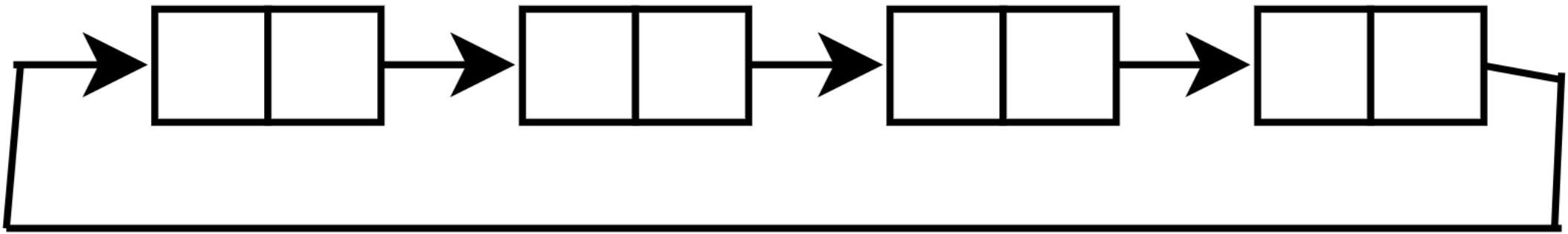


Announcements

- We should be getting UGTAs soon! In the meantime, we'll be hosting a few office hours this week (so far, 1pm-2pm Wednesday and 2pm-3pm this Thursday, hopefully I'll have more to announce soon)
- Homework 1 is now assigned. It can be found on the course website. It'll be due next Tuesday at 3:30pm (submit via Gradescope).
- After consulting with other faculty, I've decided to post my slides after class, not before

Topic 1: Review

What is this?



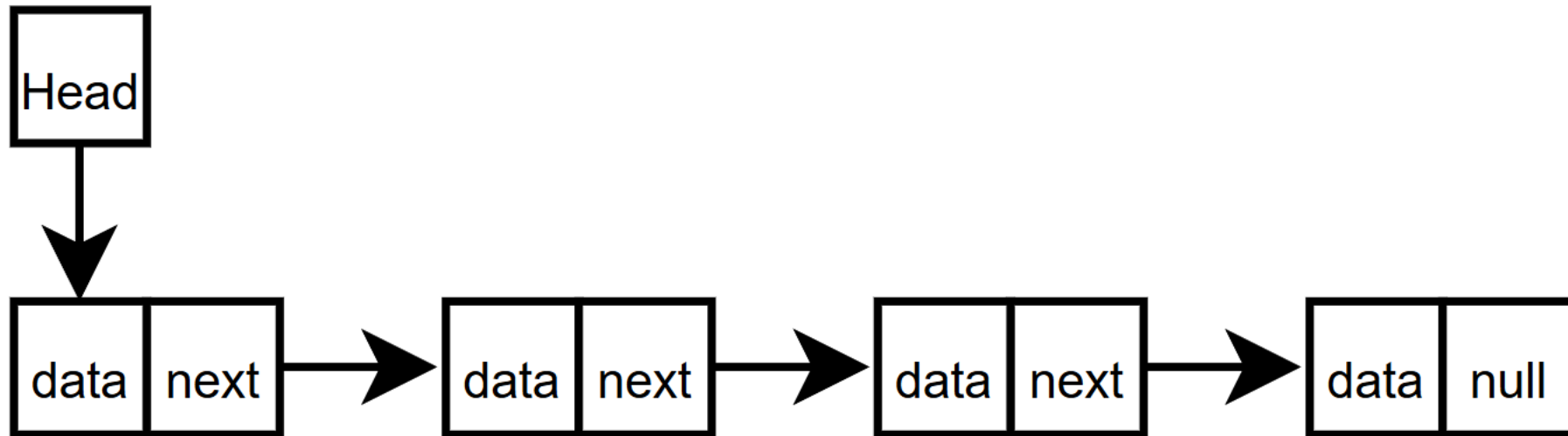
- A circular linked list! ...But something's missing...
- We need to be able to access the list. Hence, we need a “head” pointer

Data Structures

- We can use linked lists to make basic data structures, like a queue or a stack
- A **Queue** takes data in on one end, and outputs the oldest data on the other end (like waiting in a line)
- A **Stack** take in data on one end, and output the most recent data on the same end (like a pile of books or plates)
- An acronym that describes these behaviors is FIFO (first-in, first out) for queues, and LIFO (last-in, first out) for stacks

Back to Linked Lists

- There are lots of different types of linked lists. First, there's the **singly-linked list**



