

The Bitcoin Bridge

Mitch Lowry

December 1, 2016

This project is a careful, organized attempt at implementing, discussing, and evaluating different econometric models in the context of explaining the price formation of Bitcoin. It is important to note here that this project does not necessarily strive to create a way to predict Bitcoin prices. I will give an introduction explaining important background information about Bitcoin, provide the most comprehensive literature review of work done in any Bitcoin paper, carefully explain the assumptions and limitations of multiple regression, the vector auto-regression model, structural equation models, and some models for economic bubbles, and investigate whether the use of the Ripple payment protocol system has influenced the price of Bitcoin. I review the literature of Bitcoin pricing and hope to incorporate ideas and data from many papers so as to create and evaluate a *VAR* model from an econometrically sound perspective by considering all of the variables from the onset, and I also hope to incorporate new, more innovative measures of investor interest in Bitcoin into a model used to detect multiple bubbles in the Bitcoin price time-series data.

1 Introduction

Since the introduction of the Bitcoin by Satoshi Nakamoto on January 3, 2009, an unforeseen number of cryptocurrencies have been created, many of which are based heavily on Bitcoin. This strange math based phenomenon of the cryptocurrency piques much debate and interest among economists. Not surprisingly, most economic research on cryptocurrencies is devoted to the most highly publicized and valued of cryptocurrencies, Bitcoin; however, there is a relatively new currency that could significantly impact the cryptocurrency market and international business. This currency is Ripples XRP. The XRPs most important role is to act as a bridge currency within Ripples free, open source payment protocol. This payment protocol allows parties from any part of the globe to

perform transactions between any fiat currencies, commodities, cryptocurrencies, or other stores of value in as little as five seconds with little to no transaction fees.

There are many large questions to be tackled about the impact of Ripple on the global economy; however, the objective of this study is to tackle a somewhat complex one. I would like to determine whether or not usage of Ripple has affected the price of the Bitcoin. The rationale of this possibility stems from my belief that the Ripple payment protocol could have a positive influence on the demand of Bitcoins by making transactions with Bitcoins safer. Specific details about this will be covered in the conceptual framework section.

This paper uses much of the discussion of the fundamental concepts of Bitcoin described in Fantazzini (2016), and also includes some other information. For more detailed descriptions of Bitcoin see Becket et al. (2013), Segendorf (2014), Dywer (2014), Boehme et al. (2015), Bitcoin (2015), Velde (2013), Lo and Wang (2014), Baden and Chen (2014), Ali et al. (2014), and ECB (2012, 2015).

1.1 How does Bitcoin Work?

Bitcoin is a decentralized payment protocol system. It is composed of a network of many computers that are connected through the internet. Each of these computers are called nodes (Cocco and Marschesi 2016). The Bitcoin payment system is based off of two concepts: (i) digital signatures and (ii) a cryptographic hash function. The digital signatures include a public key and a private key. That is, the location of each Bitcoin address is represented by an alphanumeric key, known as the public key, and there exists a private key, known only to the owner of that Bitcoin address that gives one control of the Bitcoins at that location. For any payment sent from a specific Bitcoin address, that payment must be verified by the owner of that Bitcoin address by signing the payment with the private key associated with that address. This means that knowledge of a Bitcoin's private key means that you own it (or can at least make transactions with it, which is essentially the same). These signatures allow three important things for payments: one can verify who the sender was; one cannot deny having sent the message; and the message was not altered in transit. These signatures provide a security as far as transactions go. At every point in time, there is a public ledger in Bitcoin balance of every Bitcoin address is given. Additionally, for each transaction there are one or more sending addresses, each of which has an associated amount being sent to one or more receiving

addresses, and each of these receiving addresses has an amount received; note that this information does not include how much was sent from each sending address to each receiving address. One has the amount total sent to the receiving addresses and how much each received, but it is frequently not possible to link sending addresses to receiving addresses. This ledger is updated about every 10 minutes in blocks of transactions (Fantazzini 2016).

