

ERRATA TO STABLY ERGODIC SKEW PRODUCTS

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The statement of the lemma should be amended to

Lemma. Let f be a measure preserving, Anosov diffeomorphism of \mathbb{T}^n and f_\sharp be the induced map on the fundamental group of \mathbb{T}^n . Let φ be in $H^1(\mathbb{T}^n, \mathbb{S}^1)$. If f_φ is not ergodic then $\varphi^{\det(I-f_\sharp)}$ is cohomologous to a constant function, $\exp(2\pi i \frac{k}{r})$, for some $k, r \in \mathbb{Z}$.

Proof. The proof is the same down to following the line. We take the maps φ and h_r induce on the fundamental groups and get the equation

$$r\varphi_\sharp = (h_r)_\sharp - (h_r)_\sharp f_\sharp = (h_r)_\sharp (I - f_\sharp).$$

Since f is Anosov $(I - f_\sharp)$ is invertible over \mathbb{Q} and $\det(I - f_\sharp)(I - f_\sharp)^{-1}$ is an integer matrix. It follows that there is a map g_\sharp on the fundamental group with

$$rg_\sharp = \det(I - f_\sharp)(h_r)_\sharp.$$

By standard covering space arguments we can conclude there is a g in $H^1(\mathbb{T}^n, \mathbb{S}^1)$ with $(g)^r = (h_r)^{\det(I-f_\sharp)}$.

The rest of the proof follows as before. \square

The proof of the theorem also follows as before.

Thanks to Amy Wilkinson for pointing out the mistake.

We take this opportunity to add a reference to a paper which should have been included in our original paper.

REFERENCES

- [B] Brin M.I., *Topological Transitivity of One Class of Dynamic Systems and Flows of Frames on Manifolds of Negative Curvature*, Funktsional'nyi Analiz i Ego Prilozheniya 9 (1975); English transl. in Functional Analysis and Its Applications 9 (1975), 8-16.