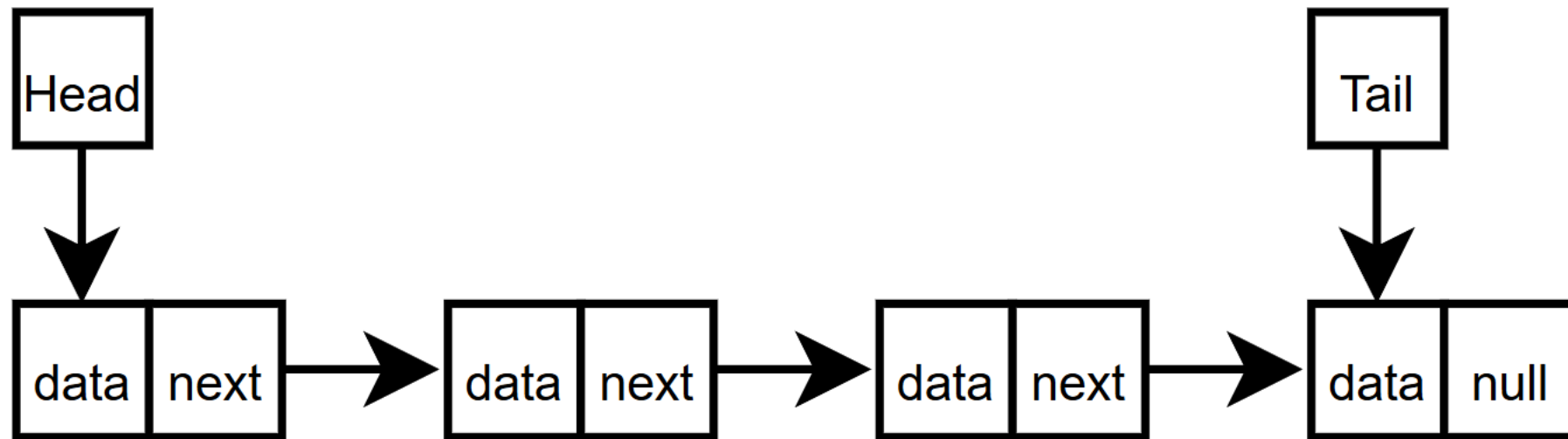
- Remember python's list data structure? The underlying data structure is not actually a linked list at all, it's an array!

Back to Linked Lists

- So we have Singly-Linked Lists... What can we do with them? What are some common operations?
 - Insert
 - Delete
 - Traverse, maybe searching for a value, or find the length/size of the list
 - Sort
 - isEmpty
 - toString
 - Create
 - Destroy

Linked Lists: Tail References

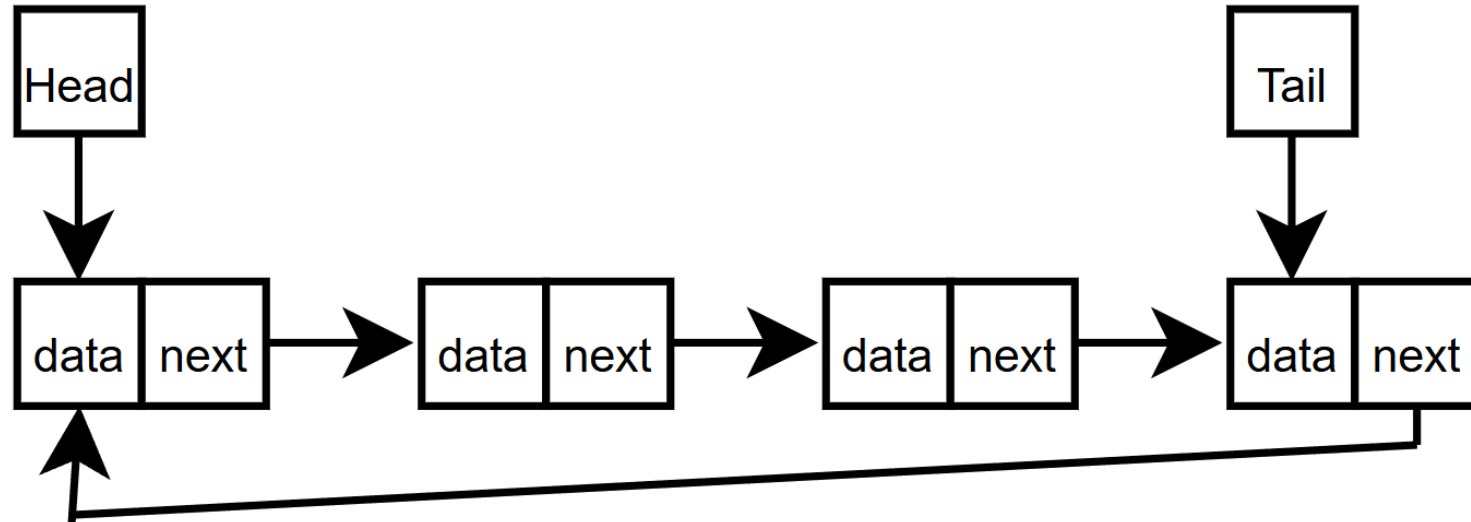
- We have the head pointer. Do we need (or want) a tail pointer? Is it worth the trouble?



- Pros: Makes appending to the end of the list easy! Great for queues!
- Cons: Anything that requires modifying or deleting the end of the list becomes a hassle. Also there's the memory cost for an extra pointer

