Scipy.org (http://scipy.org/) Docs (http://docs.scipy.org/) SciPy v0.14.0 Reference Guide (../index.html)

Optimization and root finding (scipy.optimize) (../optimize.html)

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# scipy.optimize.fsolve¶

scipy.optimize.fsolve(func, x0, args=(), fprime=None, full\_output=0, col\_deriv=0, xtol=1.49012e-08, maxfev=0, band=None, epsfcn=None, factor=100, diag=None) [source] (http://github.com/scipy/scipy/blob/v0.14.0/scipy/optimize/minpack.py#L41)

Find the roots of a function.

Return the roots of the (non-linear) equations defined by func(x) = 0 given a starting estimate.

**Parameters:** func : callable f(x, \*args)

A function that takes at least one (possibly vector) argument.

x0 : ndarray

The starting estimate for the roots of func(x) = 0.

args: tuple, optional

Any extra arguments to func.

fprime: callable(x), optional

A function to compute the Jacobian of *func* with derivatives across the rows. By default, the Jacobian will be estimated.

full\_output : bool, optional

If True, return optional outputs.

col\_deriv : bool, optional

Specify whether the Jacobian function computes derivatives down the columns (faster, because there is no transpose operation).

xtol: float

The calculation will terminate if the relative error between two consecutive iterates is at most *xtol*.

maxfev: int, optional

The maximum number of calls to the function. If zero, then 100\*(N+1) is the maximum where N is the number of elements in x0.

band : tuple, optional

If set to a two-sequence containing the number of sub- and super-diagonals within the band of the Jacobi matrix, the Jacobi matrix is considered banded (only for fprime=None).

epsfcn: float, optional

A suitable step length for the forward-difference approximation of the Jacobian (for fprime=None). If *epsfcn* is less than the machine precision, it is assumed that the relative errors in the functions are of the order of the machine precision.

factor : float, optional

A parameter determining the initial step bound (factor  $* \mid \mid$  diag  $* x \mid \mid$ ). Should be in the interval (0.1, 100).

diag: sequence, optional

N positive entries that serve as a scale factors for the variables.

#### Returns:

x : ndarray

The solution (or the result of the last iteration for an unsuccessful call).

infodict : dict

A dictionary of optional outputs with the keys:

nfev

number of function calls

njev

number of Jacobian calls

fvec

function evaluated at the output

fjac

the orthogonal matrix, q, produced by the QR factorization of the final approximate Jacobian matrix, stored column wise

r

upper triangular matrix produced by QR factorization of the same matrix

qtf

the vector (transpose(q) \* fvec)

ier: int

An integer flag. Set to 1 if a solution was found, otherwise refer to *mesg* for more information.

mesg: str

If no solution is found, mesg details the cause of failure.

#### See also:

root (scipy.optimize.root.html#scipy.optimize.root) Interface to root finding algorithms for multivariate

functions.

#### **Notes**

fsolve is a wrapper around MINPACK's hybrd and hybrj algorithms.

### Previous topic

scipy.optimize.root (scipy.optimize.root.html)

## Next topic

scipy.optimize.broyden1 (scipy.optimize.broyden1.html)