Machine Learning using Python

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Agenda

1. **Machine Learning Engineering - Introduction**
2. **Python Fundamentals – Hands On**
3. **Decision Tree Learning**
4. **Machine Learning Lab Problems and Programs**

Machine Learning Engineering

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Contents

1. What is Machine Learning ?

- Study of algorithms that
  - Improve their performance **P**
  - At some task **T**
  - With Experience **E**
- Well-defined learning task<P,T,E>

Machine learning (ML) — a subset of artificial intelligence (AI) — is more than a technique for analyzing data. It's a system that is fueled by data, with the ability to learn and improve by using algorithms that provide new insights without being explicitly programmed to do so.

Figure 1. Learning From Data Without Being Explicitly Programmed

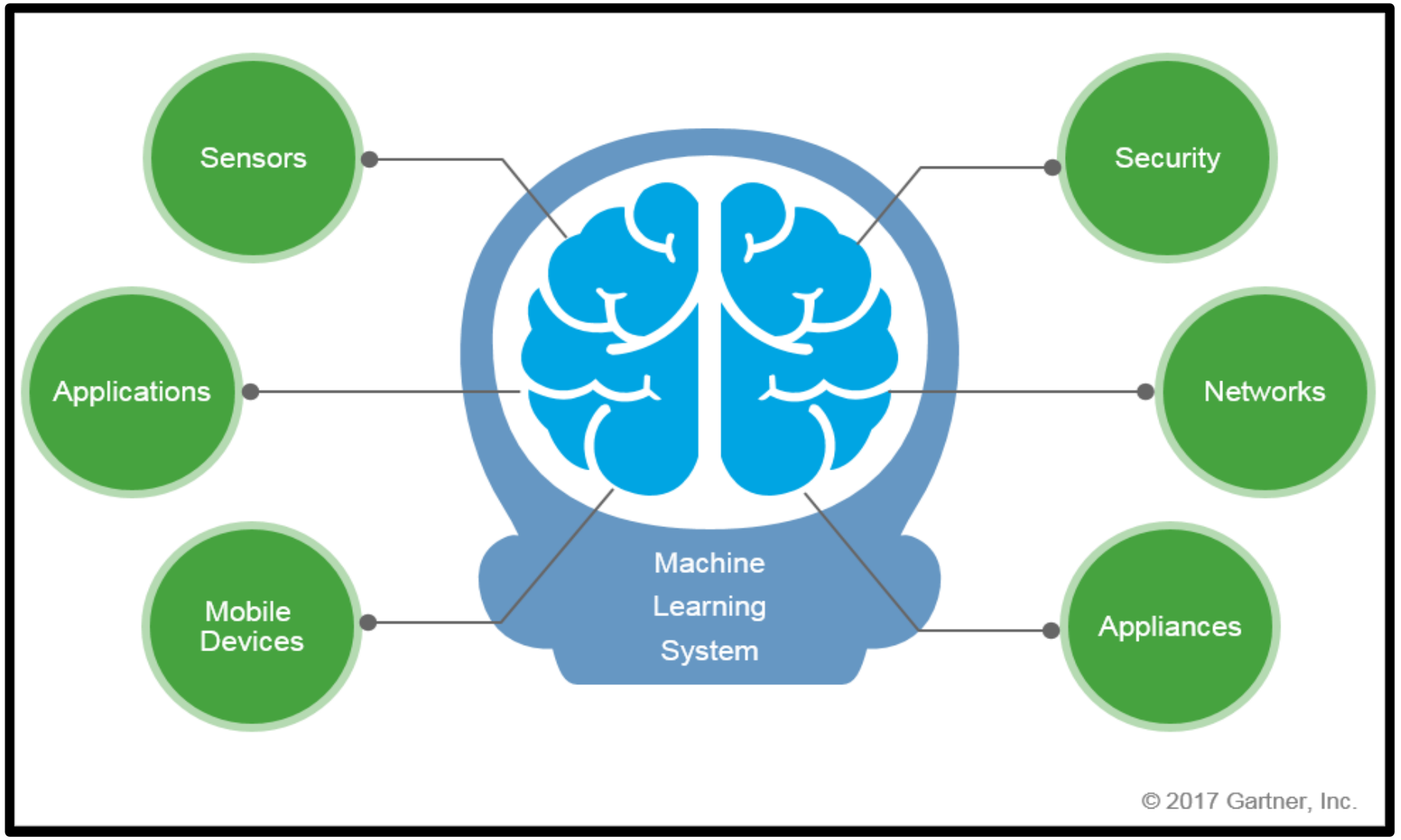


Figure 2. The Basics of Machine Learning Technology

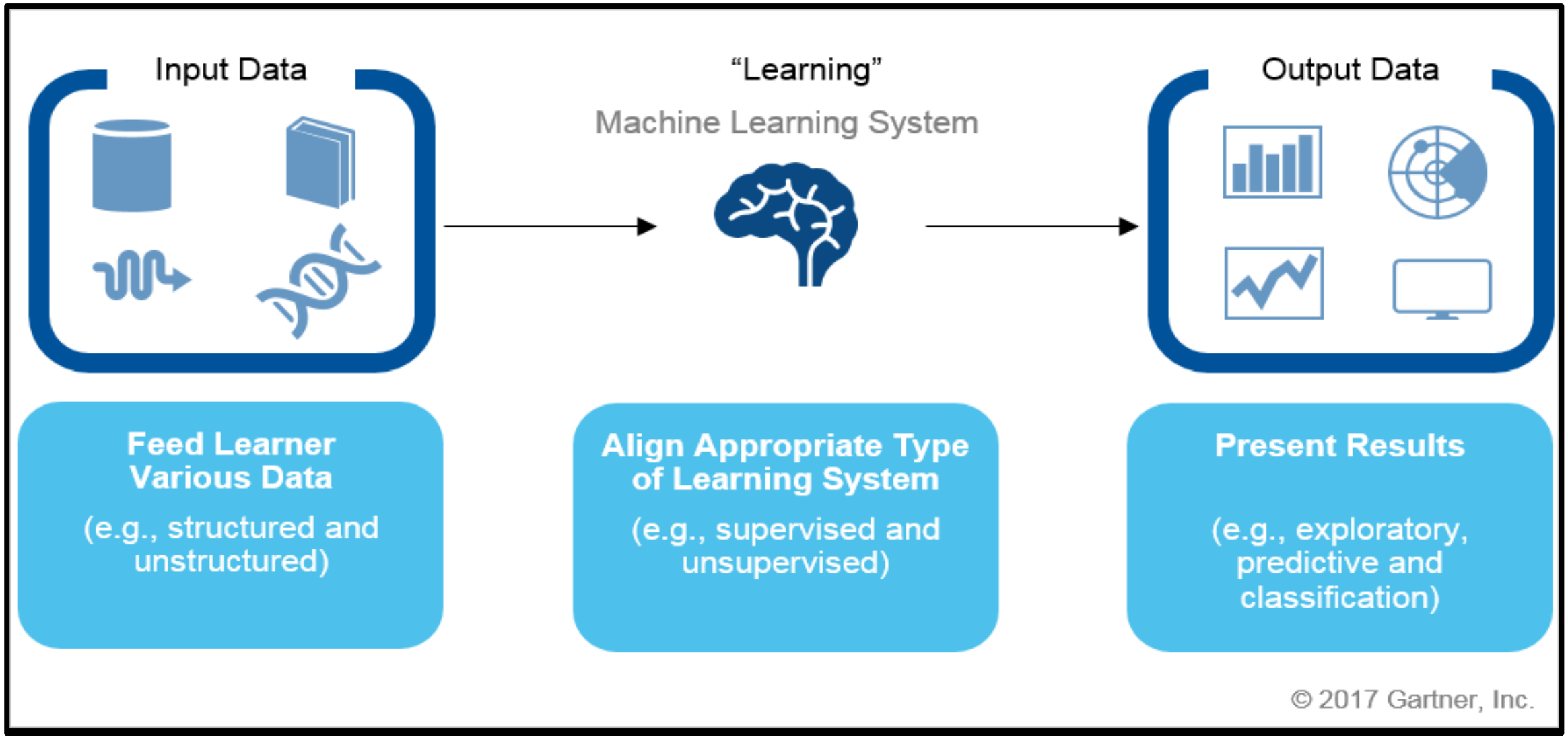
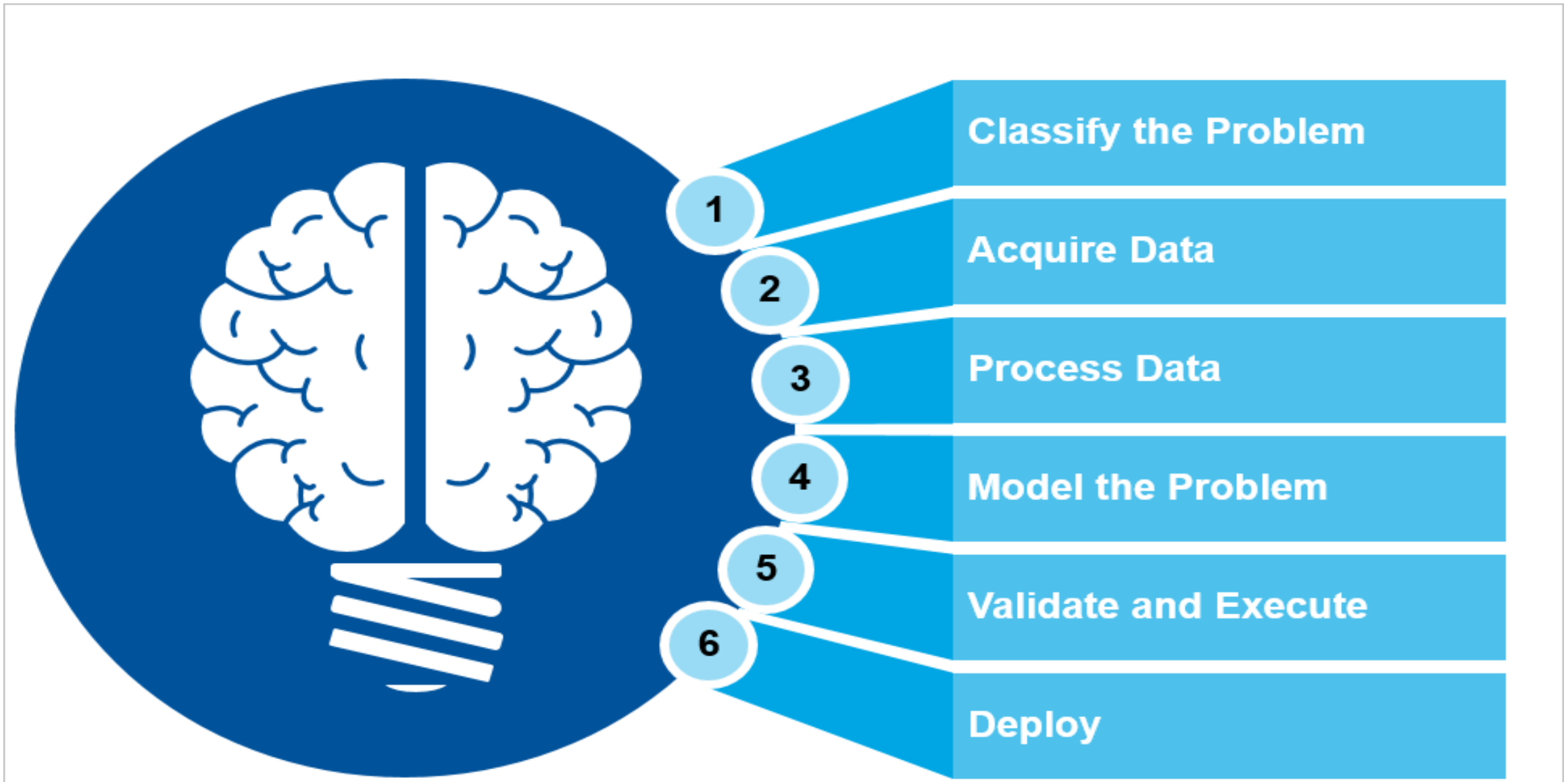


Figure 3. Stages of the Machine Learning Process



2. Machine Learning Engineer

- Machine learning engineers are sophisticated programmers who ***develop machines and systems that can learn and apply knowledge*** without specific direction.
- The algorithms they create allow a machine to find patterns in its own programming data, teaching it to understand commands and even think for itself.

Example : An example of a system a machine learning engineer would work on is a ***self-driving car and*** *automatic vacuum cleaner****.***

3. Skills required for MLE

1. **Math Skills**
2. **Programming Skills**
3. **Data Engineering Skills**
4. **Knowledge of Machine Learning Algorithms**
5. **Knowledge of Machine Learning Frameworks**
6. **Knowledge of IoT and Cloud Computing**
7. **Excellent Communication Skills**

3.1. Math Skills

- **Probability and Statistics** : Descriptive Statistics , Bayes Rule and Random Variables , Probability Distributions , Sampling Hypothesis , Testing Regression and Decision Analysis.

- **Linear Algebra :** Matrices , Vector Spaces

- **Calculus :** Basics of Differential and Integral calculus

3.2. Programming Skills

- Coding Skills , Algorithms , Data Structure and OOPS Concepts
- Languages like Python , R , Java and C (Master of any one or two)

3.3. Data Engineering Skills

- Ability to work with large amount of Data , Data Preprocessing , Knowledge of SQL an No SQL .
- ETL (Extract , Transform and Load) Operations
- Data Analysis and Visualization Skills

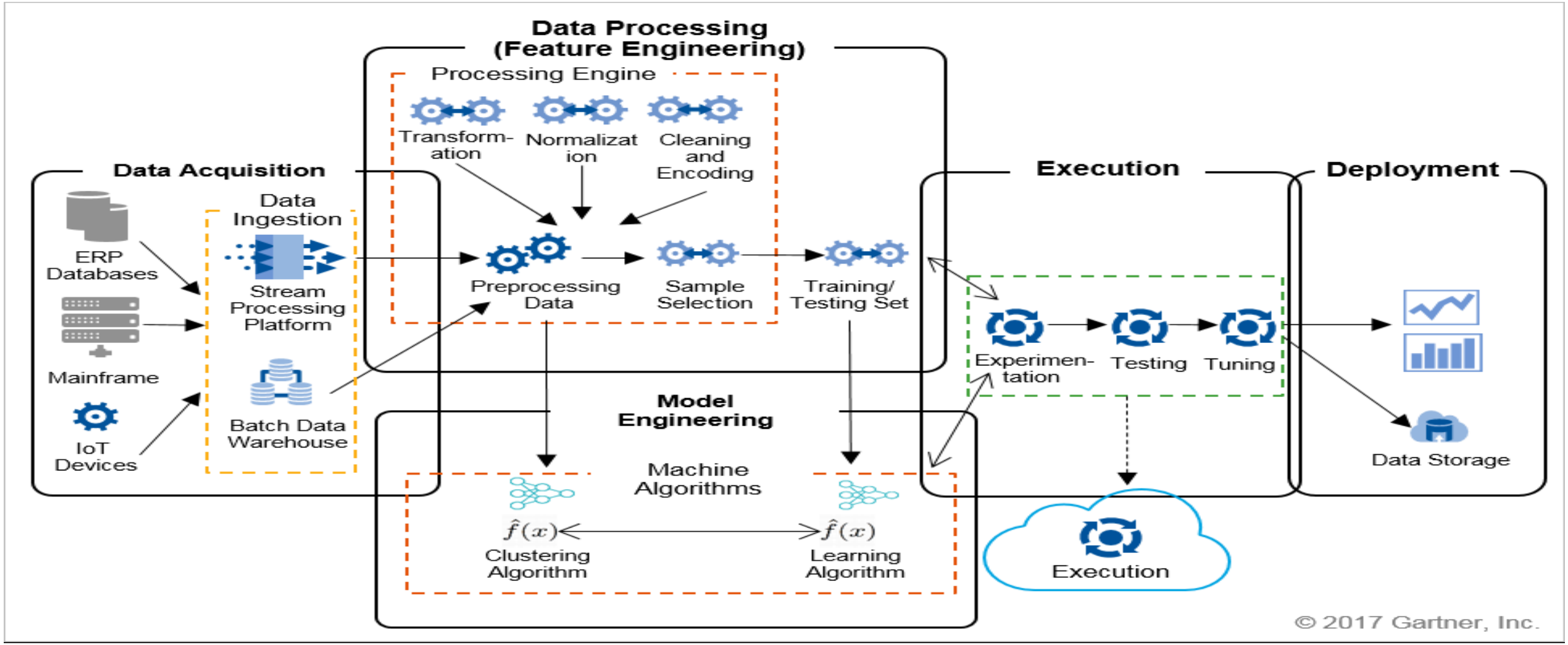
3.4. Knowledge of Machine Learning Algorithms

- Shallow and Deep Learning
- Supervised
- Unsupervised
- Semi Supervised
- Reinforcement

3.5. Knowledge of Machine Learning Frameworks

- Familiar with popular machine learning Frameworks such as
  - SCIKIT Learn,
  - TensorFlow ,
  - Azure ,
  - Caffe ,
  - Theano,
  - Spark and
  - Torch

4.Machine Learning Architecture



Terms Frequently Used

- **Labeled data**: Data consisting of a set of *training examples,* where each example is a *pair* consisting of an input and a desired output value (also called the *supervisory signal, labels, etc*)
- **Classification:** The goal is to predict discrete values, e.g. {1,0}, {True, False}, {spam, not spam}.
- **Regression:** The goal is to predict continuous values, e.g. home prices.

5. Types of Machine Learning Algorithms

1. Based on Depth of Learning
2. Based on Type of learning

5.1 Based on Depth of Learning

1. Shallow Learning
   - Algorithms with Few Layers
   - Better for Less Complex and Smaller Data sets
   - **Eg: Logistic Regression and Support vector Machines**
2. Deep Learning
   - New technique that uses many layers of neural network (a model based on the structure of human brain)
   - Useful when the target function is very complex and data sets are very large.

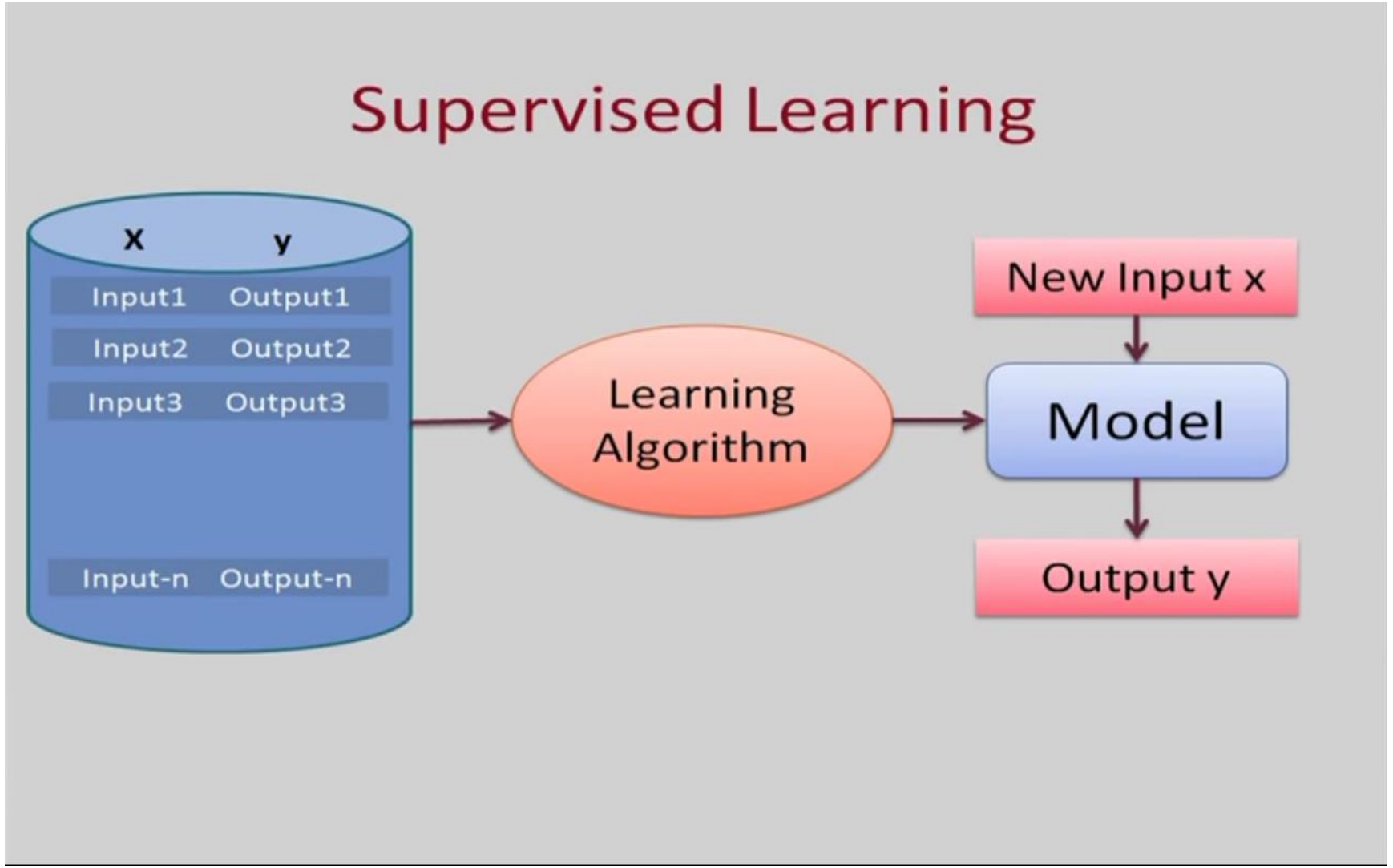
5.2 Based on Type of Learning

1. **Supervised Learning**
   - X and Y
   - Given an observation X what is the best label for Y
2. **Unsupervised Learning**
   - X
   - Given a set of X cluster or summarize them
3. **Semi Supervised Learning**
4. **Reinforcement Learning**
   - Determine what to do based on Rewards and punishments

5.2.1. Supervised Learning

- Here the training (labeled) data set containing ***input/predictors and output*** will be fed to the machine. The machine with the help of algorithm analyze the data set and ***generates a suitable model /function*** that best describes the input data. i.e it generates a function ***f(X) which makes best estimation of the output X for given X.***

- The generated model / function can be used to predict the output values for new data based on those relationships which it learned from the previous data sets.
  - When Y is discrete (True /False, ..) – **Classification**
  - When X is continuous (Real Numbers)- **Regression**


Supervised Learning
X
y
Input1
Output1
Input2
Output2
Input3
Output3
Input-n
Output-n
Learning Algorithm
New Input x
Model
Output y

Types of Supervised Learning

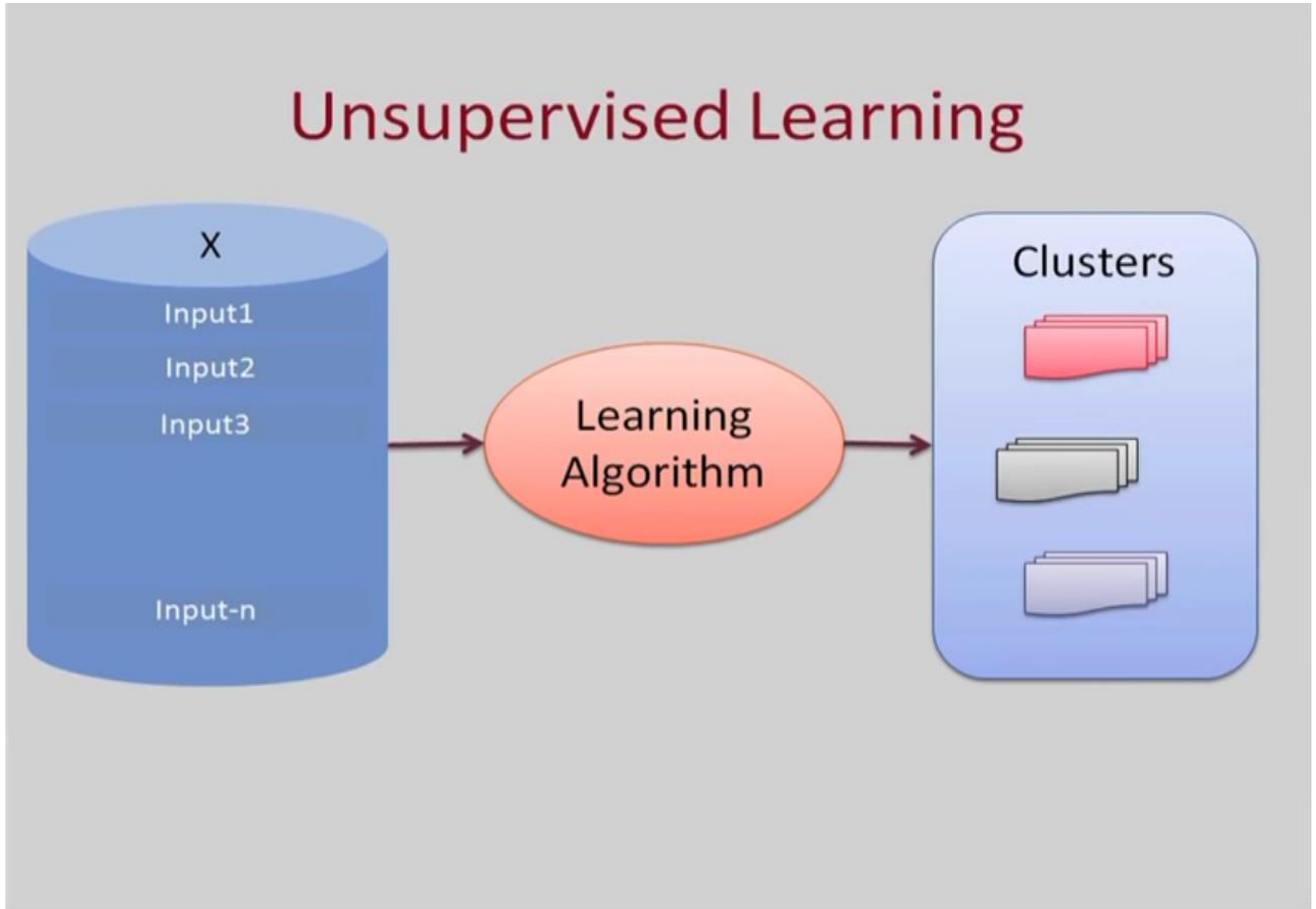
(Task Driven . Develop Prediction Model based on Input and Output Data)

1. **Classification (Discrete)**
   a) Logistic Regression
   b) KNN
   c) Decision Trees
   d) Support Vector Machines
   e) Naïve Bayesian
   f) Discriminant Analysis
   g) Random Forest
   h) AdaBoost
   i) Neural Networks

2. **Regression (Continuous)**
   a) Linear Regression
   b) SVR
   c) GPR
   d) Ensemble Methods

5.2.2: Unsupervised Learning

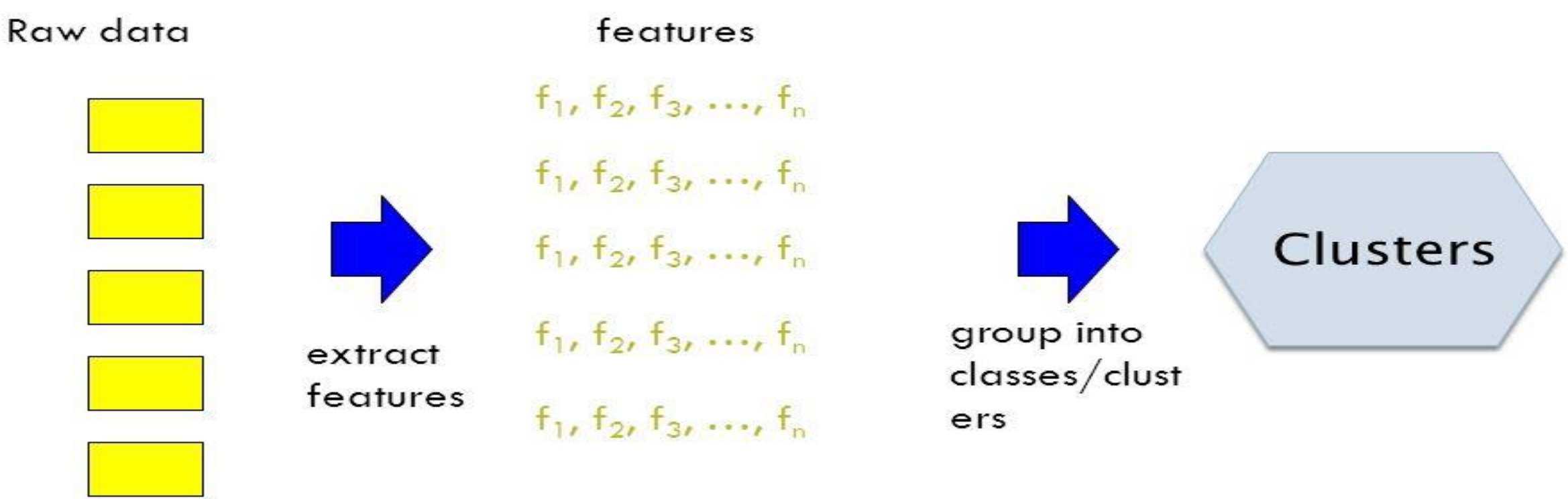
- This approach is data driven . The computer is trained with ***unlabeled*** input data.
- These algorithms try to use techniques on the input data to *mine for rules*, *detect patterns*, and *summarize and group the data points* which help in deriving meaningful insights and describe the data better to the users.


Unsupervised Learning
X
Input1
Input2
Input3
Input-n
Learning Algorithm
Clusters

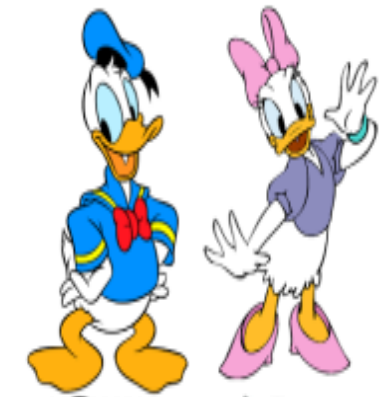
Types of Unsupervised Learning

1. Clustering
   - K Means Clustering
   - Hierarchical Clustering
   - Gaussian Mixture Models
   - Genetic Algorithms
   - Artificial Neural Networks
2. Dimensionality Reduction
   - Tensor Decomposition
   - Principal Component Analysis
   - Multidimensional statistics
   - Random Projection
   - Artificial Neural Networks
3. Association Rules

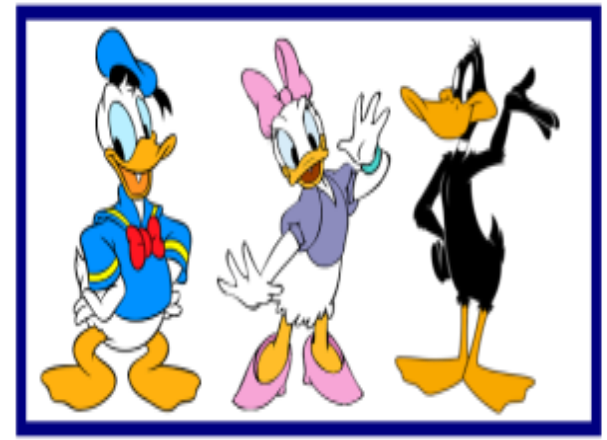
Unsupervised learning: clustering



No "supervision", we're only given data and want to find natural groupings



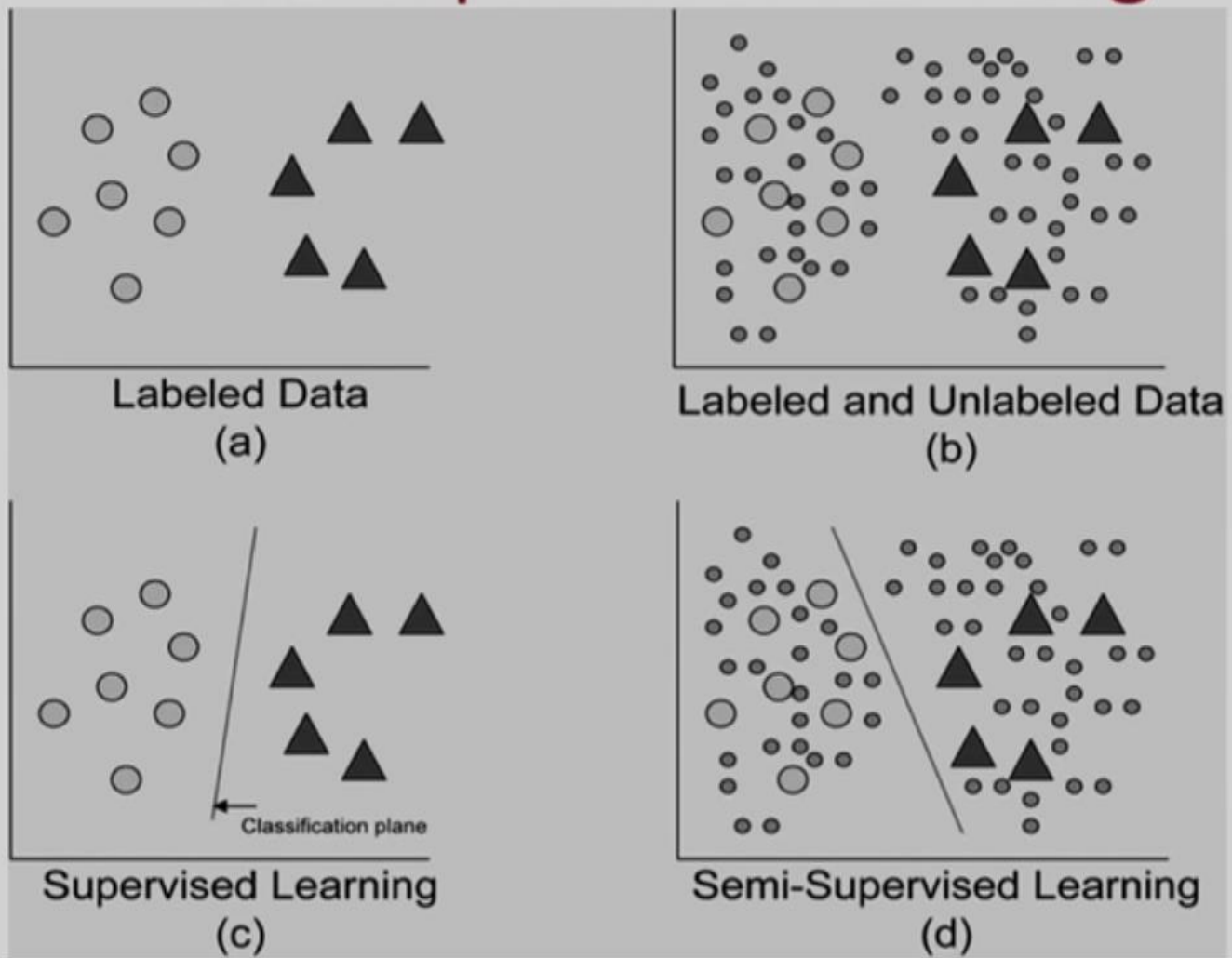
Unsupervised Learning



5.2.3. Semi Supervised

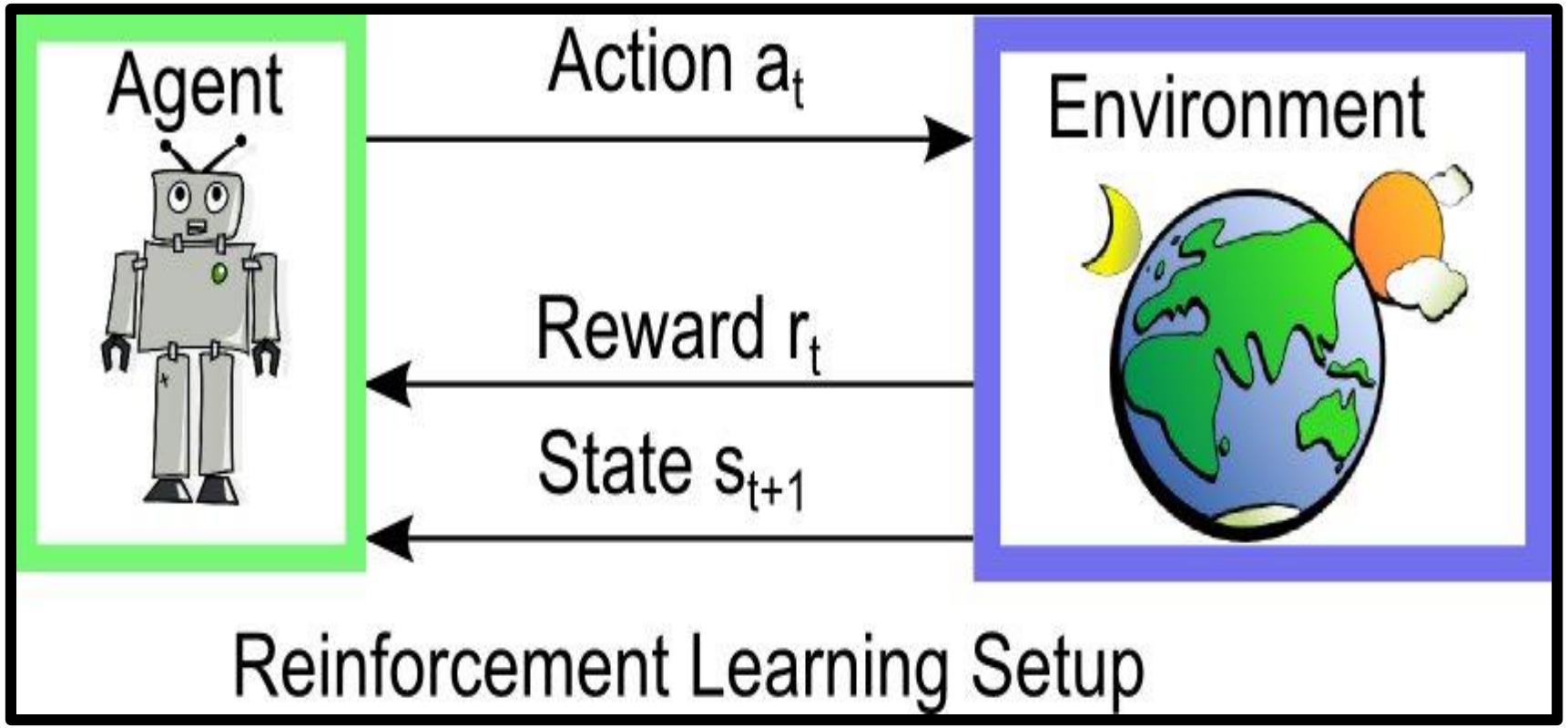
- In the previous two types, either there are no labels for all the observation in the dataset or labels are present for all the observations.
- Semi-supervised learning falls in between these two.

Semi-supervised learning



5.2.4. Reinforcement Learning

- This method aims at using observations gathered from the interaction with the environment to take actions that would maximize the reward or minimize the risk.
- Reinforcement learning algorithm (called the agent) continuously learns from the environment in an iterative fashion.


Agent
Action a_t
Environment
Reward r_t
State s_{t+1}
Reinforcement Learning Setup

Types of Reinforcement Learning Algorithms

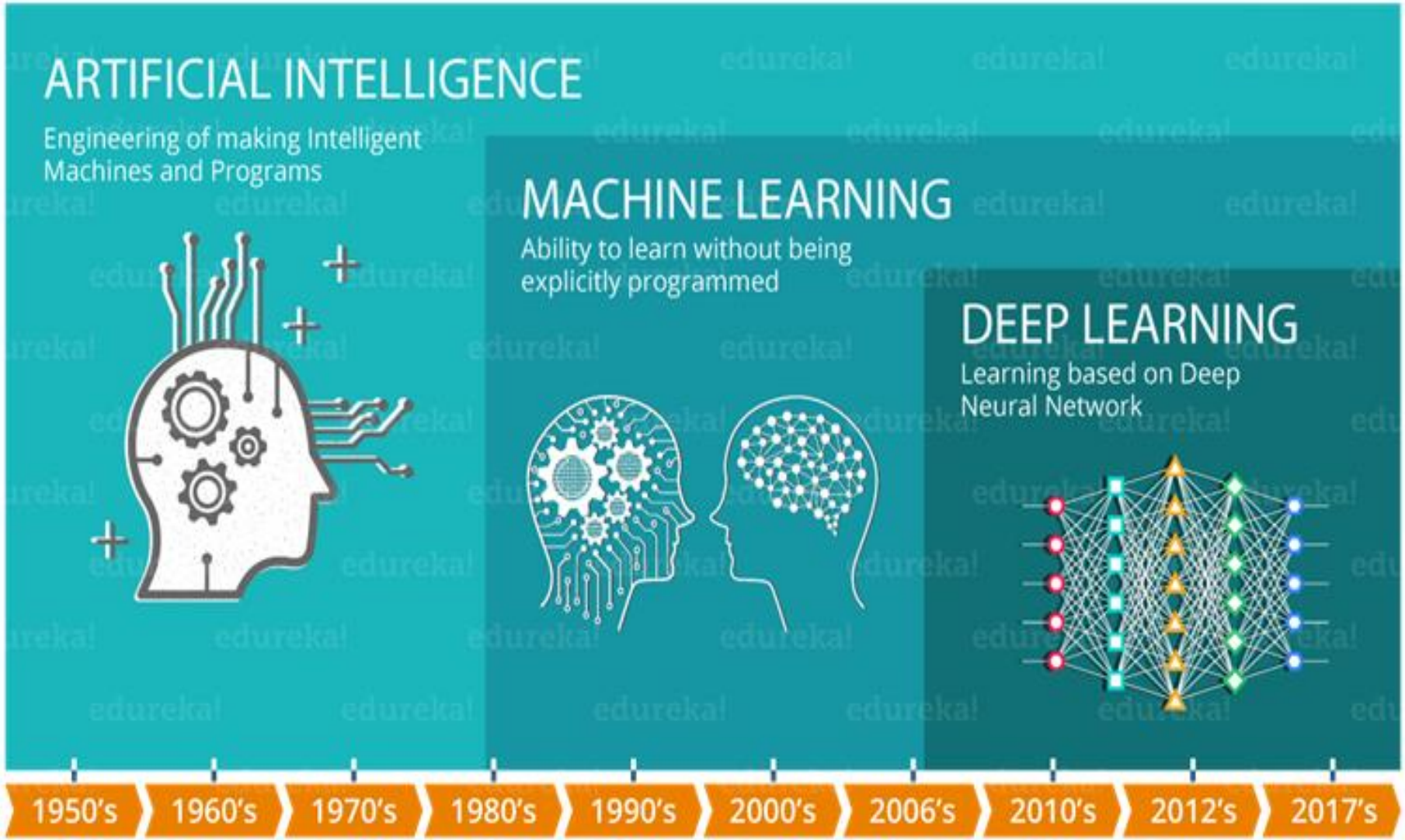
- **Q-Learning**
- **Temporal Difference (TD)**
- **Deep Adversarial Networks**

Table1: Examples of Types of Machine Learning Algorithms / Problem Solving Approaches

Type	Model /Algorithm or Task	Usage Examples in Business
Supervised	Neural network	■ Predicting financial results ■ Fraud detection
Supervised	Classification and/or Regression	■ Spam filtering ■ Fraud detection
Supervised	Decision tree	■ Risk assessment ■ Threat management systems ■ Any optimization problem where an exhaustive search is not feasible

Table1: Examples of Types of Machine Learning Algorithms / Problem Solving Approaches

Type	Model /Algorithm or Task	Usage Examples in Business
Unsupervised	Cluster analysis	■ Financial transactions ■ Streaming analytics in IoT ■ Underwriting in insurance
Unsupervised	Pattern recognition	■ Spam detection ■ Biometrics ■ Identity management
Unsupervised	Association rule learning	■ Security and intrusion detection ■ Bioinformatics ■Manufacturing and Assembly


ARTIFICIAL INTELLIGENCE
Engineering of making Intelligent Machines and Programs
MACHINE LEARNING
Ability to learn without being explicitly programmed
DEEP LEARNING
Learning based on Deep Neural Network
1950's
1960's
1970's
1980's
1990's
2000's
2006's
2010's
2012's
2017's

6. Open Source and Commercial Tools

Open Source Tools

1. Scikit Learn
2. Shogun
3. Accord.NET Framework
4. Spark MLlib
5. H20
6. Coudera Oryx
7. GoLearn
8. Weka
9. Deep Learn.js
10. ConvNet.Js
11. OpenAI
12. TensorFlow
13. Keras
14. Charnn
15. PaddlePAddle
16. CNTK
17. R
18. Monte Carlo ML Library
19. Octave Forge

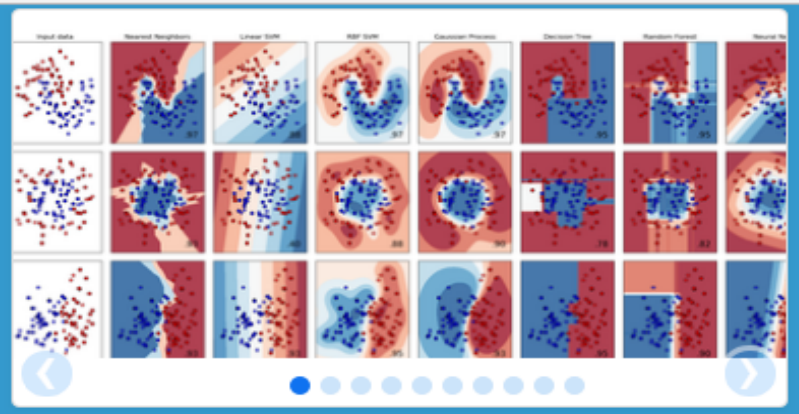
Commercial Tools

1. Microsoft Azure Machine Learning
2. SAS Enterprise Miner
3. IBM SPSS Modeler
4. RapidMiner
5. Apache Mahout
6. MATLAB
7. Oracle Data Mining

7. Introduction to Scikit Learn – A Python Machine Learning Library

Scikit Learn : http://scikit-learn.org/stable/index.html

scikit-learn.org/stable/index.html



scikit-learn

Machine Learning in Python

- Simple and efficient tools for data mining and data analysis
- Accessible to everybody, and reusable in various contexts
- Built on NumPy, SciPy, and matplotlib
- Open source, commercially usable - BSD license

Classification

Identifying to which category an object belongs to.

Applications: Spam detection, Image recognition.
Algorithms: SVM, nearest neighbors, random forest, ... — Examples

Regression

Predicting a continuous-valued attribute associated with an object.

Applications: Drug response, Stock prices.
Algorithms: SVR, ridge regression, Lasso, ... — Examples

Clustering

Automatic grouping of similar objects into sets.

Applications: Customer segmentation, Grouping experiment outcomes
Algorithms: k-Means, spectral clustering, mean-shift, ... — Examples

Dimensionality reduction

Reducing the number of random variables to consider.

Applications: Visualization, Increased efficiency
Algorithms: PCA, feature selection, non-negative matrix factorization. — Examples

Model selection

Comparing, validating and choosing parameters and models.

Goal: Improved accuracy via parameter tuning
Modules: grid search, cross validation, metrics. — Examples

Preprocessing

Feature extraction and normalization.

Application: Transforming input data such as text for use with machine learning algorithms.
Modules: preprocessing, feature extraction. — Examples

Where did it Come From ?

- **Scikit-learn** was initially developed by David Cournapeau as a Google summer of code project in 2007.
- Later Matthieu Brucher joined the project and started to use it as apart of his thesis work. In 2010 INRIA got involved and the first public release (v0.1 beta) was published in late January 2010.
- The project now has more than 30 active contributors and has had paid sponsorship from INRIA, Google, Tinyclues and the Python Software Foundation.

What is scikit-learn?

- Scikit-learn provides a range of supervised and unsupervised learning algorithms via a consistent interface in Python.
- It is licensed under a permissive simplified BSD license and is distributed under many Linux distributions, encouraging academic and commercial use.
- The library is built upon the SciPy (Scientific Python) that must be installed before you can use scikit-learn.

Scikit Stack

- **NumPy**: Base n-dimensional array package
- **SciPy**: Fundamental library for scientific computing
- **Matplotlib**: Comprehensive 2D/3D plotting
- **IPython**: Enhanced interactive console
- **Sympy**: Symbolic mathematics
- **Pandas**: Data structures and analysis

Some popular groups of models provided by scikit-learn include:

- **Clustering**: for grouping unlabeled data such as KMeans.
- **Cross Validation**: for estimating the performance of supervised models on unseen data.
- **Datasets**: for test datasets and for generating datasets with specific properties for investigating model behavior.
- **Dimensionality Reduction**: for reducing the number of attributes in data for summarization, visualization and feature selection such as Principal component analysis.
- **Ensemble methods**: for combining the predictions of multiple supervised models.
- **Feature extraction**: for defining attributes in image and text data.
- **Feature selection**: for identifying meaningful attributes from which to create supervised models.
- **Parameter Tuning**: for getting the most out of supervised models.
- **Manifold Learning**: For summarizing and depicting complex multi-dimensional data.
- **Supervised Models**: a vast array not limited to generalized linear models, discriminate analysis, naive bayes, lazy methods, neural networks, support vector machines and decision trees.

Example : Scikit learn Machine Learning

There are 5 key libraries that you will need to install. Below is a list of the Python SciPy libraries required for this tutorial:

1. scipy
2. numpy
3. matplotlib
4. pandas
5. sklearn

7.1. Check the versions of libraries

```
# Python version
import sys
print('Python: {}'.format(sys.version))
# scipy
import scipy
print('scipy: {}'.format(scipy.__version__))
# numpy
import numpy
print('numpy: {}'.format(numpy.__version__))
# matplotlib
import matplotlib
print('matplotlib: {}'.format(matplotlib.__version__))
# pandas
import pandas
print('pandas: {}'.format(pandas.__version__))
# scikit-learn
import sklearn
print('sklearn: {}'.format(sklearn.__version__))
```

```
Python: 3.6.3 |Anaconda, Inc.| (default, Oct 15 2017, 07:29:16) [MSC v.1900 32
bit (Intel)]
scipy: 0.19.1
numpy: 1.13.3
matplotlib: 2.1.0
pandas: 0.20.3
sklearn: 0.19.1
```

7.2. Load The Data

- We are going to use the iris flowers dataset. This dataset is famous because it is used as the "*hello world*" dataset in machine learning and statistics by pretty much everyone.
- The dataset contains 150 observations of iris flowers. There are ***four columns of measurements*** of the flowers in centimeters. The ***fifth column*** is the species of the flower observed. All observed flowers belong to one of ***three species***.