Circular Linked Lists

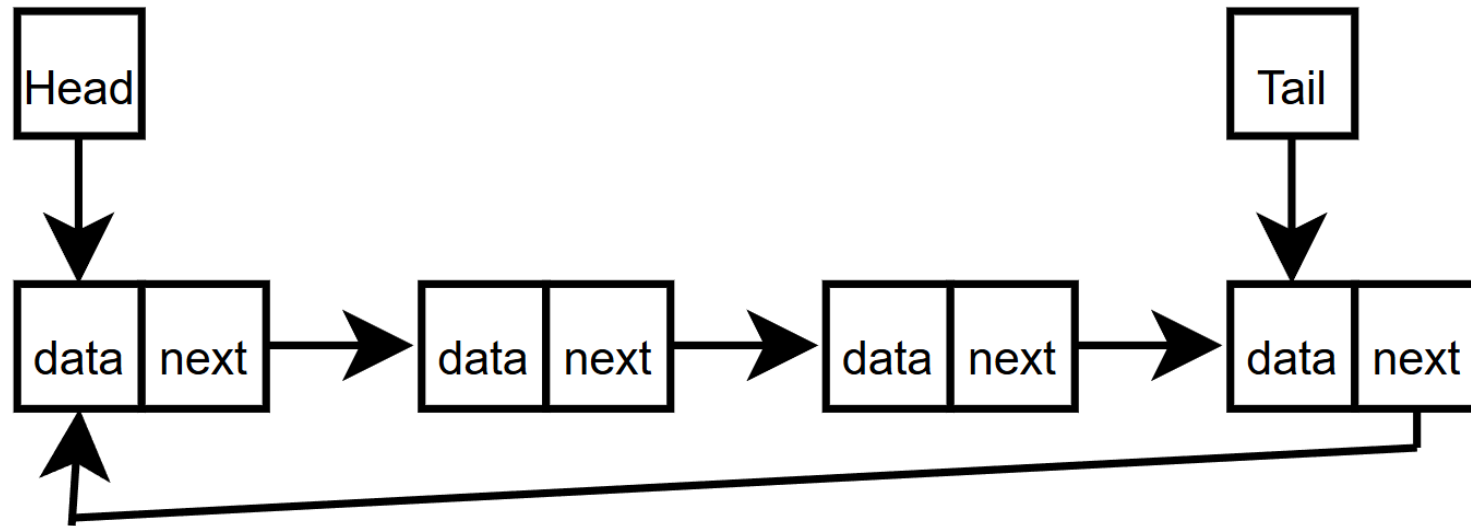
- The idea is to allow easy travel from the last node to the first



- Question: Do we even need the head pointer anymore?
 - Answer: Probably not! It only costs one extra dereference operation to get to the head from the tail pointer!

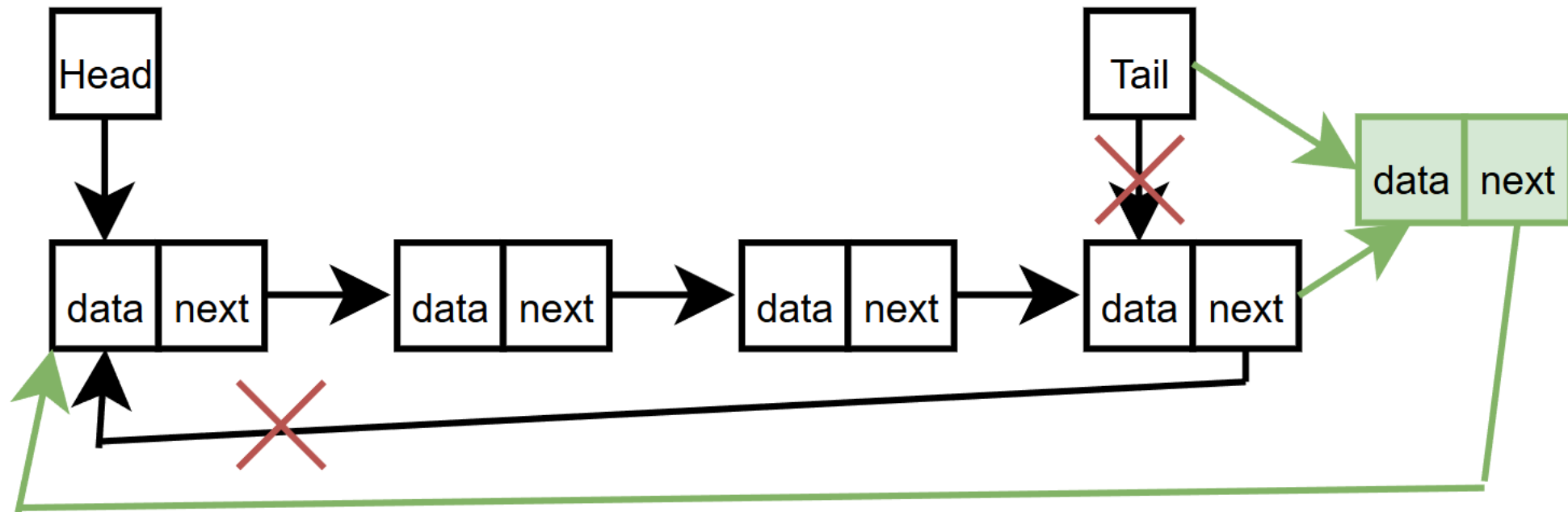
Circular Linked Lists: Operations

- Take a look at this Circular Linked-List. How would we append to it? How many operations would it take?