The cryptographic function (in the case of Bitcoin, this is the secure hash algorithm SHA-256 / type Secure Hash Algorithm SHA-2 (see Dang 2002 for details)) is used in conjunction with past transaction history to verify the transactions in the new block. After the check of a transaction is made through digital signatures and assuring there is enough money for the transaction, validation nodes compete to record the transaction into the new Blockchain. In this way, all transactions since the previous block are recorded by different network members. In this way, the work is distributed. Once this is done, the new block is put into the hash function and we receive a hash called a digest. This digest is used with some given one-time use alphanumeric code (nonce), and these two are used in the second hash function to create a hash for the new block. This is a computationally heavy task because one must find some random nonce such that the hash of the new block has some specific number of initial zeros (Cocca and . Once a node, say node a, has found a correct nonce, node a tells this nonce to everyone else on the network, who are called validation nodes; the validation nodes to see if the nonce works; and the new block chain is recorded and node a is given a reward. (Cocco and Merchesi 2016). This reward is in the form of new Bitcoins and some voluntary contributions. (Fantazzini 2016).

2 Literature Review

2.1 Time-Series Bitcoin Pricing Models

Upon reviewing the literature, I came across a literature review published in May of 2014 by Ciaian et al. (2014), and another literature review published in 2016 (Fantazzini et al. 2016). I review many of the papers used in these literature reviews and provide a bit more detail. All of the discussed paper make use of the plentiful amount of time-series data available about the Bitcoin network. I have also included papers not included in these literary analyses. In the previous literature there are quite a few factors that have been identified as important for determining the price of Bitcoin: (i) interacting between BitCoin demand and supply (Buchholz et al. 2012; Ciaian

et al 2014; Kanacs et al. 2015); *(ii)* global financial indicators (van Wijk 2013; Bouoiyour 2015); *(iii)* attractiveness for investors (Kristoufek 2013; MacDonell 2014; Ciaian et al 2014; Kanacs et al 2015; Bouoiyour 2015); and *(iv)* and information related to the creation of Bitcoins (Cocco and Marchesi 2016; Garcia et al. 2014).

Buchholz et al. (2012) use VAR modeling to determine the price of Bitcoins. The study concludes that the interaction between Bitcoin supply and demand is a major determinant of Bitcoin prices. These results are consistent with the results of Ciaian et al. (2014) that the day lag of Bitcoin prices in US dollars, the four day lag of total Bitcoins that have been mined, and the one and two day lags of Bitcoin days destroyed. Krancs et al. (2015) also find that the lag of Bitcoin prices is important. Kristoufek (2013), however, explains that the price formation of Bitcoin cannot be explained by standard economic theories because supply-demand fundamentals are absent from Bitcoin markets. He says this for the following reasons: *(i)*, Bitcoin exists independently of any financial regulatory systems, so the supply of Bitcoin is detached from what is going on in the economy, and *(ii)* there are no interest rates for cryptocurrencies, so profits can only be made on price changes. The problem with Kristoufek’s model and explanation is that only bivariate VAR for the weekly log-returns of Bitcoin prices and is employed, and other variables that have been found important in more contemporary literature were not considered in conjunction with these other variables, which could result in omitted variable bias, and, thus, model misspecification. Kristoufek (2013) uses a bivariate Vector Error Correction (VEC) model in conjunction with his bivariate VAR. This paper was interesting in that it used normalized daily Google search data to gauge the interest in Bitcoin, and it uses the daily views of the Bitcoin wikipedia page an alternate proxy. This was the first paper to include the speculative nature of Bitcoin. He created a positive feedback variable and a negative feedback variable and found a bidirectional relationship between search queries and prices viceversa. Again, this should be taken with a grain of salt, but including this feedback idea into models that consider more regressors is a good idea. The feedback loops used by Kristofek (2013) are discussed in Section 2.2.