7.2.1 Load Libraries

```
# Load Libraries
import pandas
from pandas.plotting import scatter_matrix
import matplotlib.pyplot as plt
from sklearn import model_selection
from sklearn.metrics import classification_report
from sklearn.metrics import confusion_matrix
from sklearn.metrics import accuracy_score
from sklearn.linear_model import LogisticRegression
from sklearn.tree import DecisionTreeClassifier
from sklearn.neighbors import KNeighborsClassifier
from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
from sklearn.naive_bayes import GaussianNB
from sklearn.svm import SVC
```

7.2.2 Load Dataset

```
# Load dataset
url = "https://archive.ics.uci.edu/ml/machine-learning-databases/iris/iris.data"
names = ['sepal-length', 'sepal-width', 'petal-length', 'petal-width', 'class']
dataset = pandas.read_csv(url, names=names)
```

7.3. Summarize the Dataset

- In this step we are going to take a look at the data a few different ways:
  1. Dimensions of the dataset.
  2. Peek at the data itself.
  3. Statistical summary of all attributes.
  4. Breakdown of the data by the class variable

7.3.1 Dimensions of Dataset

```
# shape
print(dataset.shape)
```

```
(150, 5)
```

7.3.2 Peek at the Data

```
# head
print(dataset.head(10))
```

```
   sepal-length  sepal-width  petal-length  petal-width        class
0           5.1          3.5           1.4          0.2  Iris-setosa
1           4.9          3.0           1.4          0.2  Iris-setosa
2           4.7          3.2           1.3          0.2  Iris-setosa
3           4.6          3.1           1.5          0.2  Iris-setosa
4           5.0          3.6           1.4          0.2  Iris-setosa
5           5.4          3.9           1.7          0.4  Iris-setosa
6           4.6          3.4           1.4          0.3  Iris-setosa
7           5.0          3.4           1.5          0.2  Iris-setosa
8           4.4          2.9           1.4          0.2  Iris-setosa
9           4.9          3.1           1.5          0.1  Iris-setosa
```

7.3.3 Statistical Summary

```
# descriptions
print(dataset.describe())
```

```
       sepal-length  sepal-width  petal-length  petal-width
count    150.000000   150.000000    150.000000   150.000000
mean       5.843333     3.054000      3.758667     1.198667
std        0.828066     0.433594      1.764420     0.763161
min        4.300000     2.000000      1.000000     0.100000
25%        5.100000     2.800000      1.600000     0.300000
50%        5.800000     3.000000      4.350000     1.300000
75%        6.400000     3.300000      5.100000     1.800000
max        7.900000     4.400000      6.900000     2.500000
```

7.3.4 Class Distribution

```
# class distribution
print(dataset.groupby('class').size())
```

```
class
Iris-setosa        50
Iris-versicolor    50
Iris-virginica     50
dtype: int64
```

7.4. Data Visualization

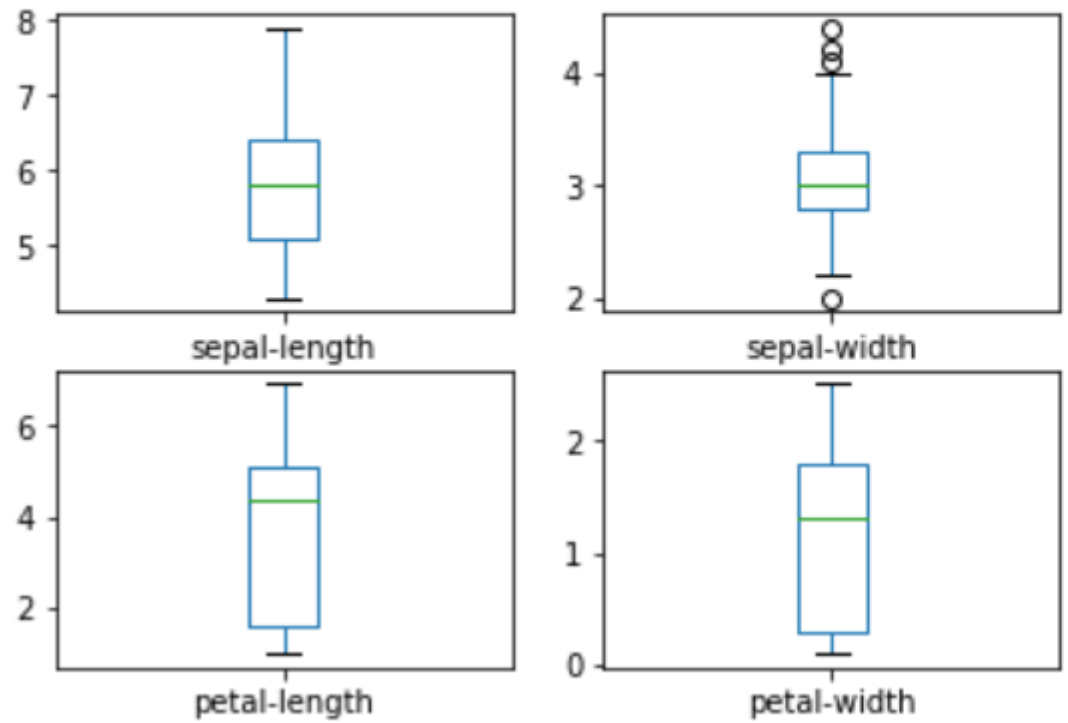
We now have a basic idea about the data. We need to extend that with some visualizations.

We are going to look at two types of plots:

1. **Univariate plots to better understand each attribute.**
2. **Multivariate plots to better understand the relationships between attributes**.

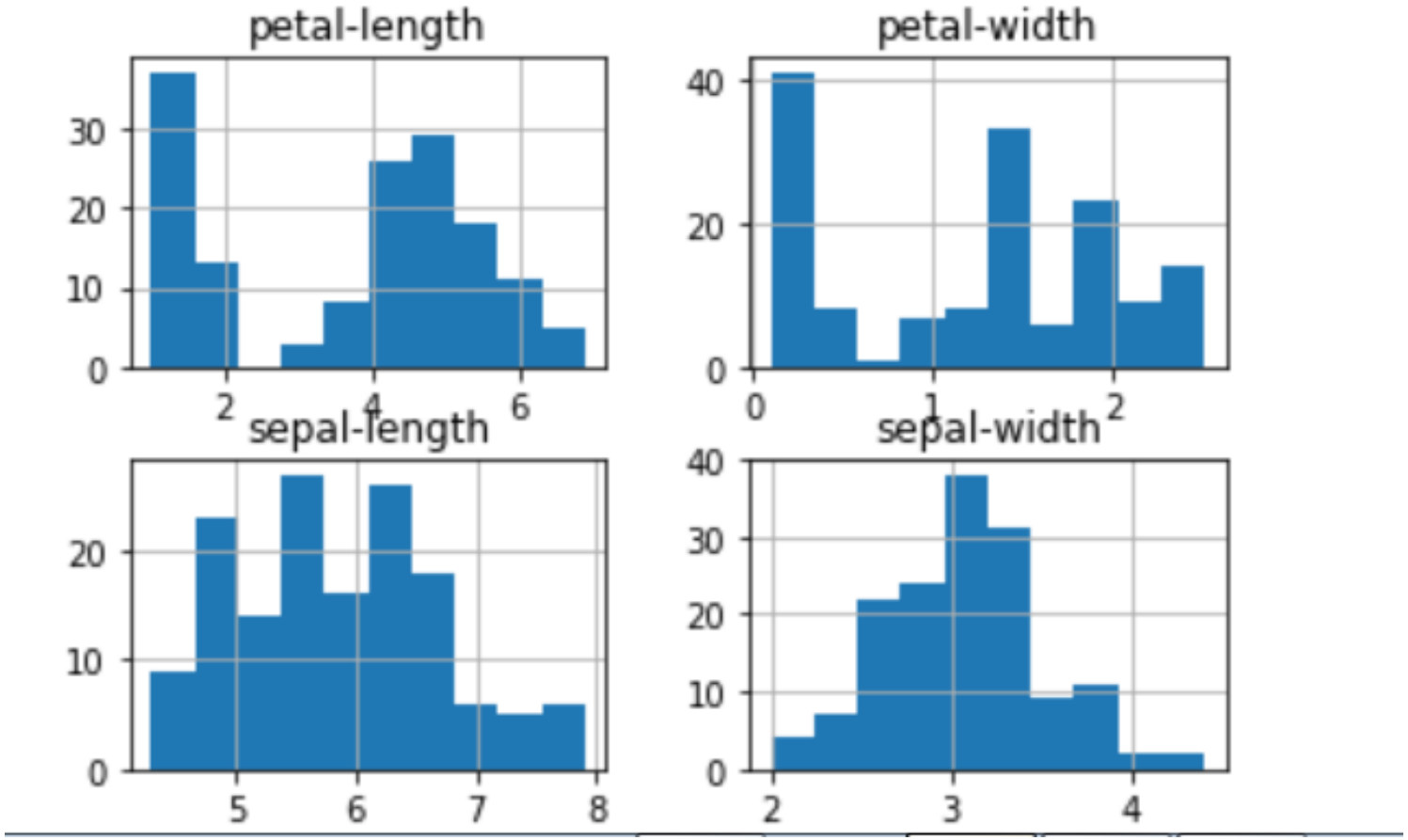
7.4.1 Univariate Plots

```
# box and whisker plots
dataset.plot(kind='box', subplots=True, layout=(2,2), sharex=False, sharey=False)
plt.show()
```



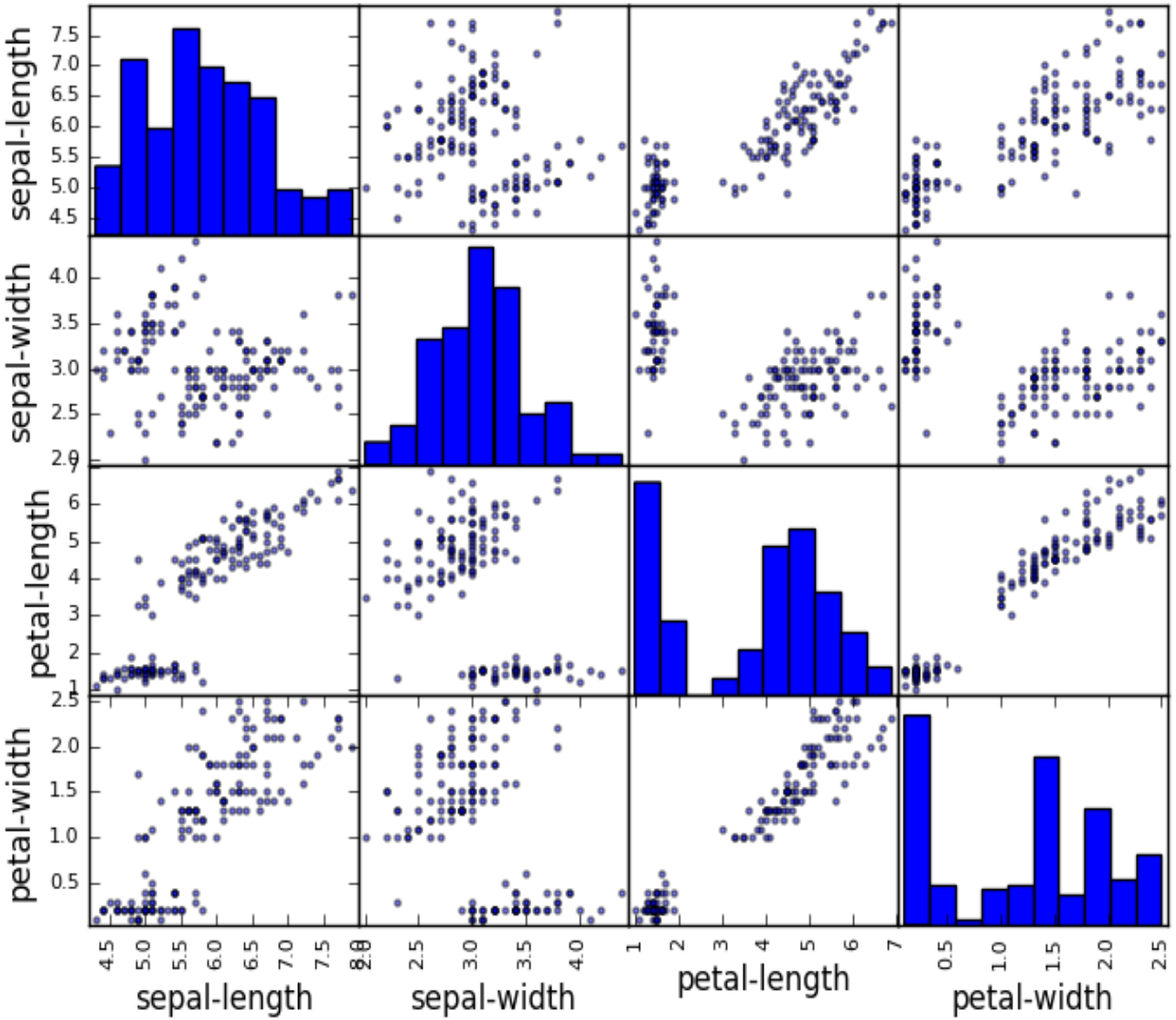
Histograms

```
# histograms
dataset.hist()
plt.show()
```



7.4.2 Multivariate Plots

```
# scatter plot matrix
scatter_matrix(dataset)
plt.show()
```



7.5. Evaluate Some Algorithms

- Here is what we are going to cover in this step:
  - Separate out a validation dataset.
  - Set-up the test harness to use 10-fold cross validation.
  - Build 5 different models to predict species from flower measurements
  - Select the best model.

7.5.1 Create a Validation Dataset

- We will split the loaded dataset into two, 80% of which we will use to train our models and 20% that we will hold back as a validation dataset

```
# Split-out validation dataset
array = dataset.values
X = array[:,0:4]
Y = array[:,4]
validation_size = 0.20
seed = 7
X_train, X_validation, Y_train,Y_validation = model_selection.train_test_split(X,
                                                    test_size=validation_size,
                                                    random_state=seed)
```

7.5.2 Test Harness

We will use 10-fold cross validation to estimate accuracy.
This will split our dataset into 10 parts, train on 9 and test on 1 and repeat for all combinations of train-test splits.

```
# Test options and evaluation metric
seed = 7
scoring = 'accuracy'
```

7.5.3 Build Models

- Let’s evaluate 6 different algorithms:
  - Logistic Regression (LR)
  - Linear Discriminant Analysis (LDA)
  - K-Nearest Neighbors (KNN).
  - Classification and Regression Trees (CART).
  - Gaussian Naive Bayes (NB).
  - Support Vector Machines (SVM).

```
# Spot Check Algorithms
models = []
models.append(('LR', LogisticRegression()))
models.append(('LDA', LinearDiscriminantAnalysis()))
models.append(('KNN', KNeighborsClassifier()))
models.append(('CART', DecisionTreeClassifier()))
models.append(('NB', GaussianNB()))
models.append(('SVM', SVC()))
# evaluate each model in turn
results = []
names = []
for name, model in models:
    kfold = model_selection.KFold(n_splits=10, random_state=seed)
    cv_results = model_selection.cross_val_score(model, X_train, Y_train, cv=kfol
    results.append(cv_results)
    names.append(name)
    msg = "%s: %f (%f)" % (name, cv_results.mean(), cv_results.std())
    print(msg)
```

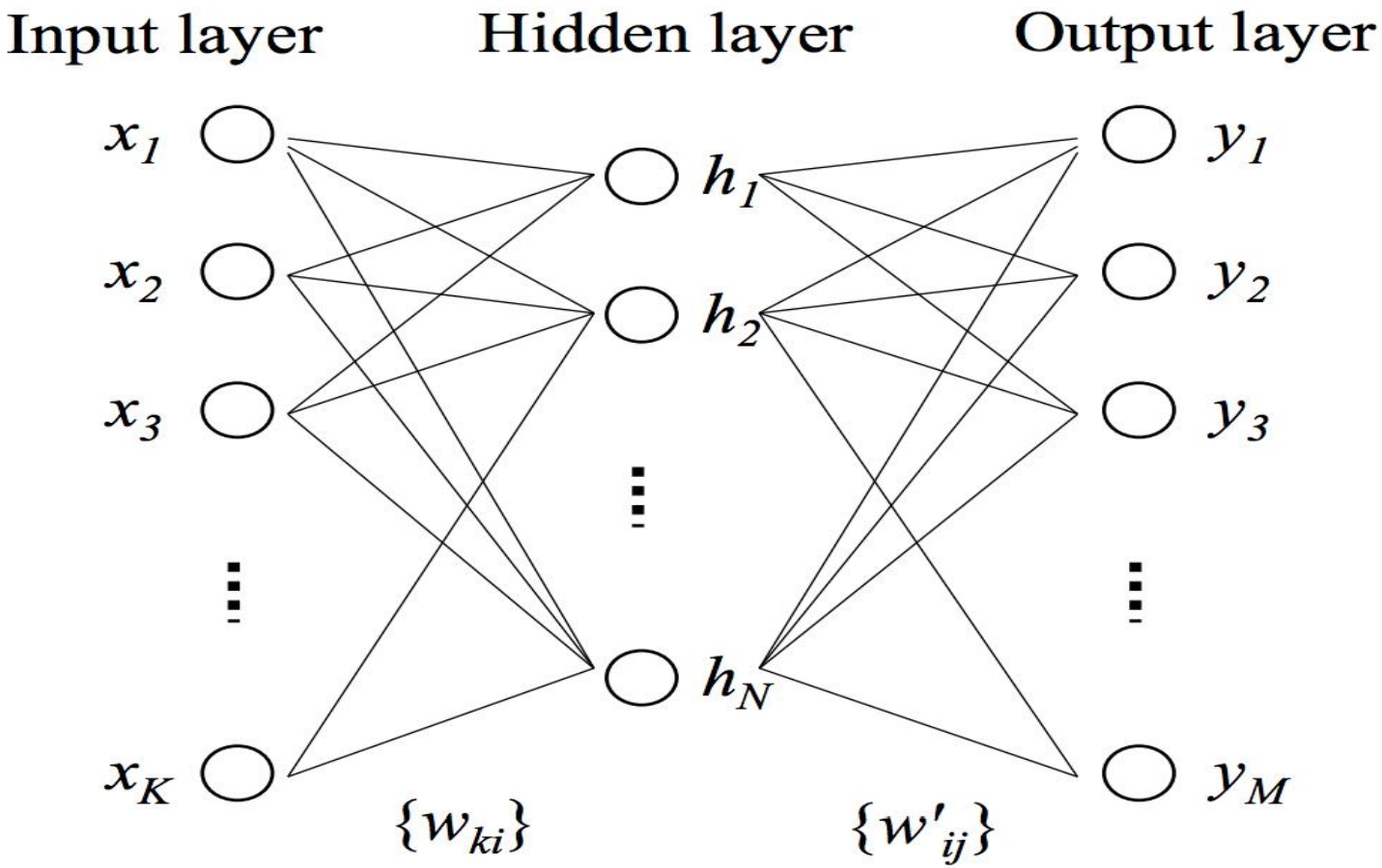
7.5.4 Select Best Model

```
LR: 0.966667 (0.040825)
LDA: 0.975000 (0.038188)
KNN: 0.983333 (0.033333)
CART: 0.975000 (0.038188)
NB: 0.975000 (0.053359)
SVM: 0.991667 (0.025000)
```

8. Introduction to Deep Learning

- Deep learning is a type of machine learning that is based on algorithms with extensive connections or layers between inputs and outputs.
- ML neural nets have inputs (variables), hidden layers (functions that compute the output) and output (results).
- In a simple example, imagine an ML neural net to detect a dog. This seemingly simple example may include a tail detector, ear detector, hair detector and so on.
- These detectors are combined into layers that contribute to detecting a dog. The more "detectors" you have, the deeper the neural net.

Deep Learning



Deep Learning Tools

- Neural Designer
- Torch
- Apache SINGA
- Microsoft Cognitive ToolKit
- Keras
- Deeplearning4j
- Theano
- MXNet
- H2O.ai
- ConvNetjs
- DeepLEarningkit
- Gensim
- Caffe
- ND4J
- DeepLearnToolBox

2.Python Fundamentals

Python Introduction

- Python is a general-purpose interpreted, interactive, object-oriented, and high-level programming language.
- It was created by *Guido van Rossum* during 1985- 1990.
- Python is named after a TV Show called '*Monty Python's Flying Circus*' and not after Python-the snake.

Features of Python

- **High-level Language and Simple**
- **Free and Open Source**
- **Portable**
- **Interactive and Interpreted**
- **Object Oriented**
- **Scalable**
- **Embeddable**
- **Extensive Libraries**
- **Database Support**
- **Programming GUI/APP**

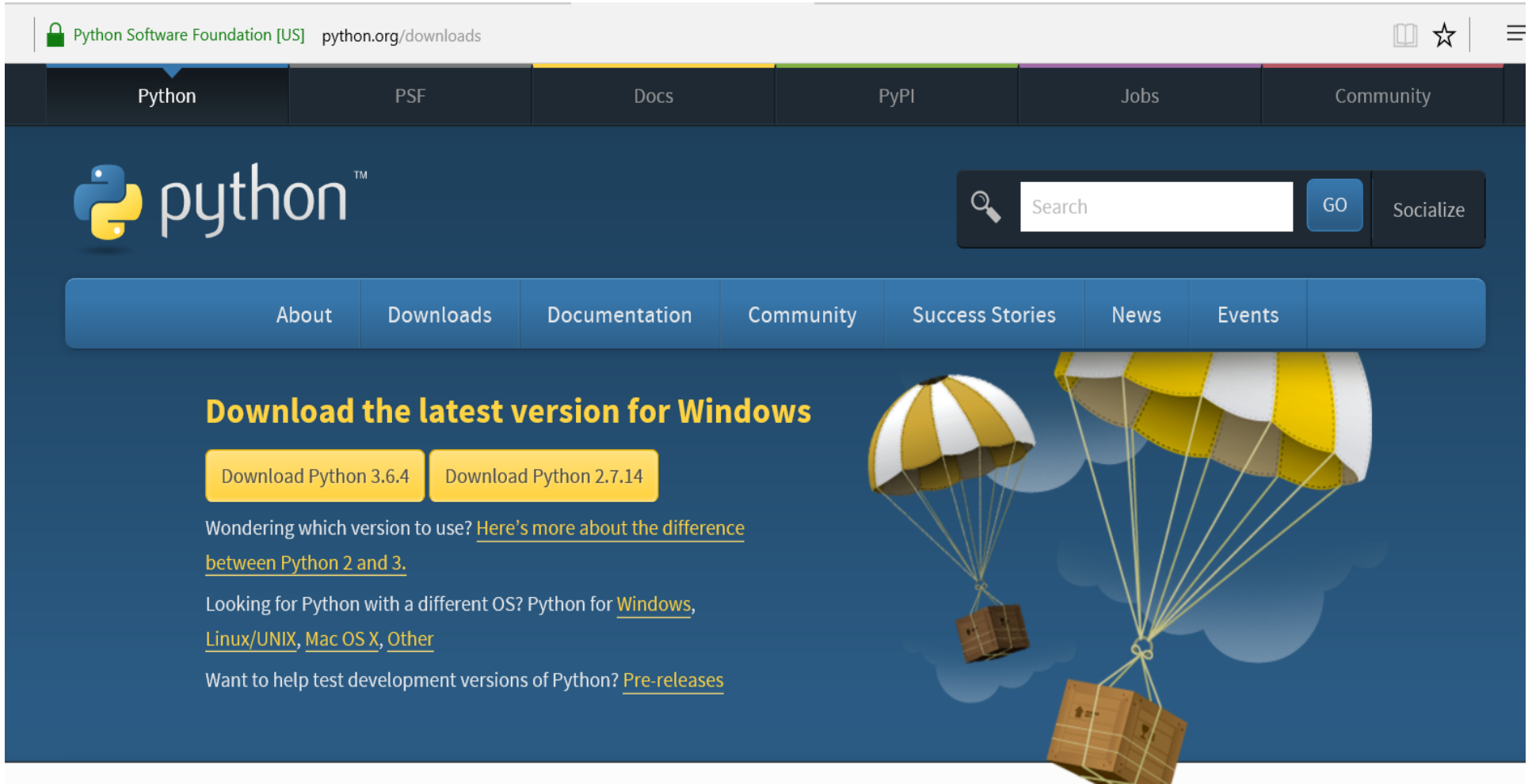
Programming Editors

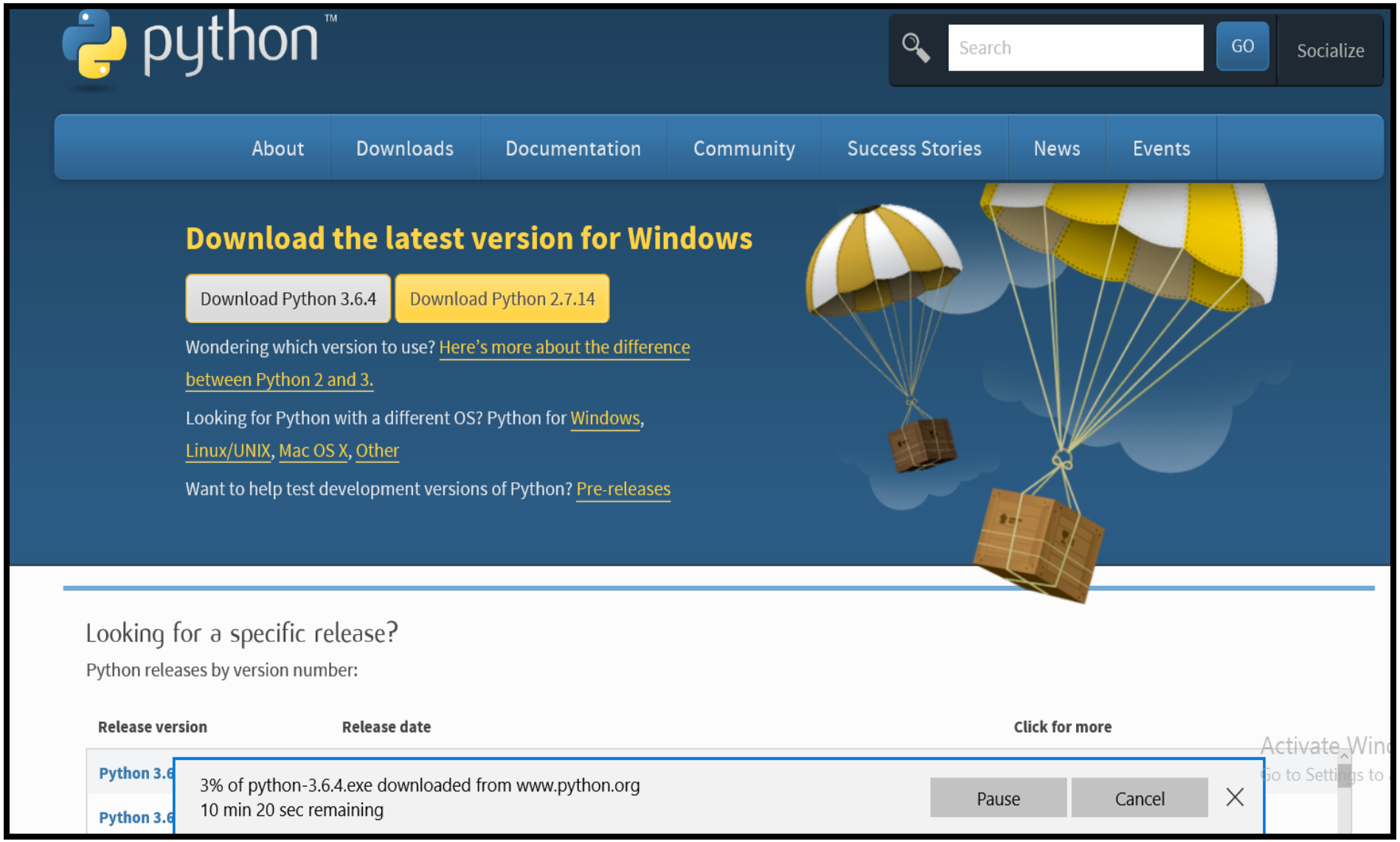
- Python 3.6 Command Prompt
- Python 3.6 Idle
- Anaconda Prompt
- Anaconda Jupyter Notebook
- Anaconda Spider
- JetBrains PyCharm

Python 3.6

Python3.6 Installation

- Go to web page : https://www.python.org/downloads/




python™
Search
GO
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Downloads
Documentation
Community
Success Stories
News
Events
Download the latest version for Windows
Download Python 3.6.4
Download Python 2.7.14
Wondering which version to use? Here's more about the difference between Python 2 and 3.
Looking for Python with a different OS? Python for Windows, Linux/UNIX, Mac OS X, Other
Want to help test development versions of Python? Pre-releases
Looking for a specific release?
Python releases by version number:
Release version
Release date
Click for more
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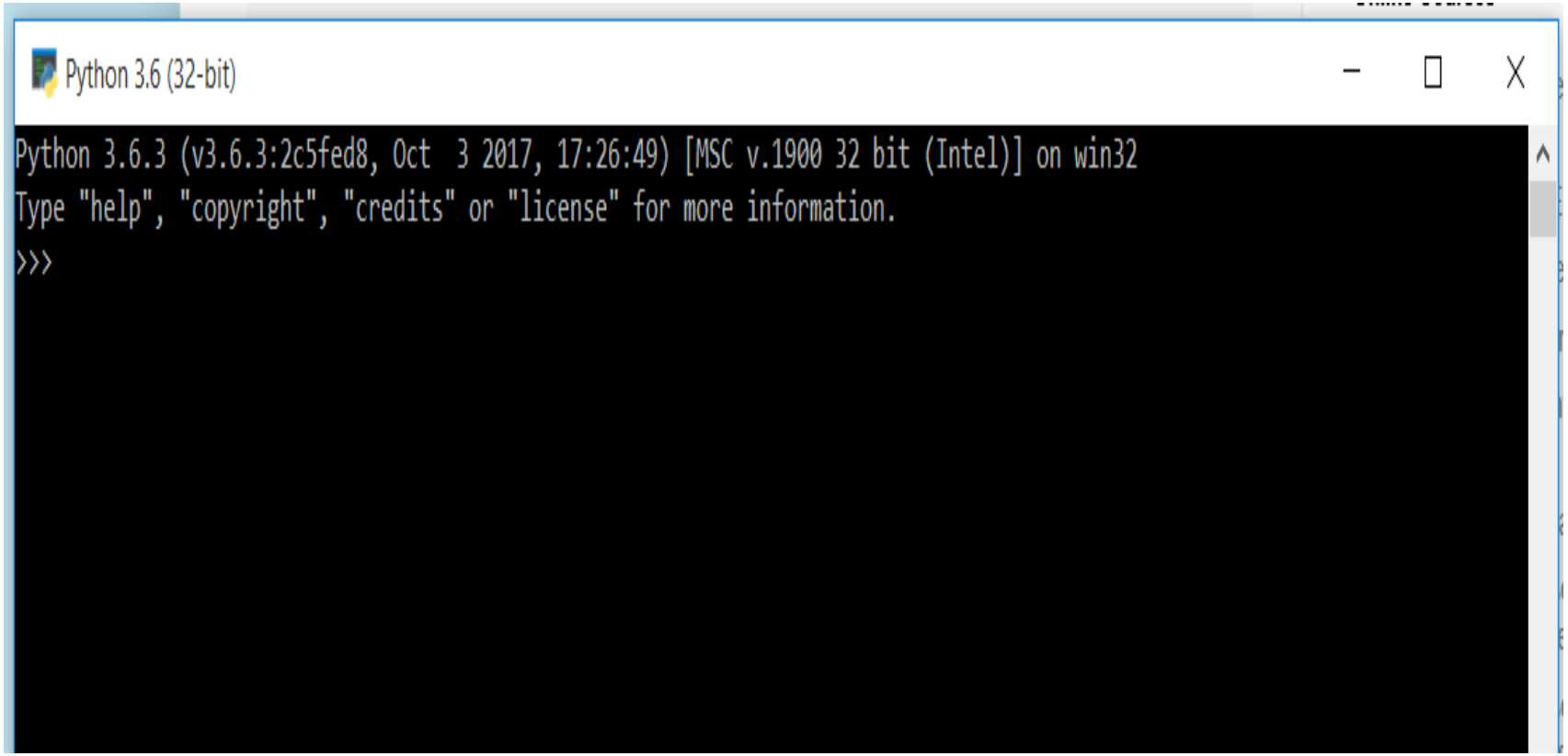
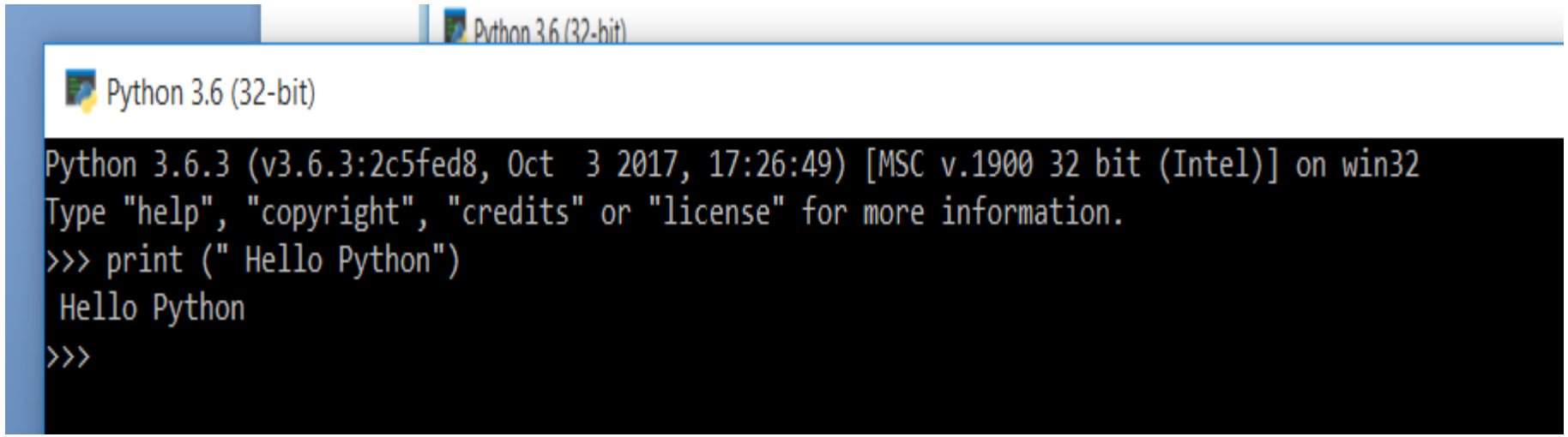
Interactive Python Programming




Python 3.6 (32-bit)
Python 3.6 (32-bit)
Python 3.6.3 (v3.6.3:2c5fed8, Oct 3 2017, 17:26:49) [MSC v.1900 32 bit (Intel)] on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> print (" Hello Python")
Hello Python
>>>

What is Anaconda?

- The open source Anaconda Distribution is the easiest way to do Python data science and machine learning.
- It includes hundreds of popular data science packages and the *conda* package and virtual environment manager for Windows, Linux, and MacOS.

Use Python for…

- **Web Development**: Django, Pyramid, Bottle, Tornado, Flask, web2py
- **GUI Development**: tkInter, PyGObject, PyQt, PySide, Kivy, wxPython
- **Scientific and Numeric**: SciPy, Pandas, IPython
- **Software Development**: Buildbot, Trac, Roundup
- **System Administration**: Ansible, Salt, OpenStack

Some Python Packages/Libraries

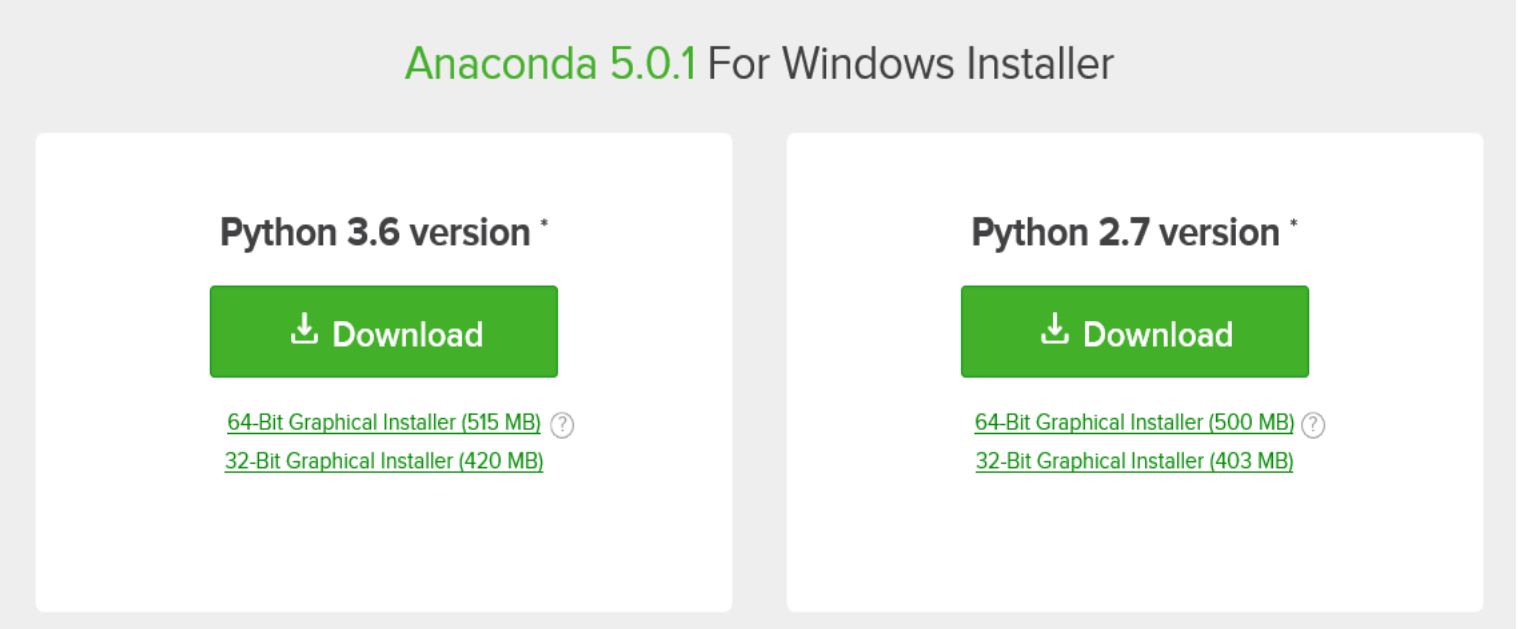
- Numpy
- Scipy
- Pandas
- Matplotlib
- Seaborn
- Bokeh
- Scikit Learn
- Pygames
- dJango
- Flask
- Bottle
- Pyramid
- PyBrain
- PyMongo

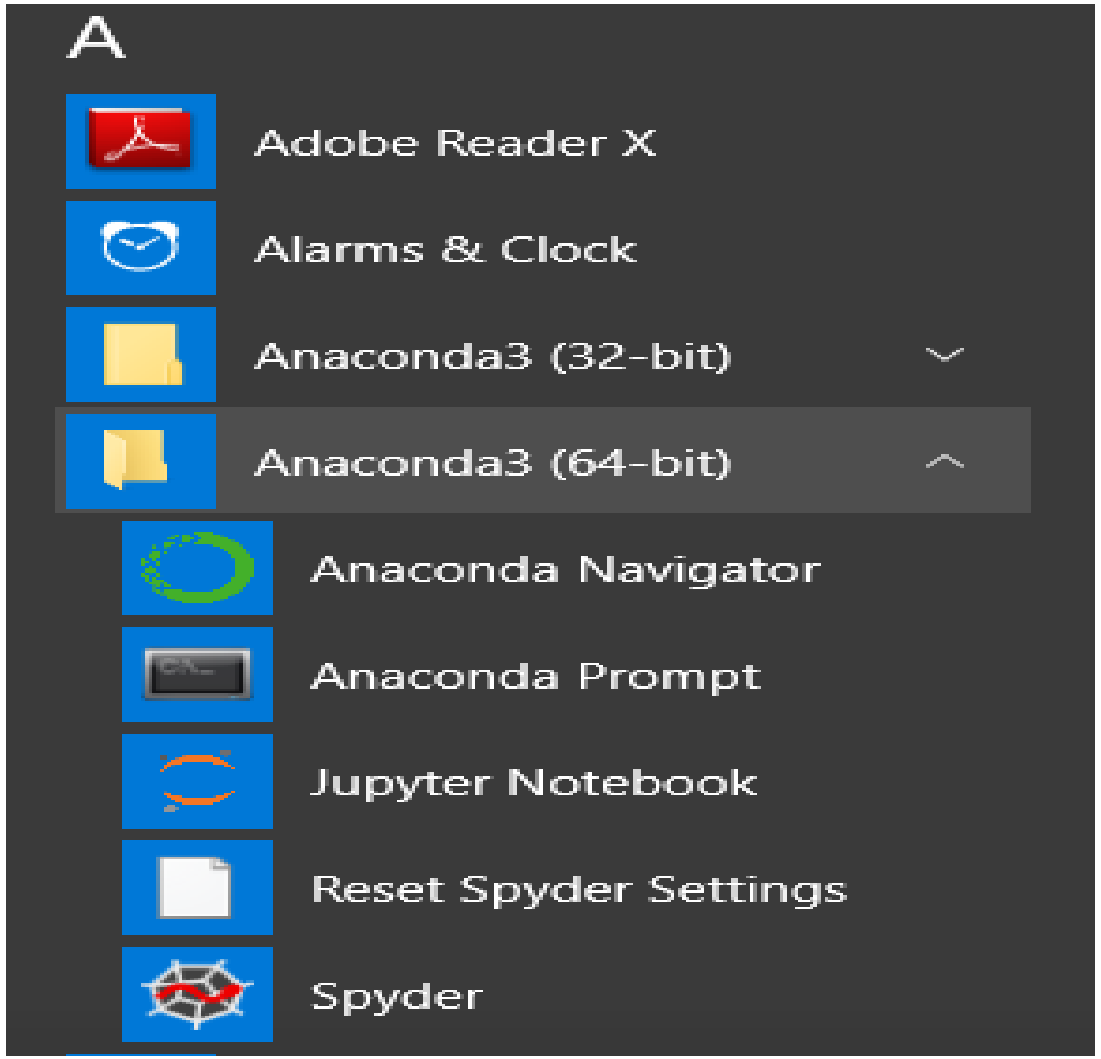
- Tornado
- Web2py
- Json
- tKinter
- OpenCV
- PyGObject
- PyQt
- wxPython
- Kivy
- Buildozer
- Buildbot
- Trac
- Roundup

- Ansible
- Salt
- OpenStack
- Keras
- Tensor Flow
- Theano
- nltk
- Spacy
- TextBlog
- ScikitLearn
- Pattern
- SQLalchemy
- pyMySql
-

Downloading Anaconda

- The latest version of Anaconda is available for download from **https://www.anaconda.com/download/**




A
Adobe Reader X
Alarms & Clock
Anaconda3 (32-bit)
Anaconda3 (64-bit)
Anaconda Navigator
Anaconda Prompt
Jupyter Notebook
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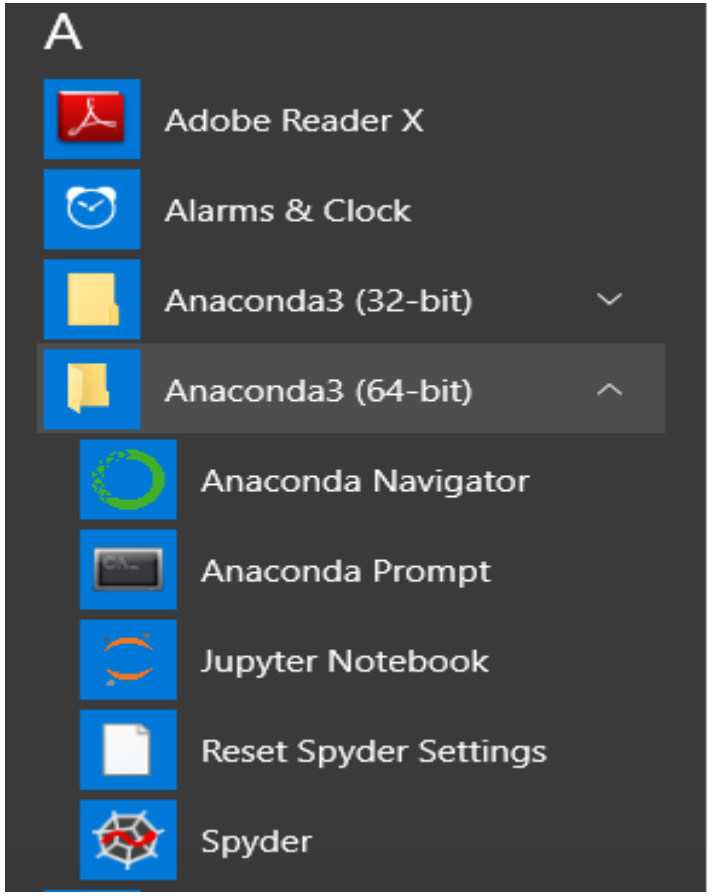
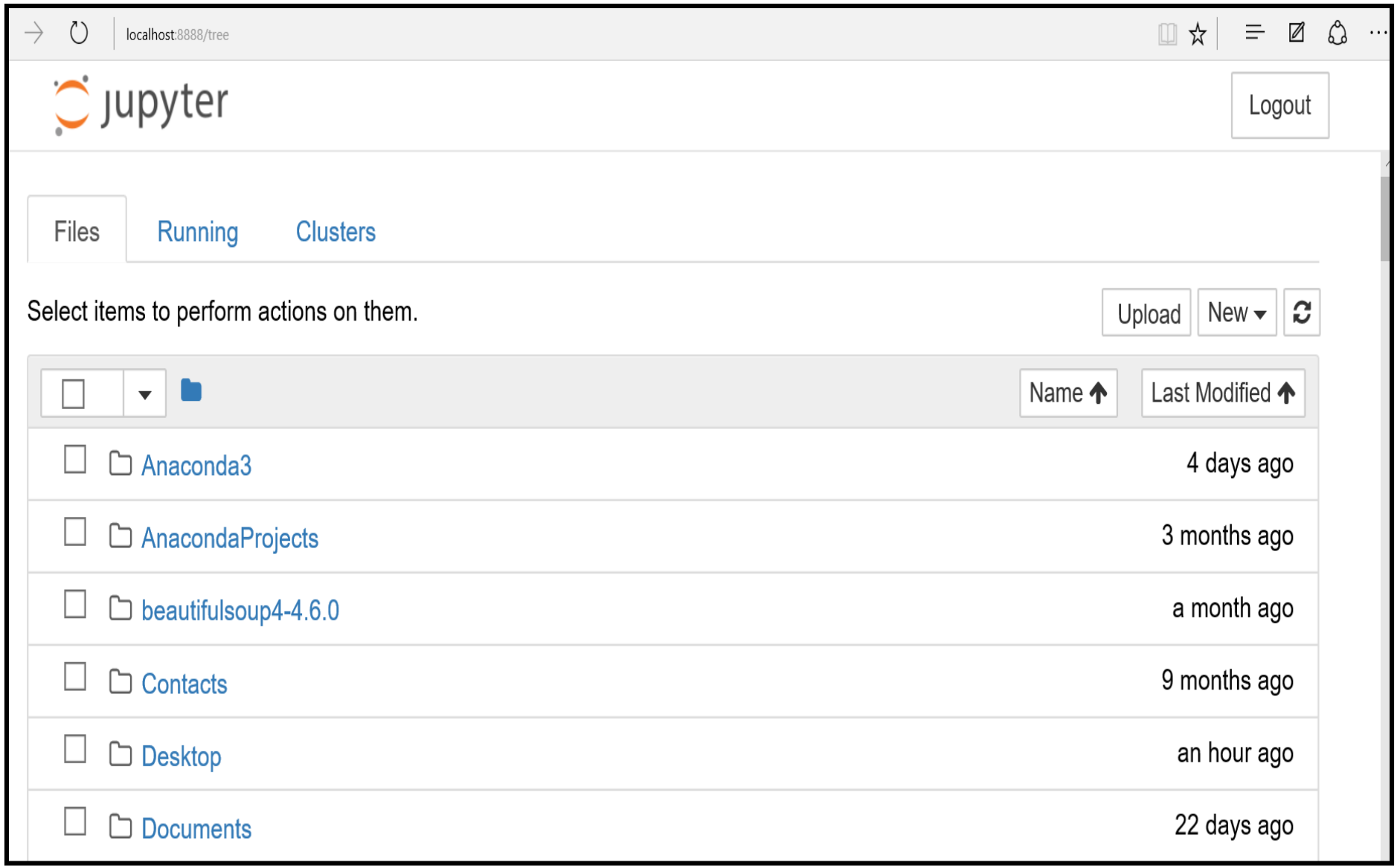
Spyder