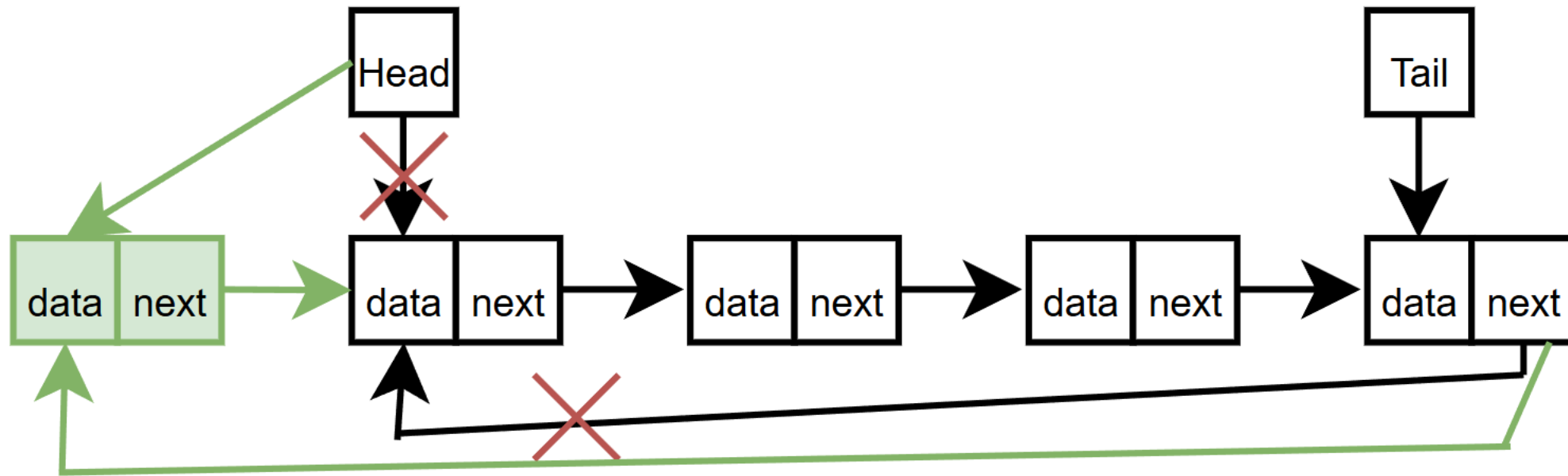
Circular Linked Lists: Operations

- Step 1: set the new node's next pointer to the front node
- Step 2: set the last node's next point to the new node
- Step 3: set the tail pointer to the new node



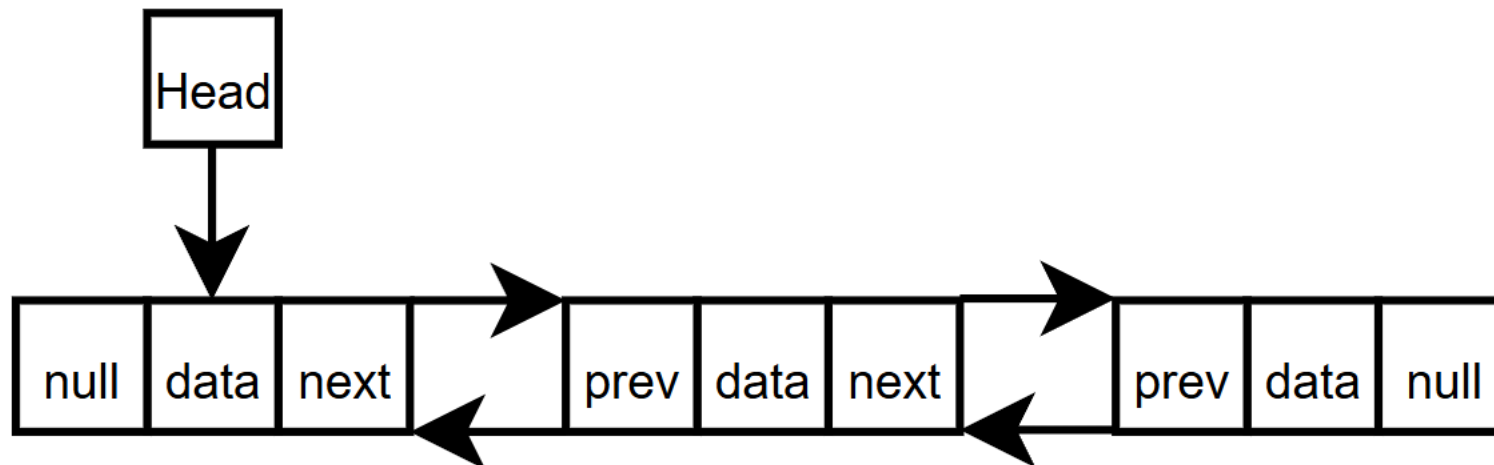
Circular Linked Lists: Operations

- What about prepending to the list? What would the steps be for that?
- Step 1: Set the new node's next pointer to the front node
- Step 2: Set the end node's next pointer to the new node
- Step 3: Set the head pointer to the new node