Van Wijk (2013) stresses that since Bitcoin is a fiat currency, the only reason Bitcoin has value is because investors and other buying agents believe that Bitcoins will retain their value. He claims that general economic indicators are good indicators of whether or not Bitcoin will retain its value, so he performs Ordinary Least Squares (OLS) on Bitcoin prices with such indicators and then applies an

error correction model to get long term relationships because performing OLS on differenced variables results in loss of long run effects in the outcome of the analysis. Van Wijk (2013) found that in the short run the only variable that had a significant influence on the value of Bitcoin was the closing value of the Dow Jones index (positive influence) but that there were insignificant variables, namely the closing value of the Nikkei 225 (negative influence), the euro-dollar exchange rate (positive influence) and the yen-dollar exchange rate (positive influence), with large coefficients that may explain some of the variation in Bitcoin. Whether this is a legitimate claim or he is just trying to make himself look better is up for debate. In the long run he found that the following variables were important for determining the price of Bitcoin: *(i)* Dow Jones index (positive influence), *(ii)* the euro-dollar exchange rate (negative influence), and *(iii)* the yen-dollar exchange rate (negative influence). Dimitrova (2005) claims that there could be a negative relationship between Bitcoin prices and financial indicators. Dimitrova (2005) says that if stock prices fall, then foreign investors may decrease their stock with BitCoin; however, what Dimitrova does not account for here is that a decline in the price of some stock may also be a signal to purchase that stock if one does not currently hold any of it (or even if they do). Ciaian et al. (2014) and MacDonell (2014) find no such relationships between Bitcoin prices and macroeconomic indicators.

MacDonell (2014) used log-periodic power law (LPPL) modeling in an attempt to make a model that can predict crashes in Bitcoin prices. The motivation from this clearly stems from the major Bitcoin bubble of 2013. Of the variables MacDonell tested, only the CBOE Volatility Index was found to be significant, which implies that only investor behavior matters for determining the prices of Bitcoins. This is likely due to the fact that MacDonell used news mentions as a proxy for consumer participation. This does not seem like a good enough proxy, and so the regression would not really parallel consumer participation. Both Kristoufek (2013) and Ciaian (2014) found that indicators of the Bitcoin supply and demand were significant in determining the price of Bitcoin in the short run and in the long run. They used a somewhat more reasonable proxy for attractiveness for investors, the volume of daily BitCoin views on Wikipedia. According to Kristoufek (2013) this proxy is a good indicator of how interested investors are in Bitcoin. Fry (2014) and Fry (2015) continue improving and using the LPPL model and confirm that there was a bubble in December of 2013 before the large price crash. They also found that the long term fundamental value of Bitcoin is zero, and that the bubble component of the model accounts for 48.7 percent of all prices. Work has been

done to create tests for multiple bubbles by using a moving time window (Phillips and Yu 2011; Phillips et al. 2011; and Phillips et al. 2015). This model is called the generalized-supremum ADF test (GSADF). Malhotra and Maloo (2014) implement the ADF and find bubble like behavior from August - October 2012 and November 2013 - February 2014. These bubble models demonstrate the importance of including speculative variables in regressions involving Bitcoin prices. These bubble models are discussed in section

Glaser et al. (2014) used a vector auto-regressive model with lagged effects and GARCH effects. They found, unlike anyone before them, that Bitcoin attractiveness and Bitcoin supply and demand were both important regressors. This paper follows the lead of Kristoufek (2013) and also uses the daily views on the English Bitcoin Wikipedia as a proxy for user interest. This paper was also helpful for future modeling in that dummy variables for 24 events gathered from <https://en.bitcoin.it/wiki/History>. These events were either significant positive or negative events. This work was done using a four-variate VAR(1) model with first-differenced data from January 2009 to October 2013. This model, like that of Kristoufek, finds a couple of positive feedback loops. The first one is that increased Bitcoin popularity, leads to more searches of Bitcoin, which is related to more social media posts about Bitcoin, which causes more people to buy Bitcoin, which increases Bitcoin prices. Secondly, after users get information about Bitcoin, they download the client, and the increase in the number of users, which drives up prices because supply is deterministic.