JUPYTER NOTEBOOK

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a month ago
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9 months ago
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an hour ago
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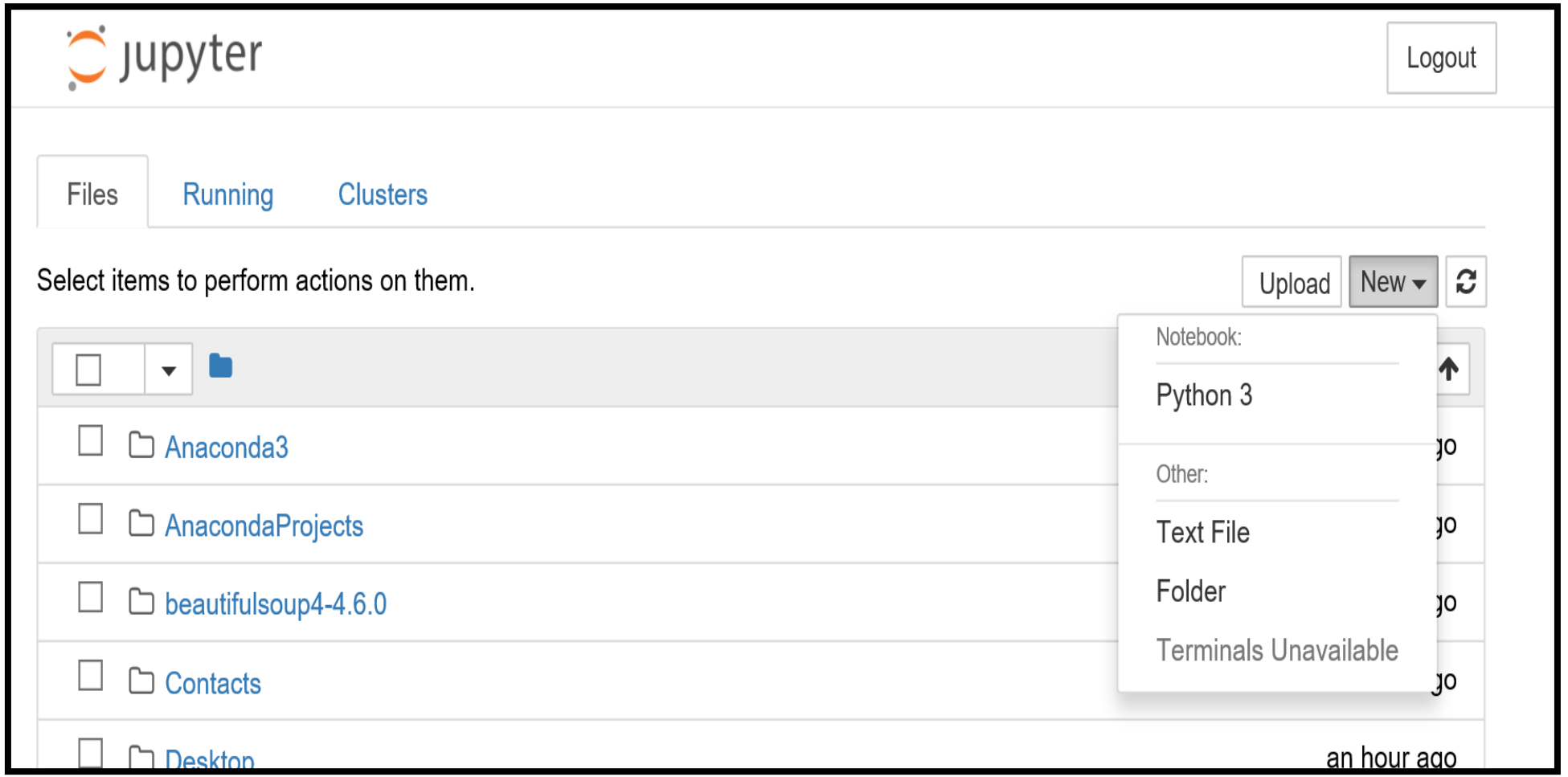
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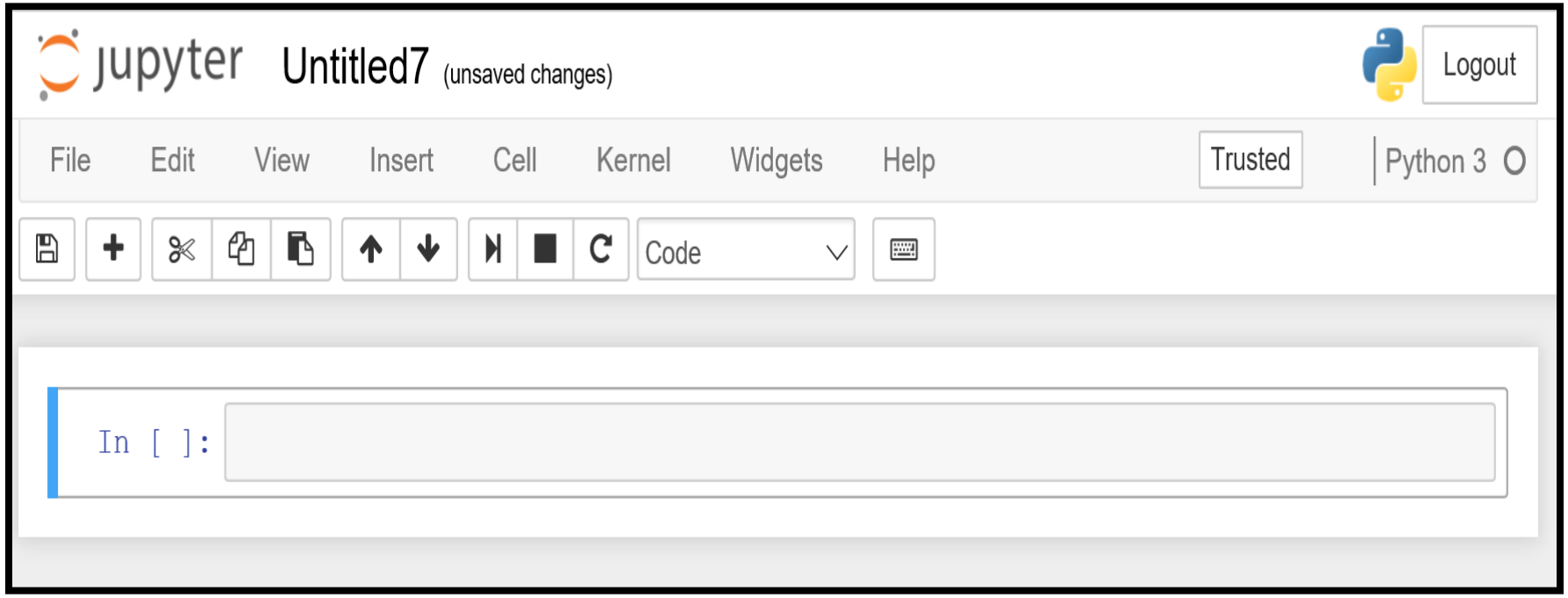
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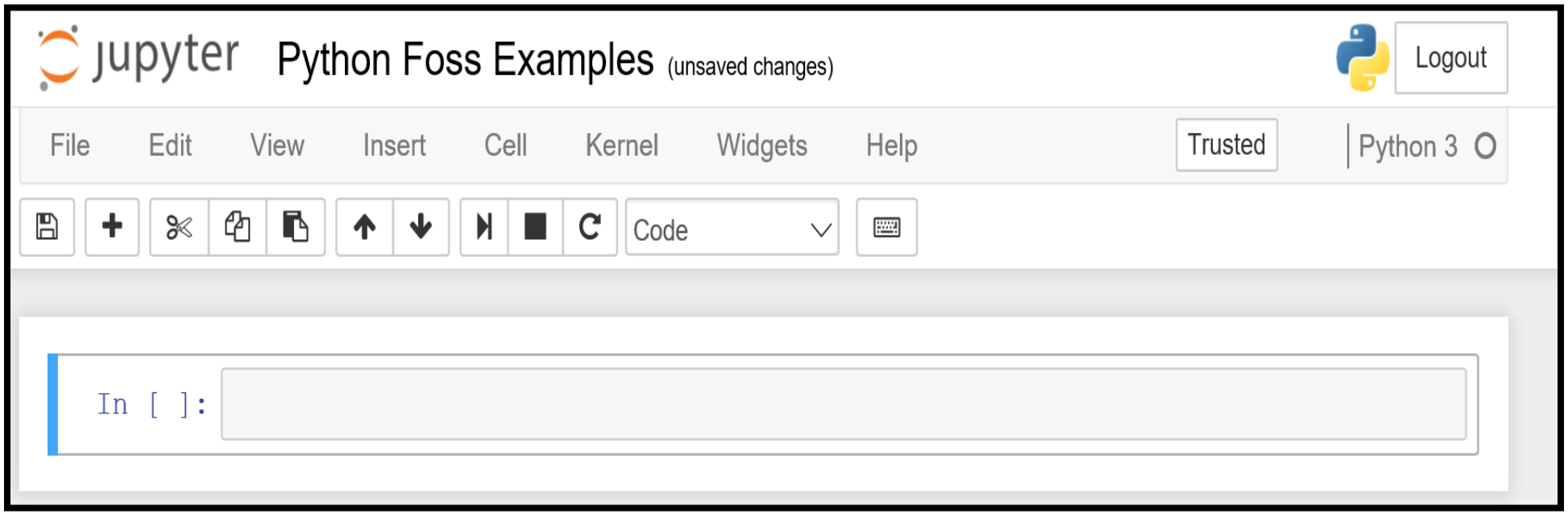
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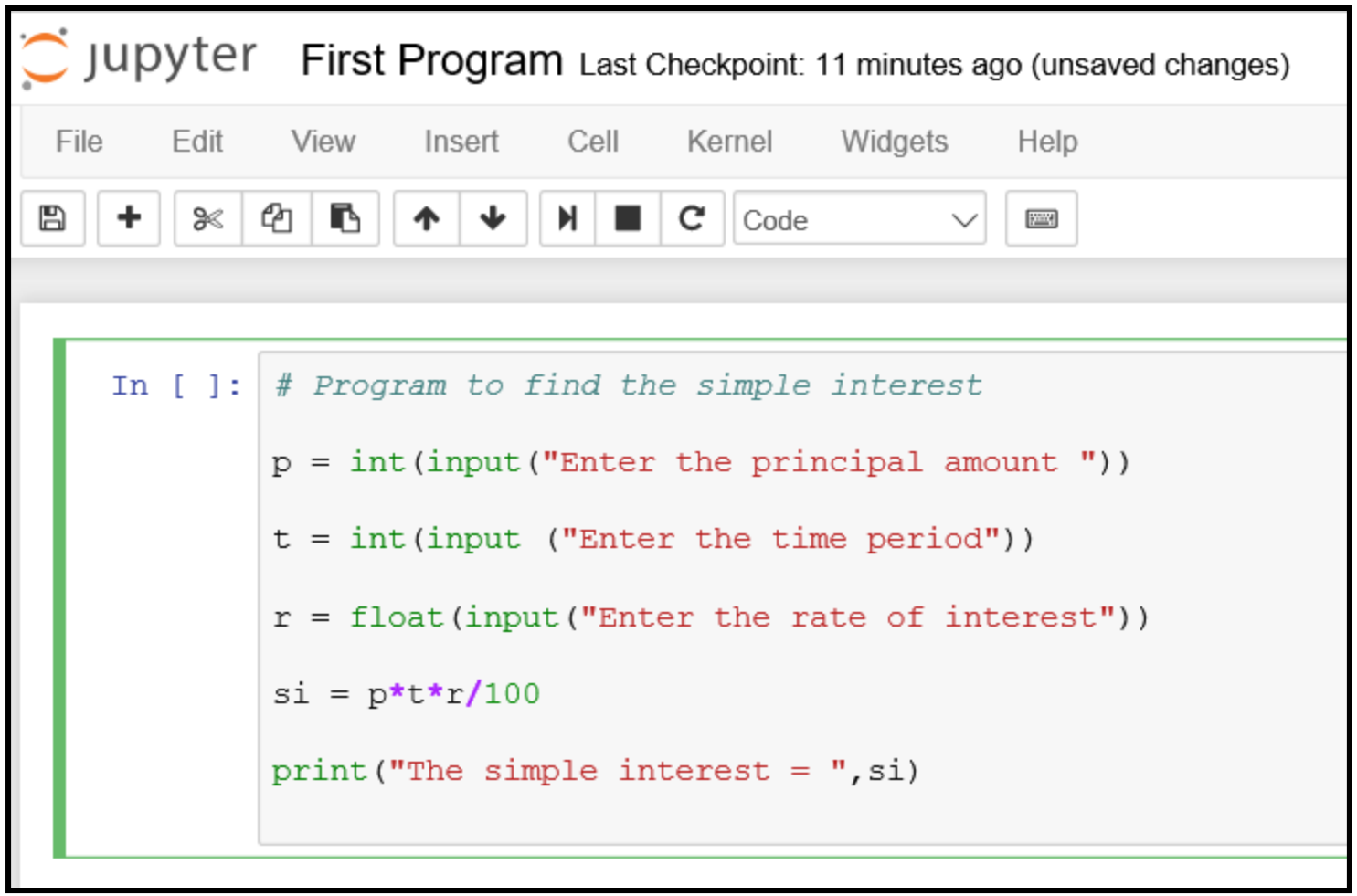
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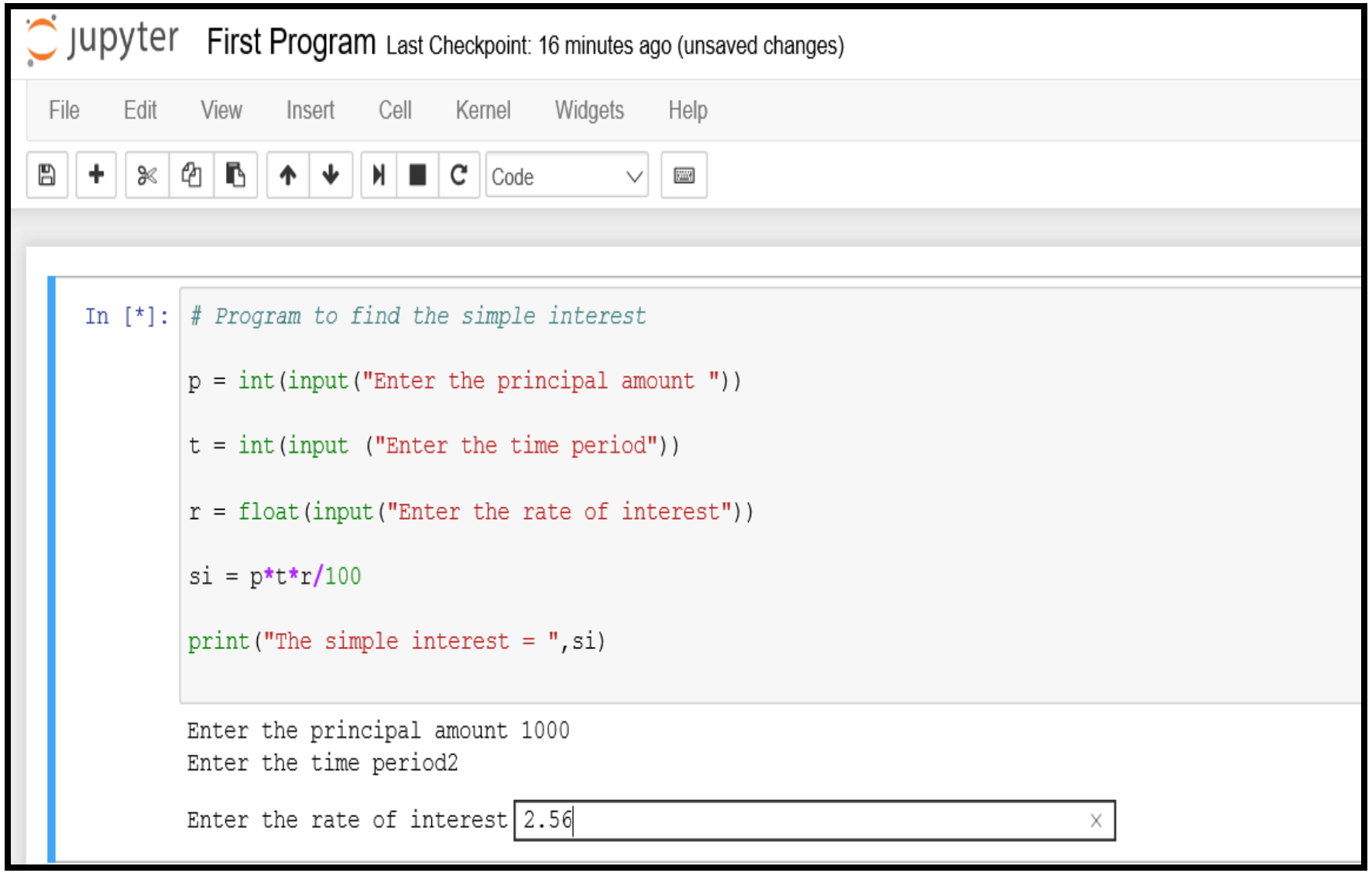
Code
In [ ]:
# Program to find the simple interest
p = int(input("Enter the principal amount "))
t = int(input ("Enter the time period"))
r = float(input("Enter the rate of interest"))
si = p*t*r/100
print("The simple interest = ",si)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In [*]:
# Program to find the simple interest
p = int(input("Enter the principal amount "))
t = int(input ("Enter the time period"))
r = float(input("Enter the rate of interest"))
si = p*t*r/100
print("The simple interest = ",si)
Enter the principal amount 1000
Enter the time period2
Enter the rate of interest 2.56

In [1]:

```
# Program to find the simple interest

p = int(input("Enter the principal amount "))

t = int(input ("Enter the time period"))

r = float(input("Enter the rate of interest"))

si = p*t*r/100

print("The simple interest = ",si)
```

```
Enter the principal amount 1000
Enter the time period 2
Enter the rate of interest 2.56
The simple interest =  51.2
```

Data Types in Python

Floating Point Numbers	**1.2**	Immutable
Integer Numbers	**2**	Immutable
Complex Numbers	**1+2j**	Immutable
Strings	**“context”**	Immutable
Lists	**a = [1, 2.2, 'python']**	Mutable
Tuples	**t = (5,'program', 1+3j)**	Immutable
Dictionaries	**d = {1:'value','key':2}**	Immutable+ Mutable

Fundamentals of Python for ML

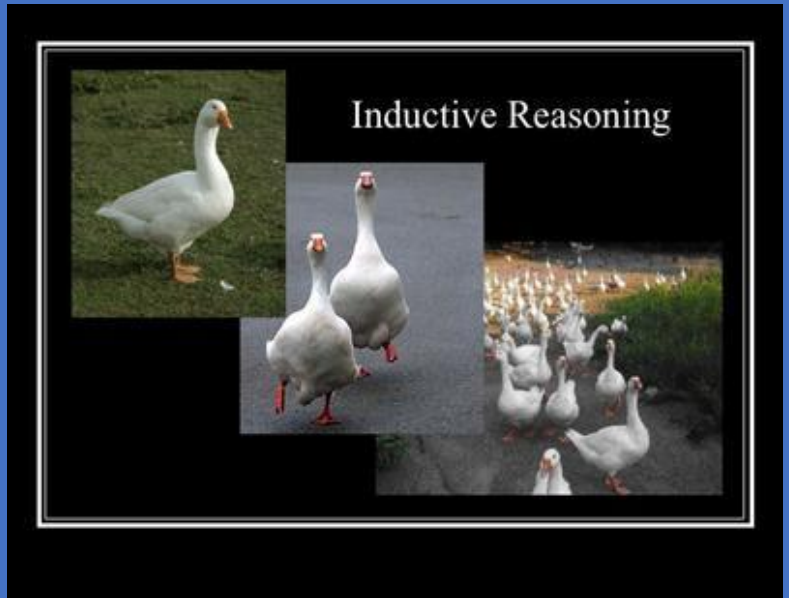
- Hands On

3.Decision Tree Learning

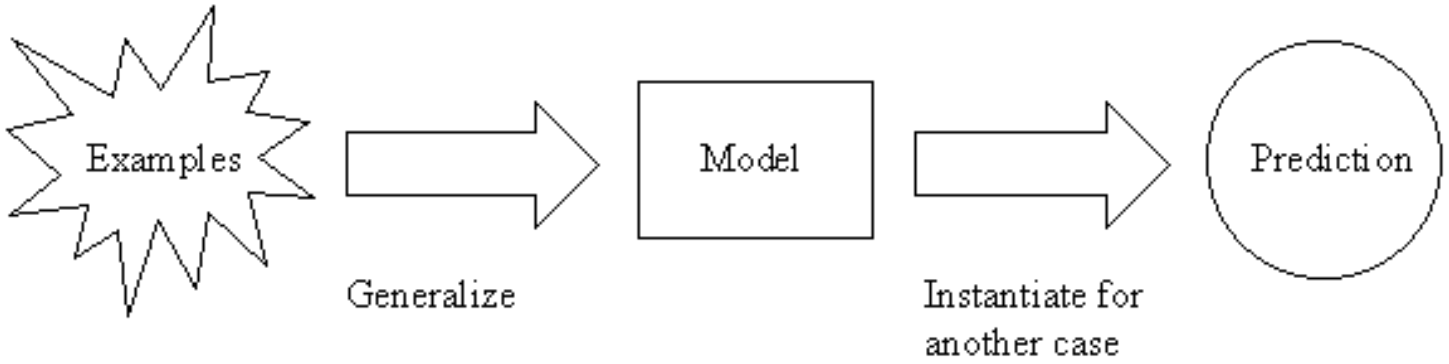
Topics

1. Decision Tree Learning
2. Decision Trees
3. Decision Tree Representation
4. Appropriate Problems for Decision Tree Learning
5. Basic Decision Tree Learning Algorithm (ID3)
6. Advantages and Disadvantages of ID3 based Decision Tree Learning

1. Decision Tree Learning



- **Decision tree learning is one of the most widely used and practical methods for inductive inference. It is a method for approximating discrete-valued target functions, in which the learned function is represented by a decision tree.**

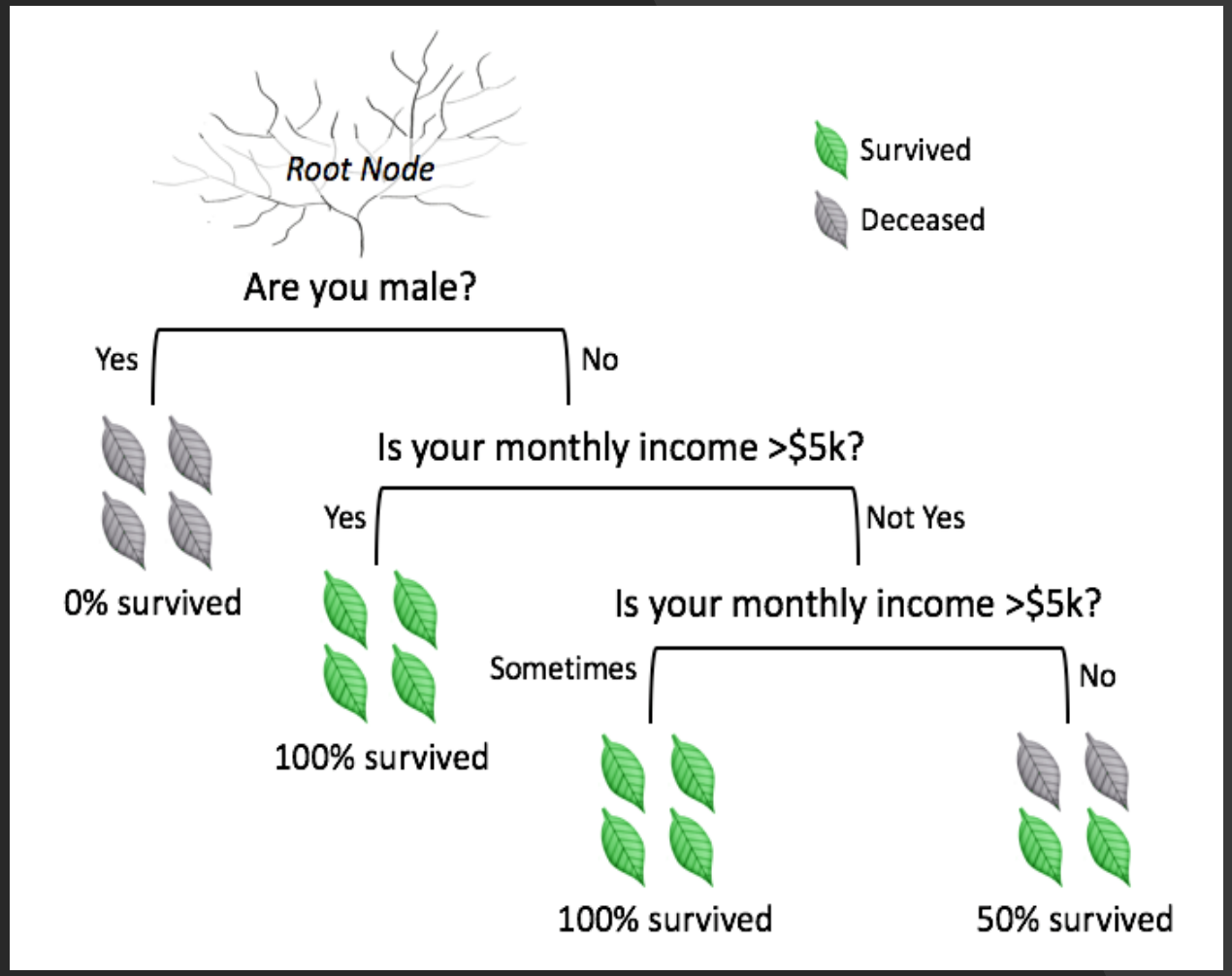


Inductive inference is the process of reaching a general conclusion from specific examples.

- **Is a type of supervised machine learning that is mostly used in classification .**

2. Decision Trees

- A decision tree is a graphical representation of all possible solutions to decisions based on certain conditions.
- A tree structured classifier with two types of nodes :
  - **Decision Nodes** and
  - **Leaf Nodes**.



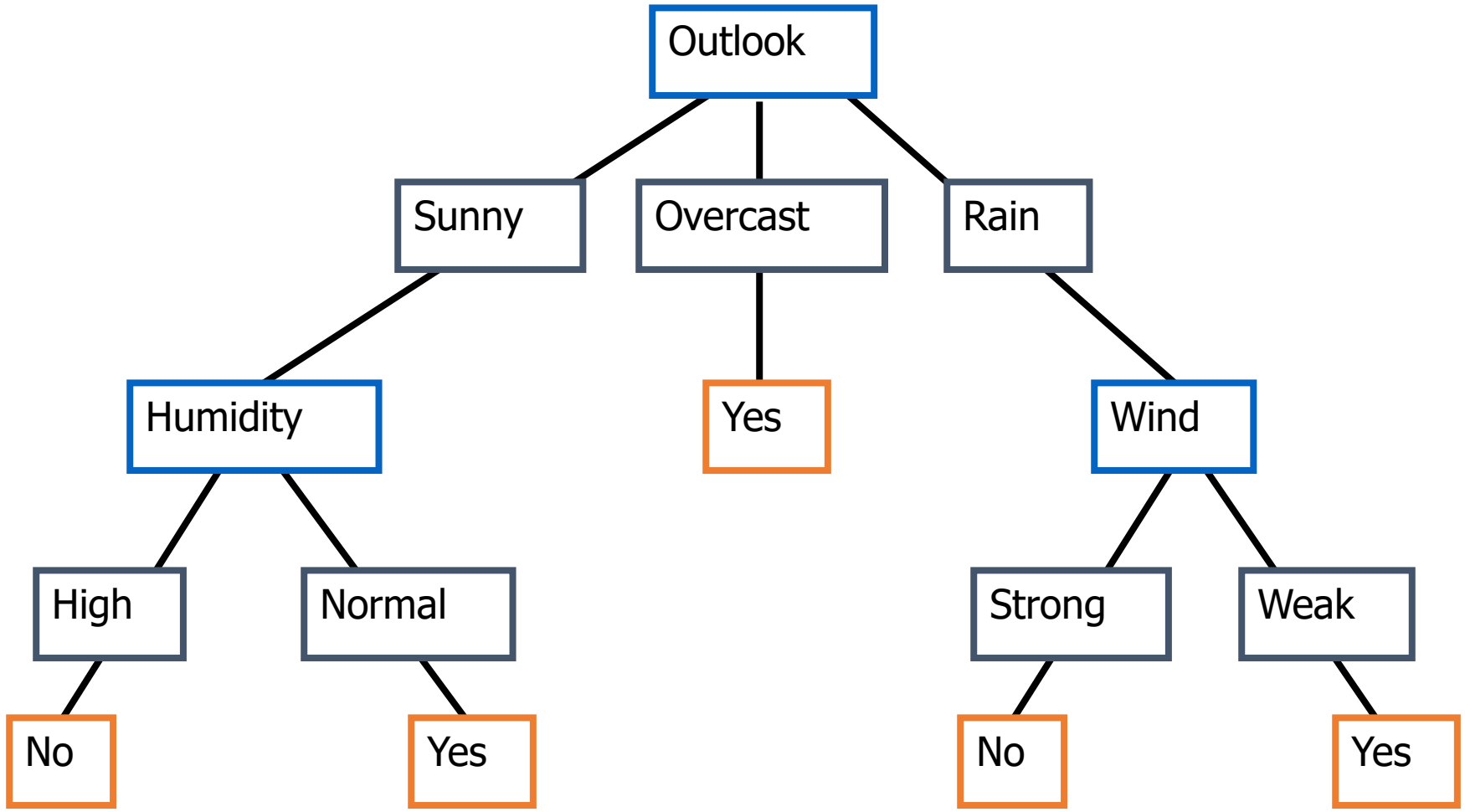
3. Decision Tree Representation

- **Decision trees** classify instances by sorting them down the tree *from the root to some leaf node*, which provides the classification of the instance.
- In the **decision tree representation**:
  - An inner node represents an attribute
  - Edge / branch represents an attribute value
  - Leaf represents a class
  - The paths from root to leaf represent **classification rules**.
- **Decision trees represent a disjunction of conjunctions.**
  - Each path from root to a leaf is a conjunction of attribute tests.
  - The tree itself is a disjunction of these conjunctions.

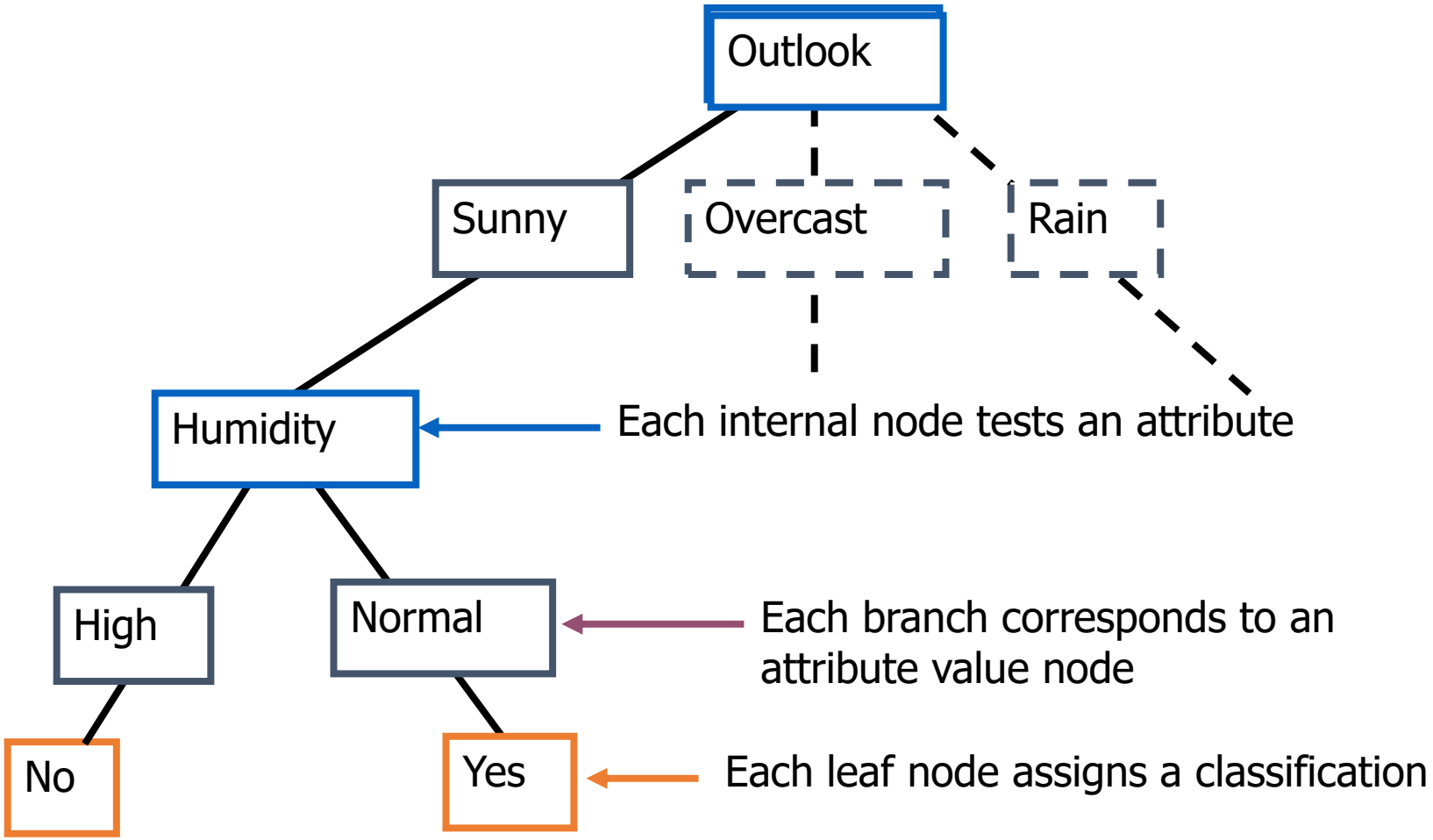
Training Examples (Data Set)

Day	Outlook	Temp.	Humidity	Wind	Play Tennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Weak	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cold	Normal	Weak	Yes
D10	Rain	Mild	Normal	Strong	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Decision Tree for PlayTennis

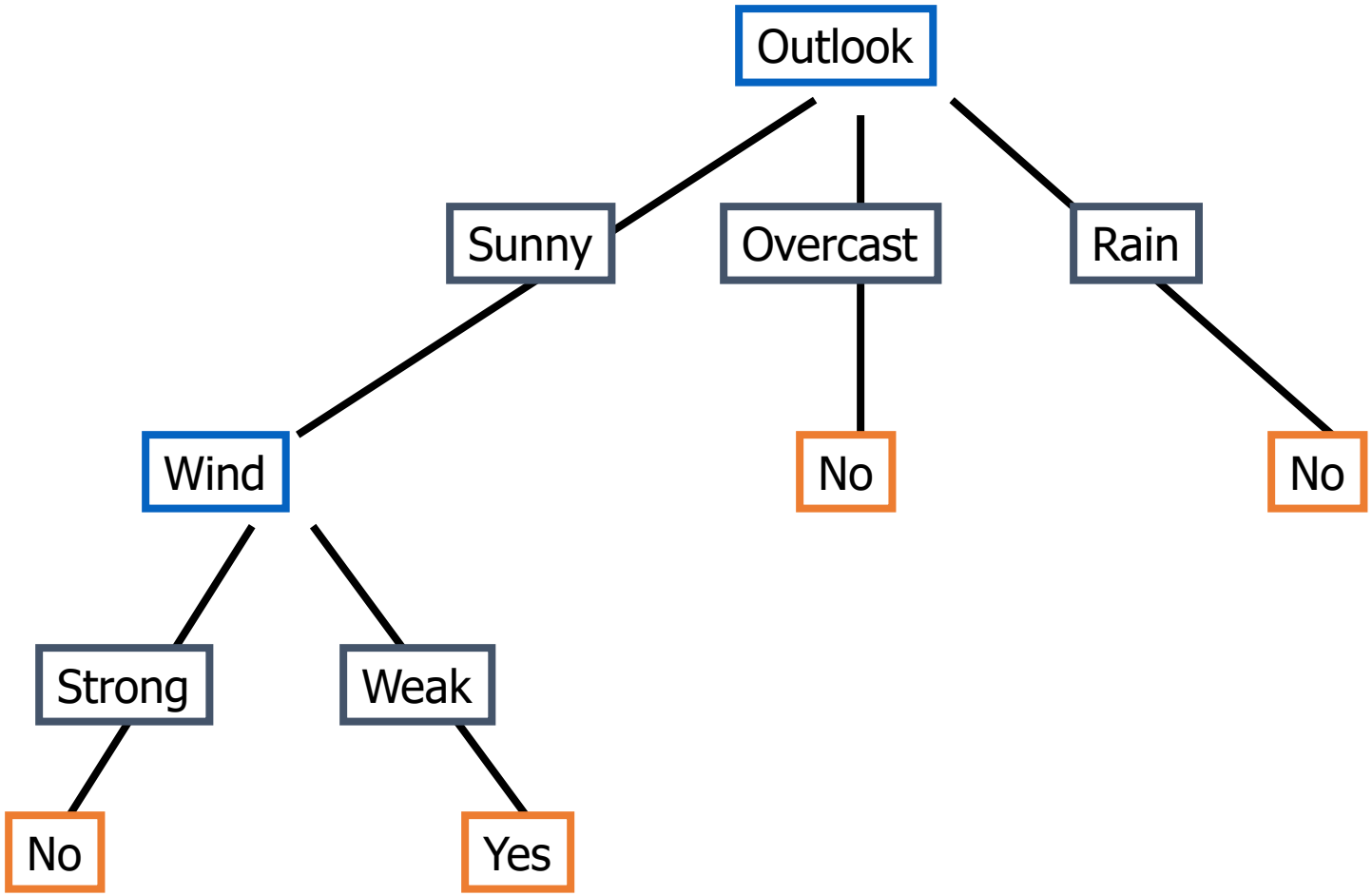


Decision Tree for PlayTennis



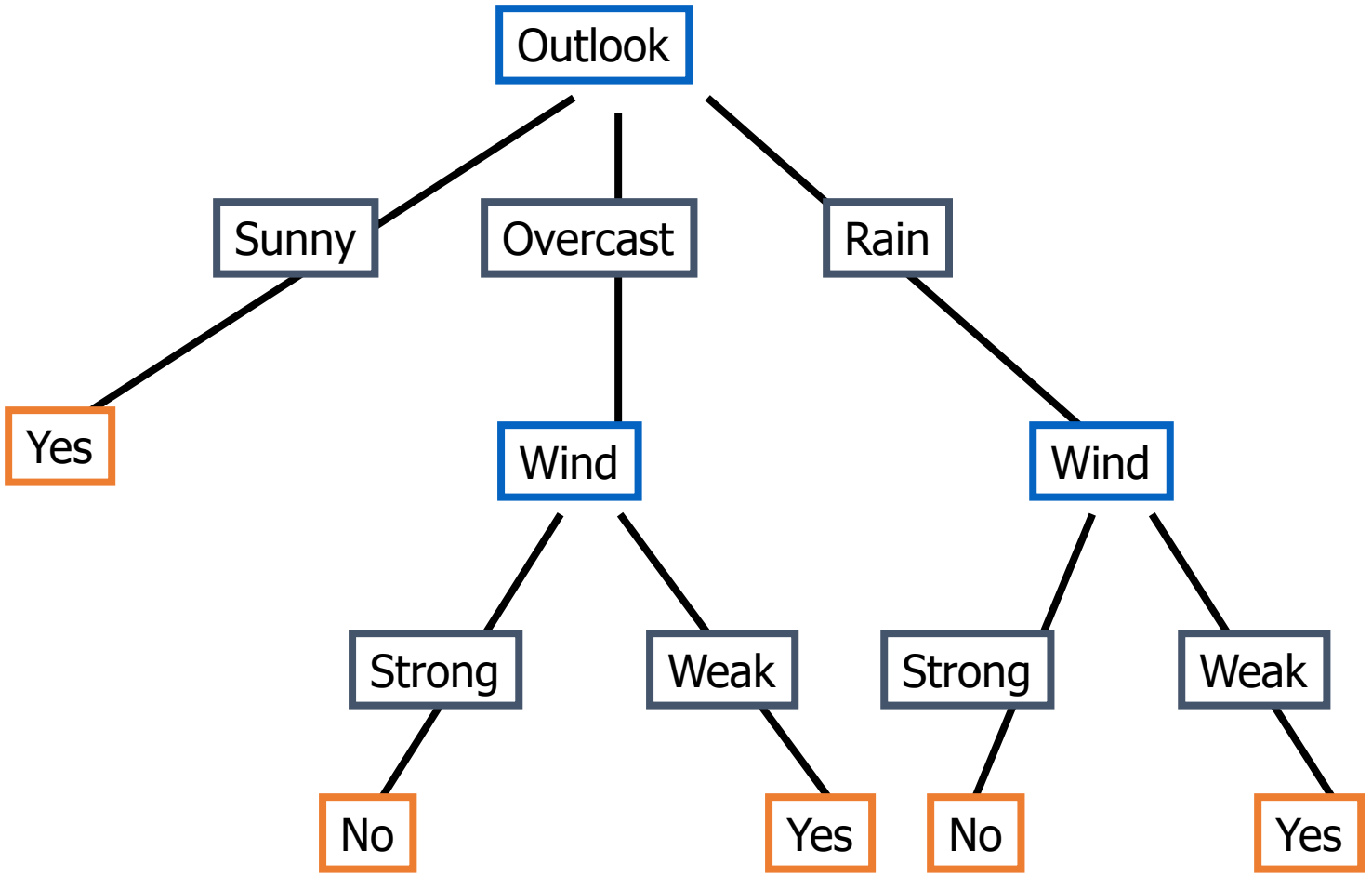
Decision Tree for Conjunction

Outlook=Sunny $\wedge$ Wind=Weak



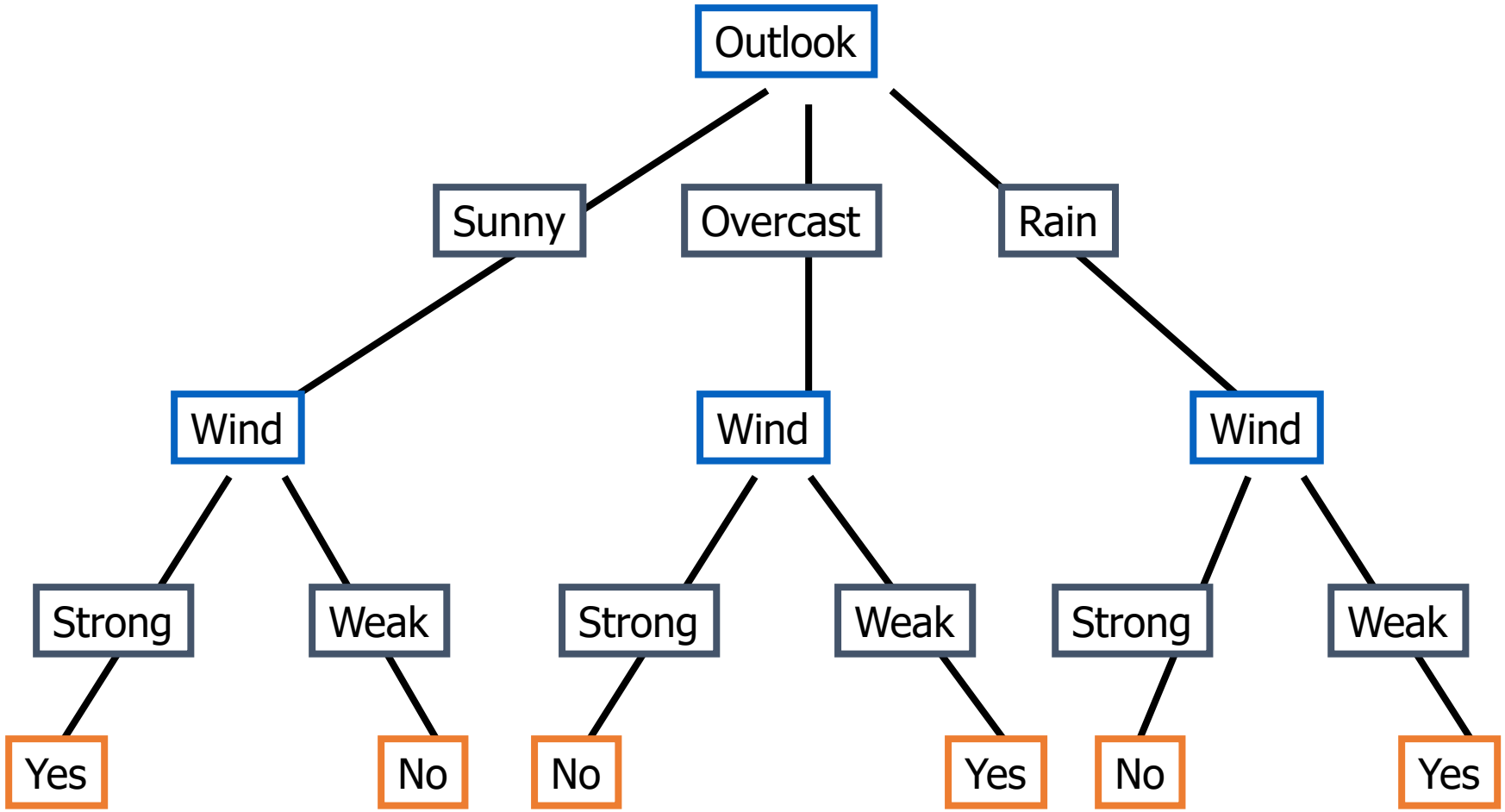
Decision Tree for Disjunction

Outlook=Sunny ∨ Wind=Weak



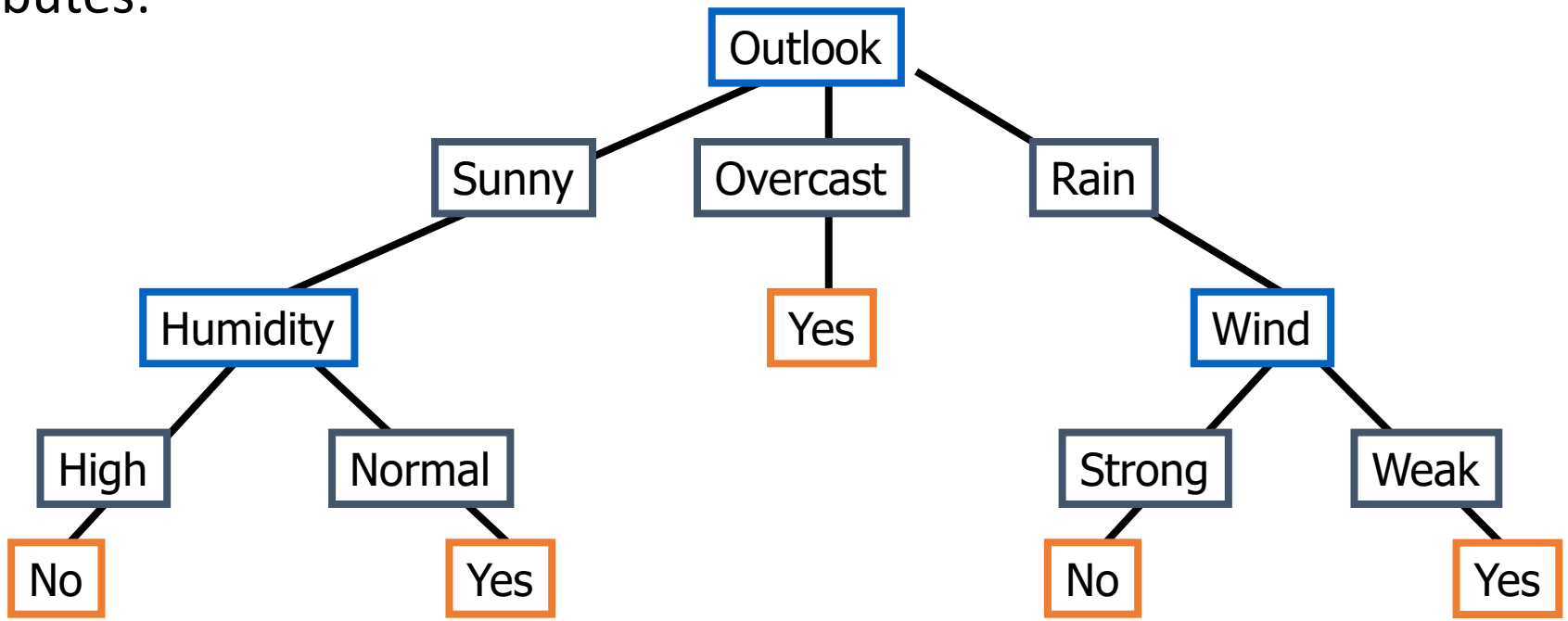
Decision Tree for XOR

Outlook = Sunny XOR Wind = Weak



Decision Tree Expressivity

- Decision trees represent a disjunction of conjunctions on constraints on the value of attributes:

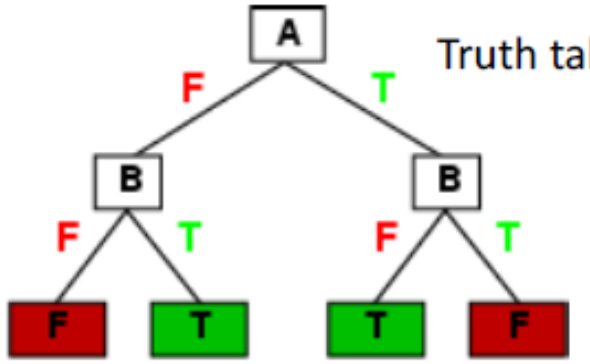


(Outlook=Sunny ∧ Humidity=Normal)
∨ (Outlook=Overcast)
∨ (Outlook=Rain ∧ Wind=Weak)

Expressiveness

- Decision trees can represent any boolean function of the input attributes

A	B	A xor B
F	F	F
F	T	T
T	F	T
T	T	F



Truth table row → path to leaf

- In the worst case, the tree will require exponentially many nodes

4. Appropriate Problems for Decision Tree Learning

- **Decision tree learning is generally best suited to problems with the following characteristics**:
  - Instances describable by attribute-value pairs. (Hot, Mild, Cold)
  - Target function has discrete output values (yes or no).
  - Disjunctive hypothesis/description may be required.
  - The training data may contain errors/noisy data.
  - The training data may contain missing attribute values.
- **Some examples of problems that fit to these characteristics are:**
  - Medical or equipment diagnosis
  - Credit risk analysis
  - Modelling calendar scheduling preferences

5.Basic Decision Tree Learning Algorithm (ID3)

- The basic decision tree learning algorithm, ID3, employs a top-down, greedy search through the space of possible decision trees, beginning with the question ”**which attribute should be tested at the root of the tree?**”.

Day	Outlook	Temperature	Humidity	Wind	PlayTennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	No
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	Yes
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Description of PlayTennis Training Data Examples

- **No of Data Examples : 14**
  - No of Yes (+) : 9
  - No of No (-) : 5
- **Data Example Attributes and their possible Values :**
  - [Outlook] Values : { Sunny ,Overcast ,Rain }
  - [Temperature] Values : { Hot , Mild , Cold }
  - [Humidity] Values : { High, Normal }
  - [Wind] Values : { Weak, Strong }
- **Target Attribute :**
  - [PlayTennis] Values : {Yes, No}

Choosing the Best Attribute

Key problem: choosing which attribute to split a given set of examples

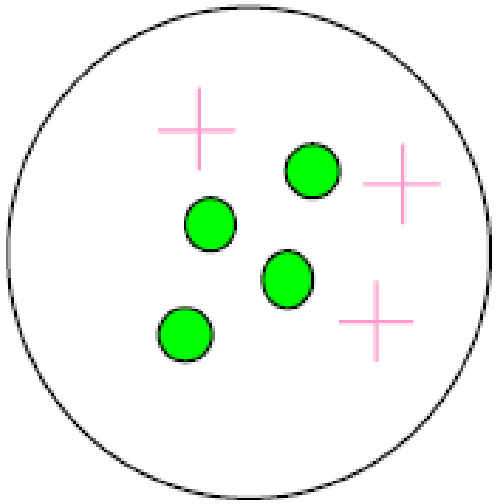
- Some possibilities are:
  - **Random:** Select any attribute at random
  - **Least-Values:** Choose the attribute with the smallest number of possible values
  - **Most-Values:** Choose the attribute with the largest number of possible values
  - **Max-Gain:** Choose the attribute that has the largest expected *information gain*
    - i.e., attribute that results in smallest expected size of subtrees rooted at its children
- The ID3 algorithm uses the Max-Gain method of selecting the best attribute

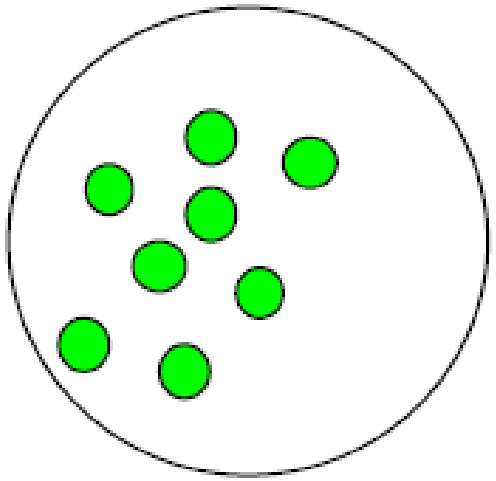
Which attribute is the Best Classifier ?

- The central choice in the ID3 algorithm is selecting which attribute to test at each node in the tree.
  - The attribute must be selected that is most useful for classifying examples .
- The statistical property called *information gain* is the good quantitative measure of the worth of an attribute .
- Information Gain measures how well a given attribute separates the training examples according to their target classification.
- ID3 uses this information gain measure to select among the candidate attributes at each step while growing the tree.
- Information gain uses the notion of *entropy*, commonly used in information theory
- Information gain = expected reduction of entropy

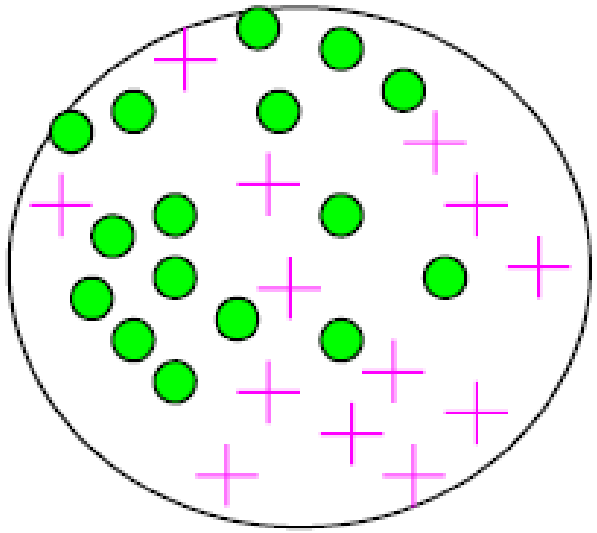
Impurity/Entropy (informal)

– Measures the level of **impurity** in a group of examples

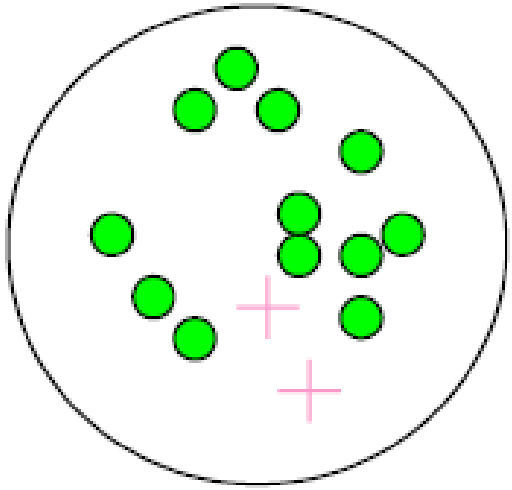




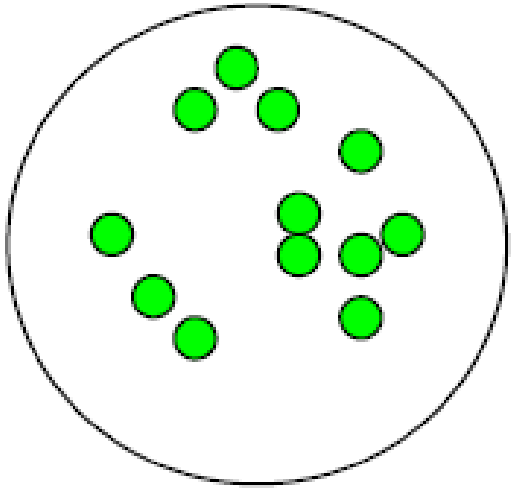
Very impure group



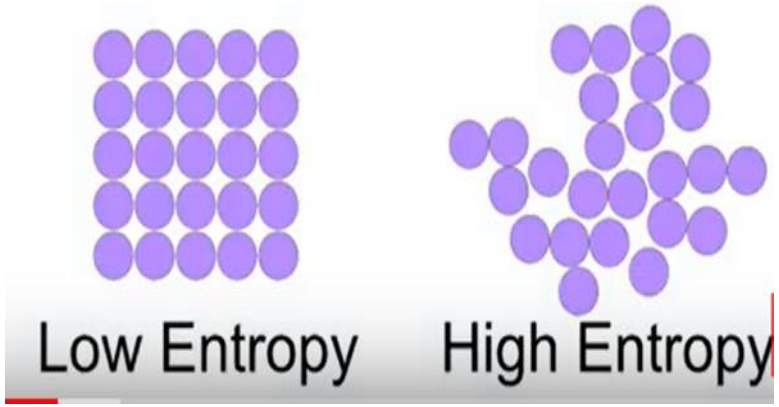
Less impure



Minimum impurity

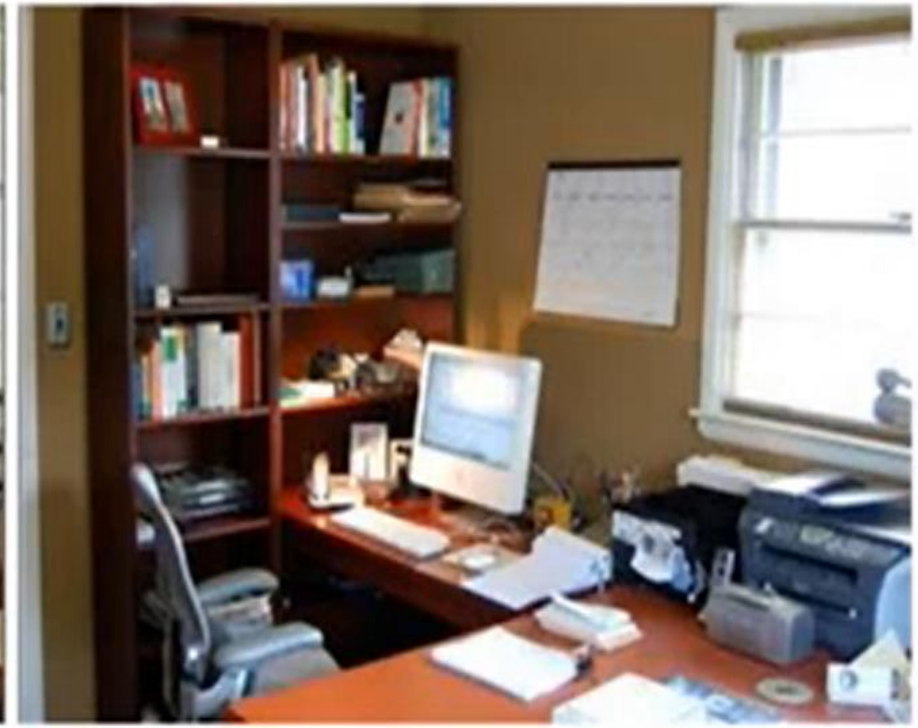


What is Entropy ?