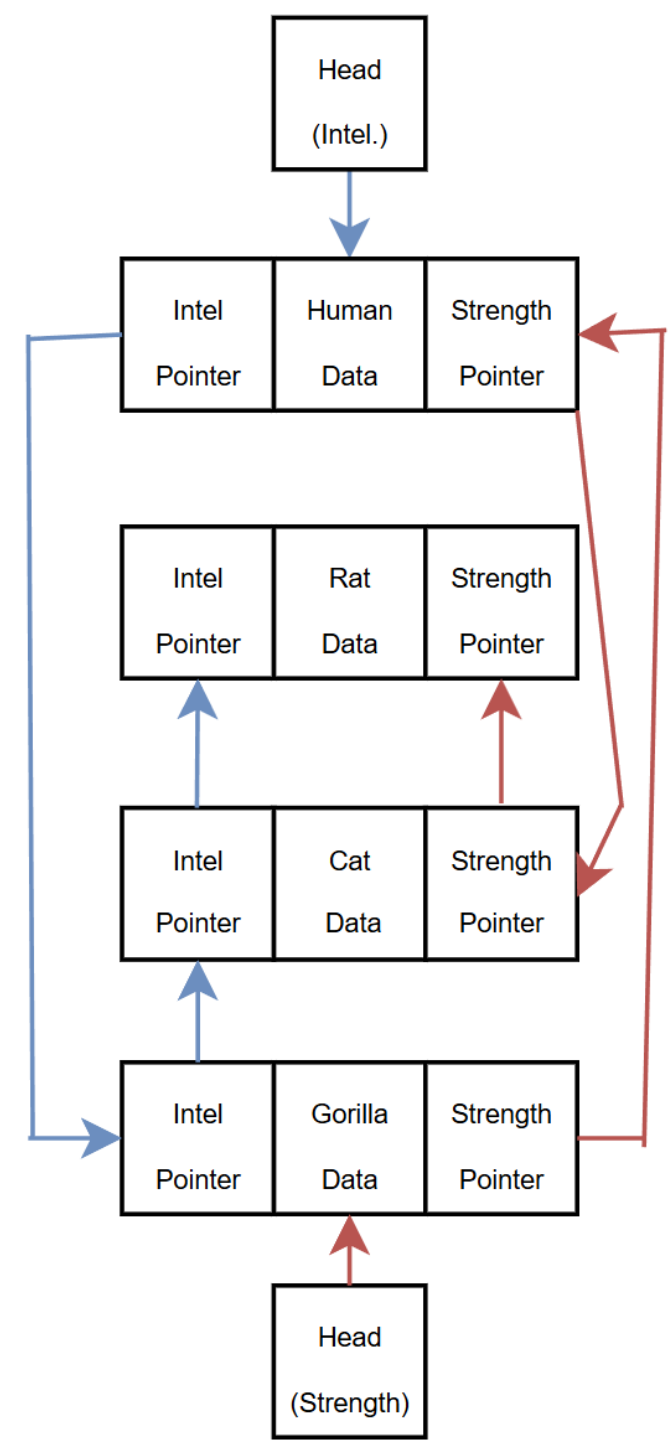
Doubly Linked Lists

- Another type of Linked Lists are **Doubly Linked Lists**. These have an extra pointer pointing to the previous node, allowing for two-way travel along the list
- Cons: memory costs, and operational costs (have to maintain both prev and next pointers for all operations)



Multilists

- A **Multilist** has multiple pointers to other nodes, representing alternate orderings for traversals
- For example, look at this figure, where animals are ranked by strength with one list, and by intelligence with another list
- Multilists can have more than two pointers, depending on how many linked lists you want the node data to be a part of
- Doubly Linked Lists can be considered a special type of multilist!

