369	
macro avg	0.7954	0.7979	0.7938	369	
weighted avg	0.8006	0.7940	0.7945	369	

Store the results into the results dataframe.

1.4 Transform data for RNN

RNN requires input of three dimensions: * The first dimension is the number of observations (games). * The second dimension is the number of time steps (minutes). * The third dimension is the number of features (in this case, 1, which is the score difference).

Our input variable (X) is a sequence of 36 observations. We will use the reshape method to reshape the data into a 3D array. The reshape method will return a 3D array with the shape (861, 36, 1) for the training data and (369, 36, 1) for the test data.

```
[]: X_train = np.reshape(X_train, (X_train.shape[0], X_train.shape[1], 1))
    X_test = np.reshape(X_test, (X_test.shape[0], X_test.shape[1], 1))
    print(X_train.shape)
    print(X_test.shape)

(861, 36, 1)
    (369, 36, 1)
```

1.5 MODEL02 - Simple RNN with one layer

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an
`input_shape`/`input_dim` argument to a layer. When using Sequential models,
prefer using an `Input(shape)` object as the first layer in the model instead.
super().__init__(**kwargs)

Model: "sequential_1"

Layer (type)	Output Shape	Param #
simple_rnn (SimpleRNN)	(None, 40)	1,680
dense_2 (Dense)	(None, 1)	41

Total params: 1,721 (6.72 KB)

Trainable params: 1,721 (6.72 KB)

Non-trainable params: 0 (0.00 B)

1.5.1 How to interpret the output shape.

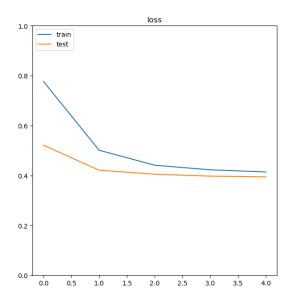
- First layer:
 - None is a wild-card representing the number of observations this will be the number of observations in a batch that is fed into the network.
 - There are 32 RNN units and each produces one output. Therefore, 32 is the output shape.
- In the second layer, there is one unit and it produces one output. Therefore, 1 * 1 = 1

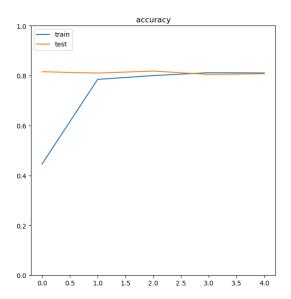
1.5.2 Calculate the number of paramaters for the model

```
[]: p = 1 # number of parameters per unit (for RNN one remember gate)
    b = 1 # number of biases per unit, for RNN this is 1 (for GRU this is 3, and
      →LSTM this is 4)
     #####################################
    # For first layer....
    h = 40 # number of units in the layer
    i = 1 # number of inputs (if we are predicting a stock price based on previous<sub>U</sub>
     ⇔stock prices, input = 1.
    # NOTE: If we are predicting a stock price based on previous stock prices and \Box
     \hookrightarrow the price of oil, input = 2), etc.
    params = p*(h**2+i*h+b*h)
    print("First layer params = ", params)
    # for the last layer
     # This is simply 40 outputs coming from the previous later plus 1 bias term
    print("Last layer params = ", 40+1)
    First layer params = 1680
    Last layer params = 41
[]: from tensorflow.keras.callbacks import EarlyStopping
     # If multiclass, use "sparse_categorical_crossentropy" as the loss function
    model.compile(
        loss="binary crossentropy",
        optimizer=tf.keras.optimizers.Nadam(learning_rate=0.001),
        metrics=['accuracy']
    )
[]: import time
    start_time = time.time()
```

```
early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5,_
      →verbose=1, mode='min')
     history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[early_stop]
     )
     end_time = time.time()
    Epoch 1/5
    27/27
                      12s 400ms/step -
    accuracy: 0.2857 - loss: 0.9109 - val_accuracy: 0.8157 - val_loss: 0.5214
    Epoch 2/5
    27/27
                      14s 516ms/step -
    accuracy: 0.7808 - loss: 0.5321 - val_accuracy: 0.8103 - val_loss: 0.4215
    Epoch 3/5
    27/27
                      16s 596ms/step -
    accuracy: 0.8074 - loss: 0.4473 - val accuracy: 0.8184 - val loss: 0.4052
    Epoch 4/5
                      15s 557ms/step -
    27/27
    accuracy: 0.8231 - loss: 0.4224 - val_accuracy: 0.8049 - val_loss: 0.3975
    Epoch 5/5
    27/27
                      16s 585ms/step -
    accuracy: 0.8188 - loss: 0.4115 - val_accuracy: 0.8076 - val_loss: 0.3946
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('RNN Model Evaluation')
     ax1.set title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
     ax2.plot(history.history['val_accuracy'])
     ax2.legend(['train', 'test'], loc='upper left')
    plt.show()
```