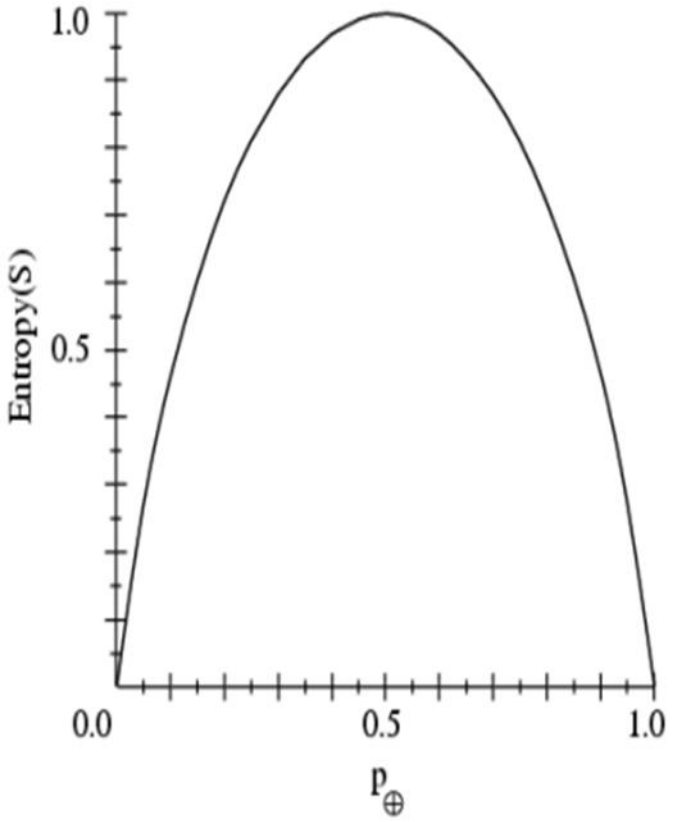
- Define and measures Randomness/impurity in the Data
- Minimum number of bits of information needed to encode the classification of an arbitrary member of Examples Space S.
- If the target attribute can take on **c** possible values the entropy can be as large as $\boldsymbol{log_2\ c}$

High Entropy (messy)



Low Entropy (Clean)

1. Entropy measures Homogeneity of Examples



$$E(S) = \sum_{i=1}^{c} - p_i \log_2 p_i$$

$$\text{Entropy(S)} \equiv -p_\oplus log_2 p_\oplus - p_\ominus log_2 p_\ominus$$

S is a sample of training examples

$p_\oplus$ is the proportion of positive examples in S

$p_\ominus$ is the proportion of negative examples in S

Examples

- E(S) = - $\boldsymbol{p_+ log_2 p_+}$ - $\boldsymbol{p_-}$ $\boldsymbol{log_2}$ $\boldsymbol{p_-}$

- E(9+,5-) = -(9/14)$\boldsymbol{log_2}$(9/14) - (5/14) $\boldsymbol{log_2}$(5/14)
  = 0.940

$$Entropy\ (S) \equiv -p_+ \log_2 p_+ - \quad p\_\log_2 p\_$$

$$Entropy\ ([14+, 0–]) = -14/14 \log_2 (14/14) - 0 \log_2 (0) = 0$$

$$Entropy\ ([9+, 5–]) = -9/14 \log_2 (9/14) - 5/14 \log_2 (5/14) = 0.94$$

$$Entropy\ ([7+, 7–]) = - 7/14 \log_2 (7/14) - 7/14 \log_2 (7/14)$$

$$= 1/2 + 1/2 = 1$$

$[\log_2 1/2 = -1]$

2. Information Gain Measures the expected reduction in Entropy

- **Information Gain** is the *expected* reduction in entropy caused by partitioning the examples on an attribute. The higher the information gain the more effective the attribute in classifying training data.

$$Gain(S, A) \equiv Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$$

$Values(A)$ is the set of all possible values for attribute A
S_v is the subset os S for which attribute A has value v

An Illustrative Example

To illustrate the operation of ID3, let's consider the learning task represented by the below examples.

Day	Outlook	Temperature	Humidity	Wind	PlayTennis
D1	Sunny	Hot	High	Weak	**No**
D2	Sunny	Hot	High	Strong	**No**
D3	Overcast	Hot	High	Weak	**Yes**
D4	Rain	Mild	High	Weak	**Yes**
D5	Rain	Cool	Normal	Weak	**Yes**
D6	Rain	Cool	Normal	Strong	**No**
D7	Overcast	Cool	Normal	Strong	**Yes**
D8	Sunny	Mild	High	Weak	**No**
D9	Sunny	Cool	Normal	Weak	**Yes**
D10	Rain	Mild	Normal	Weak	**Yes**
D11	Sunny	Mild	Normal	Strong	**Yes**
D12	Overcast	Mild	High	Strong	**Yes**
D13	Overcast	Hot	Normal	Weak	**Yes**
D14	Rain	Mild	High	Strong	**No**

Compute the Gain and identify which attribute is the best as illustrated below

- Values (Wind) = Weak, Strong
- S = [9+,5-]
- $S_{weak} = [6+, 2-]$
- $S_{strong} = [3+, 3-]$

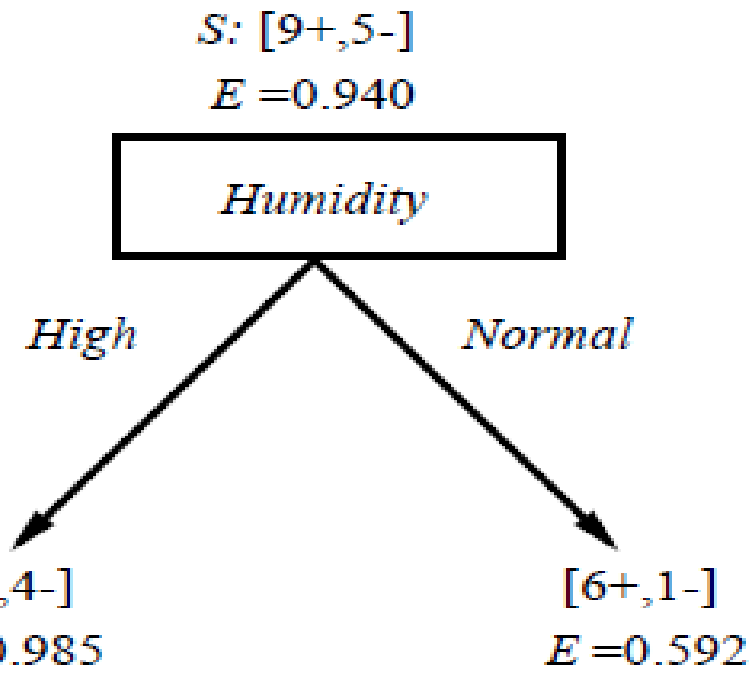
$$\text{Gain}(S, \text{wind}) = \text{Entropy}(S) - \sum_{v \in \{weak,strong\}} (|S_v| / |S|)\ \text{Entropy}(S_v)$$

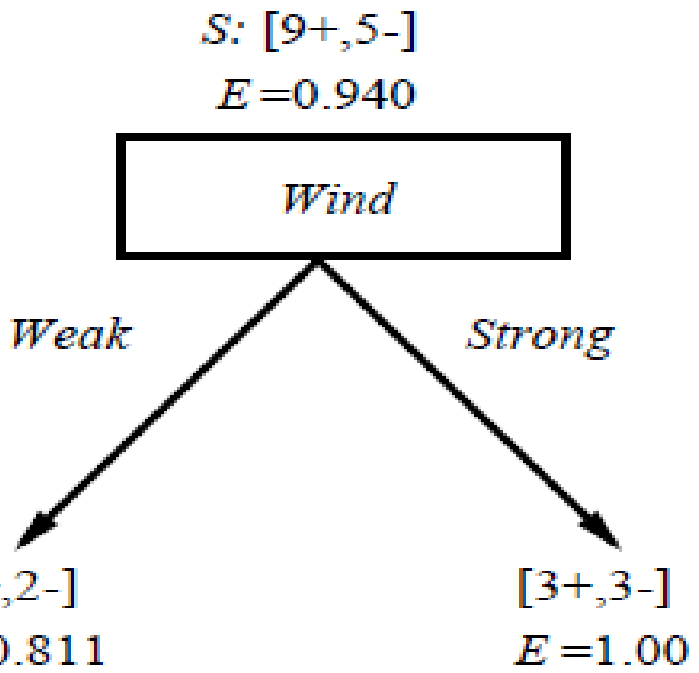
= Entropy (S) – (8/14)Entropy(S_{weak}) – (6/14)Entropy(S_{strong})

= 0.940 – (8/14)0.811 – (6/14)1.00

= 0.048

Which attribute is the best classifier?





Gain (S, Humidity)

= .940 - (7/14).985 - (7/14).592
= .151

Gain (S, Wind)

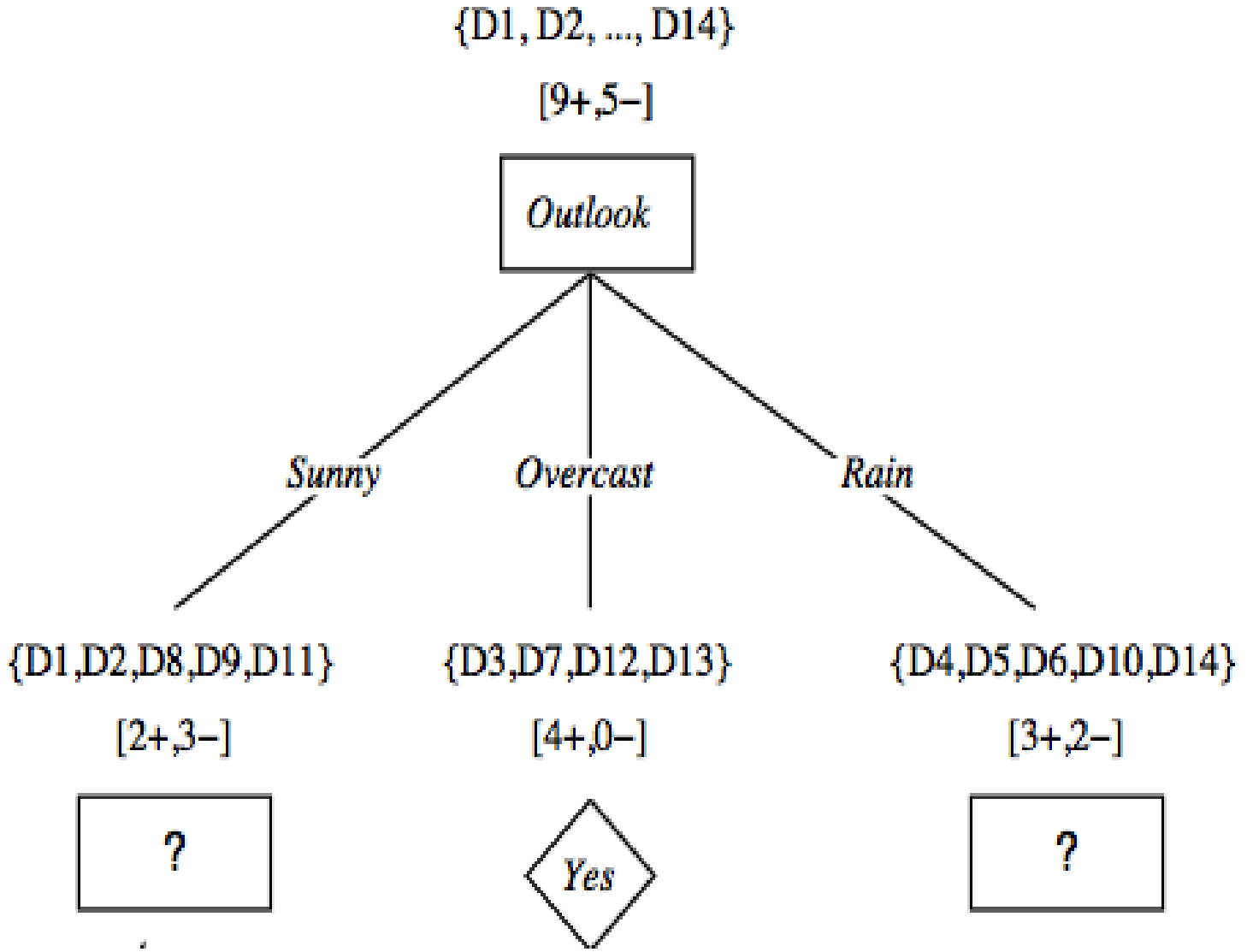
= .940 - (8/14).811 - (6/14)1.0
= .048

Which attribute to test at the root?

- $Gain(S, Outlook) = 0.246$
- $Gain(S, Humidity) = 0.151$
- $Gain(S, Wind) = 0.048$
- $Gain(S, Temperature) = 0.029$

- *Outlook* provides the best prediction for the target
- Lets grow the tree:
  - add to the tree a successor for each possible value of *Outlook*
  - partition the training samples according to the value of *Outlook*

After first step



Second step

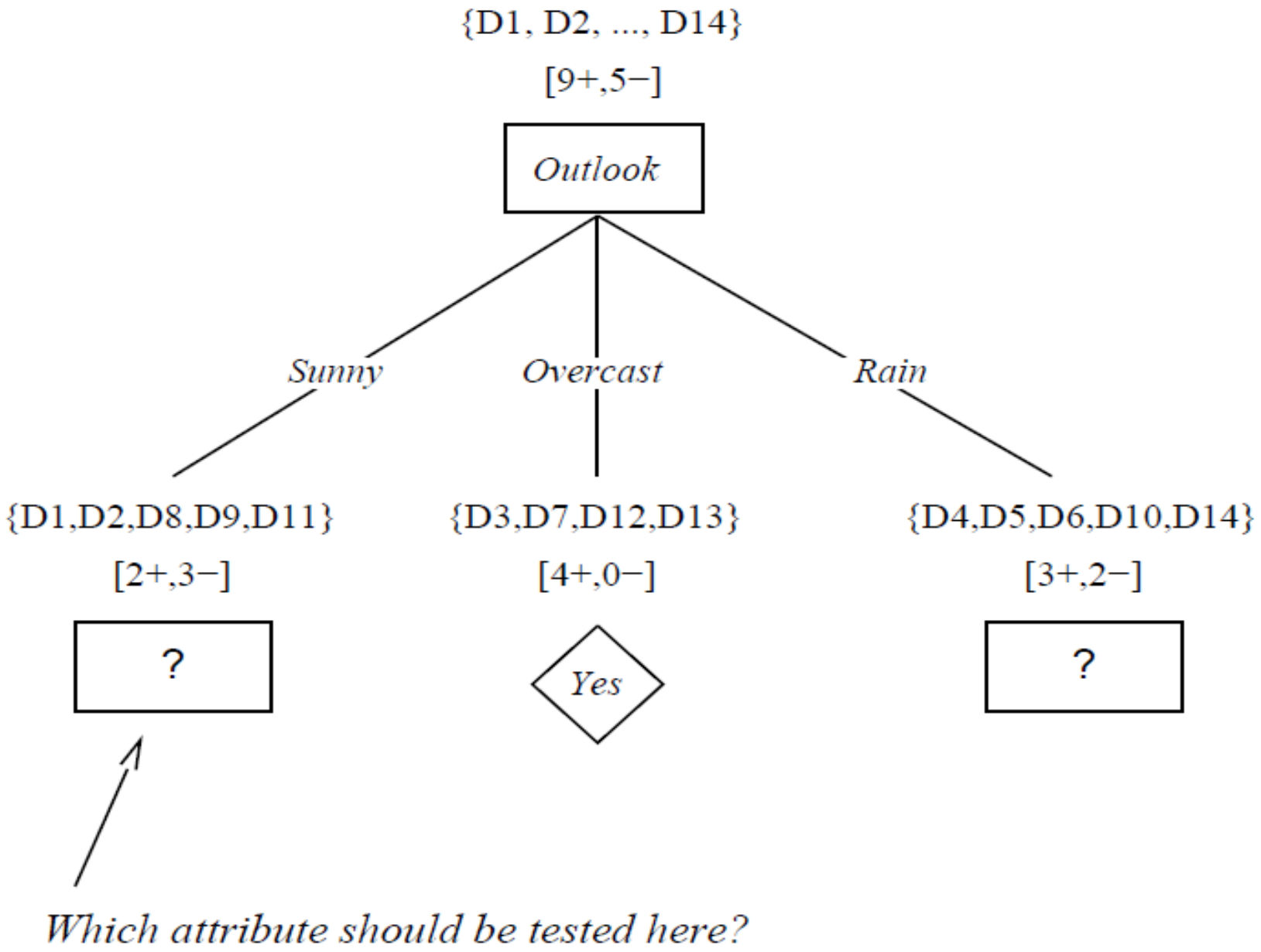
- S*sunny* = {D1,D2,D8,D9,D11}
- Working on *Outlook=Sunny* node:

  $Gain(S_{Sunny}, Humidity) = 0.970 - 3/5 \times 0.0 - 2/5 \times 0.0 = \mathbf{0.970}$

  $Gain(S_{Sunny}, Wind) = 0.970 - 2/5 \times 1.0 - 3.5 \times 0.918 = \mathbf{0\ .019}$

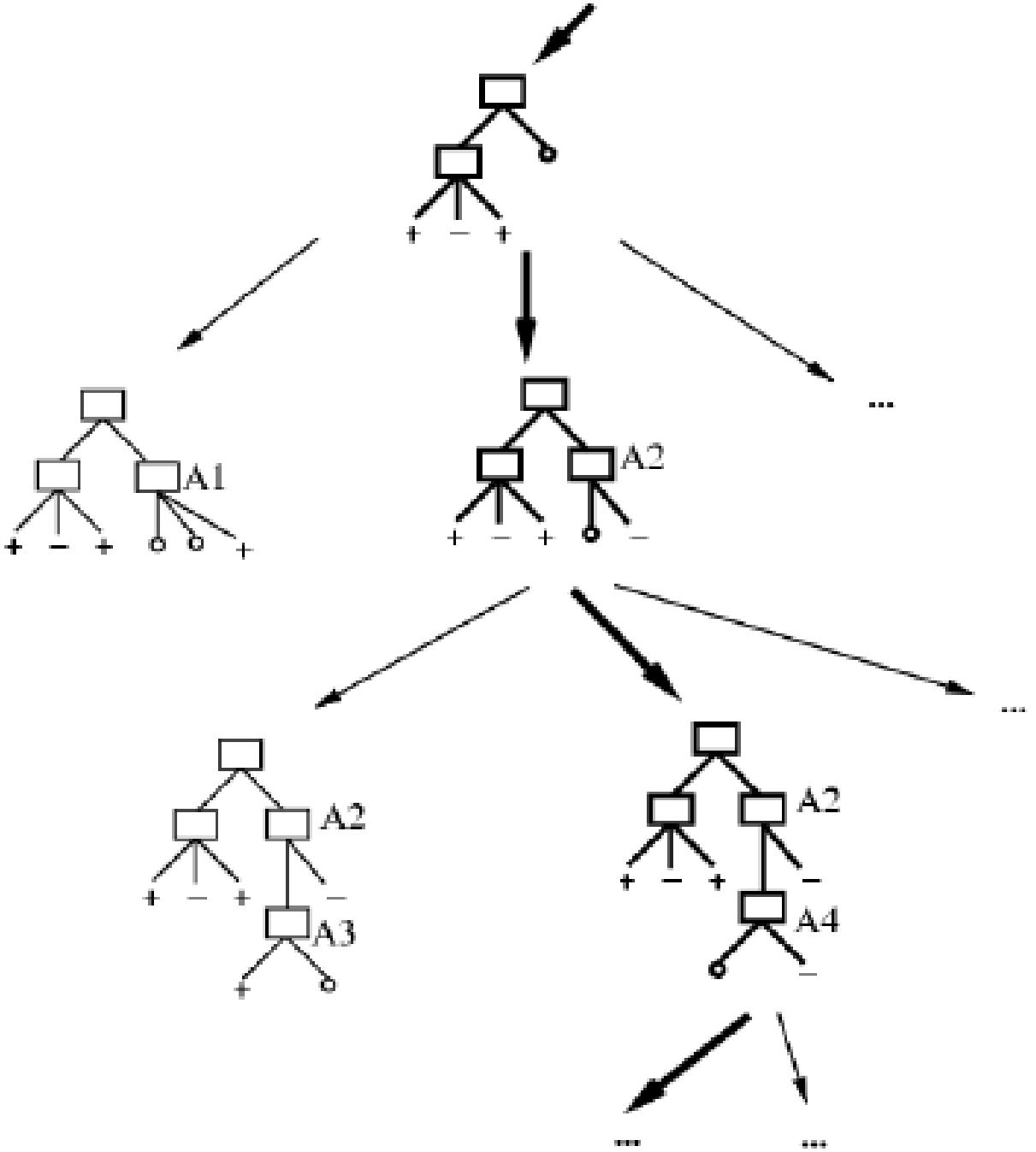
  $Gain(S_{Sunny}, Temp.) = 0.970 - 2/5 \times 0.0 - 2/5 \times 1.0 - 1/5 \times 0.0 = \mathbf{0.570}$
- *Humidity* provides the best prediction for the target
- Lets grow the tree:
  - add to the tree a successor for each possible value of *Humidity*
  - partition the training samples according to the value of *Humidity*

Second and third steps



Which Tree Should We Output?

- **ID3 performs heuristic search through space of decision trees**
- **It stops at smallest acceptable tree. Why?**



Algorithm : ID3(*Training Example, Target Attributes, Attributes*)

- Create *Root* node
- *If* all X's are +, *return Root* with class +
- *If* all X's are –, *return Root* with class –
- *If Attrs* is empty *return Root* with class most common value of *T* in *X*
- *else*

  $A \leftarrow$ best attribute; decision attribute for Root $\leftarrow A$

  For each possible value v_i of *A:*

  - add a new branch below *Root,* for test $A = v_i$

  - $X_i \leftarrow$ subset of *X* with $A = v_i$

  - *If* X_i is empty *then* add a new leaf with class the most common value of *T* in *X*

  ***else* add the subtree generated by ID3(X_i, *T, Attrs* – {*A*})**
- ***return Root***

ID3 - Algorithm

ID3 *(Examples, TargetAttribute, Attributes)*

- Create a *Root* node for the tree
- If all *Examples* are positive, Return the single-node tree *Root*, with label = +
- If all *Examples* are negative, Return the single-node tree *Root*, with label = -
- If *Attributes* is empty, Return the single-node tree Root, with label = most common value of *TargetAttribute* in *Examples*
- Otherwise Begin
  - A ← the attribute from *Attributes* that best classifies *Examples*
  - The decision attribute for *Root* ←A
  - For each possible value, vi, of A,
    - Add a new tree branch below *Root*, corresponding to the test A = vi
    - Let $Examples_{vi}$ be the subset of *Examples* that have value vi for A
    - If $Examples_{vi}$ is empty
      - Then below this new branch add a leaf node with label = most common value of *TargetAttribute* in *Examples*
      - Else below this new branch add the subtree
        ID3($Examples_{vi}$, *TargetAttribute*, *Attributes* – {A})
- End
- Return *Root*

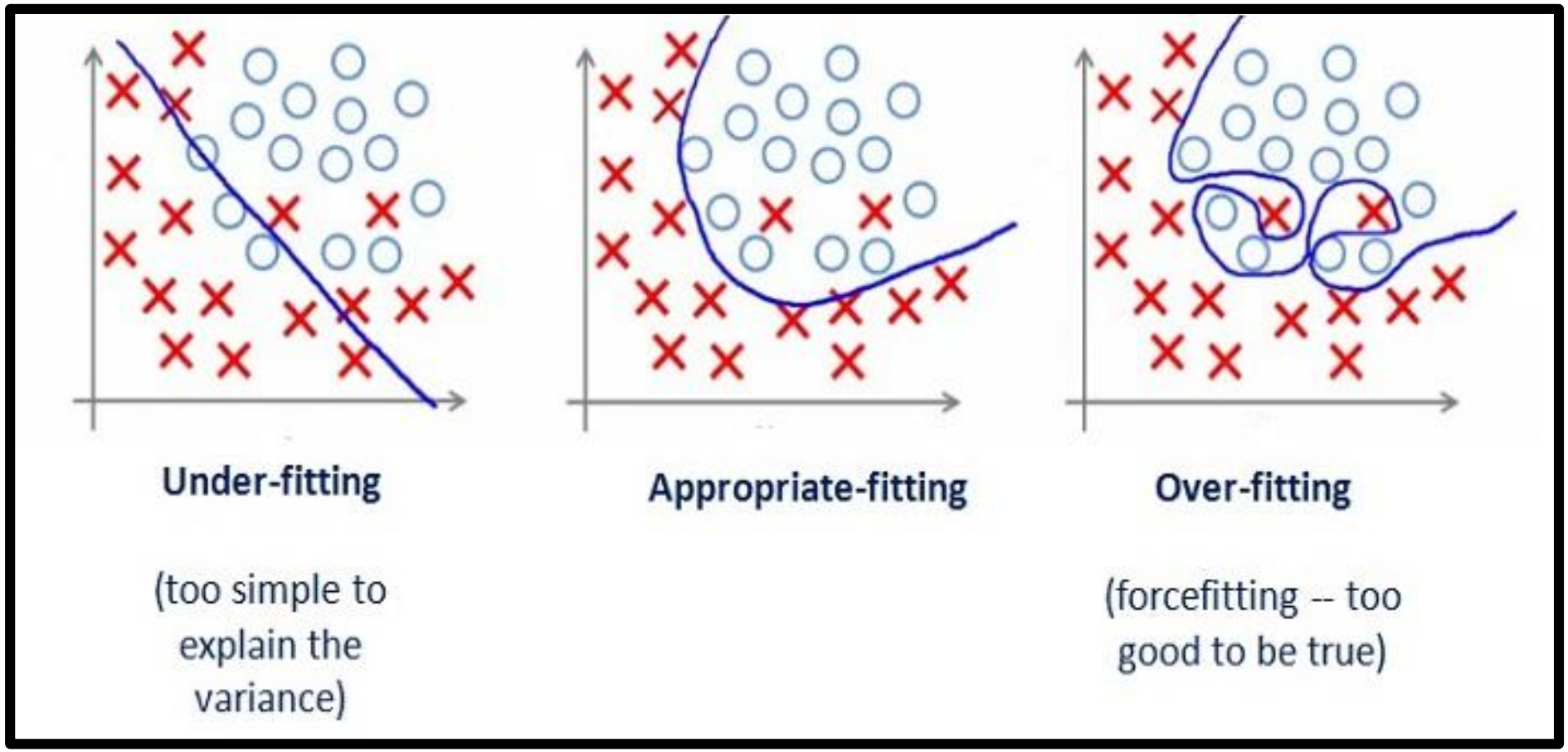
6. Advantages and Disadvantages

Advantages :

- **Computationally Inexpensive**
- **Handles both numerical and categorical attributes**
- **Outputs are easy to interpret**
- **Works well with both linear and nonlinear data**
- **Sensitive to small variations in the training data**
- **Robust with redundant and correlated data**

Disadvantages :

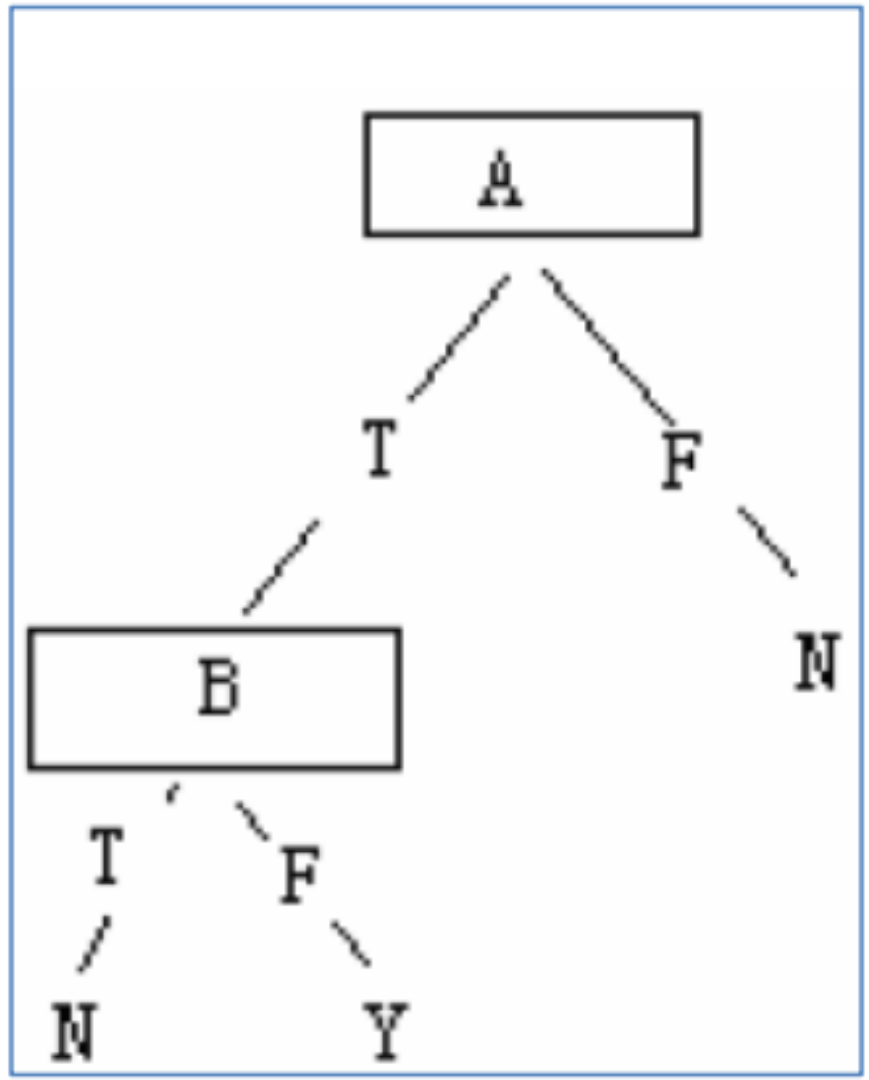
- **Overfitting**
- **Too many Layers**
- **Lack of training Data**
- **Biased Data in training set**
- **Multicollinearity among variables**


Under-fitting
(too simple to explain the variance)
Appropriate-fitting
Over-fitting
(forcefitting -- too good to be true)

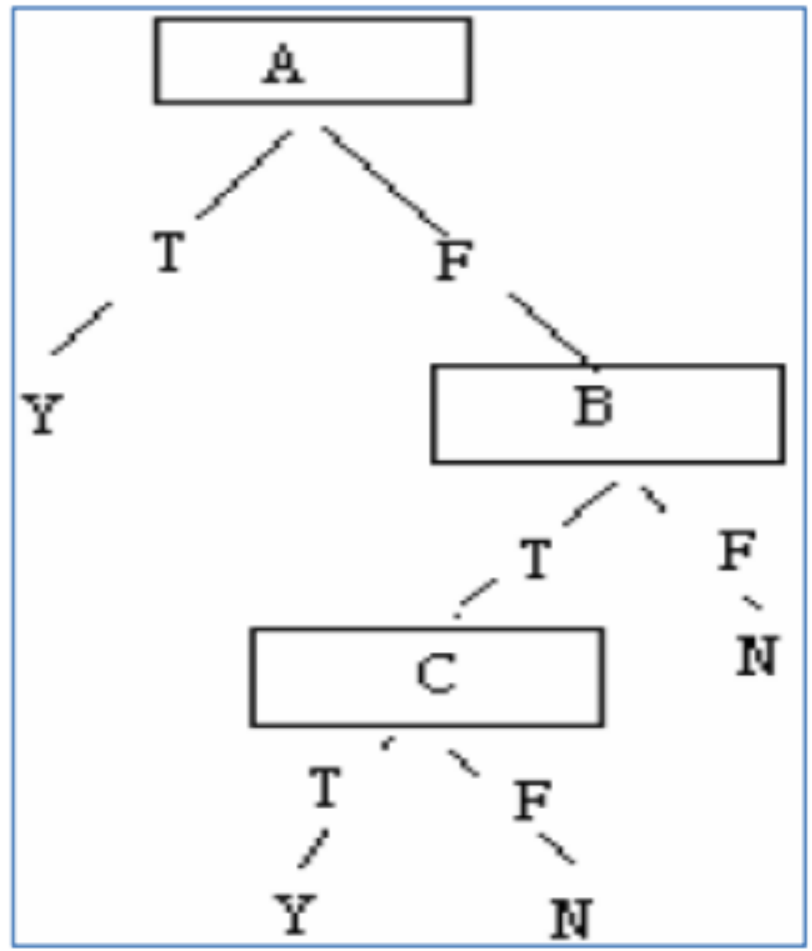
Example : Give decision trees to represent the following Boolean functions:

1) $A \wedge \neg B$
2) $A \vee [B \wedge C]$
3) A XOR B
4) $[A \wedge B] \vee [C \wedge D]$

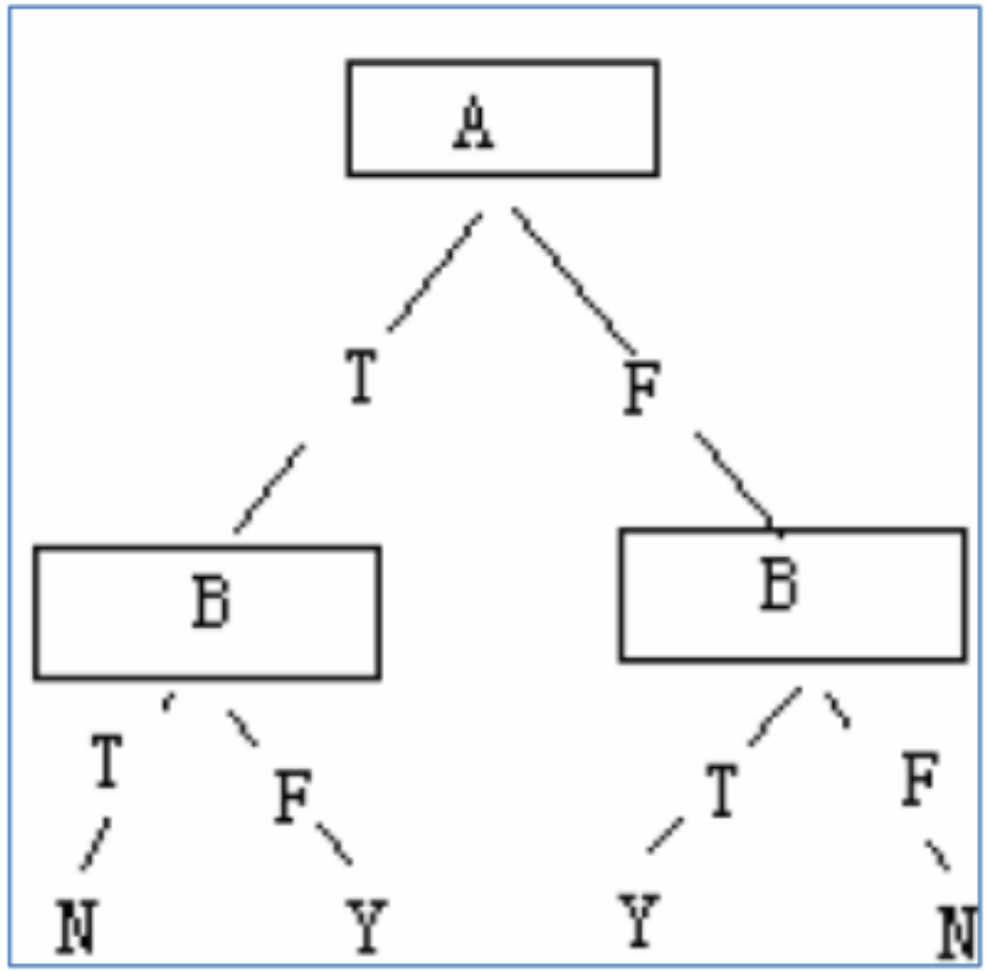
1) $A \wedge \neg B$



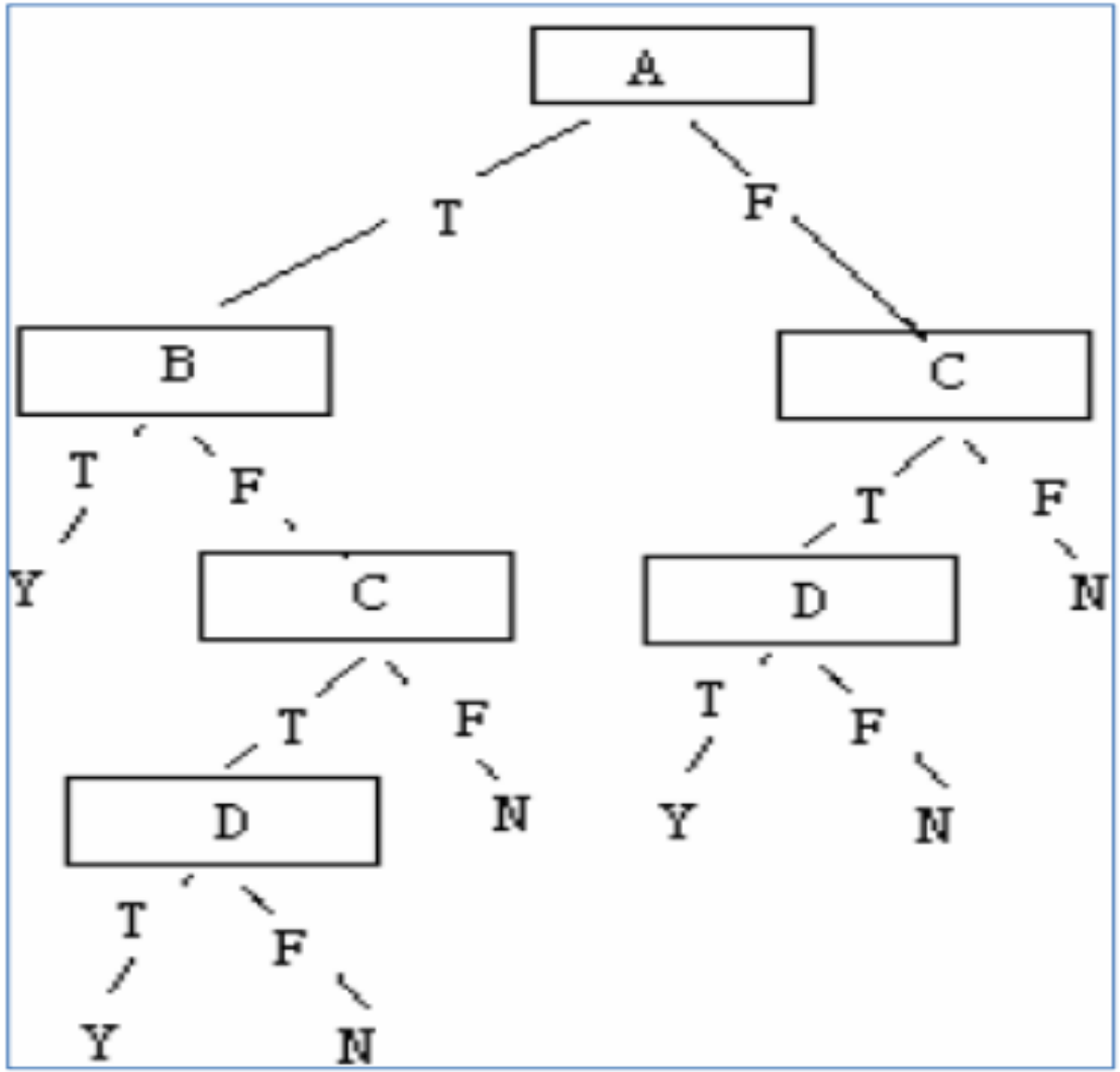
2) $A \vee [B \wedge C]$



3) A XOR B = $(A \wedge \neg B) \vee (\neg A \wedge B)$



4) $[A \wedge B] \vee [C \wedge D]$



2. Consider the following set of training examples:

Example	A1	A2	A3	class
1	T	T	T	+
2	T	T	F	+
3	T	F	T	-
4	T	F	F	+
5	F	T	T	-
6	F	T	F	-
7	F	F	T	+
8	F	F	F	-

A) What is the entropy of this collection of training examples with respect to the target function classification?

- The entropy of this collection of training examples with respect to the target function classification is E(S) = 1
- because it contains equal numbers of positive and negative examples.

B) What is the information gain of feature A2 relative to these training examples?

- The information gain of feature A2 relative to these training examples $G(S,A2) = E(S) - \sum|SA2| / |S| * E(S) = 1 – (4/8 * 1 + 4/8 * 1) = 0$

C) What is the best feature relative to these training examples, using Gain Ratio?

- The best feature relative to these training examples is the feature with the maximum information gain, and in this example any feature can selected because the gain of all features are the same.

4.Machine Learning Lab Programs using Python

https://github.com/profthyagu

Lab Programs

1. Decision tree based ID3 algorithm
2. Backpropagation algorithm to build ANN
3. Naïve Bayesian classifier for a sample training data set stored as a .CSV file
4. Naïve Bayesian classifier to cluster the set of documents
5. Bayesian Network for Medical Data Set
6. EM Algorithm + K Means Algorithm for a set of data stored in.csv file
7. K NN Algorithm for iris data
8. Locally Weighted Regression Algorithm
9. FIND-S algorithm *for a given set of training data examples stored in a .CSV file.*
10. Candidate-Elimination algorithm *for a given set of training data examples stored in a .CSV file*

Lab Program 1:

- Write a program to demonstrate the working of the decision tree based ID3 algorithm. Use an appropriate data set for building the decision tree and apply this knowledge to classify a new sample.

ID3 - Algorithm

ID3(*Examples, TargetAttribute, Attributes*)

- Create a *Root* node for the tree
- If all *Examples* are positive, Return the single-node tree *Root*, with label = +
- If all *Examples* are negative, Return the single-node tree *Root*, with label = -
- If *Attributes* is empty, Return the single-node tree Root, with label = most common value of *TargetAttribute* in *Examples*
- Otherwise Begin
  - A ← the attribute from *Attributes* that best classifies *Examples*
  - The decision attribute for *Root* ←A
  - For each possible value, vi, of A,
    - Add a new tree branch below *Root*, corresponding to the test A = vi
    - Let $Examples_{vi}$ be the subset of *Examples* that have value vi for A
    - If $Examples_{vi}$ is empty
      - Then below this new branch add a leaf node with label = most common value of *TargetAttribute* in *Examples*
      - Else below this new branch add the subtree
        ID3($Examples_{vi}$, *TargetAttribute*, *Attributes* – {A})
- End
- Return *Root*

Source Code

- https://github.com/profthyagu

Lab Program 2

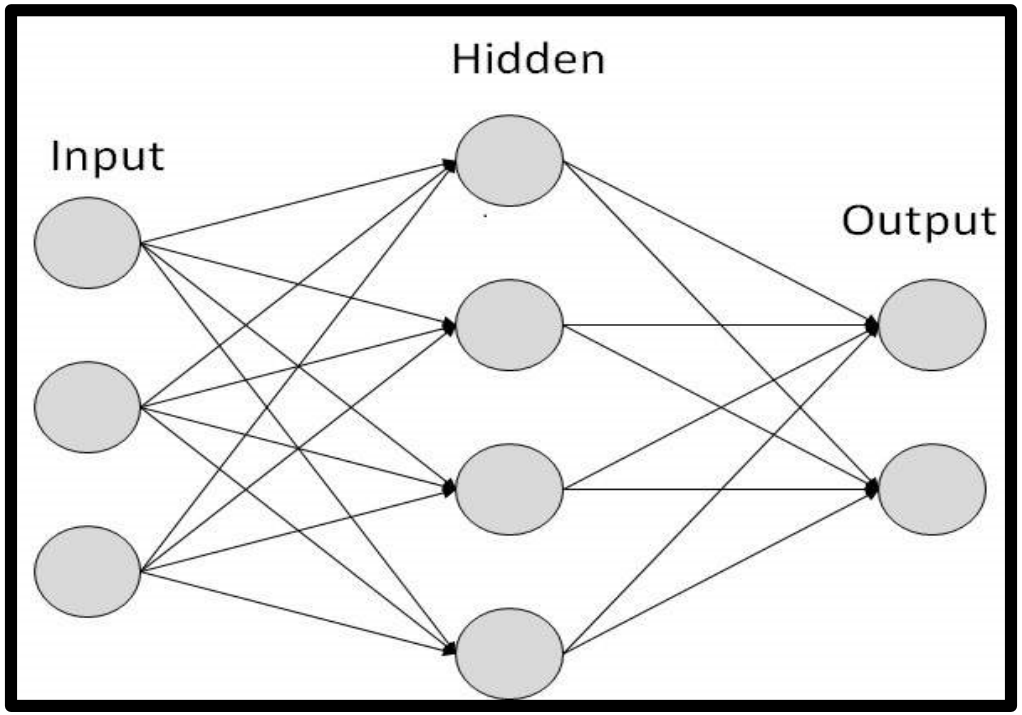
- **Build an Artificial Neural Network by implementing the Backpropagation algorithm and test the same using appropriate data sets.**

Artificial neural networks(ANN/NN)

- An ANN is a computational model based on the structure and functions of biological neural networks.
- An ANN can learn from observing data sets.
- ANN takes data samples rather than entire data sets to arrive at solutions, which saves both time and money.

Artificial neural networks

- ANNs have three layers that are interconnected.
- The first layer consists of input neurons. These neurons send data on to the second layer (Hidden) , which in turn sends the data to the third layer (Output).

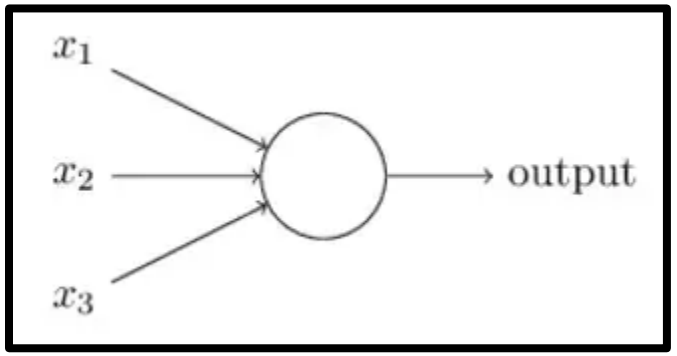


Perceptrons

- **Perceptrons** are single-layer feedforward networks
- Each output unit is independent of the others
- Can assume a single output unit
- Activation of the output unit is calculated by:
- $O = \text{Step}_0\left(\sum_{\mathbf{j}} W_j x_j\right)$

where x_j is the activation of input unit j, and we assume an additional weight and input to represent the threshold

Perceptrons



- A Perceptron is a type of artificial neuron which takes in several binary inputs x1, x2, … , xn and produces a single binary output.
- In order to compute an output, here's what you could do (O = Output):
  a) Sum up the inputs. O = x1 + x2 + x3
  b) Apply a linear mathematical operation to the inputs. O = (x1 * x2) + x3

Note : Thr approach (b) can have its output as O = x3, if x1 or x2 or both are equal to zero. If only one of them is equal to 0, this can lead to a loss of information as the input value gets multiplied by 0.

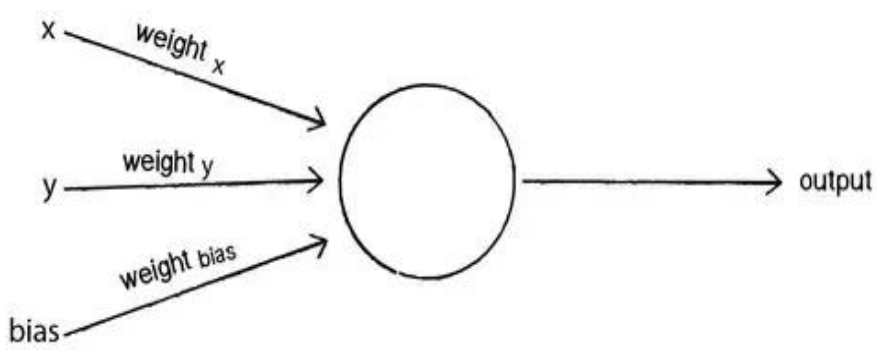
- The simple approach (a), is partially correct and what we can do to make it fully correct.
- Approach (a) sure takes into account all the inputs without one being immediately affected by the other. However, it does not take in the relative importance of the inputs.

What does weight mean in terms of neural networks?

- Consider a simple example where you want to make a perceptron for predicting whether it will rain today or not. You have a binary output as O, which can take values of 0 or 1 and inputs x1 and x2.
- Let x1 be 1 if the weather is humid today, 0 if the opposite.
- Let x2 be 1 if you are wearing a red shirt today and 0 if not.
- We can see here that wearing a red shirt has almost no correlation with the possibility of rainfall. So, a possible output function can be: O = x1 + **0.1** * x2
  - Here's what the factor **0.1** does. If x2 is 0, 0.1*x2 is still 0, but if x2 is 1, 0.1*x2 will be 0.1, not 1.
  - It basically brings down the importance of the input x2 from 1 to 0.1, and hence, it is called the **'weight'** of the input x2.
  - Consider x2 to be 1 for now. O will still be (0 + 0.1) = 0.1 or (1 + 0.1) = 1.1, i.e. not a binary value.
- In order to make it one, what we can do is use a '**threshold'** for the total value of O.
- We can say, like, O is 1 if (x1 + 0.1 * x2) > 1 and O = 0 if (x1 + 0.1 * x2) < 1. We have thus solved our problem.

What does weight mean in terms of neural networks?