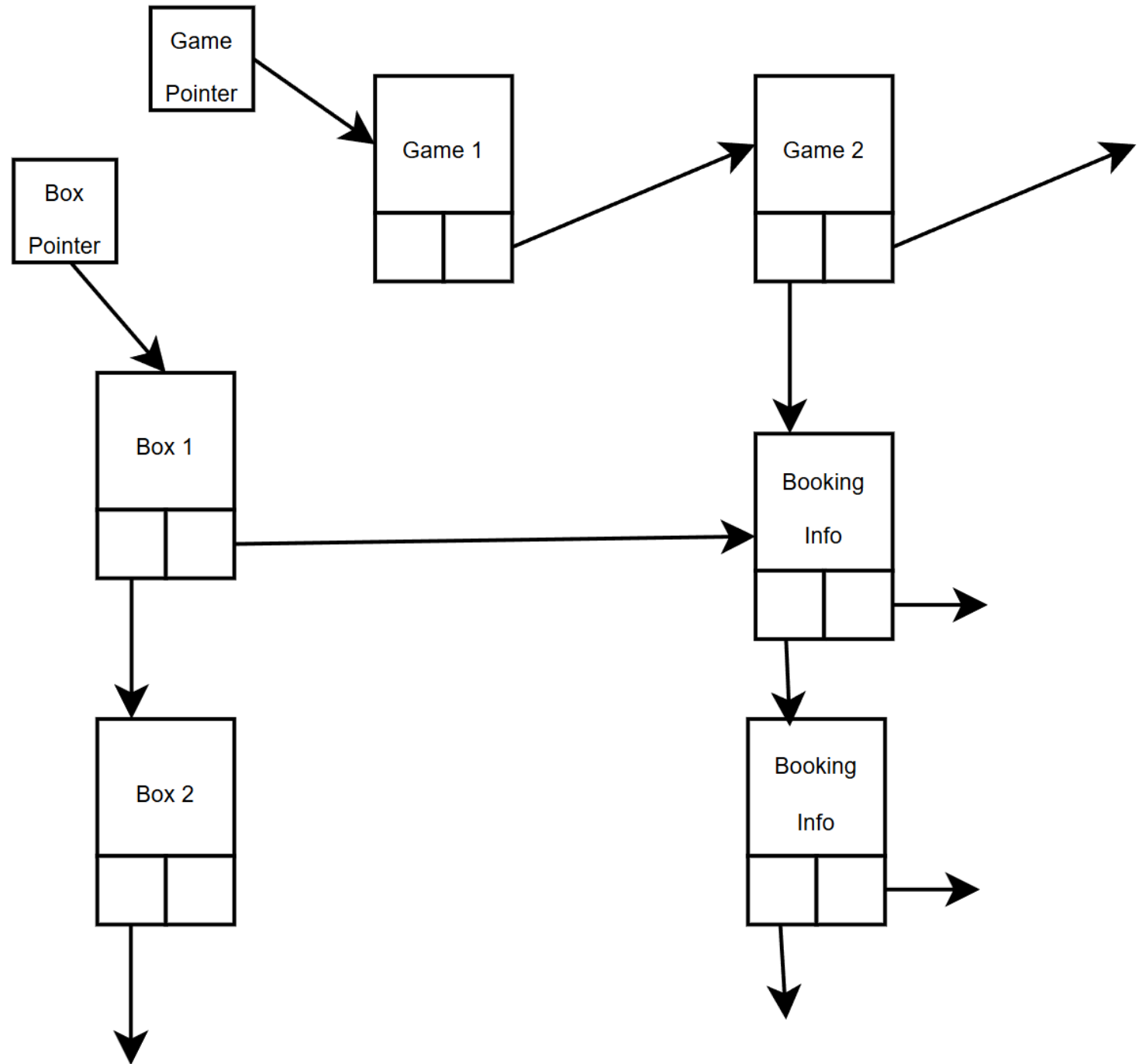


Orthogonal Lists

- An **Orthogonal List** is a group of nodes which have multiple pointers to go to its nearest neighbors node in each dimension (usually up, down, right, and left)
- This allows for efficient representation of sparse matrices (matrices that are mostly empty) or data where traveling by 'dimension' is useful.
- For example, consider software that books tickets for a football stadium by Box. People might want to buy tickets for a game, or for a season.

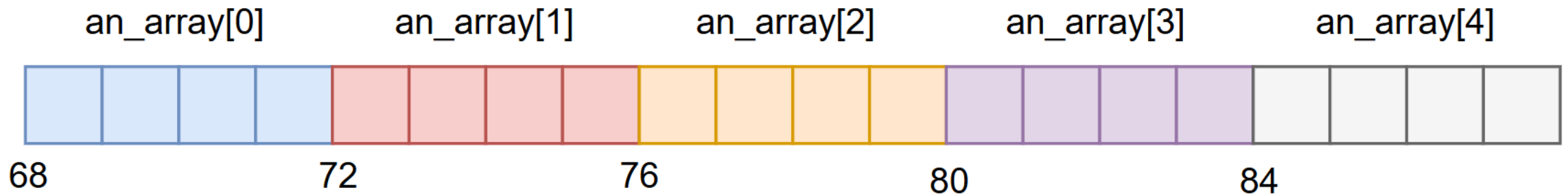
Orthogonal Lists

- How many pointers for each data object would we need if we wanted to be able to travel back/forth and up/down?
- What if we wanted to add a third list, for 3 dimensions? How many pointers would we need to travel in any direction for each data object?



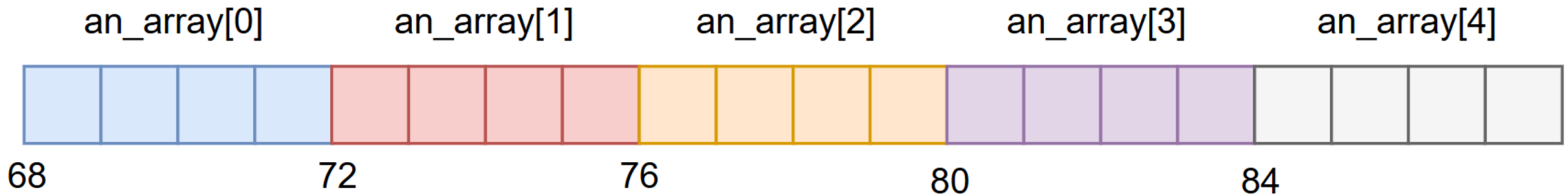
1D Array Storage

- Unlike linked lists, array elements are stored next to each other (*contiguously*) in storage.
- For example, `int[] an_array = new int[5];` might look something like this:



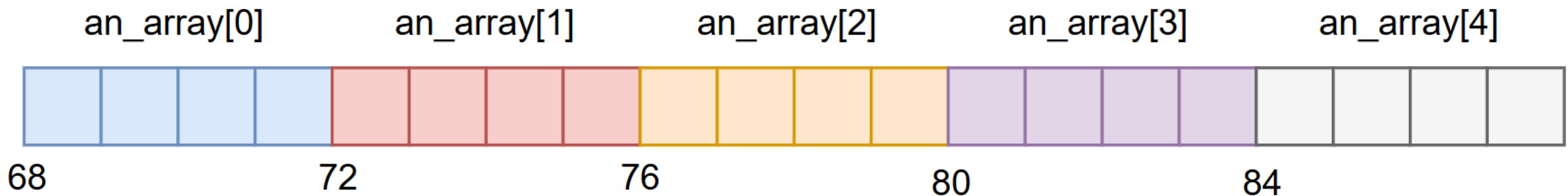
1D Array Storage

- How can we calculate the address for an arbitrary index in an array? We need to know three things:
 1. Base Address of the array (68 for array below)
 2. Element Size, esize for short. Since an int is 4 bytes, esize would be 4 for the array below
 3. Index of the array that we're interested in. Suppose `an_array[3]`. What would the calculation for finding it be?