RNN Model Evaluation





```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test)  # these predictions are probabilities (0-1)___

taken from the sigmoid function

y_pred = (y_pred > 0.5)  # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

```
12/12
                  1s 68ms/step
              precision
                            recall f1-score
                                                 support
                            0.7425
           0
                  0.8158
                                       0.7774
                                                     167
                  0.8018
                            0.8614
                                       0.8305
           1
                                                     202
                                       0.8076
                                                     369
    accuracy
                  0.8088
                            0.8020
                                       0.8040
                                                     369
   macro avg
weighted avg
                  0.8082
                            0.8076
                                       0.8065
                                                     369
```

```
'precision': [precision_score(y_test, y_pred)],
    'recall': [recall_score(y_test, y_pred)],
    'f1': [f1_score(y_test, y_pred)]
}

df_results = pd.concat([df_results, df_result], ignore_index=True, axis=0)
```

1.6 MODEL03 - Deep RNN

Be careful: when stacking RNN layers, you have to set "return_sequences" to True. This enables the layer to send a "sequence" of values to the next layer – jut like how it uses a sequence of values for training.

Since the last layer is DENSE, it can't take sequence data. Therefore, you CANNOT return sequences from the previous layer. So, remove return_sequences from previous layer.

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead. super().__init__(**kwargs)

```
[]: model.compile(
    loss="binary_crossentropy",
    optimizer=keras.optimizers.Nadam(learning_rate=0.001),
    metrics=['accuracy']
)
model.summary()
```

Model: "sequential_2"

Layer (type) Output Shape Param #

```
      simple_rnn_1 (SimpleRNN)
      (None, 36, 32)
      1,088

      simple_rnn_2 (SimpleRNN)
      (None, 36, 16)
      784

      simple_rnn_3 (SimpleRNN)
      (None, 32)
      1,568

      dense_3 (Dense)
      (None, 1)
      33
```

Total params: 3,473 (13.57 KB)

Trainable params: 3,473 (13.57 KB)

Non-trainable params: 0 (0.00 B)

1.6.1 How to interpret the output shape?

- First layer:
 - None is a wild-card representing the number of observations this will be the number of observations in a batch that is fed into the network.
 - There are 36 features (which are the 'time steps' of values in the sequence), and there are 32 RNN units.
 - * (batch size, time steps, features) = (None, 36, 32)
- etc. (see previous models where I elaborate on the output shape writing this is getting repetitive)

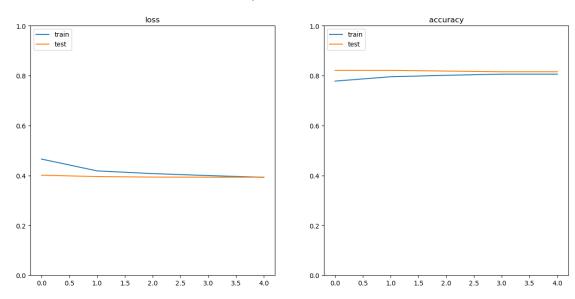
1.6.2 Calculate the number of paramaters for the model

```
# For second layer....
    h = 16 # number of units in the layer
    i = 32 # number of inputs (if we are predicting a stock price based on
     ⇔previous stock prices, input = 1.
     # NOTE: If we are predicting a stock price based on previous stock prices and
     \hookrightarrow the price of oil, input = 2), etc.
    params = p*(h**2+i*h+b*h)
    print("Second layer params = ", params)
    # For third layer....
    h = 32  # number of units in the layer
    i = 16 # number of inputs (previous layer has 16 inutes, so we have 16 inputs)
    params = p*(h**2+i*h+b*h)
    print("Third layer params = ", params)
    ####################################
    # for the last layer
    # This is simply 32 outputs coming from the previous later plus 1 bias term
    print("Last layer params = ", 32+1)
    First layer params = 1088
    Second layer params = 784
    Third layer params = 1568
    Last layer params = 33
[]: from tensorflow.keras.callbacks import EarlyStopping
     # If multiclass, use "sparse_categorical_crossentropy" as the loss function
    model.compile(
        loss="binary_crossentropy",
        optimizer=tf.keras.optimizers.Nadam(learning_rate=0.001),
        metrics=['accuracy']
[]: import time
    start_time = time.time()
    early_stop = EarlyStopping(monitor='val_loss', min_delta=0.0, patience=5,_
      ⇔verbose=1, mode='auto')
```

#####################################