In general, $$\text{output} = \begin{cases} 0 & \text{if } \sum_j w_j x_j \leq \text{ threshold} \\ 1 & \text{if } \sum_j w_j x_j > \text{ threshold} \end{cases}$$



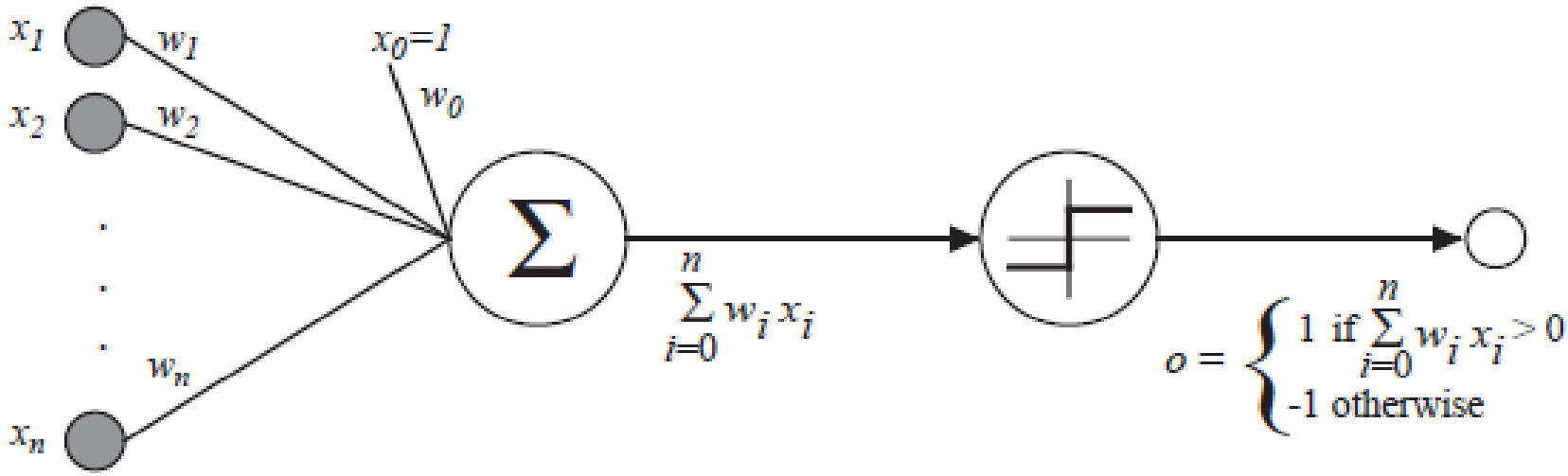
And now making some final notational simplifications, we say

$$\text{output} = \begin{cases} 0 & \text{if } w \cdot x + b \leq 0 \\ 1 & \text{if } w \cdot x + b > 0 \end{cases}$$

Where w = [w1 w2 w3 …. wn]T, x = [x1 x2 x3 …. xn] and b = -(threshold)

- **b** is commonly known as bias.

Note: ‘T’ is the transpose operation. And w.x is matrix multiplication.

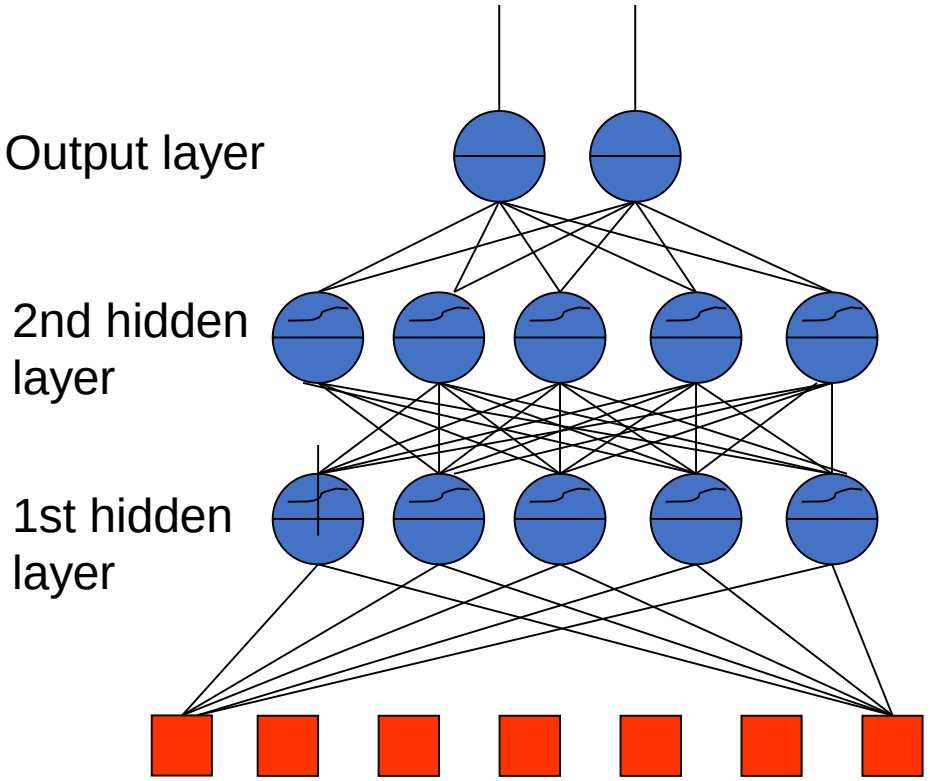


$$o(x_1, \ldots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1 x_1 + \cdots + w_n x_n \geq 0 \\ -1 & \text{otherwise.} \end{cases}$$

Sometimes we'll use simpler vector notation:

$$o(\vec{x}) = \begin{cases} 1 & \text{if } \vec{w} \cdot \vec{x} \geq 0 \\ -1 & \text{otherwise.} \end{cases}$$

Multi-Layer Perceptron



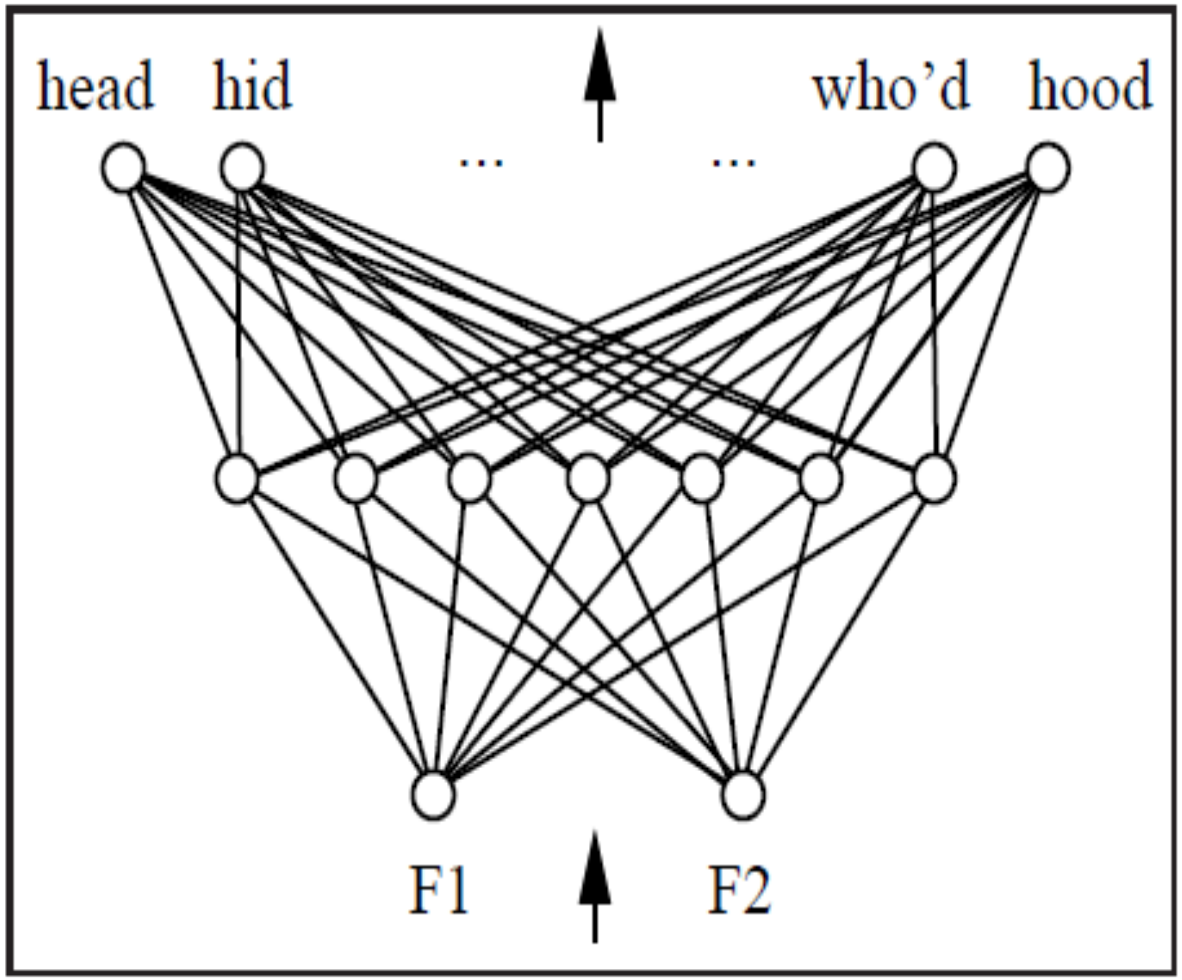
- One or more hidden layers
- Sigmoid activations functions

MULTILAYER NETWORKS AND THE BACKPROPAGATION ALGORITHM

- Single perceptron's can only express linear decision surfaces.
- In contrast, the kind of multilayer networks learned by the **BACKPROPACATION** algorithm are capable of expressing a rich variety of nonlinear decision surfaces.
- For example, a typical multilayer network and decision surface is depicted in Figure
- Here the speech recognition task involves distinguishing among 10 possible vowels, all spoken in the context of "h-d" (i.e., "hid," "had,“ "head," "hood," etc.).

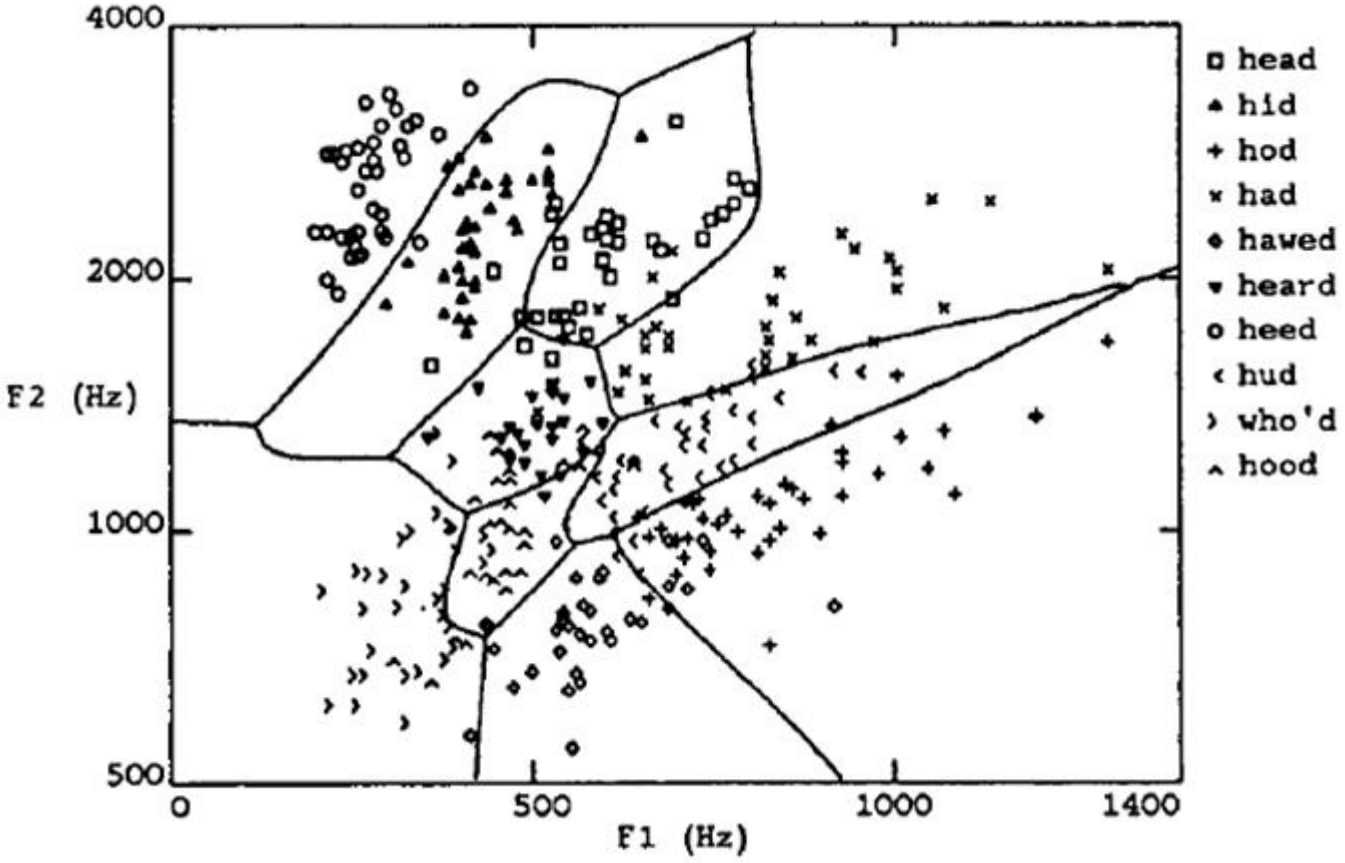
An example

- This network was trained to recognize 1 of 10 vowel sounds occurring in the context “h d” (e.g. “head”, “hid”).
- The inputs have been obtained from a spectral analysis of sound.
- The 10 network outputs correspond to the 10 possible vowel sounds. The net- work prediction is the output whose value is the highest.



An example

- This plot illustrates the highly non-linear decision surface represented by the learned network.
- Points shown on the plot are test examples distinct from the examples used to train the network.

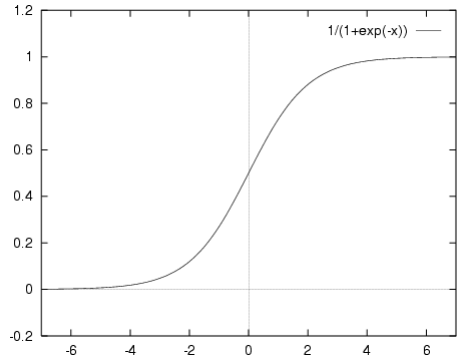


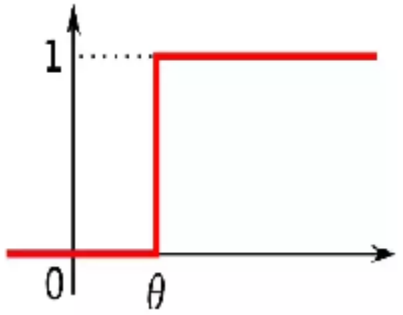
Sigmoid Function

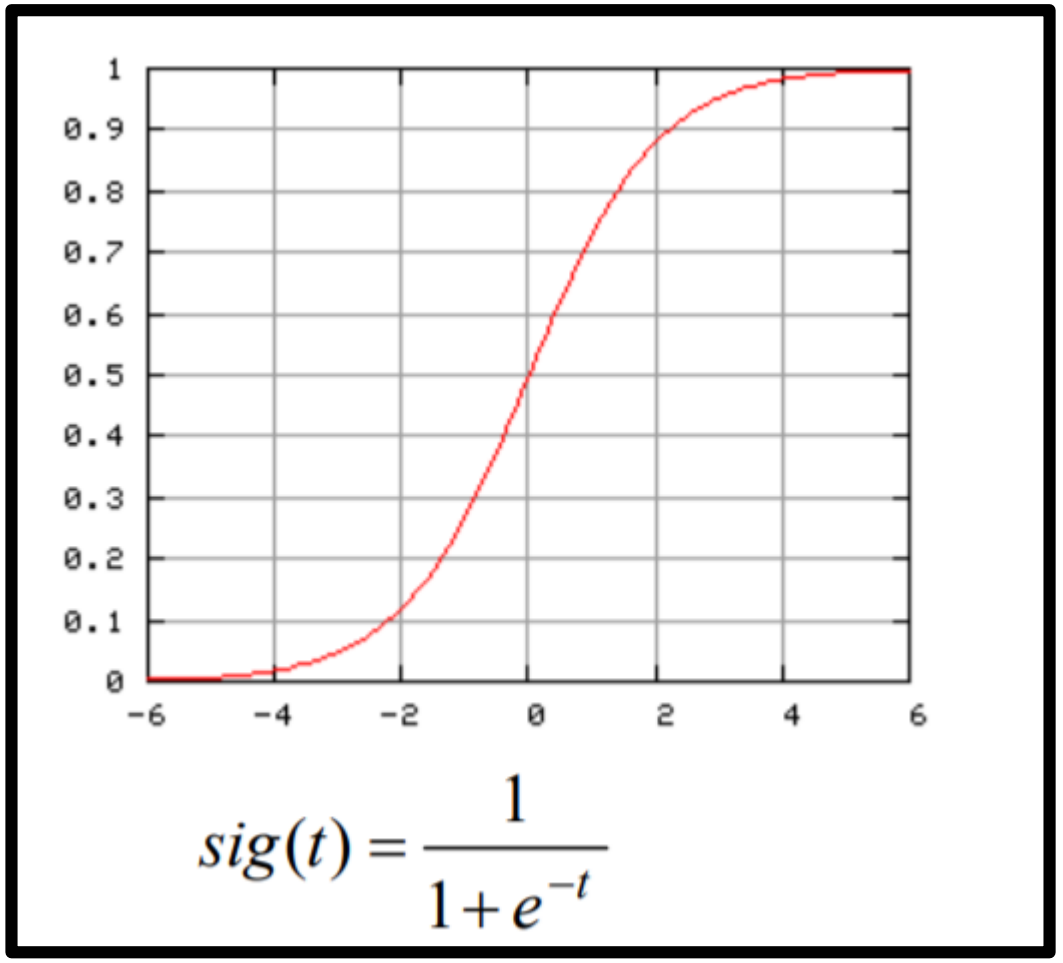
- Sigmoids essentially bring the data within a 0 to 1 range on a smooth curve.

X X X X X X X X X X X X X
X X X X X X X X X X X O X
X X O O X X X X X X X O X
X O O O O X X X X X O O X
X X X O O X X X X X X X X
X X X X X X X X X X X X X

X X X X X X
X X X O O O O
X X O O O O O
O O O O O O O

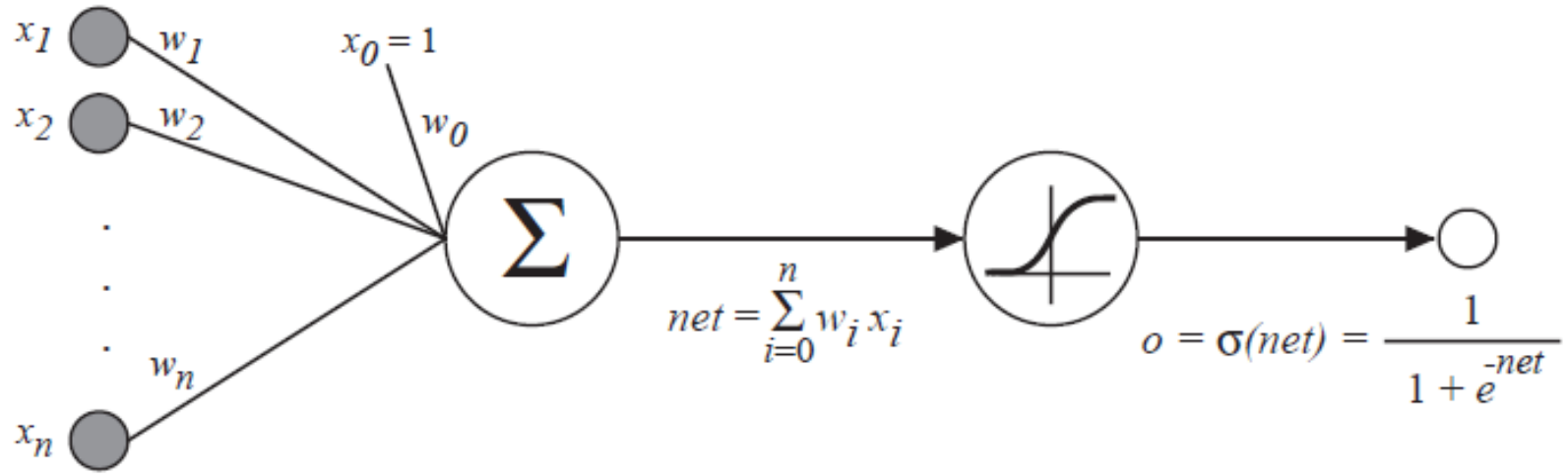






•Thinking=**Sigmoid**, Acting=**Threshold**, in general

Sigmoid Threshold Unit



$\sigma(x)$ is the sigmoid function $\frac{1}{1+e^{-x}}$

Nice property: $\frac{d\sigma(x)}{dx} = \sigma(x)(1 - \sigma(x))$

We can derive gradient descent rules to train

- One sigmoid unit
- *Multilayer networks* of sigmoid units → Backpropagation

Error Gradient for the Sigmoid Unit

$$\begin{aligned}
\frac{\partial E}{\partial w_i} &= \frac{\partial}{\partial w_i} \frac{1}{2} \sum_{d \in D} (t_d - o_d)^2 \\
&= \frac{1}{2} \sum_d \frac{\partial}{\partial w_i} (t_d - o_d)^2 \\
&= \frac{1}{2} \sum_d 2(t_d - o_d) \frac{\partial}{\partial w_i} (t_d - o_d) \\
&= \sum_d (t_d - o_d) \left(-\frac{\partial o_d}{\partial w_i} \right) \\
&= -\sum_d (t_d - o_d) \frac{\partial o_d}{\partial net_d} \frac{\partial net_d}{\partial w_i}
\end{aligned}$$

where $net_d = \sum_{i=0}^{n} w_i x_{i,d}$

But

$$\begin{aligned}
\frac{\partial o_d}{\partial net_d} &= \frac{\partial \sigma(net_d)}{\partial net_d} = o_d(1 - o_d) \\
\frac{\partial net_d}{\partial w_i} &= \frac{\partial (\vec{w} \cdot \vec{x}_d)}{\partial w_i} = x_{i,d}
\end{aligned}$$

So:

$$\frac{\partial E}{\partial w_i} = -\sum_{d \in D} o_d(1 - o_d)(t_d - o_d) x_{i,d}$$

Back Propagation Algorithm for Feed Forward networks

function BackProp (D, η, n_{in}, n_{hidden}, n_{out})

- D is the training set consists of m pairs: $\{(x_i, y_i)^m\}$
- η is the learning rate as an example (0.1)
- n_{in}, n_{hidden} e n_{out} are the numbero of imput hidden and output unit of neural network

Make a feed-forward network with n_{in}, n_{hidden} e n_{out} units
Initialize all the weight to short randomly number (es. [-0.05 0.05])
Repeat until termination condition are verifyed:
For any sample in D:

Forward propagate the network computing the output o_u of every unit u of the network

Back propagate the errors onto the network:

- For every output unit k, compute the error δ_k: $\delta_k = o_k(1-o_k)(t_k-o_k)$
- For every hidden unit h compute the error δ_h: $\delta_h = o_h(1-o_h)\sum_{k \in outputs} w_{kh}\delta_k$
- Update the network weight w_{ji}: $w_{ji} = w_{ji} + \Delta w_{ji}, \quad where \ \Delta w_{ji} = \eta \delta_j x_{ji}$

(x_{ji} is the input of unit j from coming from unit i)

The Backpropagation Algorithm for a feed-forward 2-layer network of sigmoid units, the stochastic version

Idea: Gradient descent over the entire vector of network weights.

Initialize all weights to small random numbers.

Until satisfied, // *stopping criterion* to be (later) defined

for each training example,

1. input the training example to the network, and compute the network outputs
2. for each output unit k:
   $\delta_k \leftarrow o_k(1 - o_k)(t_k - o_k)$
3. for each hidden unit h:
   $\delta_h \leftarrow o_h(1 - o_h) \sum_{k \in outputs} w_{kh}\delta_k$
4. update each network weight w_{ji}:
   $w_{ji} \leftarrow w_{ji} + \Delta w_{ji}$ where $\Delta w_{ji} = \eta \delta_j x_{ji}$,
   and x_{ji} is the ith input to unit j.

Source Code

- https://github.com/profthyagu

LabProgram 3

- **Write a program to implement the naïve Bayesian classifier for a sample training data set stored as a .CSV file. Compute the accuracy of the classifier, considering few test data sets.**

Use cases

Categorizing News

BUSINESS & ECONOMY
Paying service charge at hotels not mandatory

TECHNOLOGY & SCIENCE
The 'dangers' of being admin of a WhatsApp group

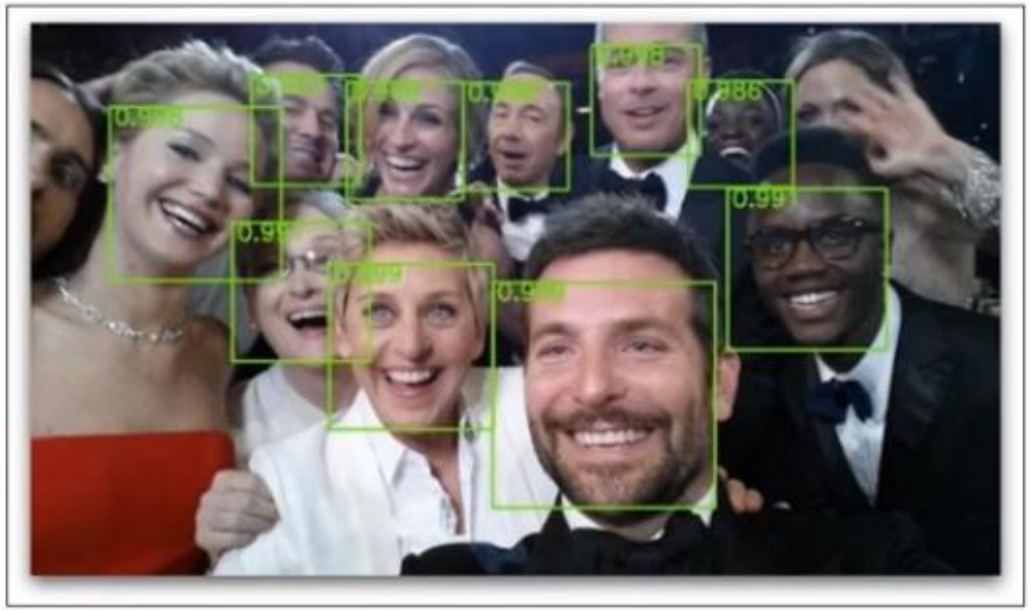
ENTERTAINMENT
This actor stars in Raabta. Guess who?

IPL 2017
Preview: Bullish KKR face depleted Lions

INDIA
Why is Aadhaar mandatory for PAN? SC asks Centre

Email Spam Detection

Face Recognition



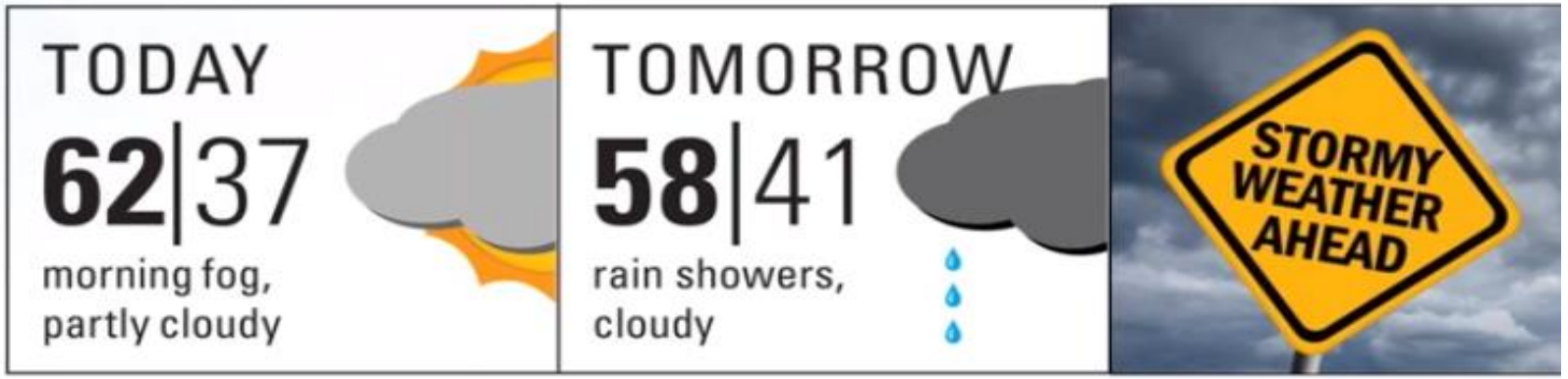
Sentiment Analysis

Use cases

Medical Diagnosis

Digit Recognition

Weather Prediction



Conditional Probability

Definition. The **conditional probability** of an event *A* given that an event *B* has occurred is written: **P(A|B)** and is calculated using:

$P(A|B) = P(A \cap B) / P(B)$ as long as $P(B) > 0$.

Example :

P(A) = 4/52

P(B) = 4/51

P(A and B) = 4/52*4/51= 0.006

$$P\left(\frac{B}{A}\right) = \frac{P(\text{A and B})}{P(A)} = \frac{0.006}{0.077} = 0.078$$

Bayes Theorem

- Bayes' theorem is stated mathematically as the following equation

$$P(h|D) = \frac{P(D|h)P(h)}{P(D)}$$

- $P(h)$ = prior probability of hypothesis h
- $P(D)$ = prior probability of training data D
- $P(h|D)$ = probability of h given D
- $P(D|h)$ = probability of D given h

$$\text{posterior} = \frac{\text{prior} \times \text{likelihood}}{\text{evidence}}$$

Bayes Theorem

- Bayes' theorem is stated mathematically as the following equation

$$P(A \mid B) = \frac{P(B \mid A)\, P(A)}{P(B)},$$

where A and B are events and $P(B) \neq 0$.

- $P(A \mid B)$ is a conditional probability: the likelihood of event A occurring given that B is true.
- $P(B \mid A)$ is also a conditional probability: the likelihood of event B occurring given that A is true.
- $P(A)$ and $P(B)$ are the probabilities of observing A and B independently of each other;

$$\text{posterior} = \frac{\text{prior} \times \text{likelihood}}{\text{evidence}}$$

Alternative form

$$P(A \mid B) = \frac{P(B \mid A)\, P(A)}{P(B \mid A)P(A) + P(B \mid \neg A)P(\neg A)}.$$

$P(\neg A)$ is the corresponding probability of the initial degree of belief against A, where $1 - P(A) = P(\neg A)$

$P(B \mid \neg A)$ is the conditional probability or likelihood, is the degree of belief in B, given that the proposition $\neg A$ is true.

Example of Bayes Theorem $P(A \mid B) = P(B \mid A)P(A) / P(B)$

Consider a drug test that is ***99 percent sensitive***(the true positive rate) and ***99 percent specific*** (the true negative rate). If half a percent ***(0.5 percent)*** of people ***use a drug***, what is the probability a random person with a positive test actually is a user?

$$
\begin{aligned}
P(\text{User} \mid +) &= \frac{P(+ \mid \text{User})P(\text{User})}{P(+)} \\
&= \frac{P(+ \mid \text{User})P(\text{User})}{P(+ \mid \text{User})P(\text{User}) + P(+ \mid \text{Non-user})P(\text{Non-user})} \\
&= \frac{0.99 \times 0.005}{0.99 \times 0.005 + 0.01 \times 0.995} \\
&\approx 33.2\%
\end{aligned}
$$

Naive Bayes classifier /Bayes Rule

Using Bayes' theorem, the conditional probability can be decomposed as

$$p(C_k \mid \mathbf{x}) = \frac{p(C_k)\, p(\mathbf{x} \mid C_k)}{p(\mathbf{x})}$$

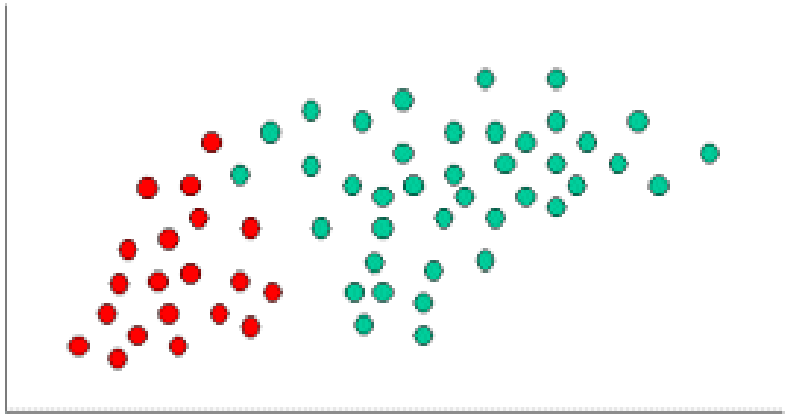
In practice, there is interest only in the numerator of that fraction, because the denominator does not depend on C

The corresponding classifier, a Bayes classifier, is the function that assigns a class label $\hat{y} = C_k$ for some *k* as follows:

$$\hat{y} = \underset{k \in \{1,\ldots,K\}}{\operatorname{argmax}}\ p(C_k) \prod_{i=1}^{n} p(x_i \mid C_k).$$

Naive Bayes classifier

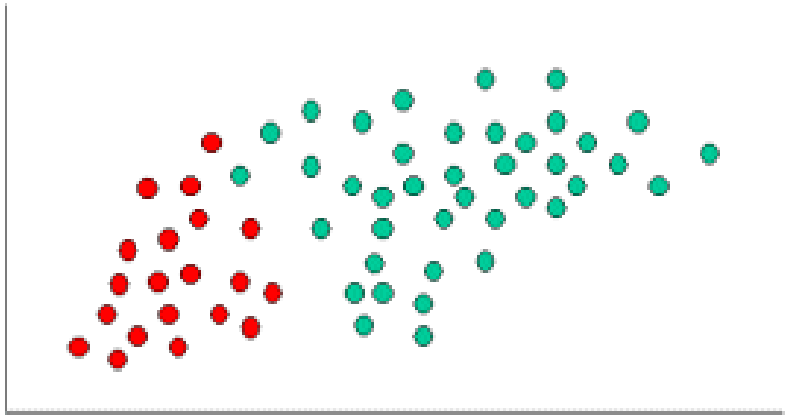
- The Naive Bayes Classifier technique is based on the so-called Bayesian theorem and is particularly suited when the dimensionality of the inputs is high. Despite its simplicity, Naive Bayes can often outperform more sophisticated classification methods.



$$\text{Prior probability for GREEN} \propto \frac{\text{Number of GREEN objects}}{\text{Total number of objects}}$$

$$\text{Prior probability for RED} \propto \frac{\text{Number of RED objects}}{\text{Total number of objects}}$$

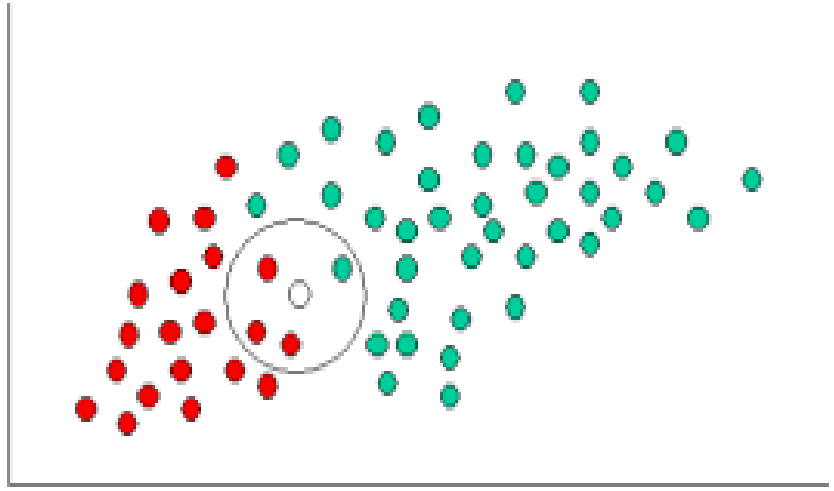
Example :Since there is a total of 60 objects, 40 of which are GREEN and 20 RED, our prior probabilities for class membership are:



$$Prior\ probability\ for\ GREEN \propto \frac{40}{60}$$

$$Prior\ probability\ for\ RED \propto \frac{20}{60}$$

Example :Having formulated our prior probability, we are now ready to classify a new object (WHITE circle).



$$Prior\ probability\ for\ GREEN \propto \frac{40}{60}$$

$$Prior\ probability\ for\ RED \propto \frac{20}{60}$$

From the illustration above, it is clear that Likelihood of X given GREEN is smaller than Likelihood of X given RED, since the circle encompasses 1 GREEN object and 3 RED ones. Thus:

$$Probability\ of\ X\ given\ GREEN \propto \frac{1}{40}$$

$$Probability\ of\ X\ given\ RED \propto \frac{3}{20}$$

Example :

In the Bayesian analysis, the final classification is produced by combining both sources of information, i.e., the prior and the likelihood, to form a posterior probability using the so-called Bayes' rule (named after Rev. Thomas Bayes 1702-1761).

$$Posterior\ probability\ of\ X\ being\ GREEN \propto$$

$$Prior\ probability\ of\ GREEN \times Likelihood\ of\ X\ given\ GREEN$$

$$= \frac{4}{6} \times \frac{1}{40} = \frac{1}{60}$$

$$Posterior\ probability\ of\ X\ being\ RED \propto$$

$$Prior\ probability\ of\ RED \times Likelihood\ of\ X\ given\ RED$$

$$= \frac{2}{6} \times \frac{3}{20} = \frac{1}{20}$$

Event Models

- The assumptions on distributions of features are called the *event model* of the Naive Bayes classifier.
- **For discrete features** like the ones encountered in document classification (include spam filtering), multinomial and Bernoulli distributions are popular.
- For Continuous feature , **Gaussian naive Bayes distributions is popular.**

1. Gaussian naive Bayes

- When dealing with continuous data, a typical assumption is that the continuous values associated with each class are distributed according to a Gaussian distribution.
- Then, the probability *distribution* of v given a class C_k, $p(x = v \mid C_k)$ can be computed by plugging V into the equation for a Normal distribution parameterized by μ_k and σ_k^2.

$$p(x = v \mid C_k) = \frac{1}{\sqrt{2\pi\sigma_k^2}} e^{-\frac{(v-\mu_k)^2}{2\sigma_k^2}}$$

2. Multinomial naive Bayes

Its is used when we have **discrete data** (e.g. movie ratings ranging 1 and 5 as each rating will have certain **frequency** to represent). In text learning we have the count of each word to predict the class or label

$$p(\mathbf{x} \mid C_k) = \frac{(\sum_i x_i)!}{\prod_i x_i!} \prod_i p_{ki}{}^{x_i}$$

The multinomial naive Bayes classifier becomes a linear classifier when expressed in log-space:

$$\begin{aligned} \log p(C_k \mid \mathbf{x}) &\propto \log\left(p(C_k) \prod_{i=1}^{n} p_{ki}{}^{x_i} \right) \\ &= \log p(C_k) + \sum_{i=1}^{n} x_i \cdot \log p_{ki} \\ &= b + \mathbf{w}_k^\top \mathbf{x} \end{aligned}$$

where $b = \log p(C_k)$ and $w_{ki} = \log p_{ki}$.

2. Multinomial naive Bayes

Its is used when we have **discrete data** (e.g. movie ratings ranging 1 and 5 as each rating will have certain **frequency** to represent). In text learning we have the count of each word to predict the class or label.
The Multinomial Naive Bayes's conditional distribution is:

$$p(\mathbf{x}|C=k) = \text{Multinomial}(n, \mathbf{p}_k) = \frac{(\sum_d x_d)!}{\prod_d x_d!} \prod_d {p_{kd}}^{x_d}$$

where $\mathbf{x}$ is feature and C is class. d is the number of dimension of feature.

When using in text domain: given an ith document's word feature $\mathbf{x}_i = (w_1, \ldots, w_d)$, $d = |Vocabulary|$.

The term frequencies can then be used to compute the maximum-likelihood estimate based on the training data to estimate the class-conditional probabilities in the multinomial model:

$$\hat{P}(x_i \mid \omega_j) = \frac{\sum tf(x_i, d \in \omega_j) + \alpha}{\sum N_{d \in \omega j} + \alpha \cdot V}$$

where

- x_i: A word from the feature vector $\mathbf{x}$ of a particular sample.
- $\sum tf(x_i, d \in \omega_j)$: The sum of raw term frequencies of word x_i from all documents in the training sample that belong to class ω_j.
- $\sum N_{d \in \omega j}$: The sum of all term frequencies in the training dataset for class ω_j.
- α: An additive smoothing parameter ($\alpha = 1$ for Laplace smoothing).
- V: The size of the vocabulary (number of different words in the training set).

The class-conditional probability of encountering the text $\mathbf{x}$ can be calculated as the product from the likelihoods of the individual words (under the *naive* assumption of conditional independence).

$$P(\mathbf{x} \mid \omega_j) = P(x_1 \mid \omega_j) \cdot P(x_2 \mid \omega_j) \cdot \ldots \cdot P(x_n \mid \omega_j) = \prod_{}^{m} P(x_i \mid \omega_j)$$

3. Bernoulli naive Bayes

It assumes that all our features are binary such that they take only two values. Means **0s** can represent “word does not occur in the document” and **1s** as "word occurs in the document" .

$$p(\mathbf{x} \mid C_k) = \prod_{i=1}^{n} p_{ki}^{x_i} (1 - p_{ki})^{(1-x_i)}$$

Example 1

- **Import**

```
import pandas as pd
import numpy as np
```

Create Data

```
# Create an empty dataframe
data = pd.read_csv("C:\\Users\\Dr.Thyagaraju\\Desktop\\Data\\Gender.csv")
# View the data
data
```

	Gender	Height	Weight	Foot_Size
0	male	6.00	180	12
1	male	5.92	190	11
2	male	5.58	170	12
3	male	5.92	165	10
4	female	5.00	100	6
5	female	5.50	150	8
6	female	5.42	130	7
7	female	5.75	150	9

```
# Creating a  New Data
```

```
# Create an empty dataframe
person = pd.DataFrame()

# Create some feature values for this single row
person['Height'] = [6]
person['Weight'] = [130]
person['Foot_Size'] = [8]

# View the data
person
```

	Height	Weight	Foot_Size
0	6	130	8

Bayes Theorem

Bayes theorem is a famous equation that allows us to make predictions based on data. Here is the classic version of the Bayes theorem:

$$P(A \mid B) = \frac{P(B \mid A)\, P(A)}{P(B)}$$

This might be too abstract, so let us replace some of the variables to make it more concrete. In a bayes classifier, we are interested in finding out the class (e.g. male or female, spam or ham) of an observation *given* the data:

$$p(\text{class} \mid \mathbf{data}) = \frac{p(\mathbf{data} \mid \text{class}) * p(\text{class})}{p(\mathbf{data})}$$

where:

- $\mathbf{class}$ is a particular class (e.g. male)
- $\mathbf{data}$ is an observation's data
- $p(\text{class} \mid \mathbf{data})$ is called the posterior
- $p(\mathbf{data}|\mathbf{class})$ is called the likelihood
- $p(\mathbf{class})$ is called the prior
- $p(\mathbf{data})$ is called the marginal probability

In a bayes classifier, we calculate the posterior (technically we only calculate the numerator of the posterior, but ignore that for now) for every class for each observation. Then, classify the observation based on the class with the largest posterior value. In our example, we have one observation to predict and two possible classes (e.g. male and female), therefore we will calculate two posteriors: one for male and one for female.

$$p(\text{person is male} \mid \textbf{person's data}) = \frac{p(\textbf{person's data} \mid \text{person is male}) * p(\text{person is male})}{p(\textbf{person's data})}$$

$$p(\text{person is female} \mid \textbf{person's data}) = \frac{p(\textbf{person's data} \mid \text{person is female}) * p(\text{person is female})}{p(\textbf{person's data})}$$

Gaussian Naive Bayes Classifier

A gaussian naive bayes is probably the most popular type of bayes classifier. To explain what the name means, let us look at what the bayes equations looks like when we apply our two classes (male and female) and three feature variables (height, weight, and footsize):

$$\text{posterior (male)} = \frac{P(\text{male})\, p(\text{height} \mid \text{male})\, p(\text{weight} \mid \text{male})\, p(\text{foot size} \mid \text{male})}{\text{marginal probability}}$$

$$\text{posterior (female)} = \frac{P(\text{female})\, p(\text{height} \mid \text{female})\, p(\text{weight} \mid \text{female})\, p(\text{foot size} \mid \text{female})}{\text{marginal probability}}$$

$$p(\text{height} \mid \text{female}) = \frac{1}{\sqrt{2\pi \text{variance of female height in the data}}} e^{-\frac{(\text{observation's height} - \text{average height of females in the data})^2}{2\text{variance of female height in the data}}}$$

- marginal probability marginal probability is probably one of the most confusing parts of Bayesian approaches.

Calculate Priors

```
# Number of males
n_male = data['Gender'][data['Gender'] == 'male'].count()

# Number of males
n_female = data['Gender'][data['Gender'] == 'female'].count()

# Total rows
total_ppl = data['Gender'].count()
```

```
# Number of males divided by the total rows
P_male = n_male/total_ppl

# Number of females divided by the total rows
P_female = n_female/total_ppl
```

```
# Calculate Likelihood
```

```
# Group the data by gender and calculate the means of each feature
data_means = data.groupby('Gender').mean()

# View the values
data_means
```

Gender	Height	Weight	Foot_Size
female	5.4175	132.50	7.50
male	5.8550	176.25	11.25

```python
# Group the data by gender and calculate the variance of each feature
data_variance = data.groupby('Gender').var()

# View the values
data_variance
```

Gender	Height	Weight	Foot_Size
female	0.097225	558.333333	1.666667
male	0.035033	122.916667	0.916667

Create All the vairables Needed

```
# Means for male
male_height_mean = data_means['Height'][data_variance.index == 'male'].values[0]
male_weight_mean = data_means['Weight'][data_variance.index == 'male'].values[0]
male_footsize_mean = data_means['Foot_Size'][data_variance.index == 'male'].values[0]

# Variance for male
male_height_variance = data_variance['Height'][data_variance.index == 'male'].values[0]
male_weight_variance = data_variance['Weight'][data_variance.index == 'male'].values[0]
male_footsize_variance = data_variance['Foot_Size'][data_variance.index == 'male'].values[0]

# Means for female
female_height_mean = data_means['Height'][data_variance.index == 'female'].values[0]
female_weight_mean = data_means['Weight'][data_variance.index == 'female'].values[0]
female_footsize_mean = data_means['Foot_Size'][data_variance.index == 'female'].values[0]

# Variance for female
female_height_variance = data_variance['Height'][data_variance.index == 'female'].values[0]
female_weight_variance = data_variance['Weight'][data_variance.index == 'female'].values[0]
female_footsize_variance = data_variance['Foot_Size'][data_variance.index == 'female'].values[0]
```

Create a function to calculate the probability density of each of the terms of the likelihood (e.g. P(height|female))

```
# Create a function that calculates p(x | y):
def p_x_given_y(x, mean_y, variance_y):

    # Input the arguments into a probability density function
    p = 1/(np.sqrt(2*np.pi*variance_y)) * np.exp((-(x-mean_y)**2)/(2*variance_y))

    # return p
    return p
```

Apply Bayes Classifier To New Data Point

Alright! Our bayes classifier is ready. Remember that since we can ignore the marginal probability (the demoninator), what we are actually calculating is this:

$$\text{numerator of the posterior} = P(\text{female})\, p(\text{height} \mid \text{female})\, p(\text{weight} \mid \text{female})\, p(\text{foot size} \mid \text{female})$$

To do this, we just need to plug in the values of the unclassified person (height = 6), the variables of the dataset (e.g. mean of female height), and the function (`p_x_given_y`) we made above:

Apply Bayes Classifier To New Data Point

```
# Numerator of the posterior if the unclassified observation is a male
P_male * \
p_x_given_y(person['Height'][0], male_height_mean, male_height_variance) * \
p_x_given_y(person['Weight'][0], male_weight_mean, male_weight_variance) * \
p_x_given_y(person['Foot_Size'][0], male_footsize_mean, male_footsize_variance)
```

```
6.1970718438780782e-09
```

```
# Numerator of the posterior if the unclassified observation is a female
P_female * \
p_x_given_y(person['Height'][0], female_height_mean, female_height_variance) * \
p_x_given_y(person['Weight'][0], female_weight_mean, female_weight_variance) * \
p_x_given_y(person['Foot_Size'][0], female_footsize_mean, female_footsize_variance)
```

```
0.00053779091836300176
```

Because the numerator of the posterior for female is greater than male, then we predict that the person is female.

Source Code

- https://github.com/profthyagu

Lab Program 4

- **Assuming a set of documents that need to be classified, use the naïve Bayesian Classifier model to perform this task. Built-in Libraries can be used to write the program. Calculate the accuracy, precision, and recall for your data set.**

Learning to Classify Text – Algorithm

S1: LEARN_NAIVE_BAYES_TEXT (*Examples*, V)

S2: CLASSIFY_NAIVE_BAYES_TEXT (*Doc*)

- *Examples is a set of text documents along with their target values. V is the set of all possible target values. This function learns the probability terms* ***P(w_k I v_j),*** *describing the probability that a randomly drawn word from a document in* ***class v_j*** *will be the English word* ***wk****. It also learns the class prior probabilities* ***P(v_j).***

S1: LEARN_NAIVE_BAYES_TEXT (*Examples*, V)

[V: Class , W: Word, doc : Documents]

1. *collect all words and other tokens that occur in Examples*

- ***Vocabulary*** ← all distinct words and other tokens in *Examples*

2. *calculate the required* ***P(v_j) and P(w_k | v_j)*** *probability terms*

- For each target value v_j in *V* do

$$P(v_j) \leftarrow \frac{|docs_j|}{|Examples|}$$

- ***$docs_j$*** **← subset of *Examples* for which the target value is v_j**
- ***$Text_j$*** **← a single document created by concatenating all members of *$docs_j$***
- ***n*** **← total number of words in *$Text_j$* (counting duplicate words multiple times)**
- **for each word w_k in *Vocabulary***

$$P(w_k|v_j) \leftarrow \frac{n_k+1}{n+|Vocabulary|}$$

n_k **← number of times word w_k occurs in *$Text_j$***

S2:CLASSIFY_NAIVE_BAYES_TEXT (*Doc*)

- *positions* ← all word positions in *Doc* that contain tokens found in *Vocabulary*
- Return v_{NB} where

$$v_{NB} = \underset{v_j \in V}{\operatorname{argmax}} P(v_j) \prod_{i \in positions} P(a_i | v_j)$$

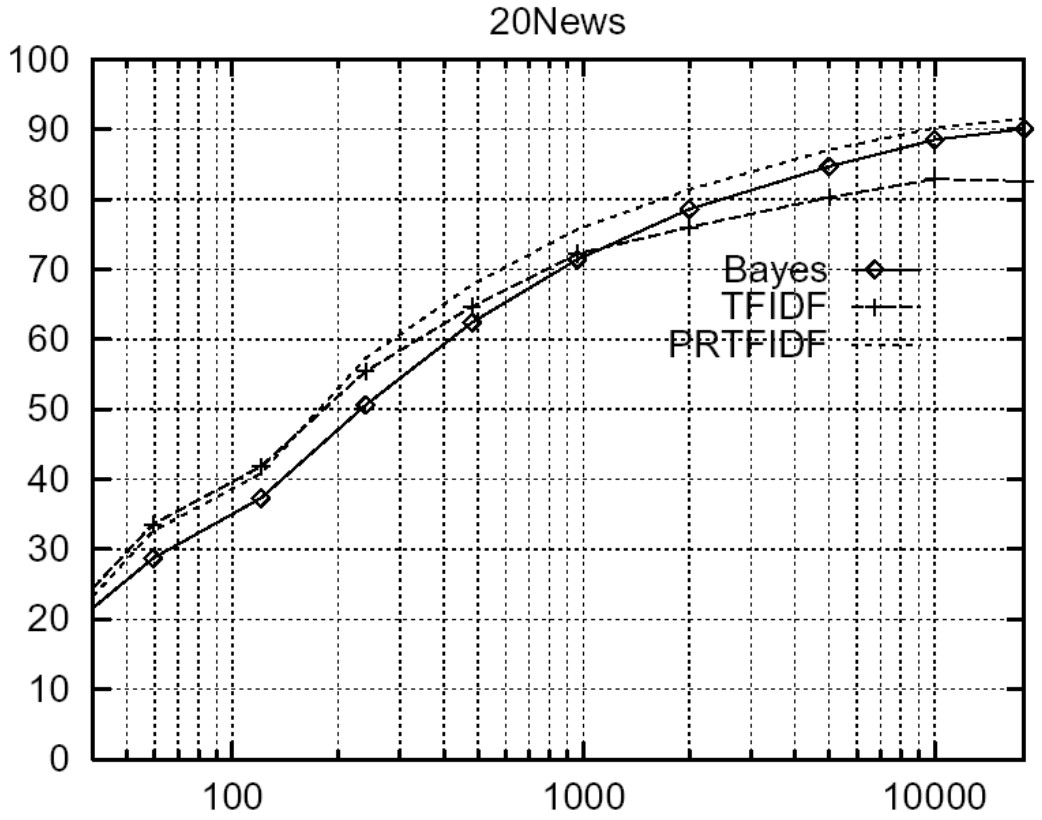
Twenty NewsGroups

- Given 1000 training documents from each group Learn to classify new documents according to which newsgroup it came from

comp.graphics	**misc.forsale**	**alt.atheism**	**sci.space**
comp.os.ms-windows.misc	**rec.autos**	**soc.religion.christian**	**sci.crypt**
comp.sys.ibm.pc.hardware	**rec.motorcycles**	**talk.religion.misc**	**sci.electronics**
comp.sys.mac.hardware	**rec.sport.baseball**	**talk.politics.mideast**	**sci.med**
comp.windows.x	**rec.sport.hockey**	**talk.politics.misc**	
		talk.politics.guns	

- Naive Bayes: 89% classification accuracy

Learning Curve for 20 Newsgroups



- Accuracy vs. Training set size (1/3 withheld for test)

Example :

- In the example, we are given a sentence " ***A very close game***", a training set of five sentences (as shown below), and their corresponding category (Sports or Not Sports).
- The goal is to build a Naive Bayes classifier that will tell us which category the sentence " ***A very close game***" belongs to.
- Applying a Naive Bayes classifier, thus the strategy would be calculating the probability of both "A very close game **is Sports**", as well as it's ***Not Sports.*** The one with the higher probability will be the result.