Garcia et al (2014) extend this research on speculation by using different variables. Garcia uses the following variables in a 4-variables in a VAR(1) model, which shows that there is a negative relationship between searches and prices:

- number of new Bitcoin users adopting the currency at time t , which is proxied by the number of downloads of Bitcoin software client;
- bitcoin price in USD, EUR, and CNY;
- information search proxied by normalized daily Google search data (and uses daily views of the Bitcoin wikipedia as a robustness check);
- information sharing (or online word-of-mouth communication) proxied by the daily number of

tweets about Bitcoin B_1 per million twitter messages. Data was taken from <http://topsy.com>, and the following terms were used to find tweets about Bitcoin: 'BTC', 'BTC', 'bitcoin', or 'bitcoin'.

- valence (some measure of general positiveness of twitter feeds)
- other thingy bob maybe.

This model, like that of Kristoufek, finds a couple of positive feedback loops. The first one is that increased Bitcoin popularity, leads to more searches of Bitcoin, which is related to more social media posts about Bitcoin, which causes more people to buy Bitcoin, which increases Bitcoin prices. Secondly, after users get information about Bitcoin, they download the client, and the increase in the number of users, which drives up prices because supply is deterministic.

A couple of econometricians (Bouoiyour and Selmi 2015;) talk about their model. It is useful because has interpretable long-term affects and short-term effects. The model also reaches an equilibrium, and has the advantage that effects found are interpretable in a meaningful way. They found blah blah blahh

2.2 Bitcoin Attractiveness to Investors

The attractiveness of Bitcoin to investors and to vendors depends on both the risk and return of buying and performing transactions with Bitcoins. Vendors accepting Bitcoin may also be worried about the costs of converting Bitcoins into other currencies because the economies that they function in do not operate with Bitcoins. One important risk to consider is the security of Bitcoin exchanges. Since Bitcoin is a digital currency there is a very real threat of cyber-attacks. In fact, Moore and Christin (2013) found that of the 40 Bitcoin exchanges that they examined 18 closed down because of cyber-attacks in which users information and or Bitcoins were stolen. Another thing to consider for investors is the cost of finding out what is worth investing in. Many studies (Gervais, Kaniel, and Mingelgrin 2001; Grullon, Kanatas, and Weston 2004; and Barber and Odean 2008) have found that the decisions of new investors may be distorted by the effect of media attention. This is the rational for the use of news mentions by MacDonell (2014); however, news mentions doesn't seem like good variable for either an explanatory or a predictive standpoint. These is good and bad news, and no way from this variable to tell whether the news is good or bad or even how significant. If one where to

have to use one or two measures of noise chasing to avoid spurious information and multicollinearity, ones that capture how the public feels about media or social media as done in Garcia et al (2014) and large positive or negative events in the Bitcoin, . Such events could potentially be covered by dummy variables.

Here is will discuss the reasoning behind and the construction of the two feedback loops used by Kristoufek (2013) and it's potential in different models or something. Especially in a regression, and what the other literature tells us about these affects, much just pulling from the literature. I will also discuss potential variable to use for these feedback loops.

2.3 Economics of Bitcoin Mining

Since BitCoin has no intrinsic value and is a fiat currency, demand for BitCoins is primarily determined by its expected value in the future, i.e. people do not want to accept or exchange for BitCoins if they believe the price of BitCoin is going to be lower when they plan on using said BitCoins. The supply of BitCoins is determined by the total number of BitCoins in circulation. BitCoins are generated by BitCoin miners who, either individually or in groups, complete the computationally difficult problem of finding and adding blocks to the BitCoin block chain, BitCoins public ledger of past transactions. As mentioned in the backgorund, when miners find a block and update the public ledger, they are given a reward in the form of Bitcoins and voluntary controbutions. New BitCoins are generated and given to the miners as compensation in addition to some donated funds. The hope here was the donated funds would eventually take over for securing interest in confirming transactions on the Bitcoin network as the award twindles. The interesting thing here is that of in the long-run, due to the slowed increase and stopping in growth that there may be large amounts of inflation. Proponents counter this by pointing out that Bitcoins are divisible up to 8 decimal places, and that could even be adjusted.