```
history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data = (X_test, y_test),
         callbacks=[early_stop]
     )
     end_time = time.time()
    Epoch 1/5
    27/27
                      76s 3s/step -
    accuracy: 0.7556 - loss: 0.5134 - val accuracy: 0.8211 - val loss: 0.4012
    Epoch 2/5
    27/27
                      69s 3s/step -
    accuracy: 0.8024 - loss: 0.4187 - val_accuracy: 0.8211 - val_loss: 0.3957
    Epoch 3/5
    27/27
                      74s 3s/step -
    accuracy: 0.8055 - loss: 0.4055 - val_accuracy: 0.8184 - val_loss: 0.3937
    Epoch 4/5
    27/27
                      74s 3s/step -
    accuracy: 0.8116 - loss: 0.3973 - val_accuracy: 0.8157 - val_loss: 0.3933
    Epoch 5/5
    27/27
                      73s 3s/step -
    accuracy: 0.8119 - loss: 0.3909 - val_accuracy: 0.8157 - val_loss: 0.3930
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('Deep RNN Model Evaluation')
     ax1.set_title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
     ax2.plot(history.history['val_accuracy'])
     ax2.legend(['train', 'test'], loc='upper left')
     plt.show()
```

Deep RNN Model Evaluation



```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test) # these predictions are probabilities (0-1)_u

taken from the sigmoid function

y_pred = (y_pred > 0.5) # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

```
12/12
                  4s 329ms/step
              precision
                            recall f1-score
                                                 support
           0
                  0.8113
                            0.7725
                                       0.7914
                                                     167
                  0.8190
                            0.8515
                                       0.8350
           1
                                                     202
                                       0.8157
                                                     369
    accuracy
                  0.8152
                            0.8120
                                       0.8132
                                                     369
   macro avg
weighted avg
                  0.8156
                            0.8157
                                       0.8152
                                                     369
```

```
'precision': [precision_score(y_test, y_pred)],
    'recall': [recall_score(y_test, y_pred)],
    'f1': [f1_score(y_test, y_pred)]
}

df_results = pd.concat([df_results, df_result], ignore_index=True, axis=0)
```

1.7 MODEL04 - LSTM with one layer

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an
`input_shape`/`input_dim` argument to a layer. When using Sequential models,
prefer using an `Input(shape)` object as the first layer in the model instead.
super().__init__(**kwargs)

```
[]: model.compile(
    loss="binary_crossentropy",
    optimizer=keras.optimizers.Nadam(learning_rate=0.001),
    metrics=['accuracy']
)
model.summary()
```

Model: "sequential_3"

```
Layer (type)
Output Shape
Param #

lstm (LSTM)
(None, 32)

4,352

dense_4 (Dense)
(None, 1)
33
```

Total params: 4,385 (17.13 KB)

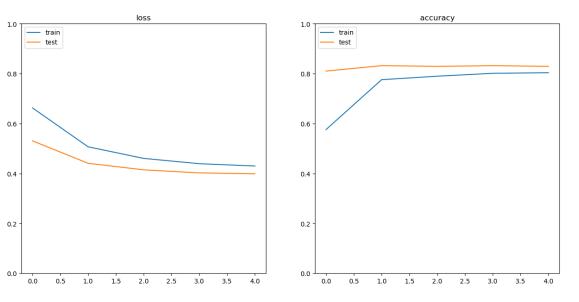
Trainable params: 4,385 (17.13 KB)