1D Array Storage

- In general, for 1-D arrays, the formula for finding an element is: $\text{base_address} + \text{esize} * \text{index}$
- Another way of thinking about it is: where do we start, how many jumps to the element we want, and how large does each jump have to be?
- Two final notes:
 - This is a pretty efficient operation!
 - The size of the array doesn't matter for the operation!



2D Array Storage

- First off, what does a 2D array look like in Java?
 - `int twod_array[][] = new int [3][4];`
 - `int twod_array[][] = {{6, 0, 8, 2}, {1, 5, 3, 6}, {9, 4, 7, 1}};`
- Which is the row, which is the column for this example?
 - [3] is the rows, [4] is the columns. We're listing the data row-by-row, **not** column-by-column

2D Array Storage

- So, how do we store a 2D structure in 1D memory? Two options:
- Row-Major Order (RMO): C, C++, Pascal
- Column-Major Order (CMO): Fortran, R, MATLAB
- What about Object-Oriented languages? We'll discuss them in a bit.

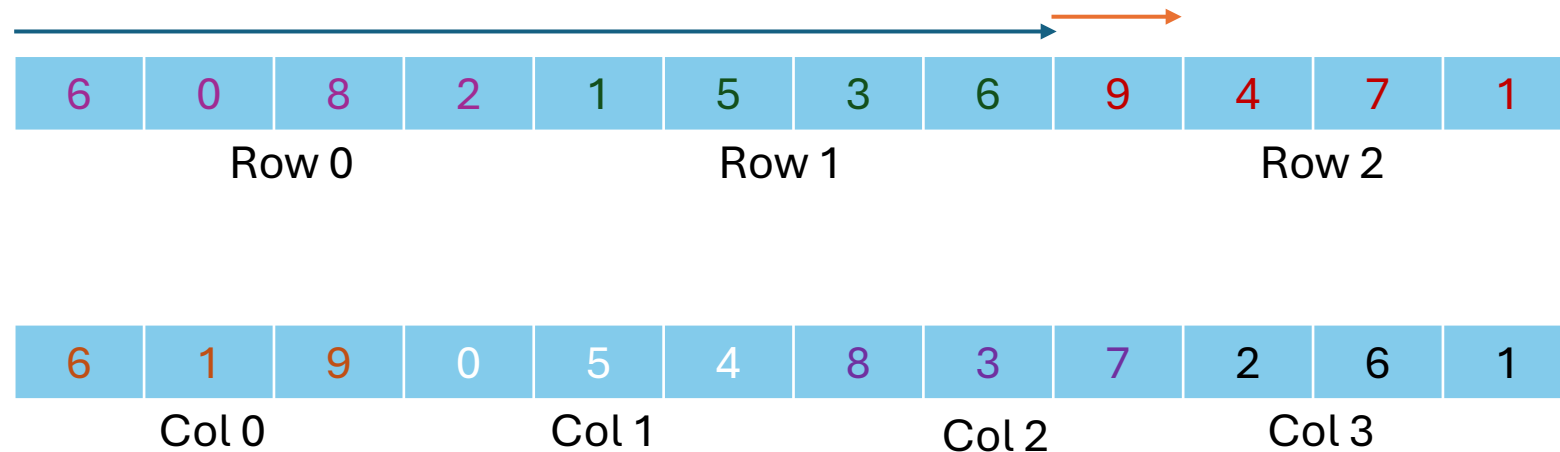
	0	1	2	3
0	6	0	8	2
1	1	5	3	6
2	9	4	7	1

6	0	8	2	1	5	3	6	9	4	7	1
Row 0				Row 1				Row 2			
6	1	9	0	5	4	8	3	7	2	6	1
Col 0			Col 1			Col 2			Col 3		

2D Array Storage

- So we have our ways of storing the data in 1D... But how will this change our address calculation? Suppose we wanted to find `twod_array[2][1]`. First, what is the number in that spot?
 - 4! Row 2, Column 1. Now, how would we have gotten there, with RMD?
- RMD, we had to jump over the first 2 rows entirely! Then we skipped over 1 element for the columns...