The difficulty of finding blocks (Usually measured in some form of Hashes/Bitcoin) is adjusted every 2016 blocks based on the total computational power going into mining. This adjustment results in a steady rate of mining; a new block is added to the ledger every ten minutes. The reward that miners receive from finding these blocks is halved every 210000 blocks, which means over two year periods there is a relatively linear increase in the number of BitCoins. This decrease in the reward also means that there is a predefined number of BitCoins in the long-run. This will be 21

million BitCoins in 2140. The process of adding blocks to the ledger is a way to insure an accurate public ledger, and, thus, is related to the security of the Bitcoin system (Nakamoto 2008). One problem here, as hinted at earlier, is that this decrease in the award for Bitcoin disincentives miners that are not optimistic about the market.

Talk about using valence in models, and twitter stuffs.

3 Theory

As previously discussed, studies have found the following things to be important for determining the price of Bitcoin: (i) interaction between Bitcoin demand and supply; (ii) global financial indicators; (iii) attractiveness for investors; and (iv) drivers related to the nature of the construction of Bitcoin.

3.1 Supply-demand Theory

In the spirit of Ciaian et al. (2014) we will also use a modified version of Barros (1979) model to discuss the theory of the interaction between money supply and demand. Firstly, we note that in perfect markets there is equilibrium between money supply and money demand. The Bitcoin model is certainly not a perfect market, but there may be a similar relationship here as with other fiat currencies. For Barros model we have the following equation for the supply of Bitcoins:

(1)

$$M^S = P^B B.$$

In the above equation M^S denotes the supply of Bitcoins, P^B denotes the price of Bitcoins in US dollars, and B denotes the total number of Bitcoins. Based on the Fischer equation money demand M^D is dependent on the general price level of goods, P , the size of the Bitcoin economy, Y , and the velocity of Bitcoins, V . The assumed equation is as follows:

(2)

$$M^D = \frac{PY}{V}.$$

Using the equations one can derive the following price relationship:

(3)

$$P^B = \frac{PY}{VB}.$$

This equation implies the following things about the price of Bitcoin: (i) Bitcoin prices decrease as the velocity and total stock of Bitcoins increases, and (ii) Bitcoin prices increase as the general price level and the size of the Bitcoin economy increases. Thus, we can construct some model of Bitcoin prices by the following:

(4)

$$p_t^B = \beta_0 + \beta_1 p_t + \beta_2 y_t + \beta_3 v_t + \beta_4 b_t + \epsilon_t$$

where each lower case variable is a some measure its corresponding uppercase variable and ϵ_t is the error term at time t .

3.2 Adding Attractiveness to Investors and Vendors and Macroeconomic Indicators

Those things that should increase the security of using Bitcoin and reduce transaction costs or potential transaction costs should increase attractiveness of Bitcoins to both investors and vendors. Theoretically, this should increase the demand of Bitcoins, thereby, increasing the price of Bitcoins by a loose interpretation of equation (3); however, the previous literature review demonstrates that this is not necessarily true. Besides what we have already discussed, one of the largest risks of investing in and accepting Bitcoins as compensation is the high price volatility that Bitcoin is plagued with. This volatility may actually simulate investment, especially when the volatility of the stock market is especially low due to the allure of the possibility of large returns; however, there is obviously good reason to shy from investing in things with such volatility. This high volatility also imposes additional risk on vendors because vendors who do accept Bitcoins may receive less (or more) money than they were supposed to receive due to prices changing before they are able to convert their Bitcoins into whatever currency they would like.