1.7.1 Calculate the number of paramaters for the model

```
[]: p = 4 # number of parameters per unit (for LSTM: 1 forget gate, 2 input gates, u
      \rightarrow and 1 output gate)
     b = 1 # number of biases per unit, for LSTM this is 1
     ######################################
     # For first layer....
     h = 32  # number of units in the layer
     i = 1 # number of inputs (if we are predicting a stock price based on previous_
     \hookrightarrowstock prices, input = 1.
     # NOTE: If we are predicting a stock price based on previous stock prices and
      \hookrightarrow the price of oil, input = 2), etc.
     params = p*(h**2+i*h+b*h)
     print("First layer params = ", params)
     #####################################
     # for the last layer
     # This is simply 32 outputs coming from the previous later plus 1 bias term
     print("Last layer params = ", 32+1)
    First layer params = 4352
    Last layer params = 33
[]: import time
     start_time = time.time()
     early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5,_
      ⇔verbose=1, mode='min')
     history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[early_stop]
     end_time = time.time()
    Epoch 1/5
    27/27
                      3s 48ms/step -
```

```
accuracy: 0.4131 - loss: 0.7229 - val_accuracy: 0.8103 - val_loss: 0.5309
    Epoch 2/5
    27/27
                      1s 24ms/step -
    accuracy: 0.7732 - loss: 0.5184 - val_accuracy: 0.8320 - val_loss: 0.4410
    Epoch 3/5
    27/27
                      1s 24ms/step -
    accuracy: 0.7906 - loss: 0.4602 - val_accuracy: 0.8293 - val_loss: 0.4148
    Epoch 4/5
    27/27
                      1s 23ms/step -
    accuracy: 0.8086 - loss: 0.4378 - val_accuracy: 0.8320 - val_loss: 0.4026
    Epoch 5/5
    27/27
                      1s 21ms/step -
    accuracy: 0.8094 - loss: 0.4276 - val_accuracy: 0.8293 - val_loss: 0.3988
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('LSTM Model Evaluation')
     ax1.set_title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
     ax2.plot(history.history['val_accuracy'])
     ax2.legend(['train', 'test'], loc='upper left')
     plt.show()
```

LSTM Model Evaluation



```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test) # these predictions are probabilities (0-1)__

staken from the sigmoid function

y_pred = (y_pred > 0.5) # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

```
12/12
                  Os 15ms/step
              precision
                           recall f1-score
                                               support
           0
                 0.8210
                           0.7964
                                      0.8085
                                                    167
           1
                 0.8357
                           0.8564
                                      0.8460
                                                    202
   accuracy
                                      0.8293
                                                   369
                                      0.8272
   macro avg
                 0.8284
                            0.8264
                                                    369
weighted avg
                 0.8291
                            0.8293
                                      0.8290
                                                    369
```

1.8 MODEL05 - LSTM with more layers

```
keras.layers.Dense(1, activation='sigmoid')
])
```

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an
`input_shape`/`input_dim` argument to a layer. When using Sequential models,
prefer using an `Input(shape)` object as the first layer in the model instead.
super().__init__(**kwargs)

```
[]: np.random.seed(42)
    tf.random.set_seed(42)

model.compile(
        loss="binary_crossentropy",
        optimizer=keras.optimizers.Nadam(learning_rate=0.001),
        metrics=['accuracy']
)

model.summary()
```

Model: "sequential_4"

Layer (type)	Output Shape	Param #
lstm_1 (LSTM)	(None, 36, 32)	4,352
lstm_2 (LSTM)	(None, 36, 32)	8,320
lstm_3 (LSTM)	(None, 32)	8,320
dense_5 (Dense)	(None, 1)	33

Total params: 21,025 (82.13 KB)

Trainable params: 21,025 (82.13 KB)

Non-trainable params: 0 (0.00 B)

1.8.1 Calculate the number of paramaters for the model

```
[]: # Everything is the same as calculating the RNN, except for p
     p = 4 # number of parameters per unit (for LSTM - 1 forget gate, 2 input gates,
     \rightarrow and 1 output gate)
     b = 1 # number of biases per unit, for LSTM this is 1
     ####################################
     # For first layer....
     h = 32 # number of units in the layer
     i = 1 # number of inputs (if we are predicting a stock price based on previous_
     \hookrightarrowstock prices, input = 1.
     # NOTE: If we are predicting a stock price based on previous stock prices and \Box
     \hookrightarrow the price of oil, input = 2), etc.
     params = p*(h**2+i*h+b*h)
     print("First layer params = ", params)
     # for the second layer
     h = 32  # number of units in the layer
     i = 32 # number of inputs (previous layer has 32 units, therefore 32 incoming
      \hookrightarrow inputs)
     params = p*(h**2+i*h+b*h)
     print("Second layer params = ", params)
     #####################################
     # for the third layer
     h = 32  # number of units in the layer
     i = 32 # number of inputs (previous layer has 32 units, therefore 32 incomingu
      ⇔inputs)
     params = p*(h**2+i*h+b*h)
     print("Third layer params = ", params)
     ######################################
     # for the last layer
     # This is simply 32 outputs coming from the previous later plus 1 bias term
     print("Last layer params = ", 32+1)
```

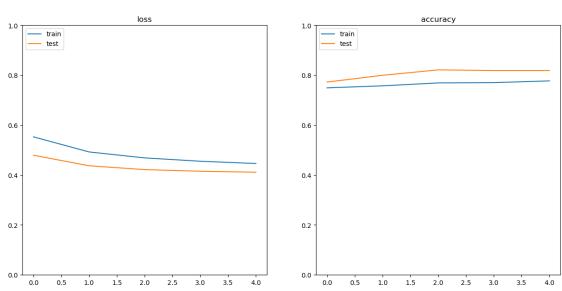
First layer params = 4352 Second layer params = 8320