Text	Category
"A great game"	Sports
"The election was over"	Not sports
"Very clean match"	Sports
"A clean but forgettable game"	Sports
"It was a close election"	Not sports

Step 1: Feature Engineering

- **word frequencies**, i.e., counting the occurrence of every word in the document.
- ***P(a very close game)*** = P(a) X P(very) X P(close) X P(game)
- ***P(a very close game | Sports)*** = P(a|Sports) X P(Very|Sports) X P(close|Sports) X P(game|Sports)
- **P(*a very close game* | *Not Sports*)** = P(*a* | *Not Sports*) x P(*very* | *Not Sports*) x P(*close* | *Not Sports*) x P(*game* | *Not Sports*)

Step 2: Calculating the probabilities

- Here , the word “close” does not exist in the category Sports,
  thus **P(*close* |*Sports*)** = 0, leading to **P(*a very close game* | *Sports*)**=0.

- Given an observation x = (x1, …, xd) from a **multinomial distribution** with N trials and parameter vector θ = (θ1, …, θd), a "smoothed" version of the data gives the estimator.

$$\hat{\theta}_i = \frac{x_i + \alpha}{N + \alpha d} \qquad (i = 1, \ldots, d),$$

- where the pseudo count **α > 0** is the smoothing parameter (α = 0 corresponds to no smoothing)

Word	P(word | Sports)	P(word | Not Sports)
a	$\frac{2+1}{11+14}$	$\frac{1+1}{9+14}$
very	$\frac{1+1}{11+14}$	$\frac{0+1}{9+14}$
close	$\frac{0+1}{11+14}$	$\frac{1+1}{9+14}$
game	$\frac{2+1}{11+14}$	$\frac{0+1}{9+14}$

$$P(w_k|v_j) \leftarrow \frac{n_k+1}{n+|Vocabulary|}$$

$$P(a|Sports) \times P(very|Sports) \times P(close|Sports) \times P(game|Sports) \times P(Sports)$$
$$= 4.61 \times 10^{-5}$$
$$= 0.0000461$$

$$\mathrm{P(a} - \mathrm{Not\ Sports)} \times P(very|Not\ Sports) \times P(close|Not\ Sports) \times P(game|Not\ Sports) \times P(Not\ Sports)$$
$$= 1.43 \times 10^{-5}$$
$$= 0.0000143$$

As seen from the results shown below, P(a very close game | Sports) gives a higher probability, suggesting that the sentence belongs to the Sports category.

Multinomial Naive Bayes

Term Frequency

A alternative approach to characterize text documents — rather than binary values — is the *term frequency (tf(t, d))*. The term frequency is typically defined as the number of times a given term *t* (i.e., word or token) appears in a document *d* (this approach is sometimes also called *raw frequency*). In practice, the term frequency is often normalized by dividing the raw term frequency by the document length.

$$\text{normalized term frequency} = \frac{tf(t,d)}{n_d}$$

where

- $tf(t,d)$: Raw term frequency (the count of term t in document d).
- n_d: The total number of terms in document d.

The term frequencies can then be used to compute the maximum-likelihood estimate based on the training data to estimate the class-conditional probabilities in the multinomial model:

$$\hat{P}(x_i \mid \omega_j) = \frac{\sum tf(x_i, d \in \omega_j) + \alpha}{\sum N_{d \in \omega j} + \alpha \cdot V}$$

where

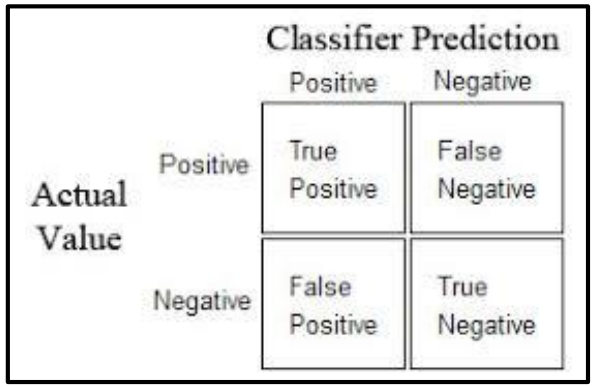
- x_i: A word from the feature vector $\mathbf{x}$ of a particular sample.
- $\sum tf(x_i, d \in \omega_j)$: The sum of raw term frequencies of word x_i from all documents in the training sample that belong to class ω_j.
- $\sum N_{d \in \omega j}$: The sum of all term frequencies in the training dataset for class ω_j.
- α: An additive smoothing parameter ($\alpha = 1$ for Laplace smoothing).
- V: The size of the vocabulary (number of different words in the training set).

The class-conditional probability of encountering the text $\mathbf{x}$ can be calculated as the product from the likelihoods of the individual words (under the *naive* assumption of conditional independence).

$$P(\mathbf{x} \mid \omega_j) = P(x_1 \mid \omega_j) \cdot P(x_2 \mid \omega_j) \cdot \ldots \cdot P(x_n \mid \omega_j) = \prod_{}^{m} P(x_i \mid \omega_j)$$

Confusion Matrix

- A confusion matrix is a summary of prediction results on a classification problem.
- The number of correct and incorrect predictions are summarized with count values and broken down by each class.
- **The confusion matrix shows the ways in which your classification model is confused when it makes predictions.**



n=165	**Predicted: NO**	**Predicted: YES**
Actual: NO	50	10
Actual: YES	5	100

Source Code

- GITHUB LINK: https://github.com/profthyagu

Lab Program5

- **Write a program to construct a Bayesian network considering medical data. Use this model to demonstrate the diagnosis of heart patients using standard Heart Disease Data Set. You can use Python ML library API.**

Bayesian Network (BAYESIAN BELIEF NETWORKS)

- Bayesian Belief networks describe conditional independence among *subsets* of variables

$\rightarrow$ allows combining prior knowledge about (in)dependencies among variables with observed training data

(also called Bayes Nets)

Conditional Independence

- **Definition:** *X* is *conditionally independent* of *Y* given *Z* if the probability distribution governing *X* is independent of the value of *Y* given the value of *Z*; that is, if

$$(\forall x_i, y_j, z_k)\ P(X= x_i | Y= y_j, Z= z_k) = P(X= x_i | Z= z_k)$$

  more compactly, we write

$$P(X | Y, Z) = P(X | Z)$$

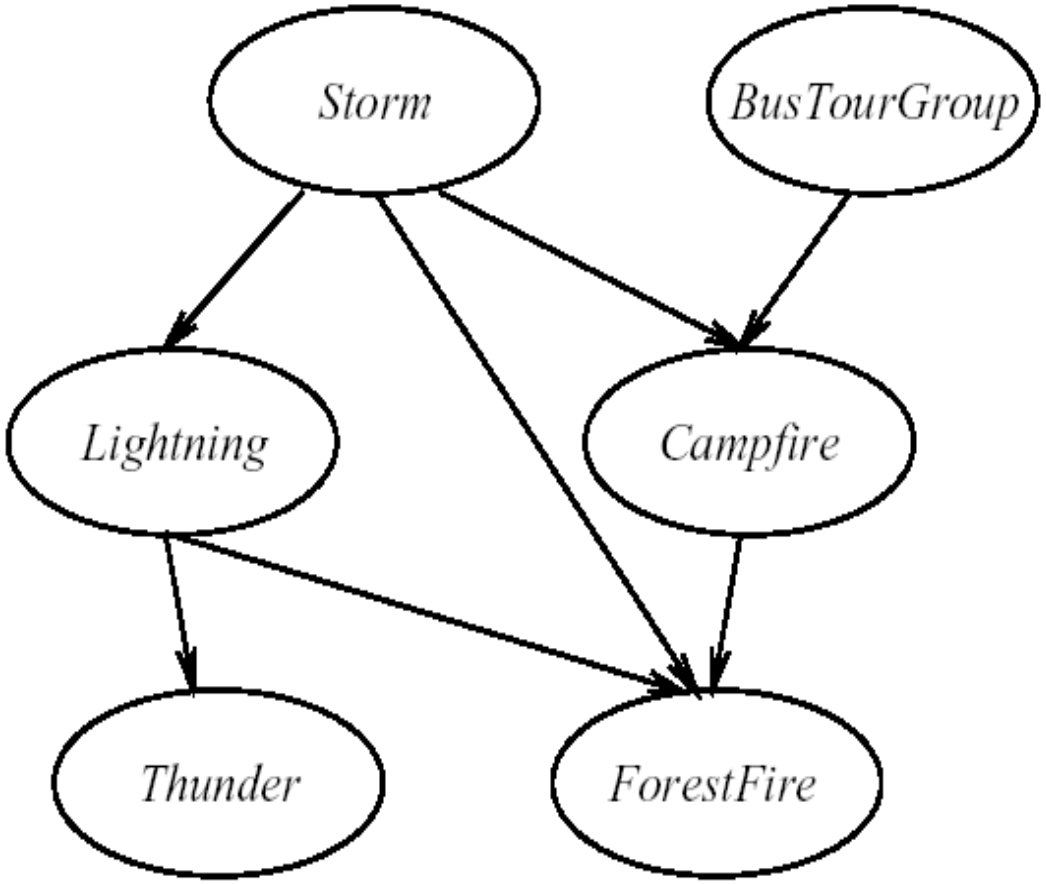
- Example: *Thunder* is conditionally independent of *Rain*, given *Lightning*

$$P(Thunder | Rain, Lightning) = P(Thunder | Lightning)$$

- Naive Bayes uses cond. indep. to justify

$$P(X, Y | Z) = P(X | Y, Z)\ P(Y | Z) = P(X | Z)\ P(Y | Z)$$

Bayesian Belief Network (1/2)



	S,B	$S,\neg B$	$\neg S,B$	$\neg S,\neg B$
C	0.4	0.1	0.8	0.2
$\neg C$	0.6	0.9	0.2	0.8

- Network represents a set of conditional independence assertions:
  - Each node is asserted to be conditionally independent of its non descendants, given its immediate predecessors.
  - Directed acyclic graph

Bayesian Belief Network (2/2)

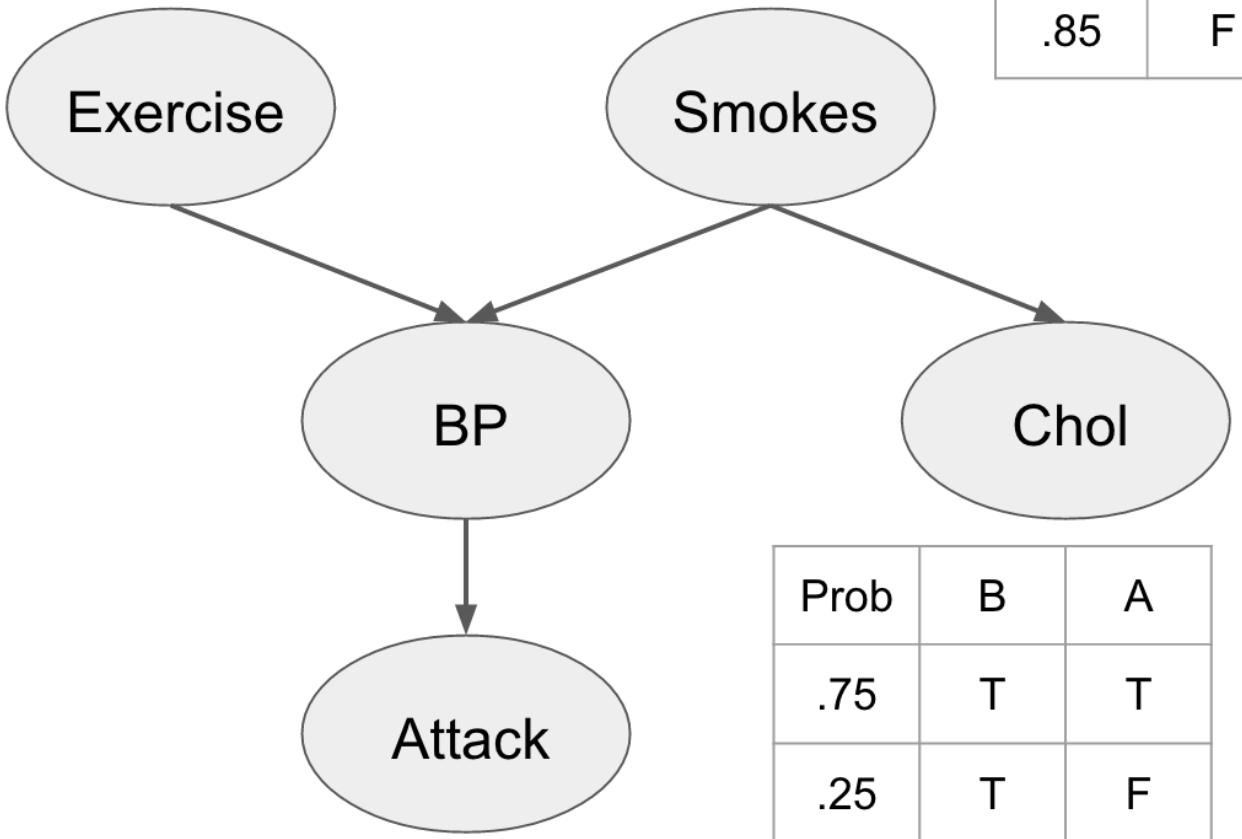
- Represents joint probability distribution over all variables
  - e.g., *P*(*Storm*, *BusTourGroup*, . . . , *ForestFire*)
  - in general,

$$P(y_1, \ldots, y_n) = \prod_{i=1}^{n} P(y_i | Parents(Y_i))$$

    where *Parents*(Y_i) denotes immediate predecessors of Y_i in graph
  - so, joint distribution is fully defined by graph, plus the P(y_i|*Parents*(Y_i))

Prob	E
.4	T
.6	F

Prob	S
.15	T
.85	F



Prob	E	S	B
.45	T	T	T
.55	T	T	F
.05	T	F	T
.95	T	F	F
.95	F	T	T
.05	F	T	F
.55	F	F	T
.45	F	F	F

Prob	S	C
.8	T	T
.2	T	F
.4	F	T
.6	F	F

Prob	B	A
.75	T	T
.25	T	F
.05	F	T
.95	F	F

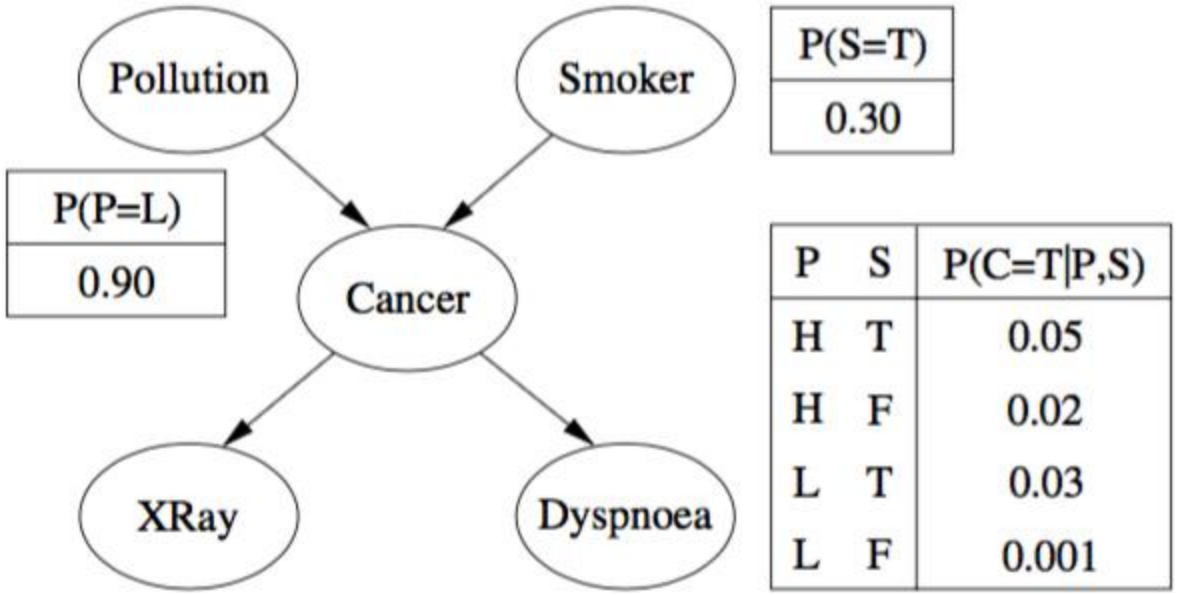


FIGURE 2.1

A BN for the lung cancer problem.

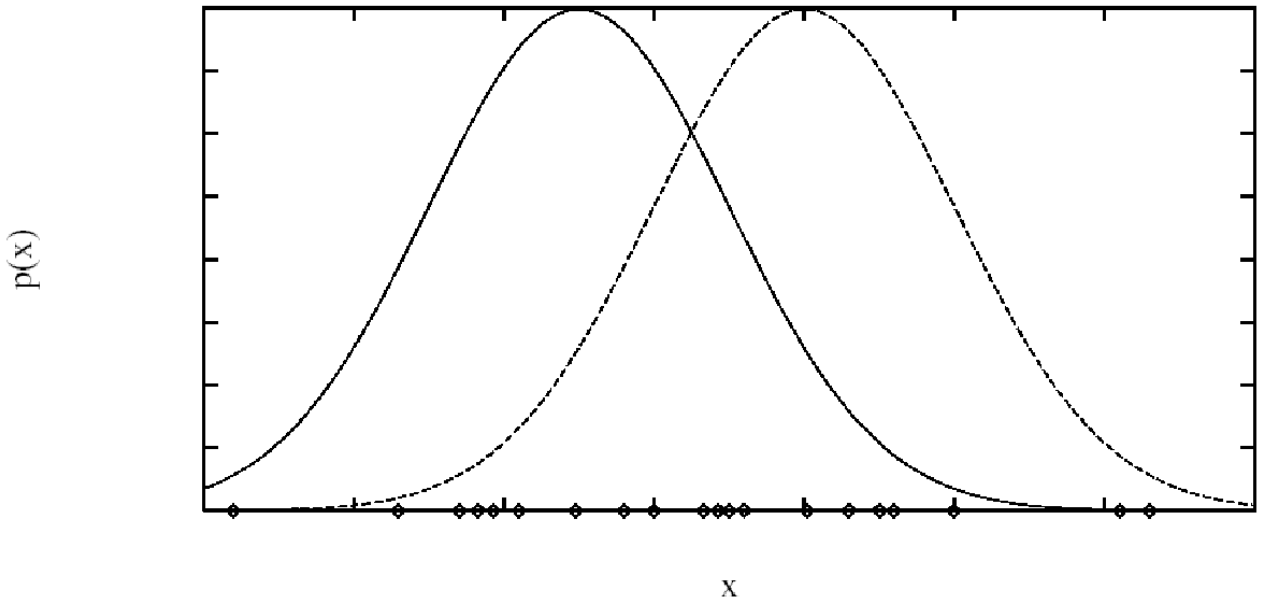
Source Code

- https://github.com/profthyagu

Lab Program 6

- Apply EM algorithm to cluster a set of data stored in a .CSV file. Use the same data set for clustering using k-Means algorithm. Compare the results of these two algorithms and comment on the quality of clustering. You can add Python ML library classes/API in the program.

Generating Data from Mixture of *k* Gaussians



- Each instance x generated by
  1. Choosing one of the *k* Gaussians with uniform probability
  2. Generating an instance at random according to that Gaussian

Gaussian Distribution

- Univariate Gaussian Distribution

$$\mathcal{N}(x \mid \mu, \sigma) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

mean variance

- Multi-Variate Gaussian Distribution

$$\mathcal{N}(x \mid \mu, \Sigma) = \frac{1}{(2\pi|\Sigma|)^{1/2}} \exp\left\{-\frac{1}{2}(x-\mu)^T \Sigma^{-1}(x-\mu)\right\}$$

mean covariance

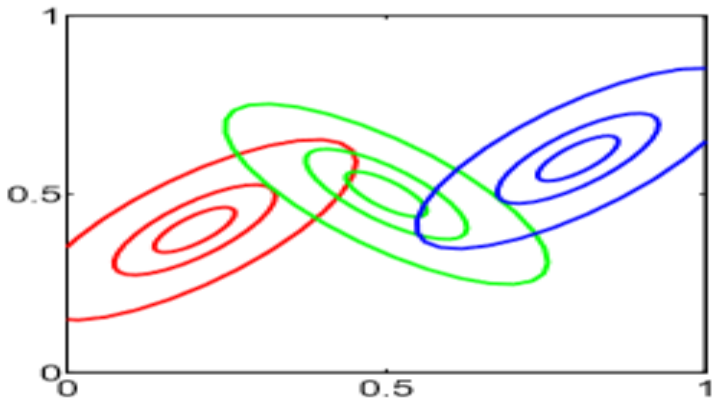
Gaussian Mixtures

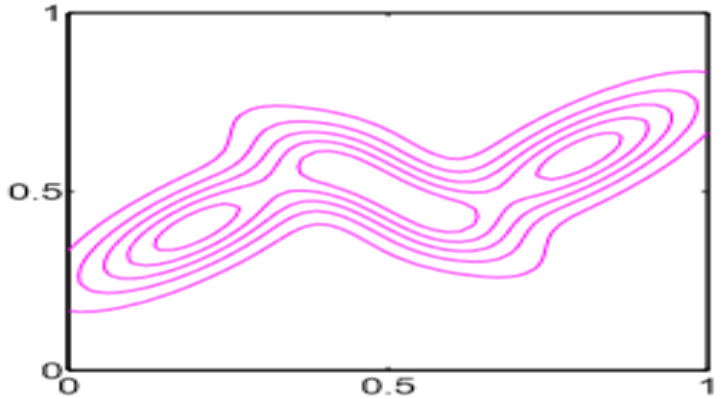
- Linear super-position of Gaussians

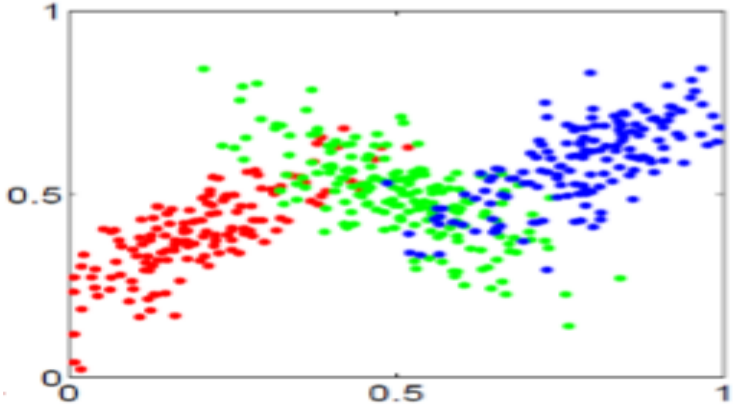
$$\mathbf{p}(\mathbf{x}) = \sum_{\mathbf{k}=1}^{\mathbf{K}} \boldsymbol{\pi}_{\mathbf{k}} \mathcal{N}(\mathbf{x} \mid \boldsymbol{\mu}_{\mathbf{k}}, \Sigma_{\mathbf{k}})$$

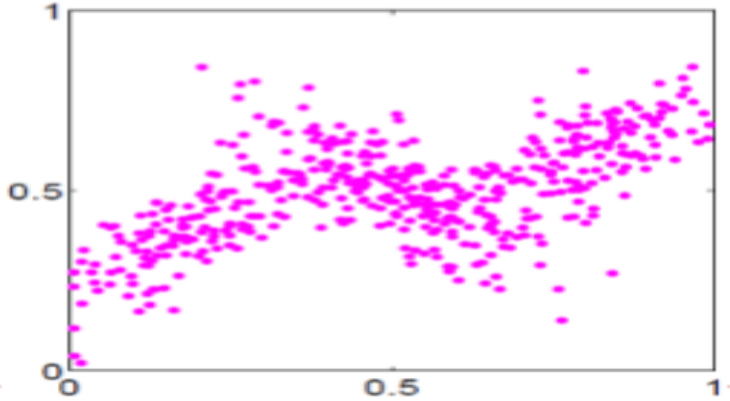
Number of Gaussians

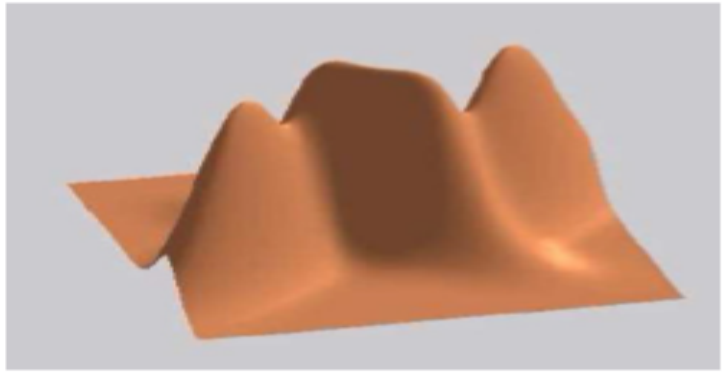
Mixing coefficient: weightage for each Gaussian dist.



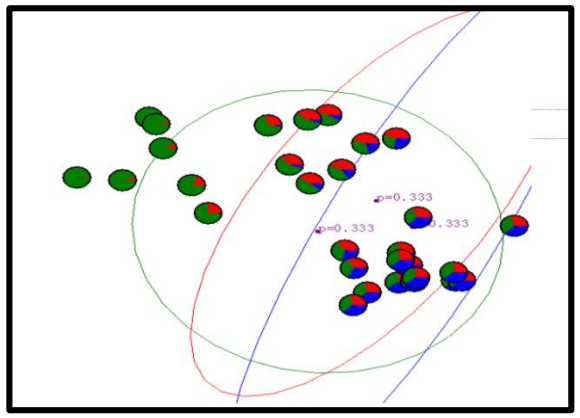


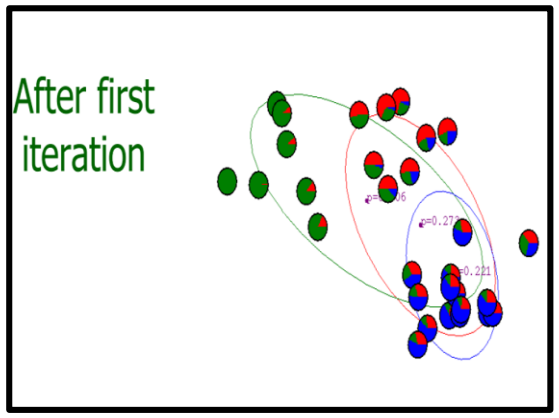


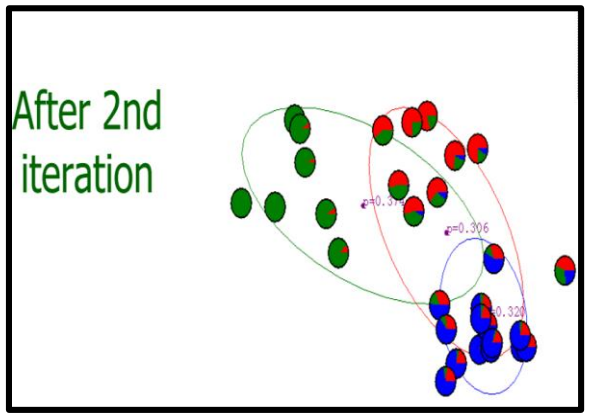


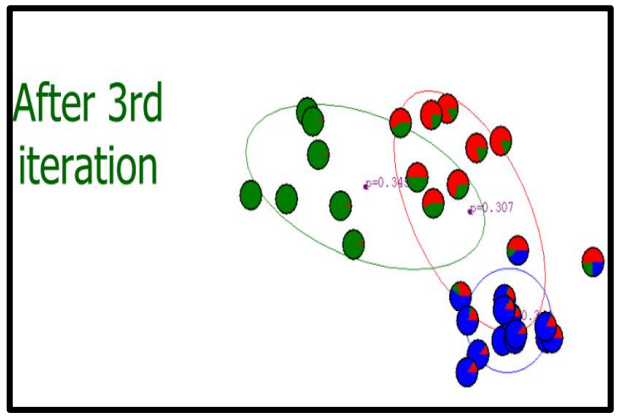


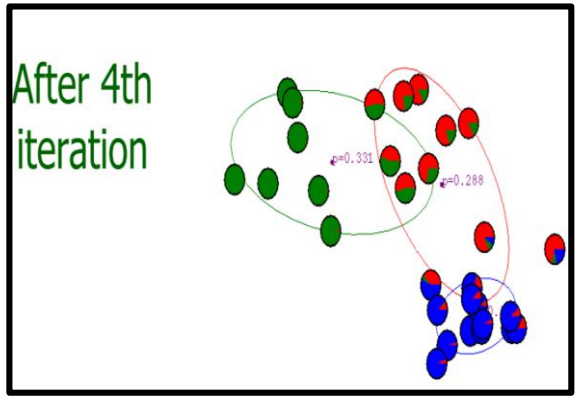
GMM : Example

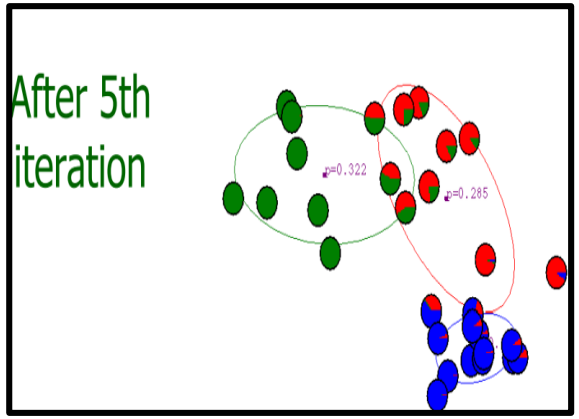

p=0.333
p=0.333
p=0.333

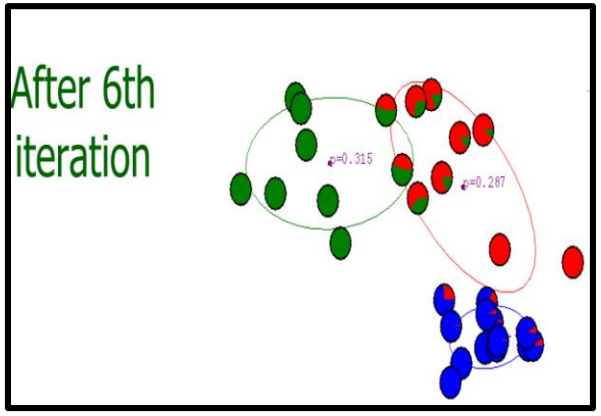

After first iteration

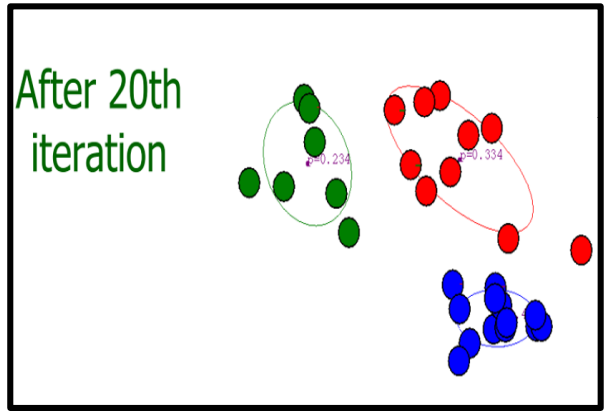

After 2nd iteration
p=0.306


After 3rd iteration
p=0.307


After 4th iteration
p=0.331
p=0.288


After 5th iteration
p=0.322
p=0.285


After 6th iteration
p=0.315
p=0.287


After 20th iteration
p=0.234
p=0.334

Expectation Maximization (EM) Algorithm

- When to use:
  - Filling in missing data in samples
  - Discovering the value of latent variables
  - Estimating the parameters of HMMs
  - Estimating parameters of finite mixtures
  - Unsupervised learning of clusters
  - Semi-supervised classification and clustering

Expectation Maximization (EM) Algorithm

- EM is typically used to compute maximum likelihood estimates given incomplete samples.
- The EM algorithm estimates the parameters of a model iteratively.
  - Starting from some initial guess, each iteration consists of
    - an E step (Expectation step)
    - an M step (Maximization step)

EM Algorithm

- Given:
  - Instances from *X* generated by mixture of *k* Gaussian distributions
  - Unknown means $<\mu_1,\ldots,\mu_k>$ of the *k* Gaussians
  - Don't know which instance x_i was generated by which Gaussian
- Determine:
  - Maximum likelihood estimates of $<\mu_1,\ldots,\mu_k>$

- EM Algorithm:
- Pick random initial $h = <\mu_1, \mu_2>$ then iterate

E step: Calculate the expected value $E[z_{ij}]$ of each ***hidden variable*** $\boldsymbol{z_{ij}}$, assuming the current hypothesis $h = <\mu_1, \mu_2>$ holds.

$$E[z_{ij}] = \frac{p(x = x_i | \mu = \mu_j)}{\sum_{n=1}^{2} p(x = x_i | \mu = \mu_n)}$$

$$= \frac{e^{-\frac{1}{2\sigma^2}(x_i - \mu_j)^2}}{\sum_{n=1}^{2} e^{-\frac{1}{2\sigma^2}(x_i - \mu_n)^2}}$$

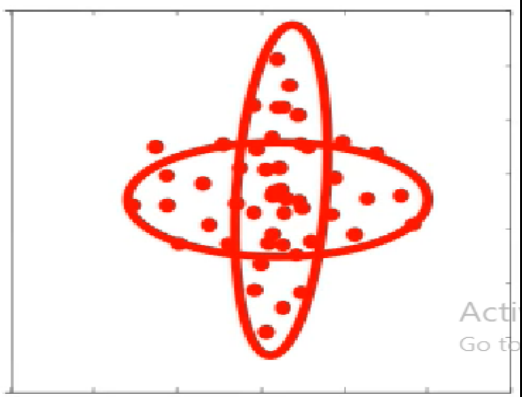
M step: Calculate a new maximum likelihood hypothesis $h' = <\mu'_1, \mu'_2>$, assuming the value taken on by each hidden variable z_{ij} is its expected value $E[z_{ij}]$ calculated above. Replace $h = <\mu_1, \mu_2>$ by $h' = <\mu'_1, \mu'_2>$.

$$\mu_j \leftarrow \frac{\sum_{i=1}^{m} E[z_{ij}] \; x_i}{\sum_{i=1}^{m} E[z_{ij}]}$$

Mixtures of Gaussians

- K-means algorithm
  - Assigned each example to exactly one cluster
  - What if clusters are overlapping?
    - Hard to tell which cluster is right
    - Maybe we should try to remain uncertain
  - Used Euclidean distance
  - What if cluster has a non-circular shape?

- Gaussian mixture models
  - Clusters modeled as Gaussians
    - Not just by their mean
  - EM algorithm: assign data to cluster with some *probability*
  - Gives probability model of x! ("generative")



Mixtures of Gaussians

- Start with parameters describing each cluster
- Mean μ_c , variance σ_c , "size" π_c
- Probability distribution: $p(x) = \sum_c \pi_c \, \mathcal{N}(x \; ; \; \mu_c, \sigma_c)$

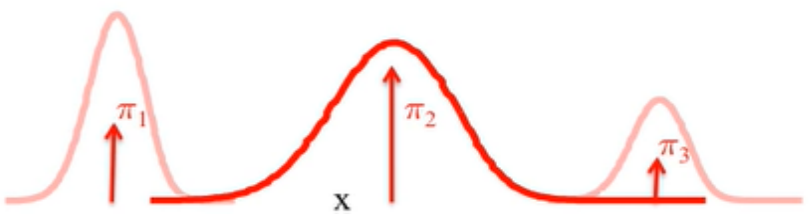
- Equivalent "latent variable" form:

$$p(z = c) = \pi_c$$ Select a mixture component with probability π

$$p(x|z = c) = \mathcal{N}(x \; ; \; \mu_c, \sigma_c)$$ Sample from that component's Gaussian

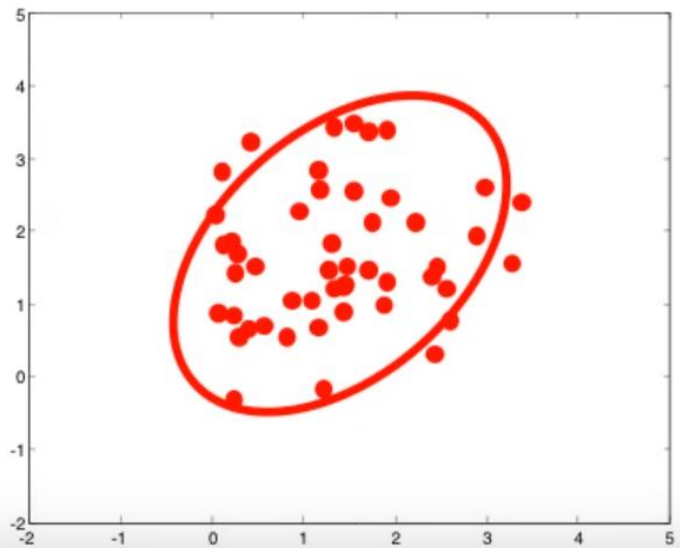
"Latent assignment" z:
we observe x, but z is hidden

p(x) = marginal over x



Multivariate Gaussian models

$$\mathcal{N}(\underline{x}\,;\,\underline{\mu},\Sigma) = \frac{1}{(2\pi)^{d/2}}|\Sigma|^{-1/2}\exp\left\{-\frac{1}{2}(\underline{x}-\underline{\mu})^T\Sigma^{-1}(\underline{x}-\underline{\mu})\right\}$$



Maximum Likelihood estimates

$$\hat{\mu} = \frac{1}{m}\sum_i x^{(i)}$$

$$\hat{\Sigma} = \frac{1}{m}\sum_i (x^{(i)}-\hat{\mu})^T(x^{(i)}-\hat{\mu})$$

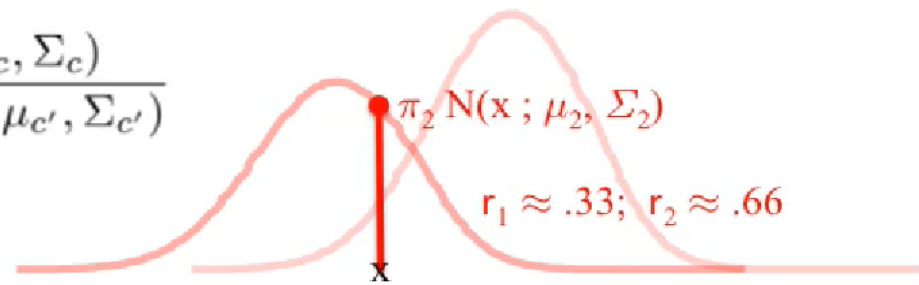
We'll model each cluster using one of these Gaussian "bells"…

EM Algorithm: E-step

- Start with clusters: Mean μ_c, Covariance Σ_c, "size" π_c

- E-step ("Expectation")
  - For each datum (example) x_i,
  - Compute "r_{ic}", the probability that it belongs to cluster c
    - Compute its probability under model c
    - Normalize to sum to one (over clusters c)

$$r_{ic} = \frac{\pi_c \mathcal{N}(x_i \; ; \; \mu_c, \Sigma_c)}{\sum_{c'} \pi_{c'} \mathcal{N}(x_i \; ; \; \mu_{c'}, \Sigma_{c'})}$$



  - If x_i is very likely under the c^{th} Gaussian, it gets high weight
  - Denominator just makes r's sum to one

EM Algorithm: M-step

- Start with assignment probabilities r_{ic}
- Update parameters: mean μ_c, Covariance Σ_c, "size" π_c

- M-step ("Maximization")
  - For each cluster (Gaussian) z = c,
  - Update its parameters using the (weighted) data points

$$m_c = \sum_i r_{ic}$$ Total responsibility allocated to cluster c

$$\pi_c = \frac{m_c}{m}$$ Fraction of total assigned to cluster c

$$\mu_c = \frac{1}{m_c} \sum_i r_{ic} x^{(i)}$$ Weighted mean of assigned data

$$\Sigma_c = \frac{1}{m_c} \sum_i r_{ic} (x^{(i)} - \mu_c)^T (x^{(i)} - \mu_c)$$ Weighted covariance of assigned data (use new weighted means here)

Expectation-Maximization

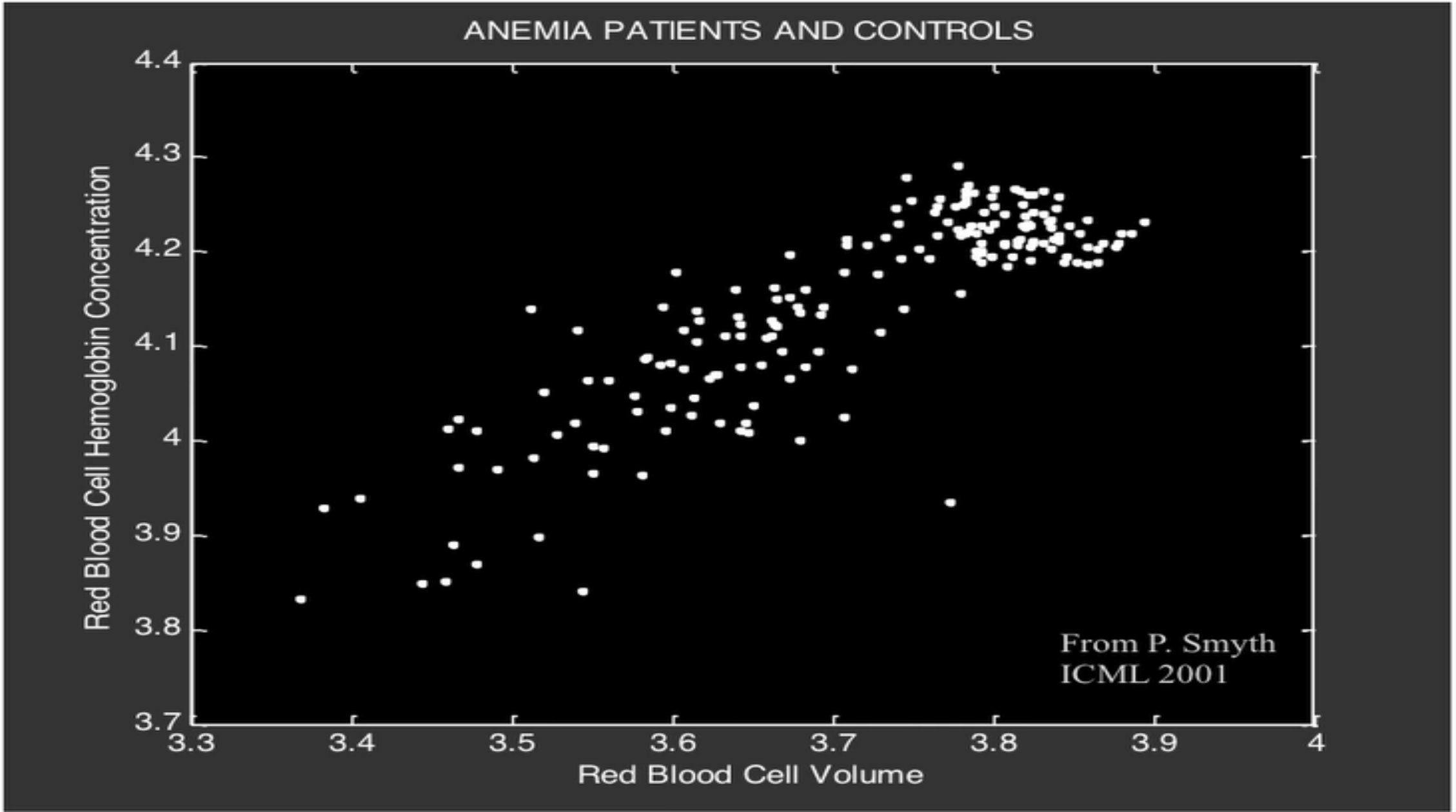
- Each step increases the log-likelihood of our model

$$\log p(\underline{X}) = \sum_i \log \left[\sum_c \pi_c \, \mathcal{N}(x_i \; ; \; \mu_c, \Sigma_c) \right]$$

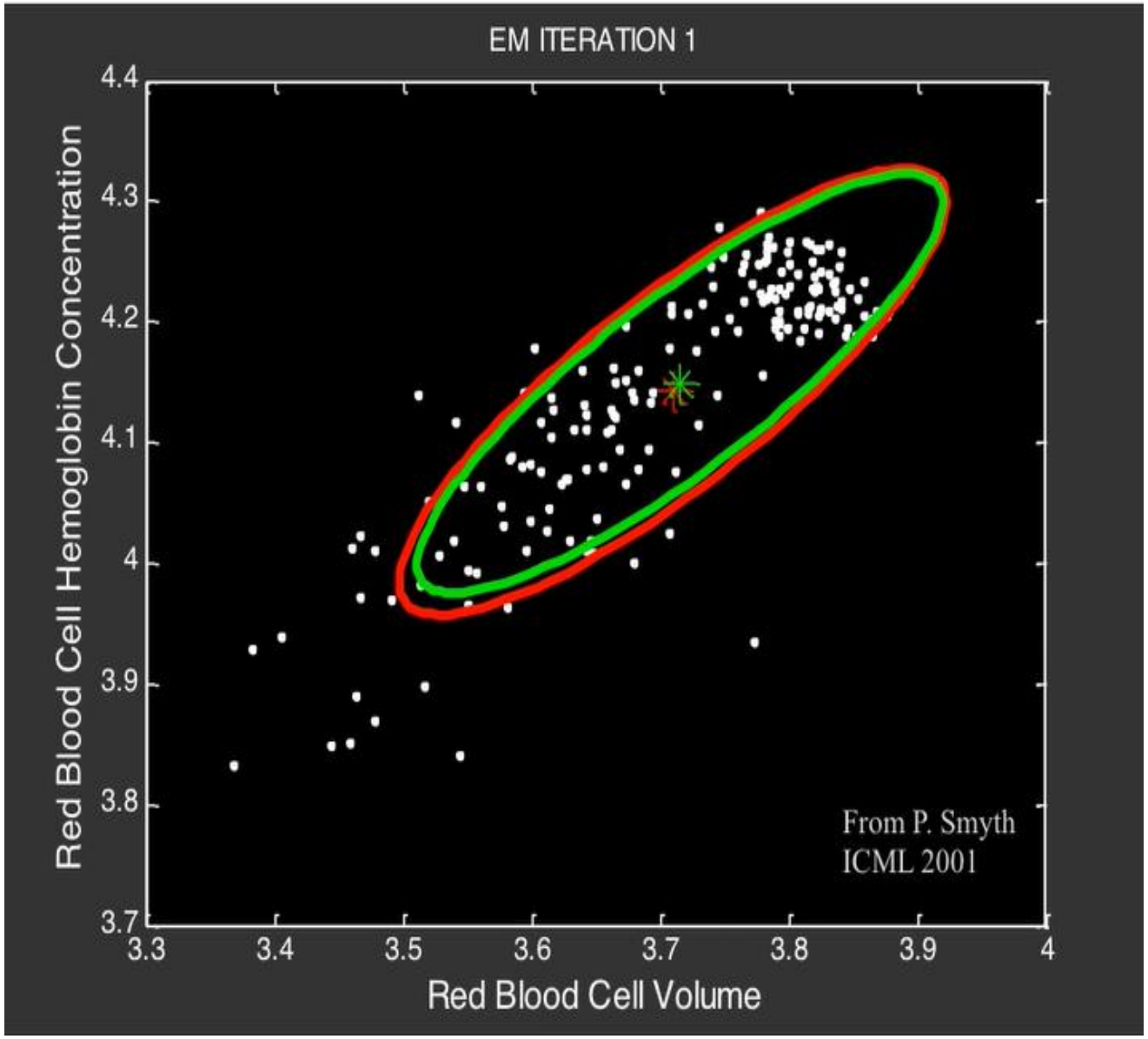
(we won't derive this here, though)

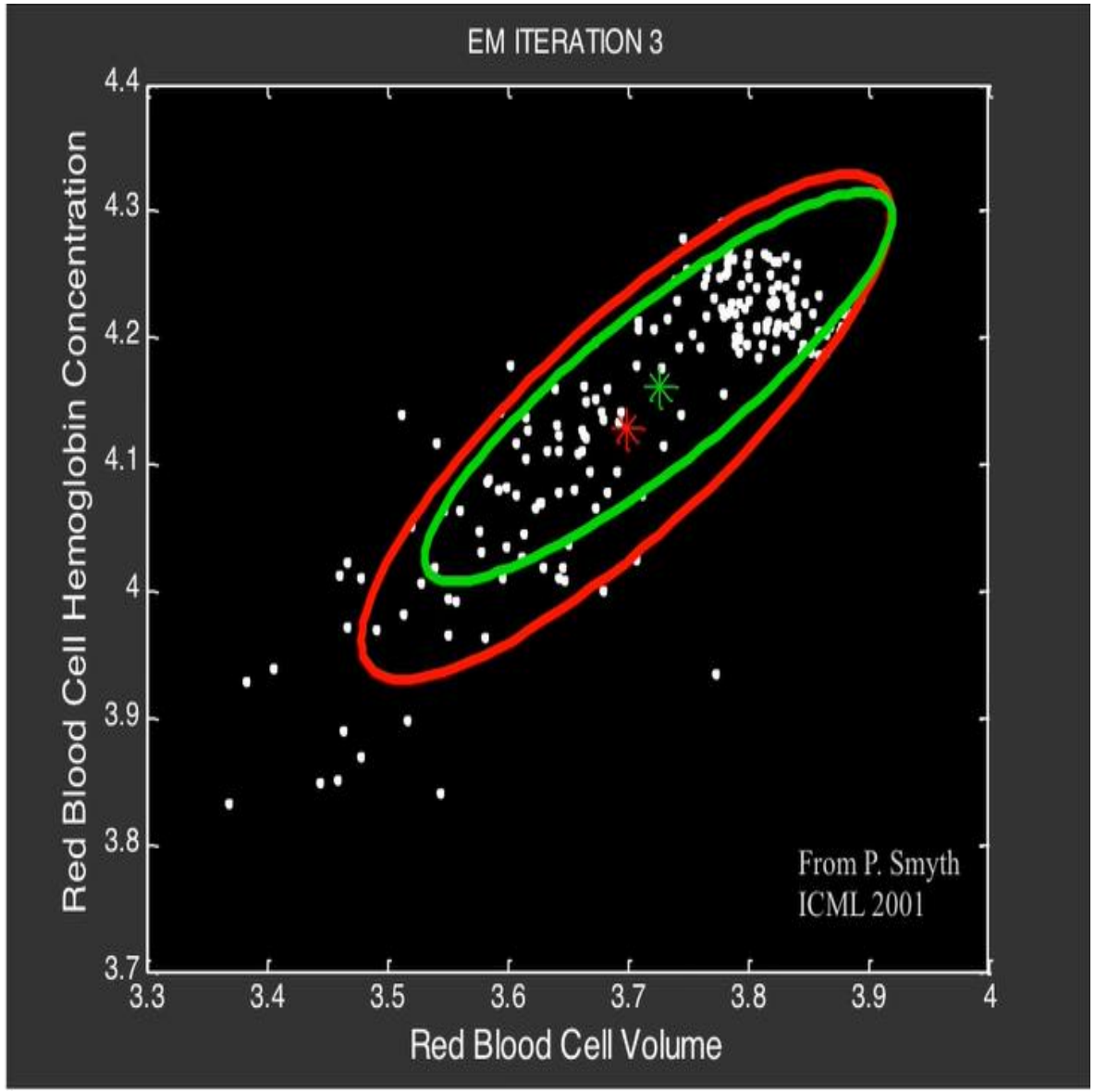
- Iterate until convergence
  - Convergence guaranteed – another ascent method
  - Local optima: initialization often important
- What should we do
  - If we want to choose a single cluster for an "answer"?
  - With new data we didn't see during training?
- Choosing the number of clusters
  - Can use penalized likelihood of training data (like k-means
  - True probability model: can use log-likelihood of test data, log p(x')