As previously discussed, a new block is added to the Bitcoin chain block every ten minutes. This means that the average time that one has to wait in order to convert their Bitcoins into another currency is five minutes. Due to the high price volatility of Bitcoin the vendor may receive less money than they had hoped, will incur transaction fees, and perhaps a little stress or actual costs from

training employees and dealing in Bitcoins. In enters Ripple. Ripple is a cryptographically secure internet protocol that is a peer-to-peer payment system. When using Ripple, XRP acts as a bridge currency so that one Ripple user can pay in the currency of their choice and the other Ripple user can receive said payment in the currency of their choice. This is done with phenomenally low transaction fees. The fees are set to be essentially zero, but not zero so as to protect from adversaries of Ripple who may try to overload the Ripple ledger by spamming transactions (Schwartz et al. 2014).

This payment system decreases many of the negative aspects of dealing in Bitcoins and investing in Bitcoins. For one thing, volatility is much less of an issue for both investors and vendors. This is because one is able to use the Bitcoin Bridge (the integration of the Bitcoin network and Ripple) to more quickly convert Bitcoins into a currency of their preference or to more quickly liquidate Bitcoin holdings. Ten minutes may be a long time given the price volatility of Bitcoin, but a matter of seconds is almost a laughable amount of risk. The Bitcoin Bridge also helps to reduce the risk associated with using Bitcoin exchanges. People with Ripple wallets need not ever directly work inside of payment systems specific to Bitcoin, and their personal information is safer and transactions, more secure.

By our previous discussions we expect those macroeconomic indicators that are positively related to the general price level of good to be positively related to the price of Bitcoins and those that are negatively related to be negatively related to the price of Bitcoins.

Thus, we adjust equation (4) as follows to account for the attractiveness to investors and macroeconomic indicators:

(5)

$$p_t^B = \beta_0 + \beta_1 p_t + \beta_2 y_t + \beta_3 v_t + \beta_4 b_t + \Sigma \gamma_i a_{i_t} + \Sigma \alpha_j m_{j_t} + \epsilon_t$$

where each a_{i_t} is an indicator of Bitcoin's attractiveness to investors and each m_{i_t} is a macroeconomic indicator.

3.3: Adding Variables Related to Mining

4 Data

All data was acquired from *quandl.com*. All data is daily data ranging from August 5, 2010 until October 28, 2016. There are different days missing for each of the variables, so the total number of observations will depend on the regression.

The dependent variable is the BTC-USD exchange rate, $price_{ave}$ in US dollars averaged over all 24 hours over all Bitcoin markets.

Data on the daily Bitcoin days destroyed, $bcdde$ is used as a proxy for the velocity of Bitcoins. This is a pretty good indicator of Bitcoin hoarding. This measure is added to after each transaction during the day. The amount added to the measure for each transaction on a given day is equal to the sum of the days since each Bitcoin was spent for each Bitcoin. That is, change in the rate of change of $bcdde$ while adjusting for the total number of Bitcoins in circulation seems like a good measurement of changes in hording. In the short-run large decreases in the Bitcoin days destroyed may signal that people who has previously been hoarding are starting to spend their BTCs. If we view people who have been hoarding for a long time as wise (they have done quite well), then a large change in their hoarding behavior may be a sign to start selling Bitcoin. These people may on average be more informed than all of the unfortunate people who didn't buy in early or sold out. Since one cannot link Bitcoin sending addresses to specific Bitcoin receiving addresses on Bitcoin (which would be a cool way to monitor other buyers), this seems like a good measurement for seeking information.

Also, as determinants of the Bitcoin economy, the number of Bitcoins in circulation, BTC_t is used for the supply of Bitcoins and the number unique Bitcoin accounts, Num_{user_day} , used in transactions are used as proxies for Bitcoin demand.

Additionally, oil prices are a good macroeconomic indicator of the future price of goods, so the prices of Brent Oil, an international oil company are used ($brent_day$). Also, the value of the DOW Jones is used as a price indicator and an indicator of attractiveness to investors. For the same reasons, the Euro-USD exchange rate, usd_eur , and the USD-JPY exchange rate, usd_jpy are considered for the model.