```
Last layer params = 33
[]: import time
     start_time = time.time()
     early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5, u
      ⇔verbose=1, mode='min')
     history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[early_stop] # we defined this early_stop callback function_
      \hookrightarrow earlier
     end_time = time.time()
    Epoch 1/5
    27/27
                      7s 84ms/step -
    accuracy: 0.7008 - loss: 0.6011 - val_accuracy: 0.7724 - val_loss: 0.4792
    Epoch 2/5
    27/27
                      1s 43ms/step -
    accuracy: 0.7459 - loss: 0.5042 - val_accuracy: 0.7995 - val_loss: 0.4370
    Epoch 3/5
    27/27
                      1s 41ms/step -
    accuracy: 0.7561 - loss: 0.4732 - val_accuracy: 0.8211 - val_loss: 0.4217
    Epoch 4/5
    27/27
                      1s 42ms/step -
    accuracy: 0.7630 - loss: 0.4568 - val_accuracy: 0.8184 - val_loss: 0.4151
    Epoch 5/5
    27/27
                      1s 41ms/step -
    accuracy: 0.7813 - loss: 0.4445 - val accuracy: 0.8184 - val loss: 0.4112
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('Deep LSTM Model Evaluation')
     ax1.set_title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
```

Third layer params = 8320

```
ax2.plot(history.history['val_accuracy'])
ax2.legend(['train', 'test'], loc='upper left')
plt.show()
```

Deep LSTM Model Evaluation



```
12/12
                  1s 47ms/step
              precision
                            recall f1-score
                                                support
           0
                  0.8425
                            0.7365
                                       0.7859
                                                     167
           1
                  0.8027
                            0.8861
                                       0.8424
                                                     202
                                       0.8184
                                                     369
    accuracy
                                       0.8141
                                                     369
   macro avg
                  0.8226
                            0.8113
weighted avg
                  0.8207
                            0.8184
                                       0.8168
                                                     369
```

```
[]: from sklearn.metrics import accuracy_score, precision_score, recall_score, 

→f1_score
```

1.9 MODEL06 - GRU with one layer

```
[]: n_steps = 36
    n_inputs = 1

model = keras.models.Sequential([
         keras.layers.GRU(32, input_shape=[n_steps, n_inputs]),
         keras.layers.Dense(1, activation='sigmoid')
])
```

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an
`input_shape`/`input_dim` argument to a layer. When using Sequential models,
prefer using an `Input(shape)` object as the first layer in the model instead.
super().__init__(**kwargs)

```
[]: model.compile(
    loss="binary_crossentropy",
    optimizer=keras.optimizers.Nadam(learning_rate=0.001),
    metrics=['accuracy']
)
model.summary()
```

Model: "sequential_5"

```
Layer (type)

Output Shape

Param #

gru (GRU)

(None, 32)

3,360

dense_6 (Dense)

(None, 1)

33
```

Total params: 3,393 (13.25 KB)

Trainable params: 3,393 (13.25 KB)

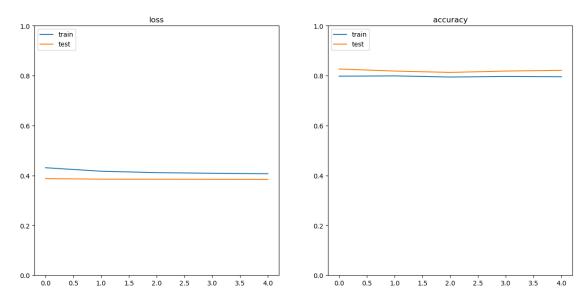
Non-trainable params: 0 (0.00 B)

1.9.1 Calculate the number of paramaters for the model

