

## Concurrency Theory

Prof. Dr. Peter Thiemann  
Marius Weidner, Leonardo Mieschendahl

University of Freiburg  
Winter 2025

### Sheet 10

Due: Monday, 2026-01-26

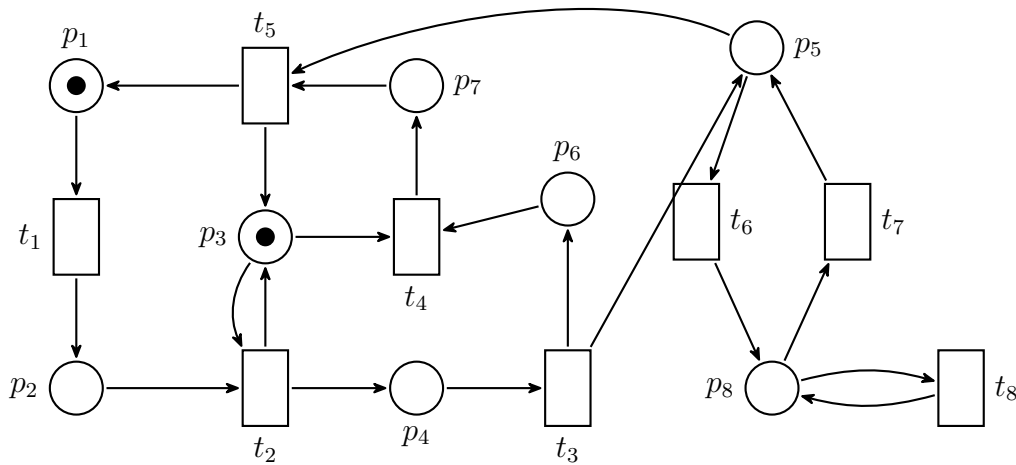
#### Exercise 10.1 (Categorical Properties of Net Homomorphisms)

Let  $N_i = (P_i, T_i, F_i, M_i)$  be nets. Based on Definition 16.1, check that net homomorphisms satisfy the following properties:

- (a) Identity: Show that for any net  $N$ , the identity mapping  $id_N : P \cup T \rightarrow P \cup T$  is a net homomorphism from  $N$  to itself.
- (b) Composition: Let  $h : N_1 \rightarrow N_2$  and  $g : N_2 \rightarrow N_3$  be net homomorphisms. Prove that their functional composition  $(g \circ h) : N_1 \rightarrow N_3$  is also a net homomorphism.

#### Exercise 10.2 (Branching Processes)

Consider the Petri Net  $N$  below.



- Give the marking graph of  $N$ .
- Provide three non-isomorphic branching processes  $B_1, B_2, B_3$  of  $N$  such that  $B_1 \subseteq B_2$  and  $B_2 \not\subseteq B_3 \not\subseteq B_1$ .

#### Exercise 10.3 (True Concurrency Semantics for CSS)

Translate the CCS process  $P = z.\text{nil} + y.(x.\text{nil} \parallel \bar{x}.\text{nil})$  into a Petri Net.