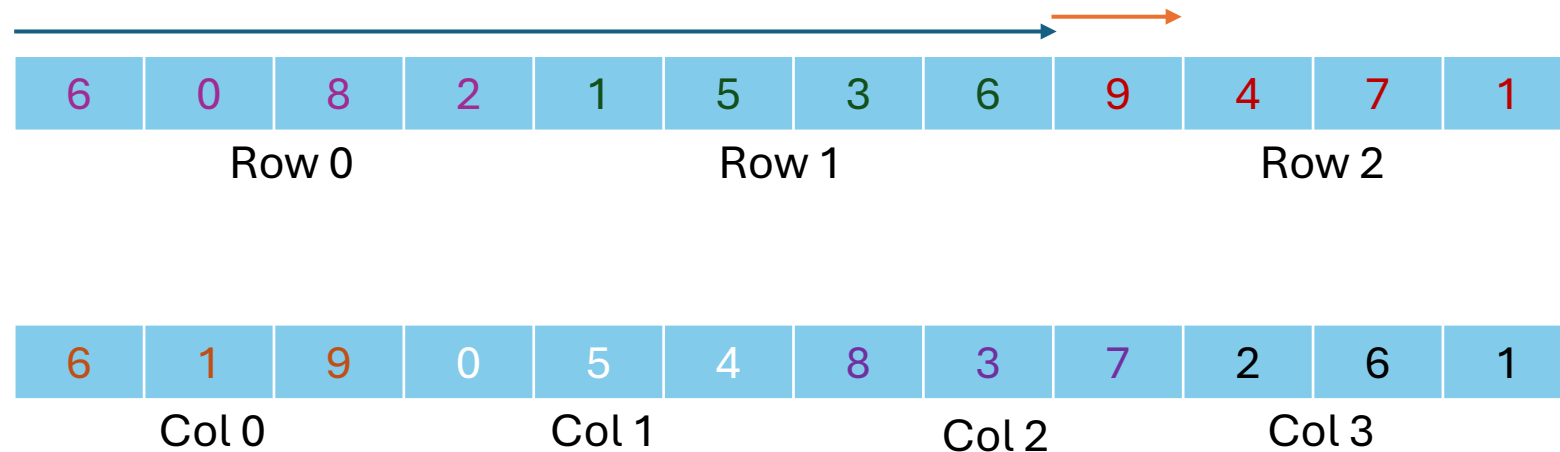
	0	1	2	3
0	6	0	8	2
1	1	5	3	6
2	9	4	7	1



2D Array Storage

- Our 1D array address calculation required three variables ($\text{base_address} + \text{esize} * \text{index}$). What additional variables do we need for a 2D calculation?
- We need... row *and* column indices. Plus the number of columns (**NUMCOLS**) per row (how else would we know the size of our jumps to skip over the rows?)

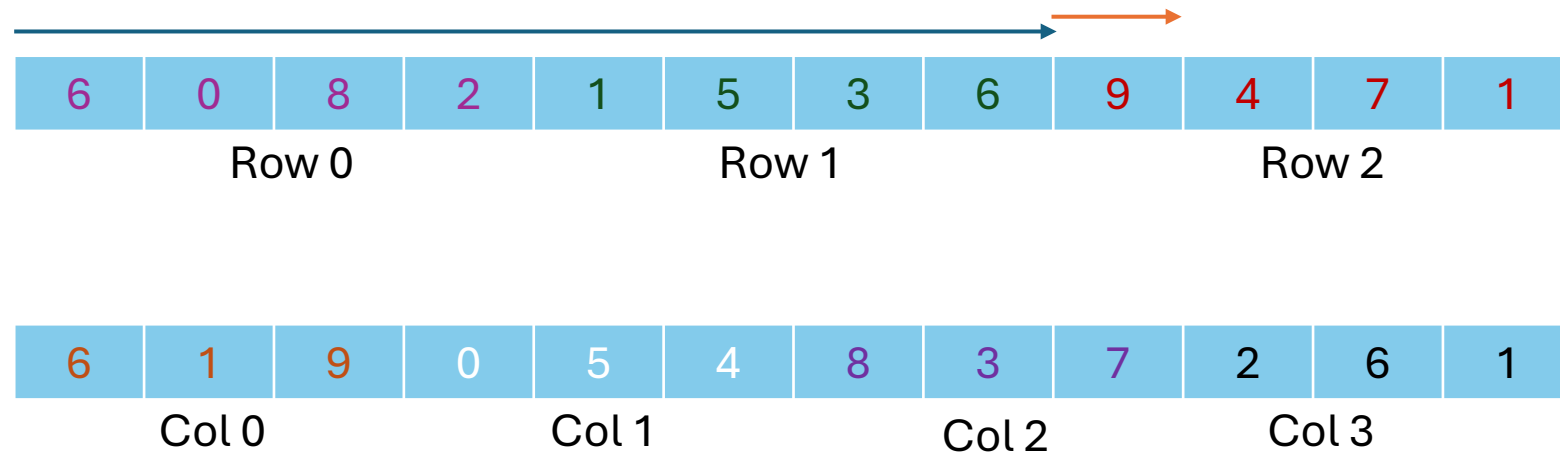
	0	1	2	3
0	6	0	8	2
1	1	5	3	6
2	9	4	7	1



2D Array Storage

- So, our equation for 2D calculations, for RMO, is:
- $\text{address} = \text{base} + \text{NUMCOLS} * \text{row_index} * \text{esize} + \text{col_index} * \text{esize}$
- Can refactor the esize for: $\text{base} + \text{esize} * (\text{row_index} * \text{NUMCOLS} + \text{col_index})$
- This is 2 additions and 2 multiplications... still pretty efficient!

	0	1	2	3
0	6	0	8	2
1	1	5	3	6
2	9	4	7	1



2D Array Storage

- Time to work a problem! Assume RMO. Given a 2D array (two_d) with 3 rows, 4 columns, a base address of 156, and an esize of 8 bytes, what is the address of two_d[2][1]?
- $\text{base} + \text{esize} * (\text{row_index} * \text{NUMCOLS} + \text{col_index})$
- $156 + 8 * (2 * 4 + 1) = 228!$

	0	1	2	3
0	6	0	8	2
1	1	5	3	6
2	9	4	7	1