```
[]: # Everything is the same as calculating the RNN or LSTM parameters, except for p
    p = 3 # number of parameters per unit (for GRU - 1 forget gate, 1 input gates,
     →and 1 output gate)
    b = 2 # number of biases per unit, for GRU this is 2
    # For first layer....
    h = 32 # number of units in the layer
    i = 1 # number of inputs (if we are predicting a stock price based on previous<sub>U</sub>
     \hookrightarrowstock prices, input = 1.
    # NOTE: If we are predicting a stock price based on previous stock prices and \Box
     → the price of oil, input = 2), etc.
    params = p*(h**2+i*h+b*h)
    print("First layer params = ", params)
    # for the last layer
    # This is simply 32 outputs coming from the previous later plus 1 bias term
    print("Last layer params = ", 32+1)
    First layer params = 3360
    Last layer params = 33
[]: import time
    start_time = time.time()
    early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5,_
     ⇔verbose=1, mode='min')
    history = model.fit(
        X_train,
        y_train,
        epochs=epoch_num,
        validation_data=(X_test, y_test),
        callbacks=[early_stop] # we defined this early_stop callback function_
      \hookrightarrow earlier
```

```
)
     end_time = time.time()
    Epoch 1/5
    27/27
                      3s 49ms/step -
    accuracy: 0.7795 - loss: 0.4419 - val_accuracy: 0.8266 - val_loss: 0.3876
    Epoch 2/5
    27/27
                      1s 23ms/step -
    accuracy: 0.7829 - loss: 0.4220 - val_accuracy: 0.8184 - val_loss: 0.3853
    Epoch 3/5
    27/27
                      1s 24ms/step -
    accuracy: 0.7908 - loss: 0.4133 - val_accuracy: 0.8130 - val_loss: 0.3851
    Epoch 4/5
    27/27
                      1s 22ms/step -
    accuracy: 0.7955 - loss: 0.4095 - val accuracy: 0.8184 - val loss: 0.3848
    Epoch 5/5
    27/27
                      1s 21ms/step -
    accuracy: 0.7946 - loss: 0.4074 - val_accuracy: 0.8211 - val_loss: 0.3845
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('GRU Model Evaluation')
     ax1.set_title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
     ax2.plot(history.history['val_accuracy'])
     ax2.legend(['train', 'test'], loc='upper left')
     plt.show()
```

GRU Model Evaluation



```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test) # these predictions are probabilities (0-1)_u

taken from the sigmoid function

y_pred = (y_pred > 0.5) # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

```
12/12
                  1s 19ms/step
              precision
                            recall f1-score
                                                 support
           0
                  0.8176
                            0.7784
                                       0.7975
                                                     167
                  0.8238
                            0.8564
                                       0.8398
           1
                                                     202
                                       0.8211
                                                     369
    accuracy
                  0.8207
                            0.8174
                                       0.8187
                                                     369
   macro avg
weighted avg
                  0.8210
                            0.8211
                                       0.8207
                                                     369
```

```
'precision': [precision_score(y_test, y_pred)],
    'recall': [recall_score(y_test, y_pred)],
    'f1': [f1_score(y_test, y_pred)]
}

df_results = pd.concat([df_results, df_result], ignore_index=True, axis=0)
```

1.10 MODEL07 - GRU with more layers

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/sitepackages/keras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead. super().__init__(**kwargs)

```
[]: model.compile(
          loss="binary_crossentropy",
          optimizer=keras.optimizers.Nadam(learning_rate=0.001),
          metrics=['accuracy']
)
model.summary()
```

Model: "sequential_6"

Layer	(type)	Output	Shape	Param #
gru_1	(GRU)	(None,	36, 32)	3,360
gru_2	(GRU)	(None,	36, 32)	6,336
gru_3	(GRU)	(None,	32)	6,336
dense_	7 (Dense)	(None,	1)	33

Total params: 16,065 (62.75 KB)

Trainable params: 16,065 (62.75 KB)

Non-trainable params: 0 (0.00 B)

1.10.1 Calculate the number of paramaters for the model

```
[]: # Everything is the same as calculating the RNN or LSTM parameters, except for p
    p = 3 # number of parameters per unit (for GRU - 1 forget gate, 1 input gates, u
     ⇔and 1 output gate)
    b = 2 # number of biases per unit, for GRU this is 2
    # For first layer....
    h = 32 # number of units in the layer
    i = 1 # number of inputs (if we are predicting a stock price based on previous<sub>U</sub>
     \hookrightarrowstock prices, input = 1.
    # NOTE: If we are predicting a stock price based on previous stock prices and
     \hookrightarrow the price of oil, input = 2), etc.
    params = p*(h**2+i*h+b*h)
    print("First layer params = ", params)
    ######################################
    # For second layer....
    h = 32 # number of units in the layer
    i = 32 # number of inputs (previous layer has 32 units, therefore 32 inputs)
    params = p*(h**2+i*h+b*h)
    print("First layer params = ", params)
    ######################################
    # For third layer....
    h = 32 # number of units in the layer
    i = 32  # number of inputs (previous layer has 32 units, therefore 32 inputs)
    params = p*(h**2+i*h+b*h)
    print("First layer params = ", params)
```