GMM : Example2

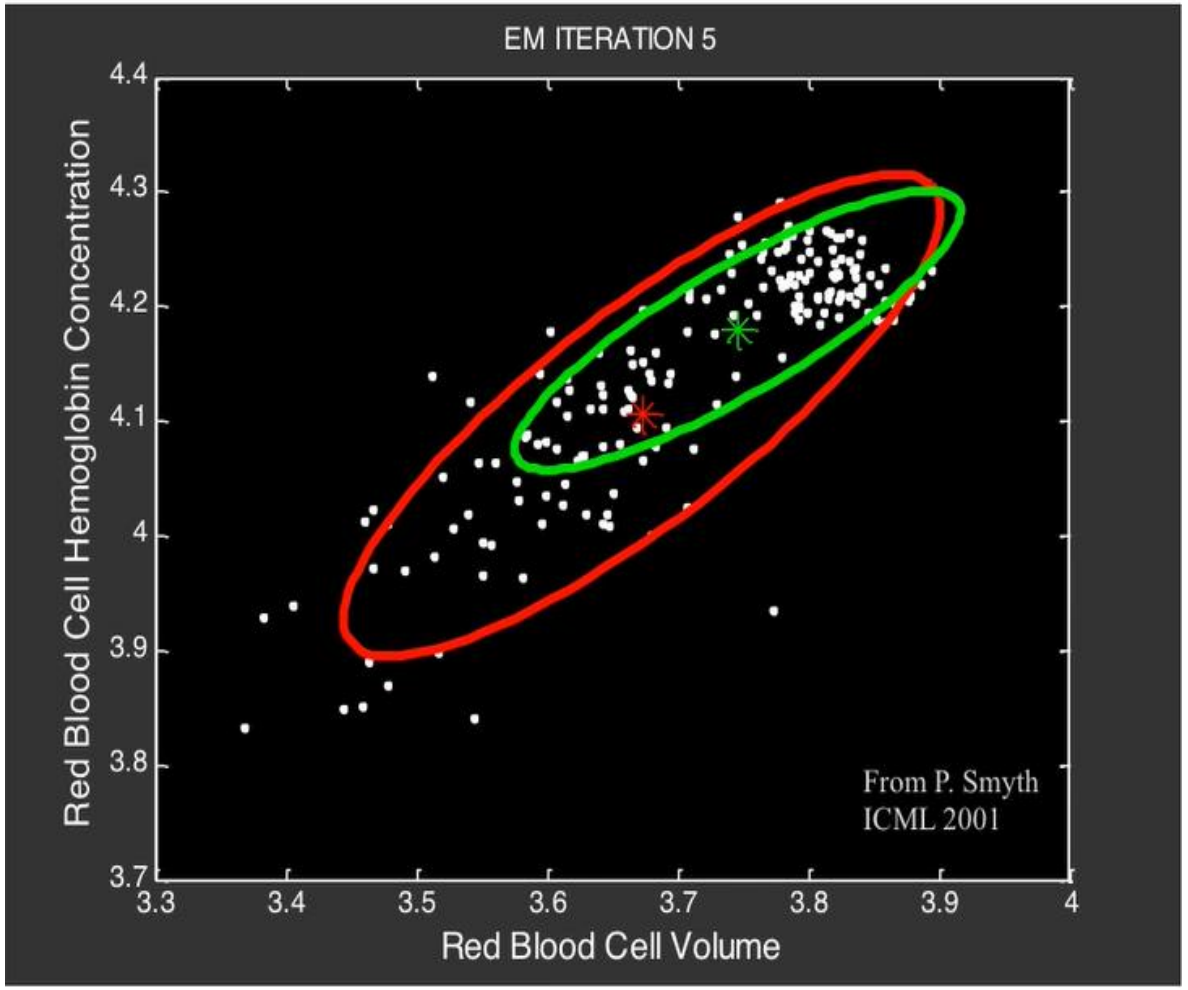


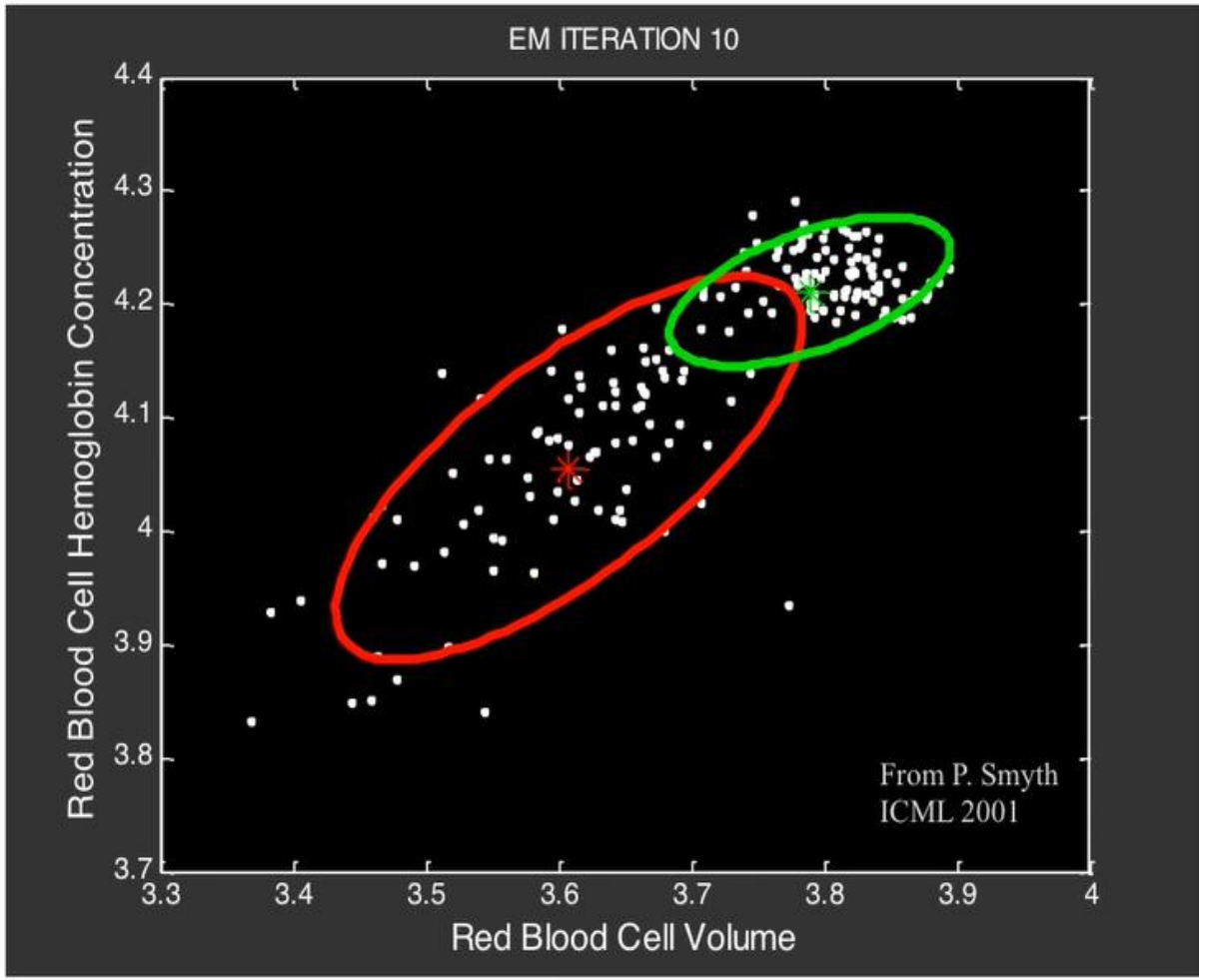
GMM : Example2



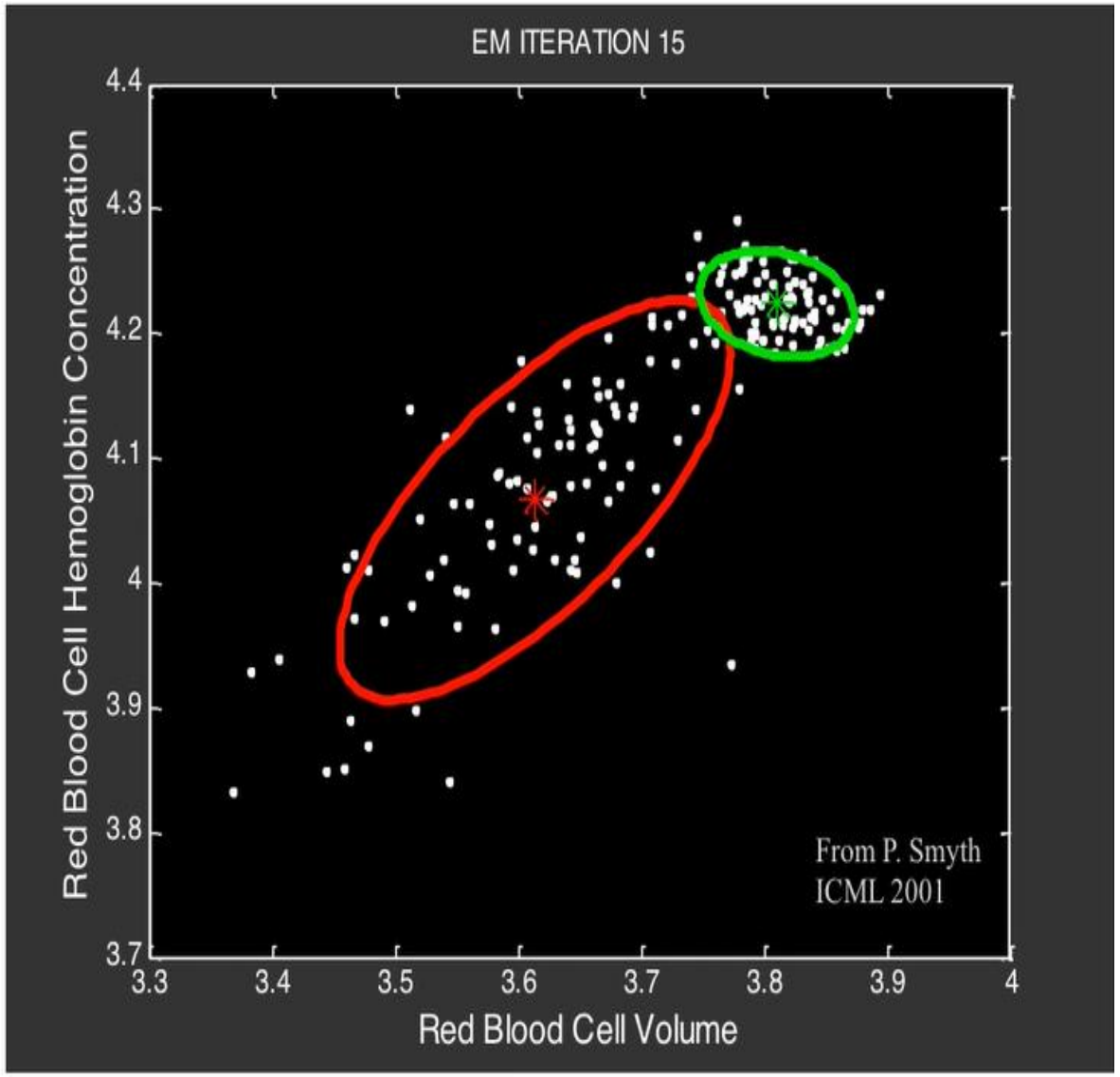


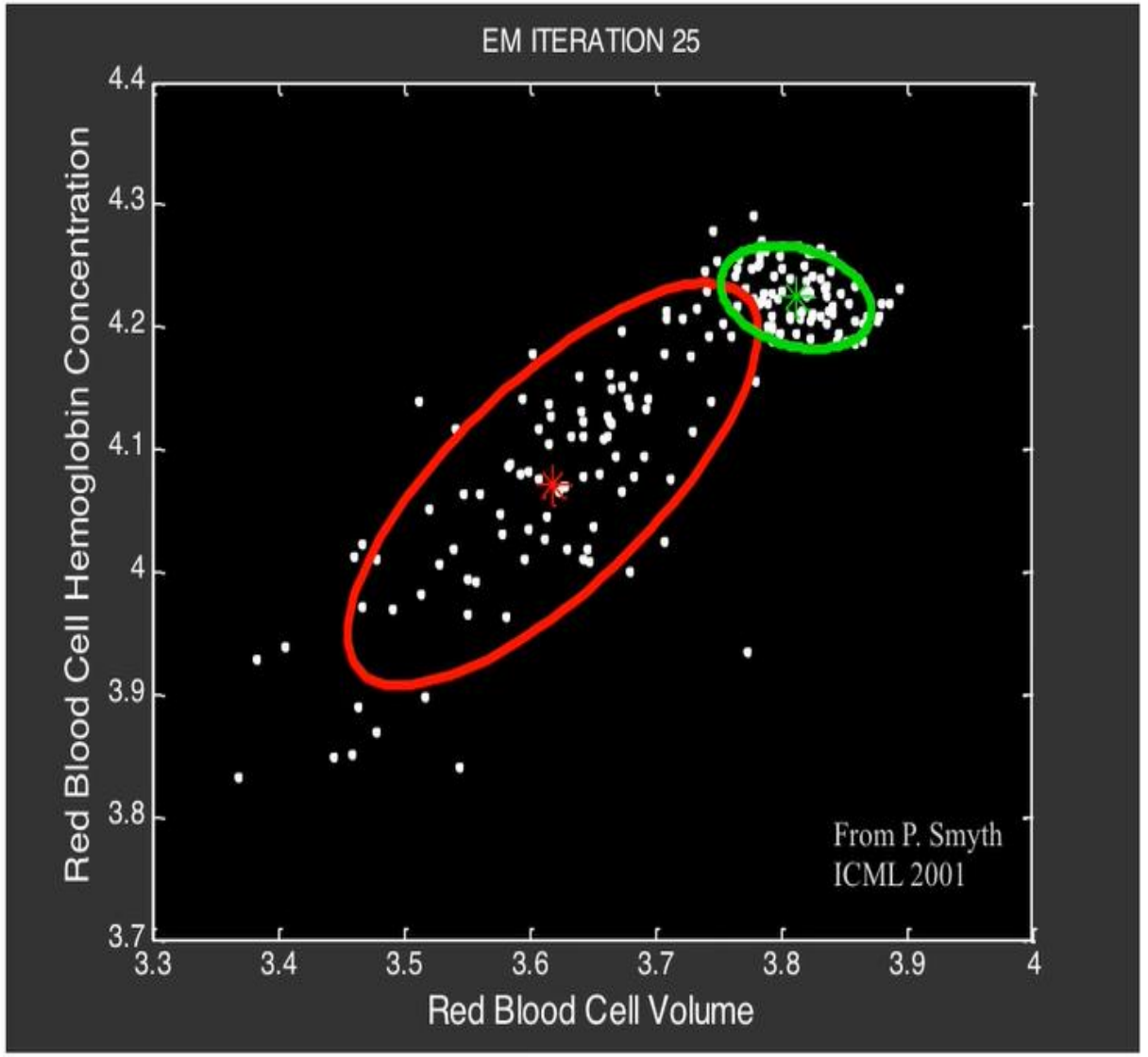
GMM : Example2



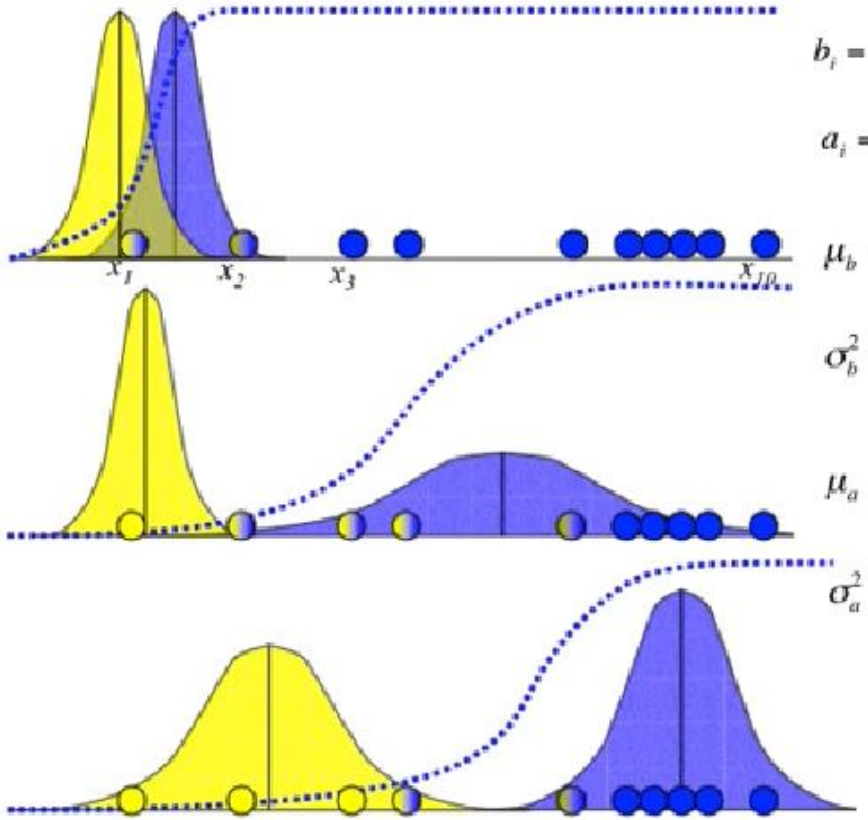


GMM : Example2





EM:



$$P(x_i \mid b) = \frac{1}{\sqrt{2\pi\sigma_b^2}} \exp\left\{-\frac{(x_i - \mu_b)^2}{2\sigma_b^2}\right\}$$

$$b_i = P(b \mid x_i) = \frac{P(x_i \mid b)P(b)}{P(x_i \mid b)P(b) + P(x_i \mid a)P(a)}$$

$$a_i = P(a \mid x_i) = 1 - b_i$$

$$\mu_b = \frac{b_1 x_1 + b_2 x_2 + \ldots + b_n x_n}{b_1 + b_2 + \ldots + b_n}$$

$$\sigma_b^2 = \frac{b_1 (x_1 - \mu_b)^2 + \ldots + b_n (x_n - \mu_b)^2}{b_1 + b_2 + \ldots + b_n}$$

$$\mu_a = \frac{a_1 x_1 + a_2 x_2 + \ldots + a_n x_n}{a_1 + a_2 + \ldots + a_n}$$

$$\sigma_a^2 = \frac{a_1 (x_1 - \mu_a)^2 + \ldots + a_n (x_n - \mu_a)^2}{a_1 + a_2 + \ldots + a_n}$$

could also estimate priors:

$P(b) = (b_1 + b_2 + \ldots b_n) / n$

$P(a) = 1 - P(b)$

K Means Algorithm

- 1. The sample space is initially partitioned into K clusters and the observations are randomly assigned to the clusters.
- 2. For each sample:
  - Calculate the distance from the observation to the centroid of the cluster.
  - IF the sample is closest to its own cluster THEN leave it ELSE select another cluster.
- 3. Repeat steps 1 and 2 untill no observations are moved from one cluster to another

Distance functions

Euclidean

$$\sqrt{\sum_{i=1}^{k}(x_i - y_i)^2}$$

Manhattan

$$\sum_{i=1}^{k}|x_i - y_i|$$

Minkowski

$$\left(\sum_{i=1}^{k}\left(|x_i - y_i|\right)^q\right)^{1/q}$$

Basic Algorithm of K-means

Algorithm 1 Basic K-means Algorithm.

1: Select K points as the initial centroids.
2: **repeat**
3: Form K clusters by assigning all points to the closest centroid.
4: Recompute the centroid of each cluster.
5: **until** The centroids don't change

Details of K-means

1. Initial centroids are often chosen randomly.
   - *Clusters produced vary from one run to another*
2. The centroid is (typically) the mean of the points in the cluster.
3. 'Closeness' is measured by **Euclidean distance**, cosine similarity, correlation, etc.
4. K-means will converge for common similarity measures mentioned above.
5. Most of the convergence happens in the first few iterations.
   - *Often the stopping condition is changed to 'Until relatively few points change clusters'*

Euclidean Distance

$$d(i,j)=\sqrt{|x_{i1}-x_{j1}|^2+|x_{i2}-x_{j2}|^2+...+|x_{ip}-x_{jp}|^2}$$

A simple example: Find the distance between two points, the original and the point (3,4)

$$d_E(O,A)=\sqrt{3^2+4^2}=5$$

Update Centroid

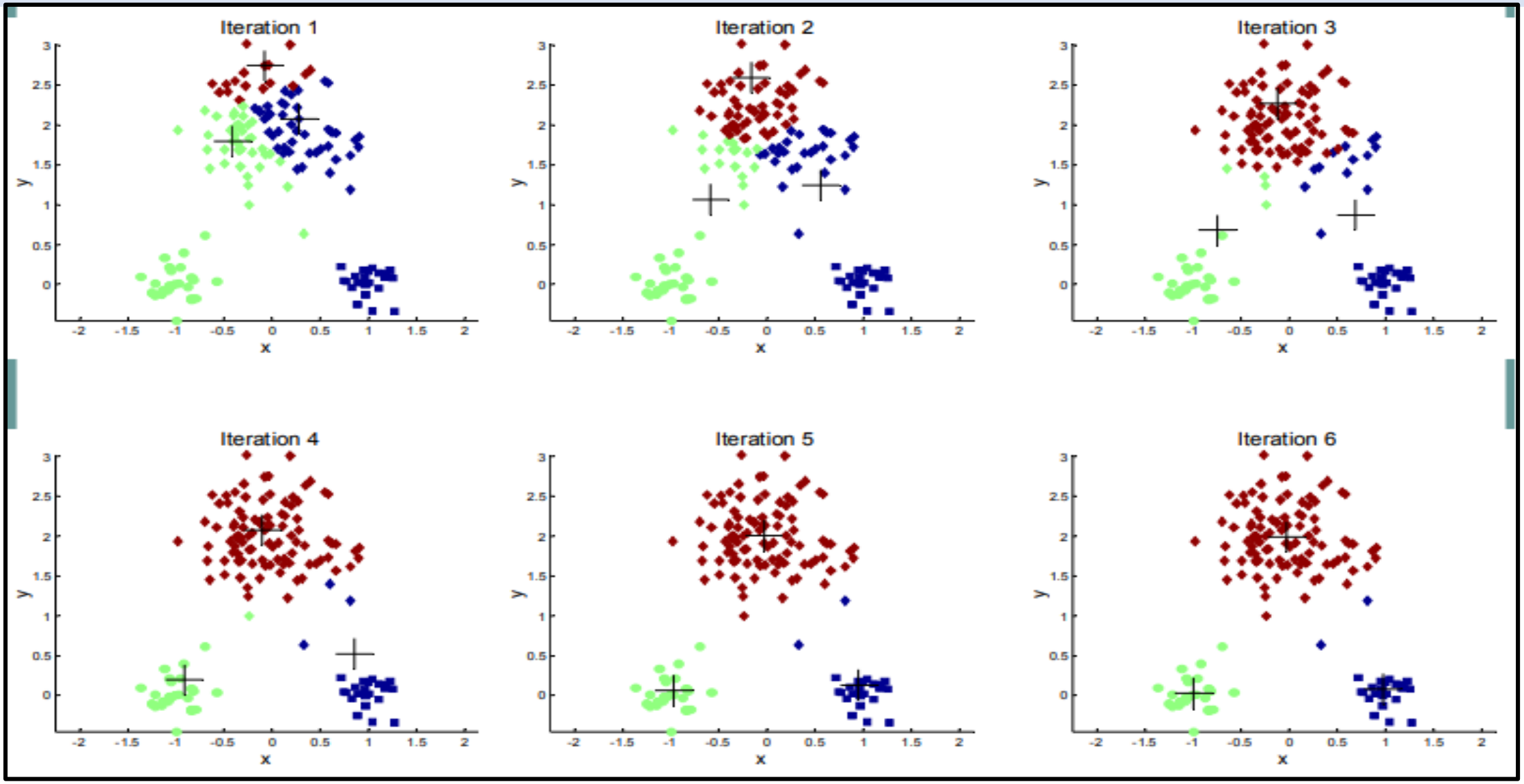
We use the following equation to calculate the n dimensional centroid point amid k n-dimensional points

$$CP(x_1,x_2,\ldots,x_k) = \left(\frac{\sum_{i=1}^{k} x1st_i}{k}, \frac{\sum_{i=1}^{k} x2nd_i}{k}, \ldots, \frac{\sum_{i=1}^{k} xnth_i}{k}\right)$$

Example: Find the centroid of 3 2D points, (2,4), (5,2) and (8,9)

$$CP = \left(\frac{2+5+8}{3}, \frac{4+2+9}{3}\right) = (5,5)$$

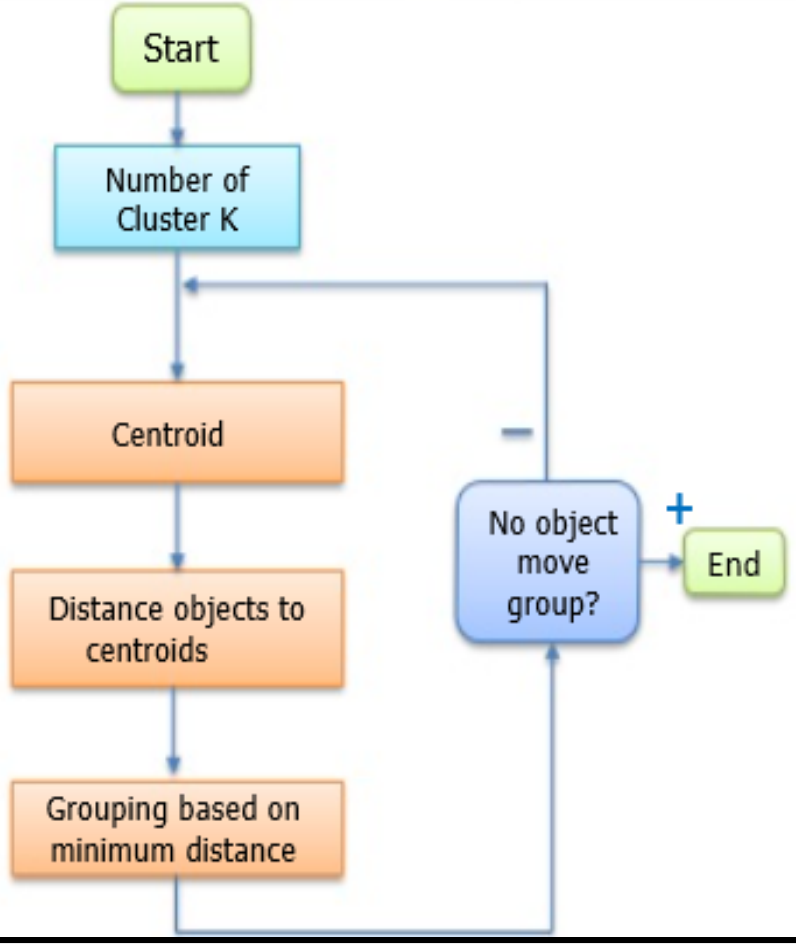
Examples of K Means



How the K-Mean Clustering algorithm works?

$$\left[\frac{x_1 + x_2 + x_3}{3} , \frac{y_1 + y_2 + y_3}{3}\right]$$

Process Flow of K-means



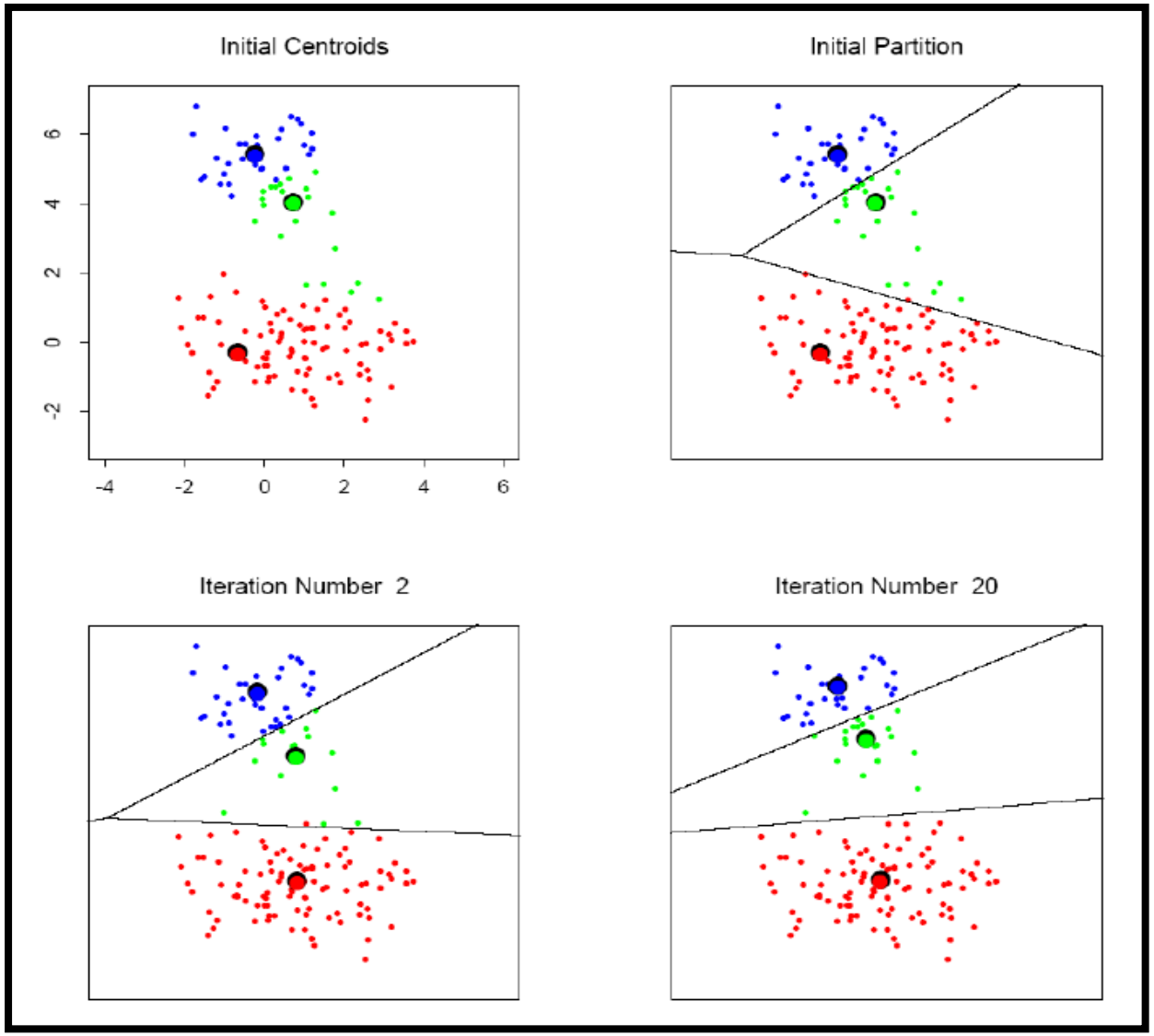
Iterate until *stable* (cluster centers converge):

1. Determine the centroid coordinate.

2. Determine the distance of each object to the centroids.

3. Group the object based on minimum distance (find the closest centroid)

K-means clustering example



Source Code

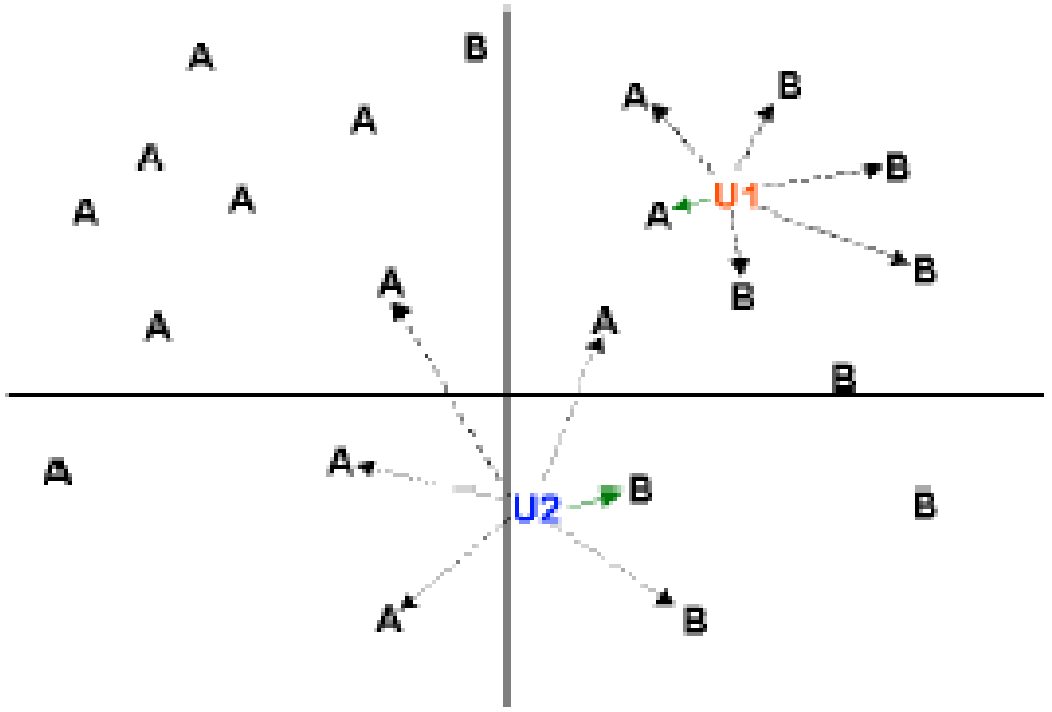
-

Lab Program 7

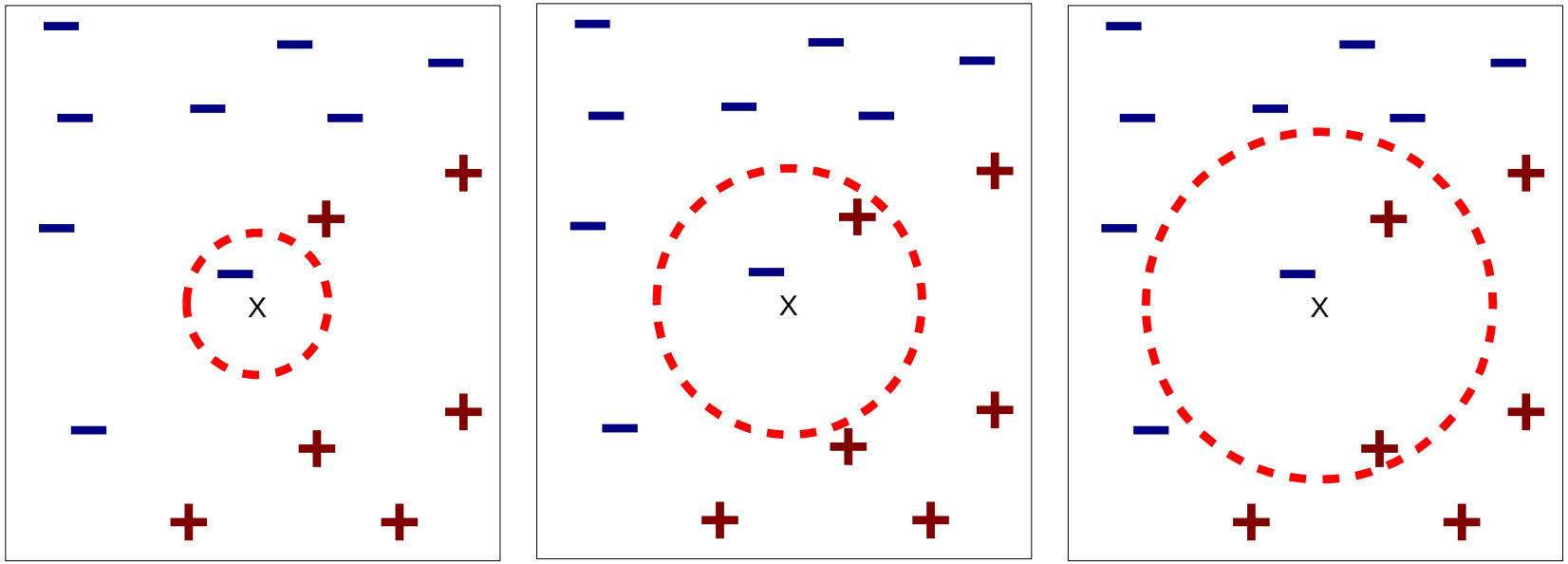
- Write a program to implement k-Nearest Neighbour algorithm to classify the iris data set. Print both correct and wrong predictions. Python ML library classes can be used for this problem.

K-Nearest-Neighbor Algorithm

- **Principle:** points (documents) that are close in the space belong to the same class



Definition of Nearest Neighbor



(a) 1-nearest neighbor (b) 2-nearest neighbor (c) 3-nearest neighbor

K-nearest neighbors of a record x are data points that have the k smallest distance to x

Nearest Neighbor Classification

- Compute distance between two points:
  - Euclidean distance

$$d(p,q) = \sqrt{\sum_i (p_i - q_i)^2}$$

Distance Metrics

Minkowsky:

$$D(\boldsymbol{x},\boldsymbol{y}) = \left(\sum_{i=1}^{m} |x_i - y_i|^r \right)^{1/r}$$

Euclidean:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sqrt{\sum_{i=1}^{m} (x_i - y_i)^2}$$

Manhattan / city-block:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} |x_i - y_i|$$

Camberra:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} \frac{|x_i - y_i|}{|x_i + y_i|}$$

Chebychev:

$$D(\boldsymbol{x},\boldsymbol{y}) = \max_{i=1}^{m} |x_i - y_i|$$

Quadratic:

$$D(\boldsymbol{x},\boldsymbol{y}) = (\boldsymbol{x} - \boldsymbol{y})^T Q(\boldsymbol{x} - \boldsymbol{y}) = \sum_{j=1}^{m} \left(\sum_{i=1}^{m} (x_i - y_i) q_{ji} \right) (x_j - y_j)$$

Q is a problem-specific positive definite $m \times m$ weight matrix

Mahalanobis:

$$D(\boldsymbol{x},\boldsymbol{y}) = [\det V]^{1/m} (\boldsymbol{x} - \boldsymbol{y})^{\mathrm{T}} V^{-1} (\boldsymbol{x} - \boldsymbol{y})$$

V is the covariance matrix of $A_1..A_m$, and A_j is the vector of values for attribute j occuring in the training set instances $1..n$.

Correlation:

$$D(\boldsymbol{x},\boldsymbol{y}) = \frac{\sum_{i=1}^{m} (x_i - \overline{x_i})(y_i - \overline{y_i})}{\sqrt{\sum_{i=1}^{m} (x_i - \overline{x_i})^2 \sum_{i=1}^{m} (y_i - \overline{y_i})^2}}$$

$\overline{x_i} = \overline{y_i}$ and is the average value for attribute i occuring in the training set.

Chi-square:

$$D(\boldsymbol{x},\boldsymbol{y}) = \sum_{i=1}^{m} \frac{1}{sum_i} \left(\frac{x_i}{size_{\boldsymbol{x}}} - \frac{y_i}{size_{\boldsymbol{y}}} \right)^2$$

sum_i is the sum of all values for attribute i occuring in the training set, and $size_{\boldsymbol{x}}$ is the sum of all values in the vector $\boldsymbol{x}$.

Kendall's Rank Correlation:

$$D(\boldsymbol{x},\boldsymbol{y}) = 1 - \frac{2}{n(n-1)} \sum_{i=1}^{m} \sum_{j=1}^{i-1} \mathrm{sign}(x_i - x_j)\,\mathrm{sign}(y_i - y_j)$$

sign(x)=-1, 0 or 1 if $x < 0$, $x = 0$, or $x > 0$, respectively.

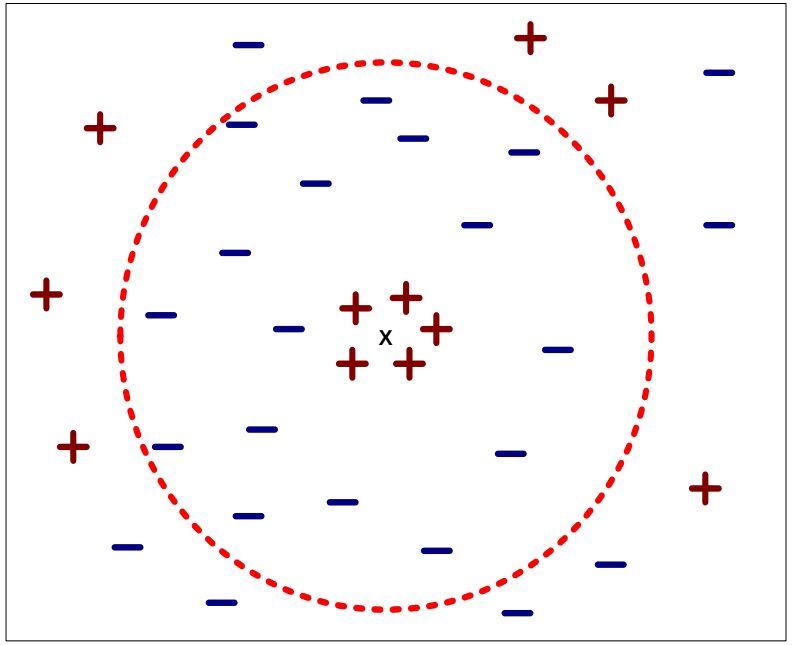
Figure 1. Equations of selected distance functions. ($\boldsymbol{x}$ and $\boldsymbol{y}$ are vectors of m attribute values).

Selection of Distance Metrics

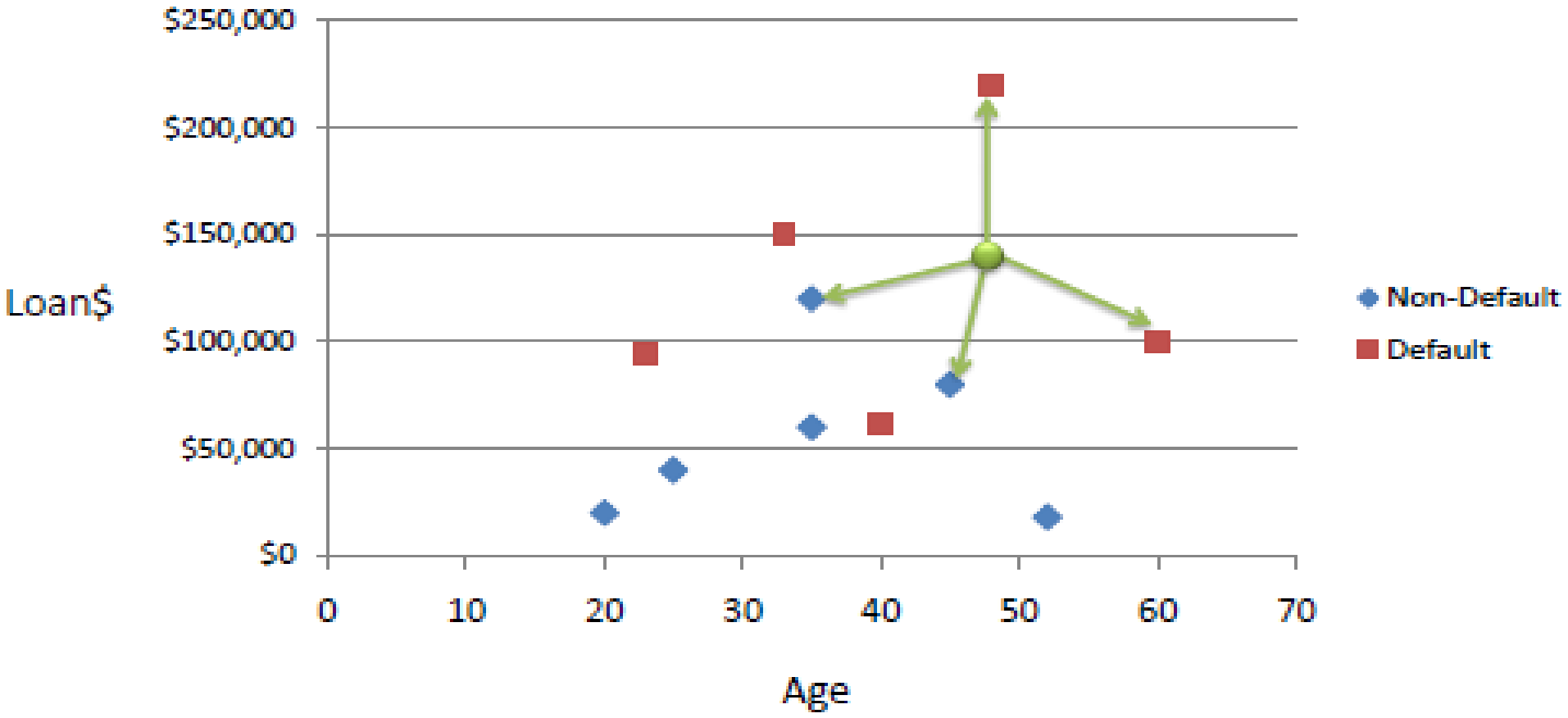
- You can choose the best distance metric based on the properties of your data. If you are unsure, you can experiment with different distance metrics and different values of K together and see which mix results in the most accurate models.
- Euclidean is a good distance measure to use if the input variables are similar in type (e.g. all measured widths and heights).
- Manhattan distance is a good measure to use if the input variables are not similar in type (such as age, gender, height, etc.).

Nearest Neighbor Classification…

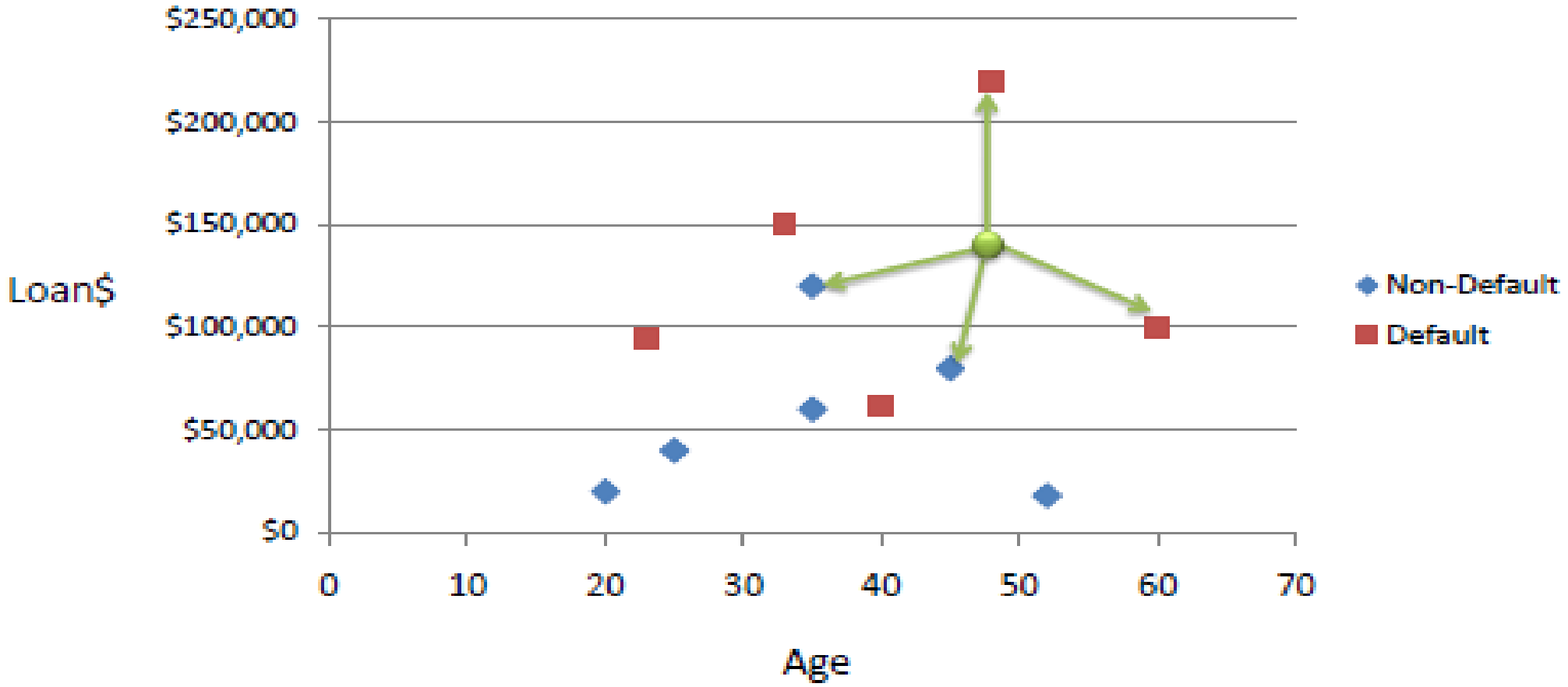
- **Choosing the value of k:**
  - If k is too small, sensitive to noise points
  - If k is too large, neighborhood may include points from other classes



Example: Consider the following data concerning credit default. Age and Loan are two numerical variables (predictors) and Default is the target.



Example: We can now use the training set to classify an unknown case (Age=48 and Loan=$142,000) using Euclidean distance. If K=1 then the nearest neighbor is the last case in the training set with Default=Y.



D = Sqrt[(48-33)^2 + (142000-150000)^2] = 8000.01 >> Default=Y

Age	Loan	Default	Distance	
25	$40,000	N	102000	
35	$60,000	N	82000	
45	$80,000	N	62000	
20	$20,000	N	122000	
35	$120,000	N	22000	2
52	$18,000	N	124000	
23	$95,000	Y	47000	
40	$62,000	Y	80000	
60	$100,000	Y	42000	3
48	$220,000	Y	78000	
33	$150,000	Y	8000	1
48	**$142,000**	**?**		

Euclidean Distance

$$D = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}$$

With K=3, there are two Default=Y and one Default=N out of three closest neighbors. The prediction for the unknown case is again Default=Y.