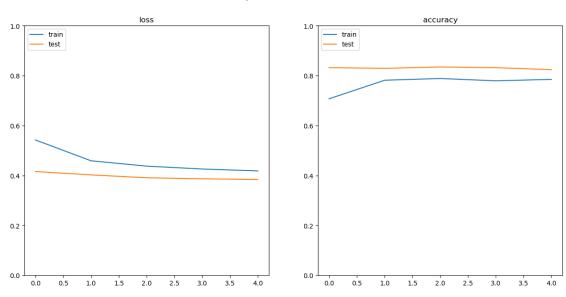
```
# for the last layer
     # This is simply 32 outputs coming from the previous later plus 1 bias term
     print("Last layer params = ", 32+1)
    First layer params = 3360
    First layer params = 6336
    First layer params = 6336
    Last layer params = 33
[]: import time
     start_time = time.time()
     early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5,_
     ⇔verbose=1, mode='min')
     history = model.fit(
         X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[early stop]
     )
     end_time = time.time()
    Epoch 1/5
    27/27
                      6s 82ms/step -
    accuracy: 0.5762 - loss: 0.6405 - val_accuracy: 0.8320 - val_loss: 0.4160
    Epoch 2/5
    27/27
                      1s 41ms/step -
    accuracy: 0.7628 - loss: 0.4734 - val_accuracy: 0.8293 - val_loss: 0.4025
    Epoch 3/5
    27/27
                      1s 40ms/step -
    accuracy: 0.7727 - loss: 0.4435 - val_accuracy: 0.8347 - val_loss: 0.3909
    Epoch 4/5
    27/27
                      1s 40ms/step -
    accuracy: 0.7716 - loss: 0.4266 - val accuracy: 0.8320 - val loss: 0.3868
    Epoch 5/5
    27/27
                      1s 40ms/step -
    accuracy: 0.7776 - loss: 0.4176 - val_accuracy: 0.8238 - val_loss: 0.3840
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('Deep GRU Model Evaluation')
     ax1.set_title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
```

```
ax1.plot(history.history['val_loss'])
ax1.legend(['train', 'test'], loc='upper left')

ax2.set_title('accuracy')
ax2.set_ylim(0, 1)
ax2.plot(history.history['accuracy'])
ax2.plot(history.history['val_accuracy'])
ax2.plot(history.history['val_accuracy'])
ax2.legend(['train', 'test'], loc='upper left')

plt.show()
```

Deep GRU Model Evaluation



```
[]: from sklearn.metrics import classification_report

y_pred = model.predict(X_test) # these predictions are probabilities (0-1)__

+taken from the sigmoid function

y_pred = (y_pred > 0.5) # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

12/12	1s 34ms/step			
	precision	recall	f1-score	support
0	0.8228	0.7784	0.8000	167
1	0.8246	0.8614	0.8426	202
accuracy			0.8238	369
macro avg	0.8237	0.8199	0.8213	369
weighted avg	0.8238	0.8238	0.8233	369

1.11 MODEL08 - LSTM with Conv1D

```
[]: n_steps = 36
n_inputs = 1

model = keras.models.Sequential([
    keras.layers.Conv1D(filters=10, kernel_size=3, strides=1, padding="valid", usinput_shape=[n_steps, n_inputs]),
    keras.layers.Conv1D(filters=20, kernel_size=3, strides=1, padding="valid"),
    keras.layers.LSTM(32, return_sequences=True),
    keras.layers.LSTM(32),
    keras.layers.Dense(1, activation='sigmoid')
])

model.summary()
```

/Users/timsmith/miniconda3/envs/dsp/lib/python3.11/site-packages/keras/src/layers/convolutional/base_conv.py:99: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` object as the first layer in the model instead.

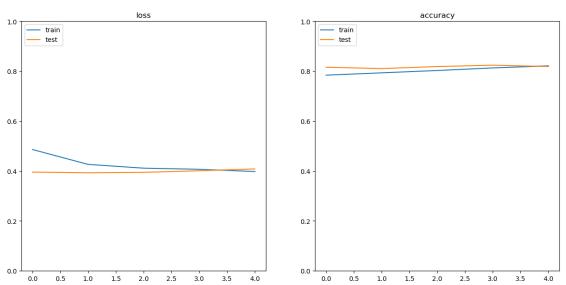
```
super().__init__(
Model: "sequential_7"
```

Layer (type)
Output Shape
Param #
conv1d (Conv1D)
(None, 34, 10)
40

```
conv1d_1 (Conv1D)
                                       (None, 32, 20)
                                                                           620
     lstm_4 (LSTM)
                                        (None, 32, 32)
                                                                         6,784
     lstm_5 (LSTM)
                                        (None, 32)
                                                                         8,320
     dense 8 (Dense)
                                        (None, 1)
                                                                            33
     Total params: 15,797 (61.71 KB)
     Trainable params: 15,797 (61.71 KB)
     Non-trainable params: 0 (0.00 B)
[]: model.compile(
         loss="binary_crossentropy",
         optimizer=keras.optimizers.Nadam(learning_rate=0.010),
         metrics=['accuracy']
     )
[]: import time
     start_time = time.time()
     early_stop = EarlyStopping(monitor='val_loss', min_delta = 0.0, patience=5, __
      →verbose=1, mode='min')
     history = model.fit(
        X_train,
         y_train,
         epochs=epoch_num,
         validation_data=(X_test, y_test),
         callbacks=[early_stop]
     )
     end_time = time.time()
    Epoch 1/5
                      8s 91ms/step -
    27/27
    accuracy: 0.7545 - loss: 0.5260 - val_accuracy: 0.8157 - val_loss: 0.3957
    Epoch 2/5
    27/27
                      1s 44ms/step -
    accuracy: 0.7831 - loss: 0.4275 - val_accuracy: 0.8103 - val_loss: 0.3928
    Epoch 3/5
    27/27
                      1s 40ms/step -
    accuracy: 0.7988 - loss: 0.4136 - val_accuracy: 0.8184 - val_loss: 0.3947
```

```
Epoch 4/5
    27/27
                      1s 40ms/step -
    accuracy: 0.8078 - loss: 0.4101 - val_accuracy: 0.8238 - val_loss: 0.4010
    Epoch 5/5
    27/27
                      1s 41ms/step -
    accuracy: 0.8257 - loss: 0.4012 - val_accuracy: 0.8184 - val_loss: 0.4084
[]: fig, (ax1, ax2) = plt.subplots(1, 2, figsize=(15, 7))
     fig.suptitle('Con1D Model Evaluation')
     ax1.set title('loss')
     ax1.set_ylim(0, 1)
     ax1.plot(history.history['loss'])
     ax1.plot(history.history['val_loss'])
     ax1.legend(['train', 'test'], loc='upper left')
     ax2.set_title('accuracy')
     ax2.set_ylim(0, 1)
     ax2.plot(history.history['accuracy'])
     ax2.plot(history.history['val_accuracy'])
     ax2.legend(['train', 'test'], loc='upper left')
     plt.show()
```

Con1D Model Evaluation



```
[]: from sklearn.metrics import classification_report
```

```
y_pred = model.predict(X_test) # these predictions are probabilities (0-1)

staken from the sigmoid function

y_pred = (y_pred > 0.5) # let's turn these into predictions (0 or 1)

print(classification_report(y_test, y_pred, digits=4))
```

```
12/12
                  1s 42ms/step
              precision
                            recall f1-score
                                                support
           0
                  0.8205
                            0.7665
                                       0.7926
                                                     167
                  0.8169
                            0.8614
                                       0.8386
                                                     202
           1
                                       0.8184
                                                     369
    accuracy
   macro avg
                  0.8187
                            0.8139
                                       0.8156
                                                     369
weighted avg
                            0.8184
                                       0.8177
                                                     369
                  0.8185
```

1.12 Summary of results

```
[]: df_results.sort_values(by=['accuracy', 'precision', 'recall', 'f1'], □

⇔ascending=False)
```

```
[]:
                  model
                              time accuracy precision
                                                          recall
                                                                       f1
    3
                   LSTM
                          5.880496 0.829268
                                              0.835749 0.856436
                                                                 0.845966
    6
               Deep GRU
                         10.679676 0.823848
                                              0.824645 0.861386
                                                                 0.842615
    5
                    GRU
                          5.929280 0.821138
                                              0.823810 0.856436 0.839806
    7
      Conv1D Deep LSTM
                         12.128046 0.818428
                                              0.816901 0.861386 0.838554
    4
              Deep LSTM
                         11.437630 0.818428
                                              0.802691 0.886139 0.842353
    2
               Deep RNN
                        367.517398 0.815718
                                              0.819048 0.851485
                                                                 0.834951
    1
                    RNN
                         72.692728 0.807588
                                              0.801843 0.861386 0.830549
    0
                          3.624414 0.794038
                                              0.850000 0.757426 0.801047
                    NN
```