Source Code

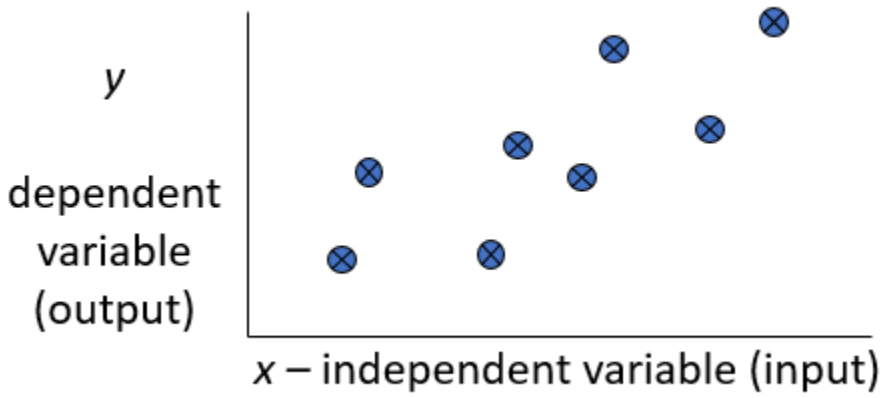
- https://github.com/profthyagu

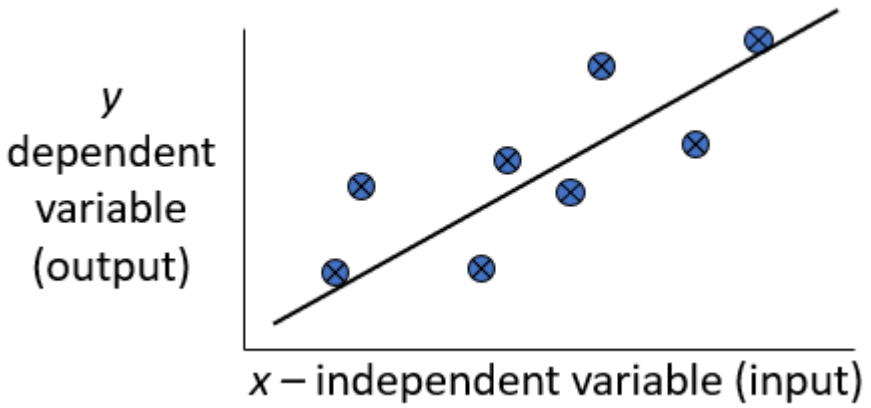
Lab Program 8

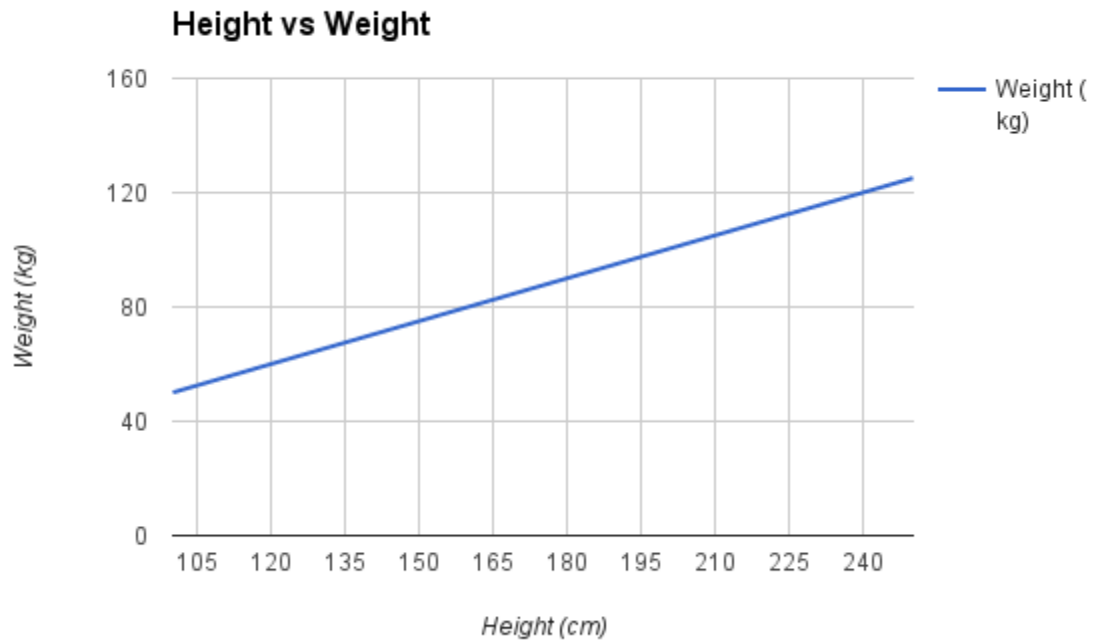
- **Implement the non-parametric Locally Weighted Regression (LOWESS) algorithm in order to fit data points. Select appropriate data set for your experiment and draw graphs.**

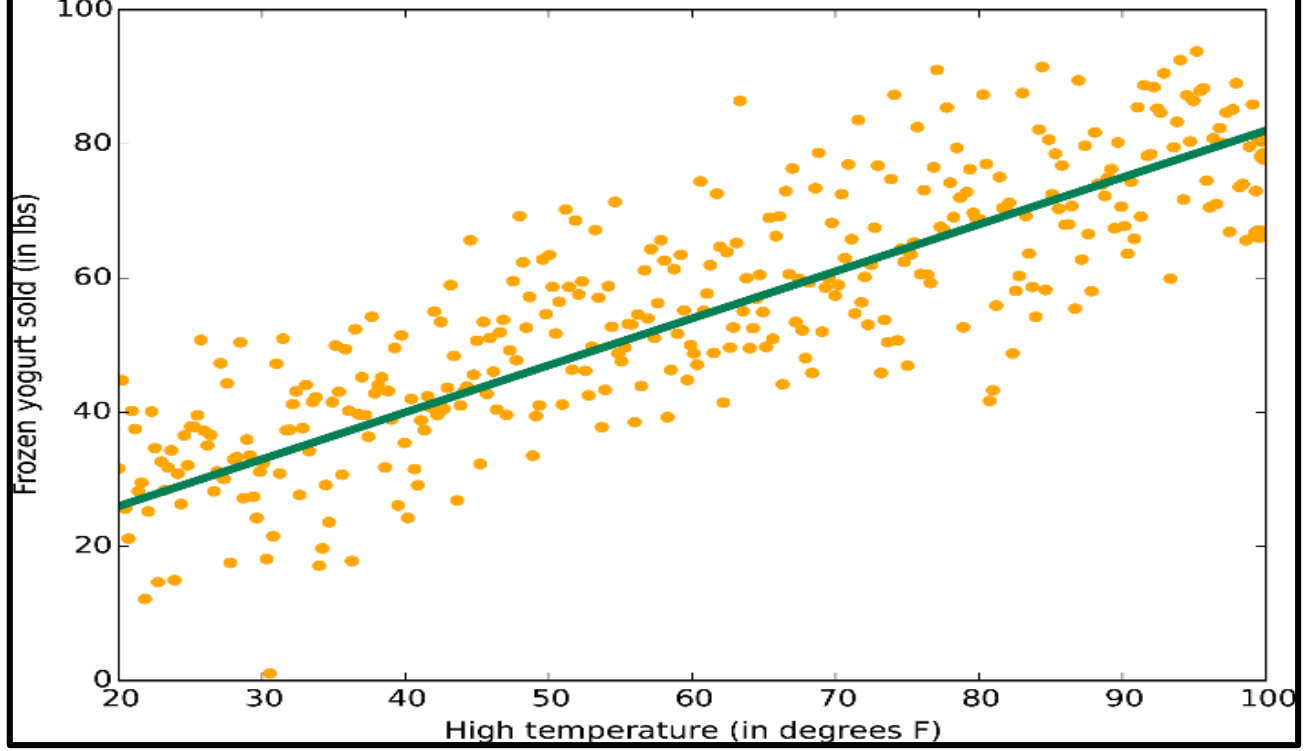
Regression

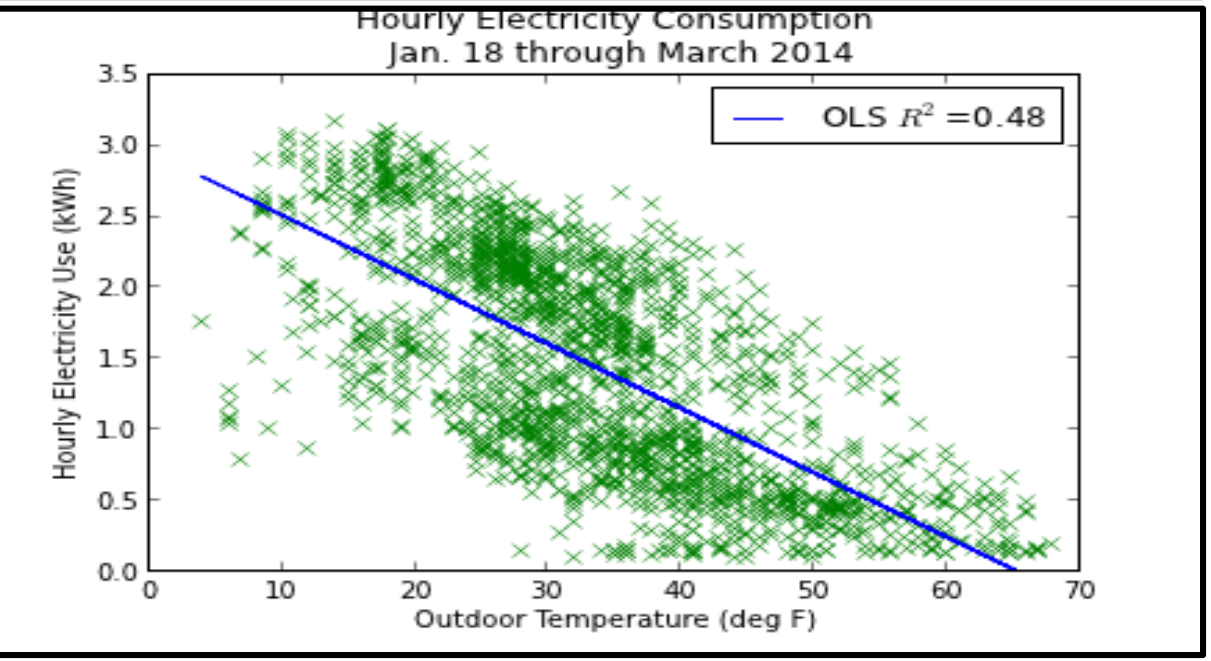
- Regression is a technique from statistics that is used to predict values of a desired target quantity when the target quantity is continuous .
- In regression, we seek to identify (or estimate) a continuous variable y associated with a given input vector x.
  - y is called the dependent variable.
  - x is called the independent variable.

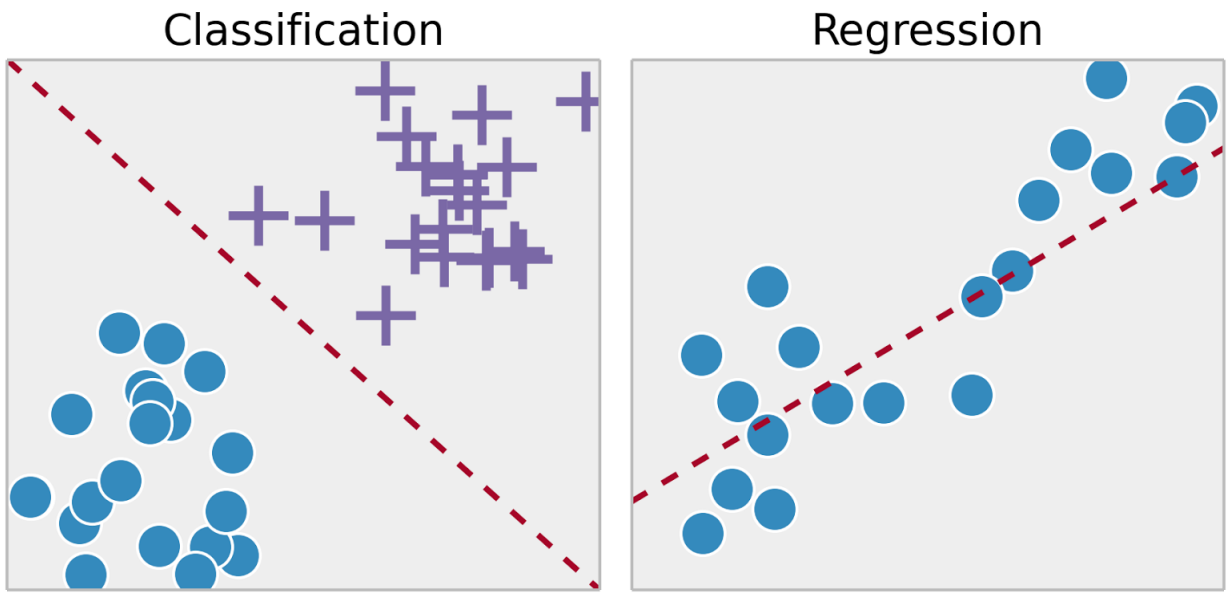




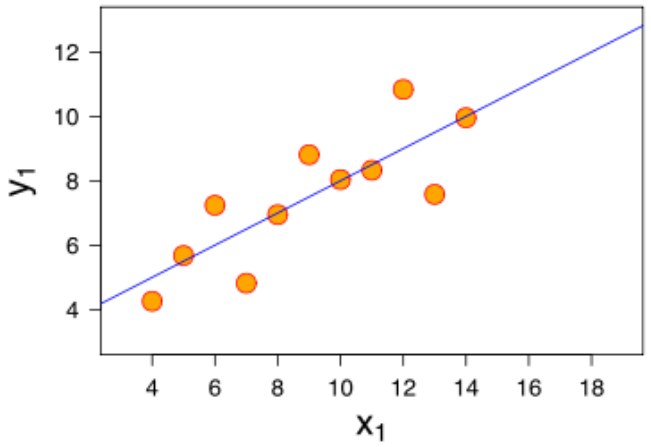

Height vs Weight
160
120
80
40
0
Weight (kg)
105 120 135 150 165 180 195 210 225 240
Height (cm)
Weight (kg)

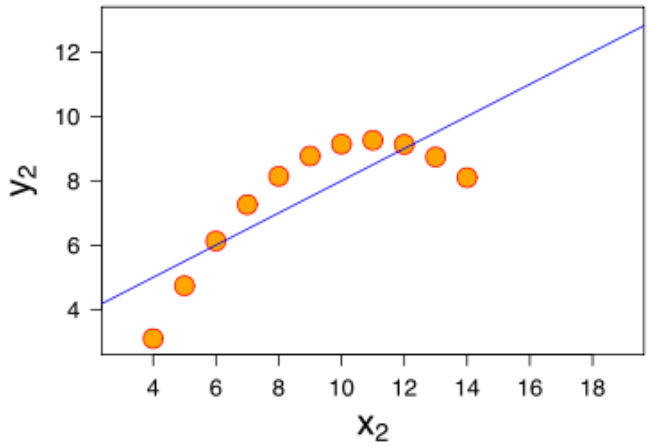

100
80
60
40
20
0
Frozen yogurt sold (in lbs)
20 30 40 50 60 70 80 90 100
High temperature (in degrees F)

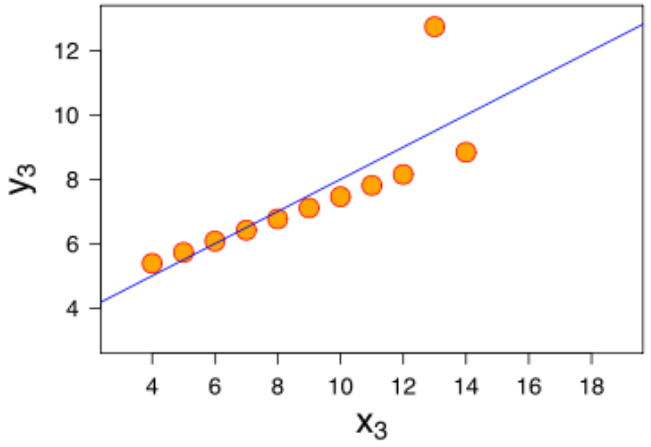

Hourly Electricity Consumption
Jan. 18 through March 2014
OLS R^2 =0.48
3.5
3.0
2.5
2.0
1.5
1.0
0.5
0.0
Hourly Electricity Use (kWh)
0 10 20 30 40 50 60 70
Outdoor Temperature (deg F)

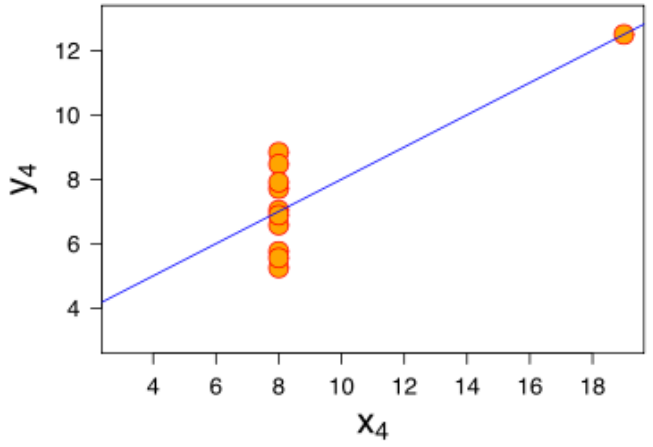

Classification
Regression

What lines "really" best fit each case?



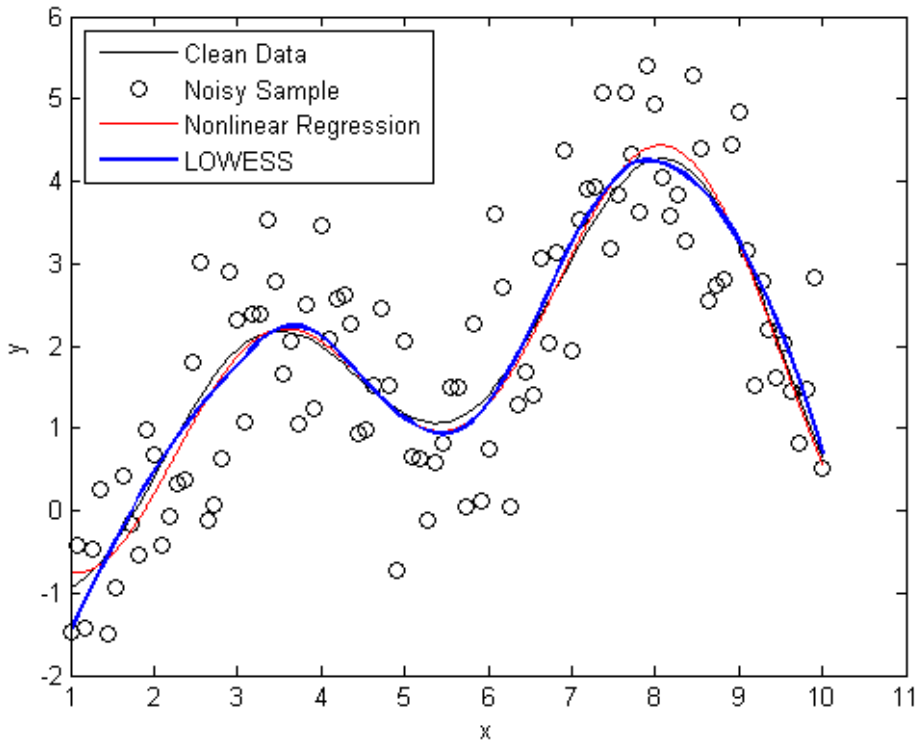


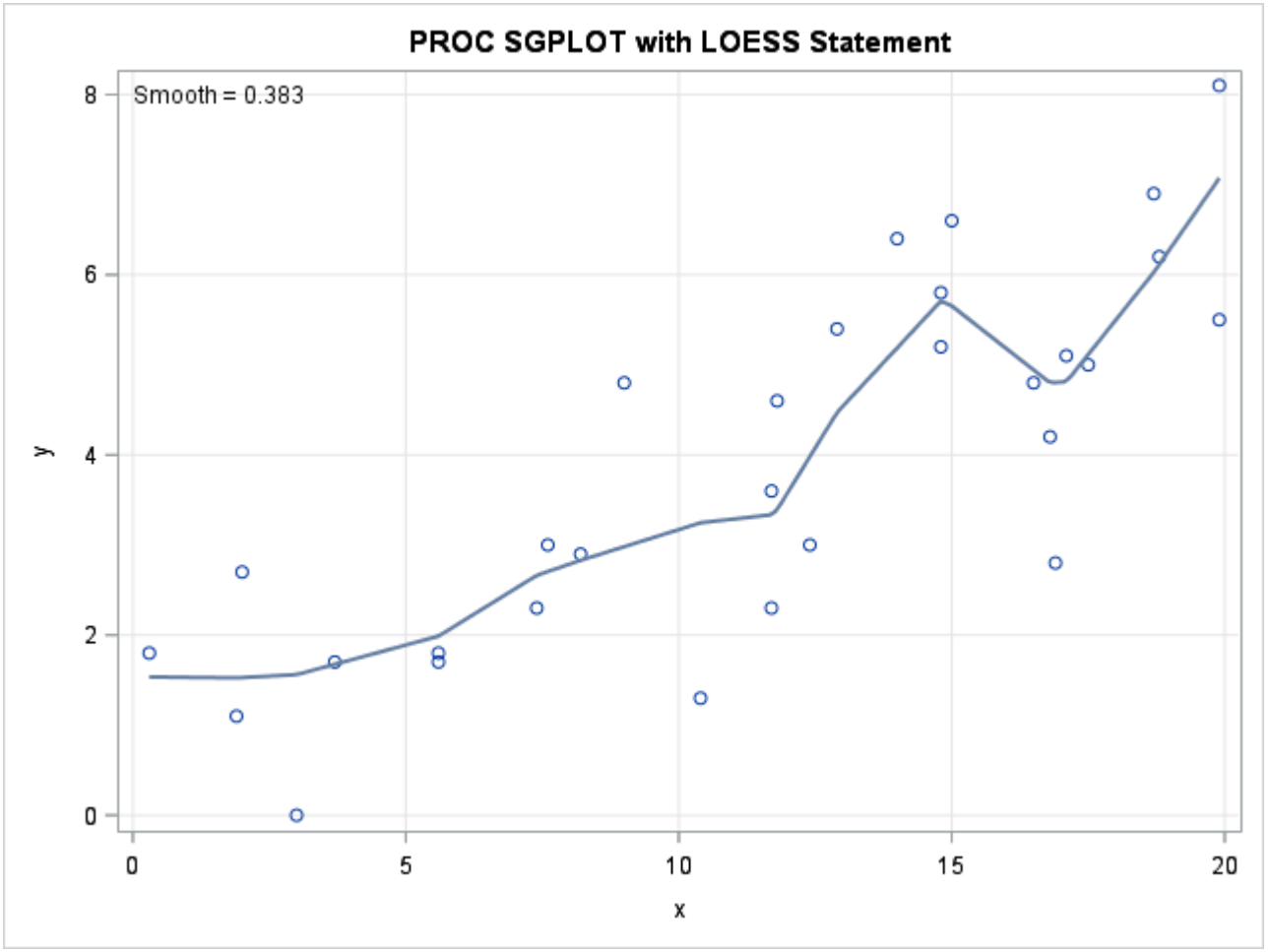




Loess/Lowess Regression

- Loess regression is a nonparametric technique that uses ***local weighted*** regression to fit a **smooth curve** through points in a scatter plot.





Lowess Algorithm

- Locally weighted regression is a very powerful non-parametric model used in statistical learning .Given a *dataset* **X**, **y**, we attempt to find a *model* parameter β**(x)** that minimizes *residual sum of* ***weighted*** *squared errors*. The weights are given by a *kernel function(k or w)* which can be chosen arbitrarily .

Algorithm

1. Read the Given data Sample to **X** and the curve (linear or non linear) to **Y**
2. Set the value for Smoothening parameter or Free parameter say **τ**
3. Set the bias /Point of interest set **X0** which is a subset of **X**
4. Determine the weight matrix using :

$$w(x, x_o) = e^{-\frac{(x-x_o)^2}{2\tau^2}}$$

5. Determine the value of model term parameter β using :

$$\hat{\beta}(x_o) = (X^T W X)^{-1} X^T W y$$

6. Prediction = $X_0 * \beta$

Source Code

https://github.com/profthyagu

Lab Program 9

- **Implement and demonstrate the FIND-S algorithm for finding the most specific hypothesis based on a given set of training data samples. Read the training data from a .CSV file.**

Day	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

Algorithm : Find-S, a Maximally Specific Hypothesis

1. Initialize **h** to the most specific hypothesis in **H**
2. **For** each positive training instance **x**
   - **For** each attribute constraint $\mathbf{a}_i$ in **h**

     If the constraint $\mathbf{a}_i$ in **h** is satisfied by **x** then do nothing

     else replace $\mathbf{a}_i$ in h by the next more general constraint that is satisfied by **x**
3. Output hypothesis **h**

Step1: Find S

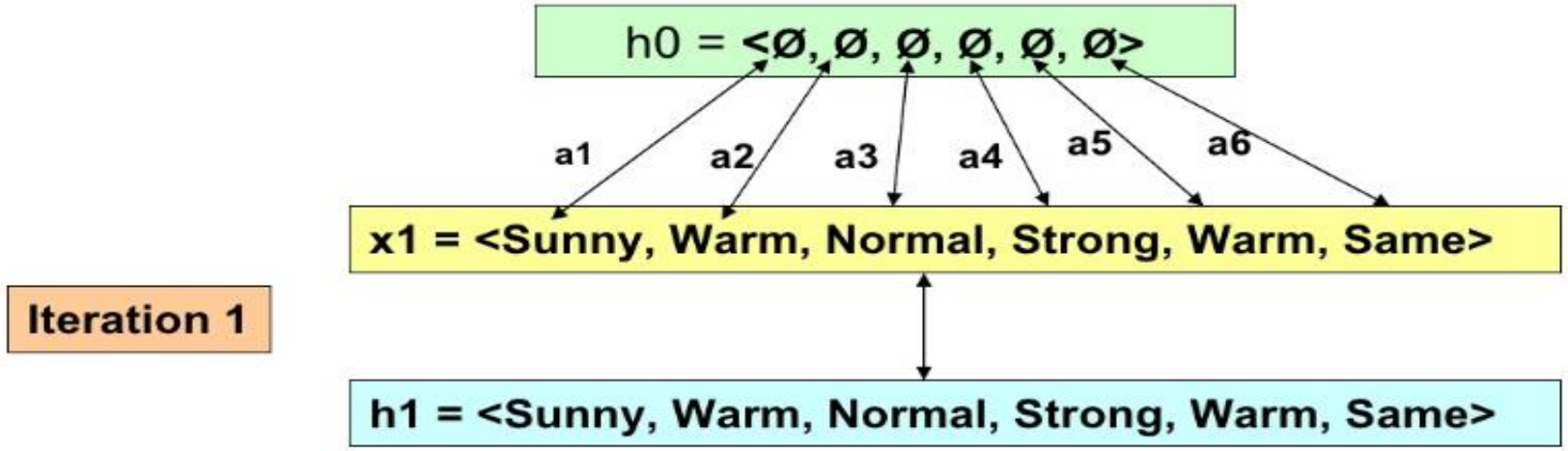
Example	*Sky*	*AirTemp*	*Humidity*	*Wind*	*Water*	*Forecast*	*EnjoySport*
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

1. Initialize h to the most specific hypothesis in H

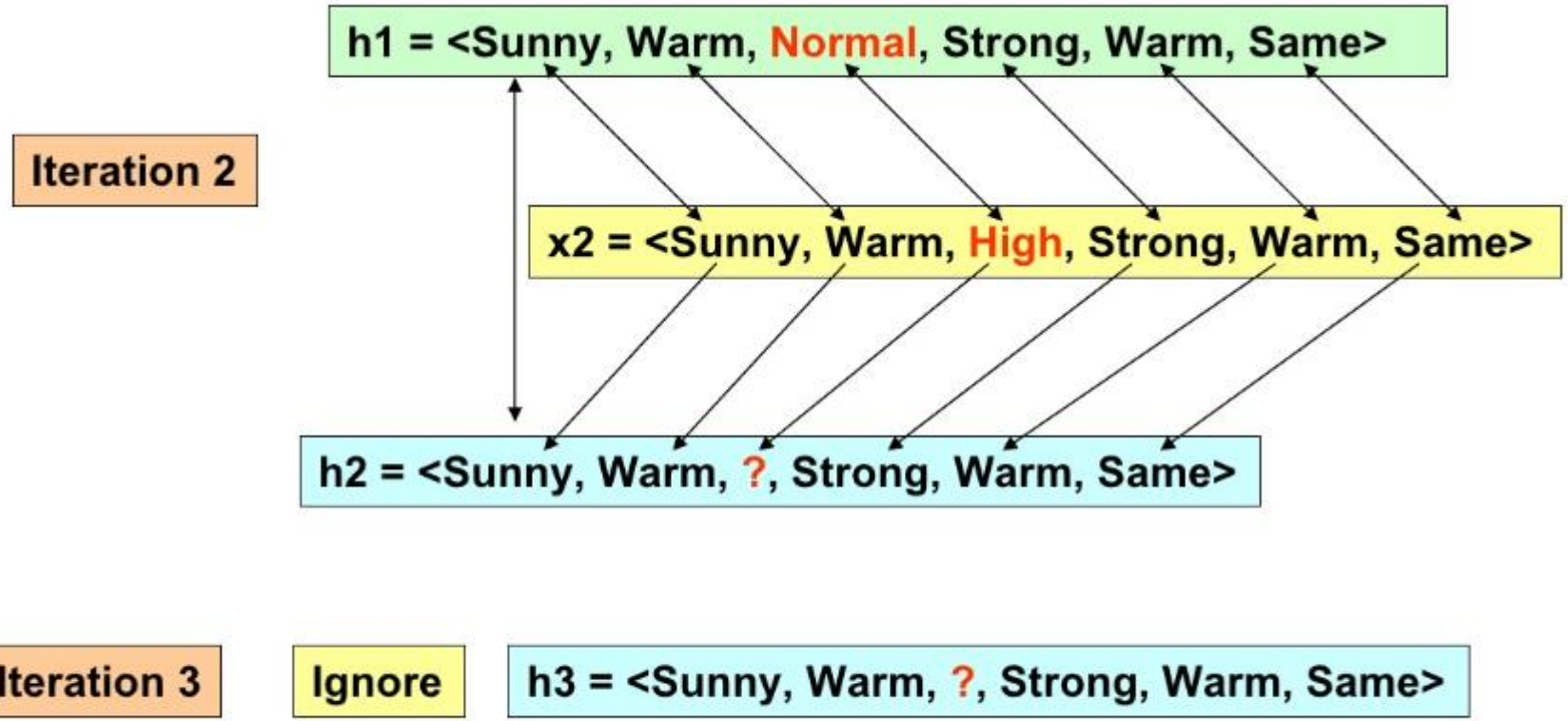
h0 = **<Ø, Ø, Ø, Ø, Ø, Ø>**

Step2 : Find S

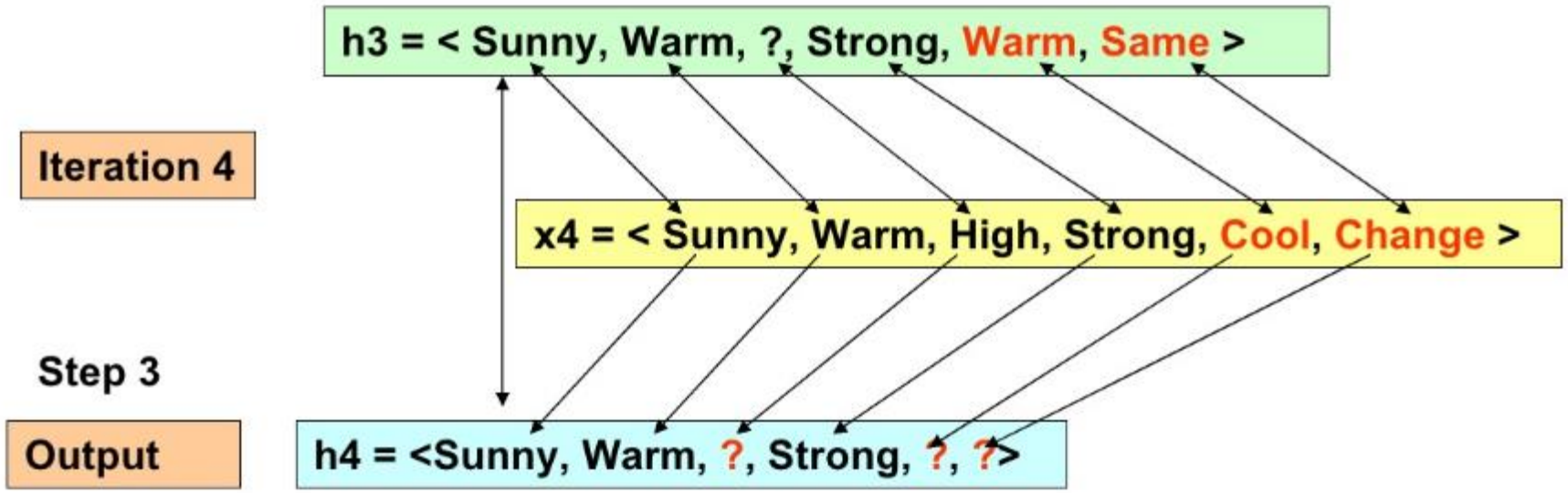
2. For each positive training instance x
   - For each attribute constraint a_i in h
     If the constraint a_i is satisfied by x
     Then do nothing
     Else replace a_i in h by the next more general constraint that is satisfied by x



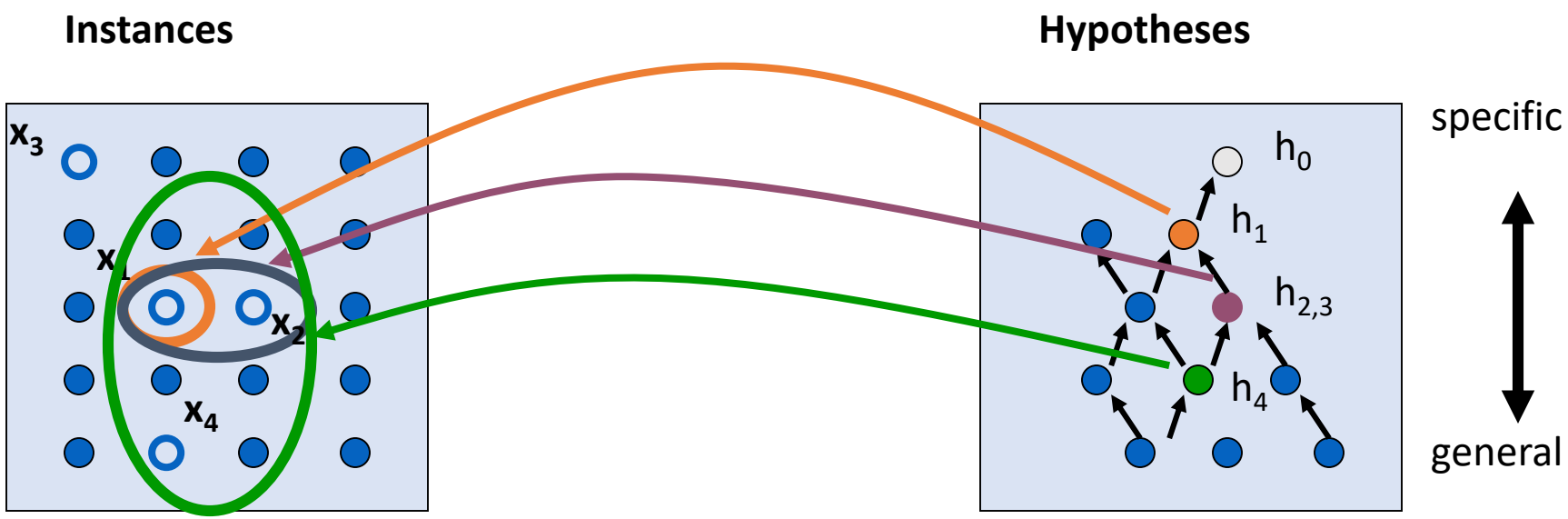
Step2 : Find S


h1 = <Sunny, Warm, Normal, Strong, Warm, Same>
Iteration 2
x2 = <Sunny, Warm, High, Strong, Warm, Same>
h2 = <Sunny, Warm, ?, Strong, Warm, Same>
Iteration 3
Ignore
h3 = <Sunny, Warm, ?, Strong, Warm, Same>

Iteration 4 and Step 3 : Find S



Hypothesis Space Search by Find-S



x_1=<Sunny,Warm,Normal,Strong,Warm,Same>+

x_2=<Sunny,Warm,High,Strong,Warm,Same> +

x_3=<Rainy,Cold,High,Strong,Warm,Change> -

x_4=<Sunny,Warm,High,Strong,Cool,Change> +

h_0 = < Ø, Ø, Ø, Ø, Ø, Ø,>

h_1=< Sunny,Warm,Normal,Strong,Warm,Same>

$h_{2,3}$=< Sunny,Warm,?,Strong,Warm,Same>

h_4=< Sunny,Warm,?, Strong,?,?>

Source Code

https://github.com/profthyagu

Lab Program 10

For a given set of training data examples stored **in** a .CSV file, implement **and** demonstrate the Candid ate - Elimination algorithm to output a description of the set of all hypotheses consistent **with** the trai ning examples

Candidate Elimination Algorithm

- The CANDIDATE-ELIMINATION algorithm computes the version space containing all hypotheses from **H** that are consistent with an observed sequence of training examples.
- It begins by initializing the version space to the set of all hypotheses in H; that is, by initializing the **G** boundary set to contain the ***most general hypothesis in H***

$$G_o \leftarrow \{(?, ?, ?, ?, ?, ?)\}$$

- and initializing the S boundary set to contain the most specific (least general) hypothesis

$$S_o \leftarrow \{(\emptyset, \emptyset, \emptyset, \emptyset, \emptyset, \emptyset)\}$$

2.5 Candidate Elimination Algorithm

$G \leftarrow$ maximally general hypotheses in H

S $\leftarrow$ maximally specific hypotheses in H

For each training example d=<x,c(x)>

Case 1 : If d is a positive example

Remove from G any hypothesis that is inconsistent with d

For each hypothesis s in S that is not consistent with d

- *Remove s from S.*
- *Add to S all minimal generalizations h of s such that*
  - *h consistent with d*
  - *Some member of G is more general than h*
- *Remove from S any hypothesis that is more general than another hypothesis in S*

Case 2: If d is a negative example

Remove from S any hypothesis that is inconsistent with d

For each hypothesis g in G that is not consistent with d

- *remove g from G.*
- *Add to G all minimal specializations h of g such that*
  - *h consistent with d*
  - *Some member of S is more specific than h*
- *Remove from G any hypothesis that is less general than another hypothesis in G*

An Illustrative Example

Figure traces the CANDIDATE-ELIMINATION algorithm applied to the first two training examples from table

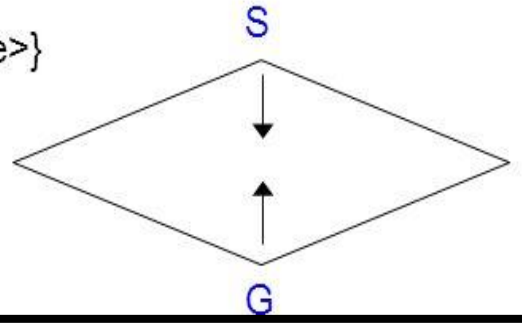
Candidate-Elimination Algorithm

Example	Sky	AirTemp	Humidity	Wind	Water	Forecast	EnjoySport
1	Sunny	Warm	Normal	Strong	Warm	Same	Yes
2	Sunny	Warm	High	Strong	Warm	Same	Yes
3	Rainy	Cold	High	Strong	Warm	Change	No
4	Sunny	Warm	High	Strong	Cool	Change	Yes

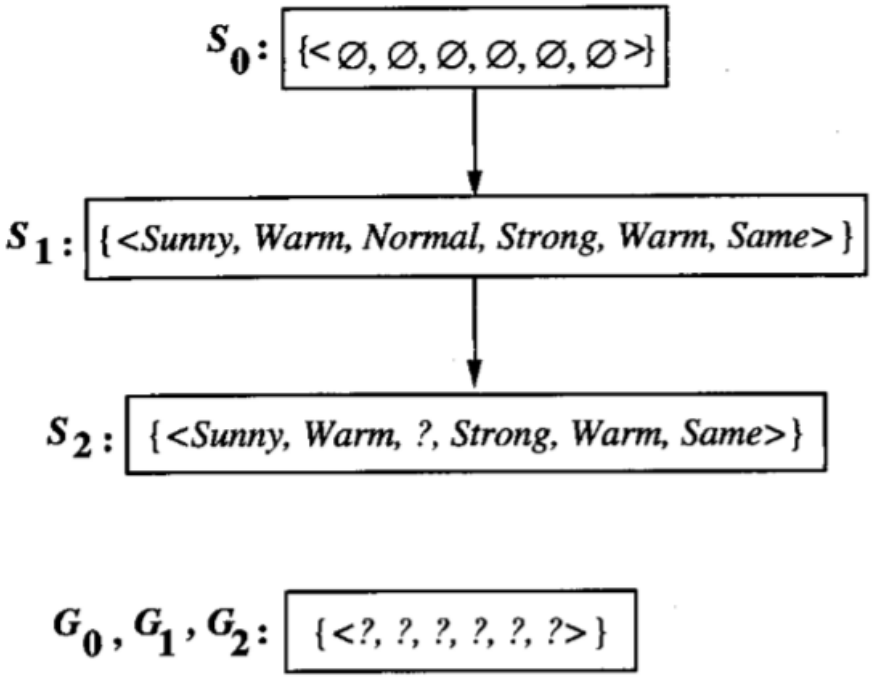
S_0 = {<∅, ∅, ∅, ∅, ∅, ∅>}
G_0 = {<?, ?, ?, ?, ?, ?>}

S_1 = {<Sunny, Warm, Normal, Strong, Warm, Same>}
G_1 = {<?, ?, ?, ?, ?, ?>}

S_2 = {<Sunny, Warm, ?, Strong, Warm, Same>}
G_2 = {<?, ?, ?, ?, ?, ?>}



Trace1



Training examples:

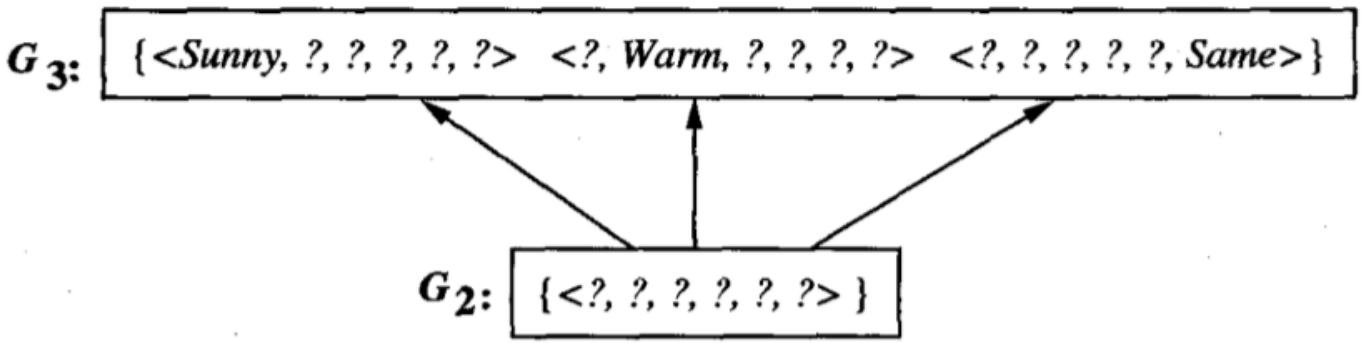
1. <*Sunny, Warm, Normal, Strong, Warm, Same*>, *Enjoy Sport = Yes*

2. <*Sunny, Warm, High, Strong, Warm, Same*>, *Enjoy Sport = Yes*

CANDIDATE-ELIMINATION Trace 1. S_0 and G_0 are the initial boundary sets corresponding to the most specific and most general hypotheses. Training examples 1 and 2 force the S boundary to become more general, as in the FIND-S algorithm. They have no effect on the G boundary.

Trace 2

S_2, S_3: { <*Sunny, Warm, ?, Strong, Warm, Same*> }

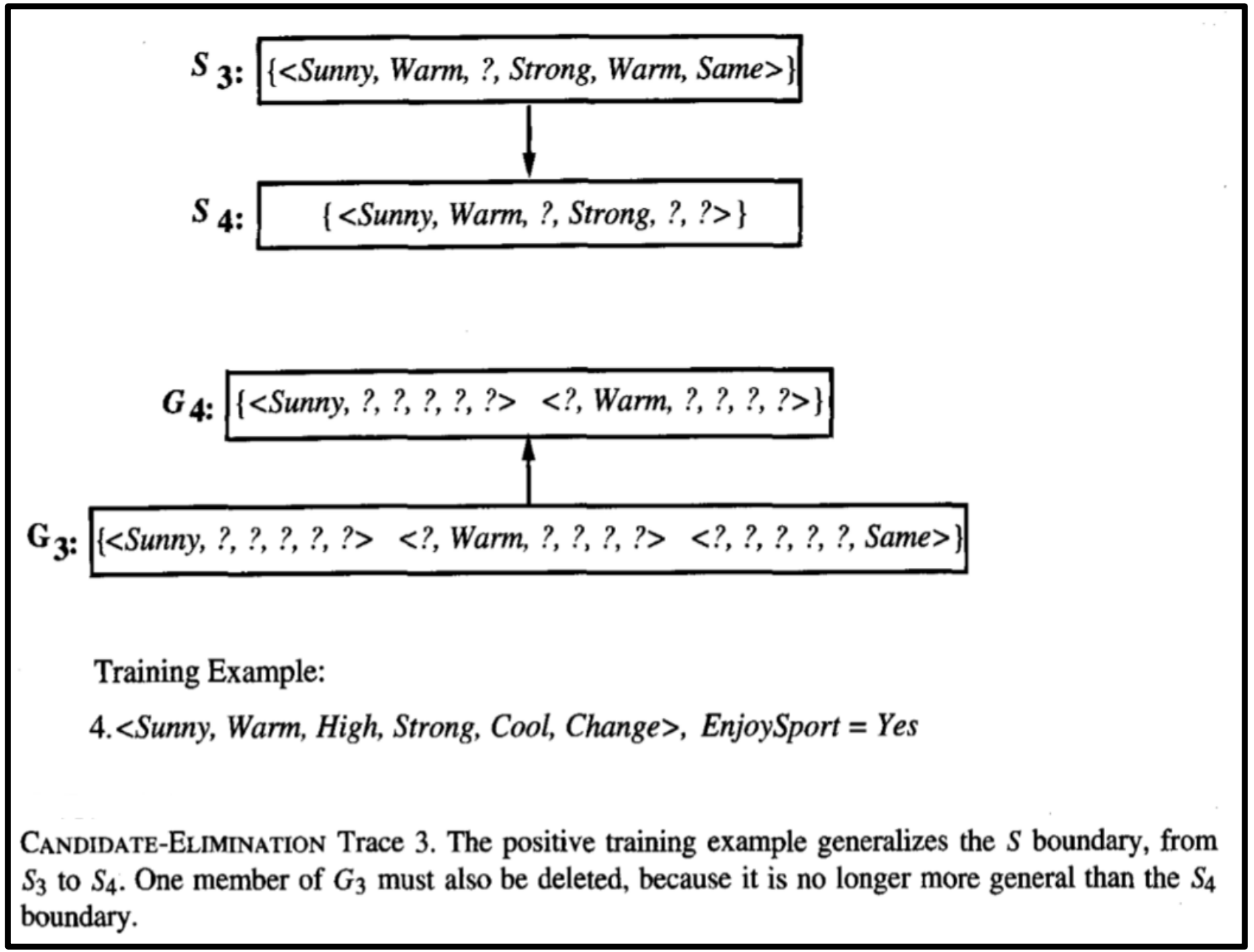


Training Example:

3. <*Rainy, Cold, High, Strong, Warm, Change*>, *EnjoySport=No*

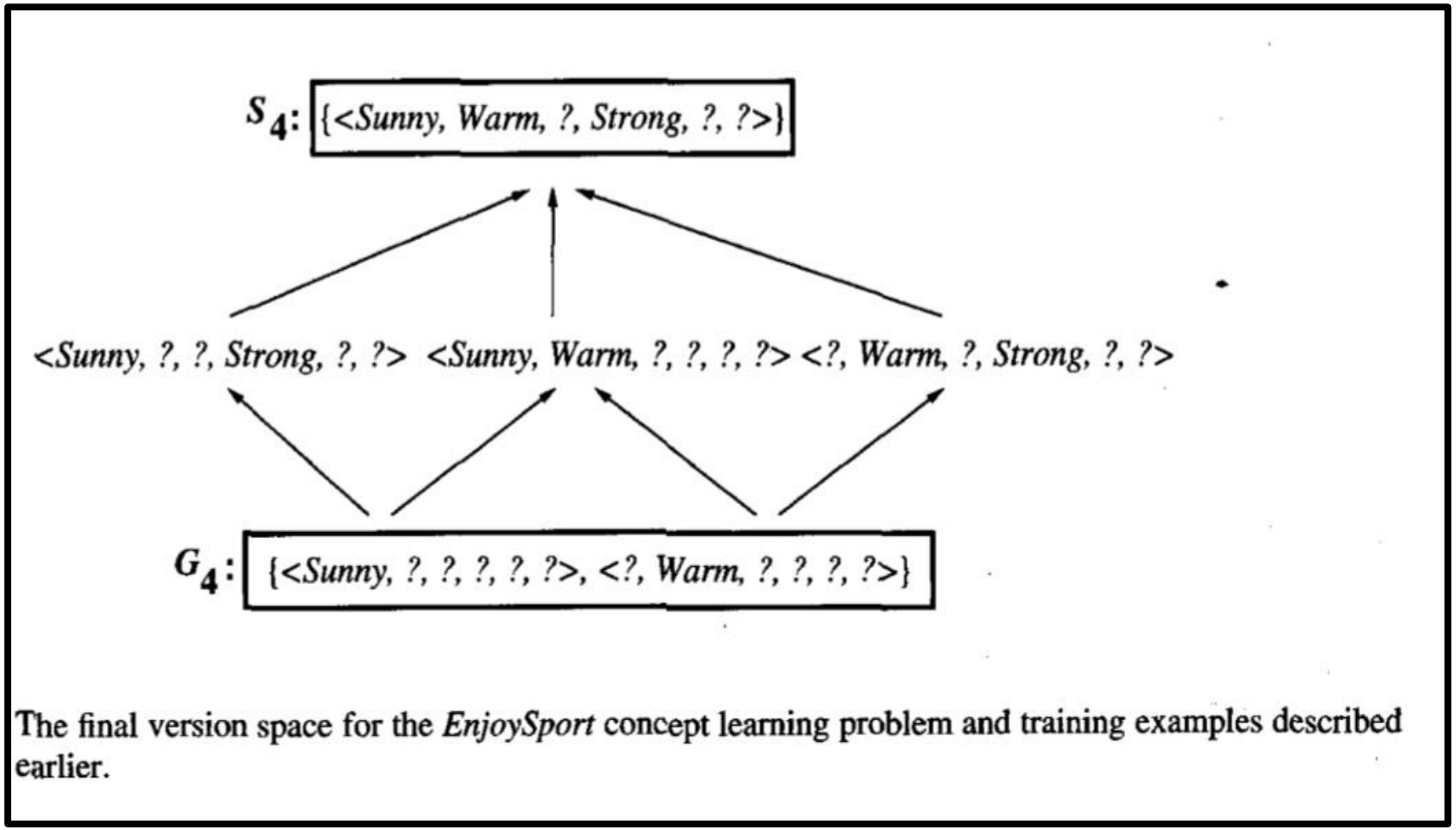
CANDIDATE-ELIMINATION Trace 2. Training example 3 is a negative example that forces the G_2 boundary to be specialized to G_3. Note several alternative maximally general hypotheses are included in G_3.

Trace3



CANDIDATE-ELIMINATION Trace 3. The positive training example generalizes the S boundary, from S_3 to S_4. One member of G_3 must also be deleted, because it is no longer more general than the S_4 boundary.

Final Version Space



The final version space for the *EnjoySport* concept learning problem and training examples described earlier.

Source Code

https://github.com/profthyagu

Github Repository

- https://github.com/profthyagu