Sadly, I could not figure out how to collect data from the Ripple charts API to find the total number of Ripple accounts over time. This would have served as a measure for how much Ripple is used. My original hypothesis is that the actual use of Ripple account, independent of the transactions

performed on said accounts, would influence the price of Bitcoin by affecting the attractiveness of Bitcoin to investors and vendors. Another important variable that would have been good for determining the attractiveness of Bitcoins to investors and vendors would have been data on the daily Wikipedia hits of Bitcoin, as noted in the literature review.

I hope also to collect data on valence and tweets. And there is one more super interesting data set I want to collect.

5 Modeling Considerations

Paragraph about models in general

5.1 VAR Modeling

Talk about the model. What is it? What are the assumptions?

What is autocorrelation?

What happens to the model if this is not met?

What are tests for it? Talk about Durbin-Watson.

What are fixes for it?

What is heteroskedasticity?

What happens to this model if this is not met?

What are tests for it?

What are fixes for it?

Talk about What happens to the model if this is not met? What are fixes for it?

What is multi-collinearity?

What happens to the model if this is not met? What are fixes for it?

Talk about modeling misspecification. Talk about spurious relationships caused by non-stationarity.

What are tests for non-stationarity? Augmented Dickey-Fuller

Talk about testing for co-integration

Talk about model misspecification test - RAMSEY Reset Test

5.2: Bubble Modeling 6: Expectations

The expectations of this model specification are hard to determine based on the lack of data. I estimate, based on the literature, that because of the inclusion of measures of the supply and demand of Bitcoin, macroeconomic indicators will mostly not be important in determining the price of Bitcoin. I believe that the measures of Bitcoin supply and demand play out as explained in the literature review and conceptual framework. Also, exchange rates may or may not be significant.

7 Preliminary Analysis

Firstly, summary statistics were calculated for all of the initial variables, and line graphs for all of the data (Appendix A). The descriptive statistics do not necessarily tell us much; however, the line graphs are quite useful. Firstly, note that the graphs suggest that we may need to do a log transformation of the prices for Bitcoin. The graphs also give us some intuition about the stationarity of the time series, as discussed below.

7.1 Handling Stationarity

In order to specify a VAR model that is not spurious, we must ensure that the variables of the model are cointegrated; however, performing tests of stationarity cannot be performed when there are gaps in the data unless specialized fixes are performed. Gaps in the data are necessary consequences of how macroeconomic indicators are recorded. Of the variables with no gaps, *price_ave*, *totcoins*, *usd_jpy*, and *usd_eur*, all are non-stationary. The augmented Dickey-Fuller tests were applied to the time series for the tests (Appendix B). Since it is outside of the scope of this project to attempt to perform specialized tests for non-stationarity, I will have to use all of the information that I have. First, we checked to see if each of *price_ave*, *totcoins*, *usd_jpy*, and *usd_eur* are $I(1)$ by performing another Augmented Dickey-Fuller test on the differenced variables (Appendix B). Indeed, there is evidence that every variable is stationary. In fact, even at $\alpha = .01$ all models are stationary all the way up to lag 23 except for *dif_totcoins*, which is stationary up to 17 lags but still stationary up to 23 lags at $\alpha = .05$.

The Bitcoin algorithm for adjusting the computational difficulty of algorithms results in a con-

stant increase of Bitcoins, as can be seen by the line graph of *totcoins* (Appendix A). Because of this, the variance may be fairly constant, but the average is not. Thus, we find it likely that *totcoins* is of order of integration one, but we may specify some models in which this is not an assumption. Looking at the line graph for daily Bitcoin days destroyed during the period in which we are using the data, the variance appears to be relatively constant, especially when excluding massive drops in Bitcoin prices and seasonal events like Christmas, Cyber-Monday, and Black Friday. Due to the relatively large number of data points, I believe even without adjustment this will result in the data being stationary. This is consistent with findings of the velocity of money that suggest a borderline relationship in some tests and stationarity indeed in others (Aslan and Korap 2007; and Brand et al. 2002). Thus, I believe it to be probable that *bcdde* is stationary. Based on the line graphs, *address_day* and *trans_day* seem to be of order integration of $I(1)$, especially as of late. This is consistent with the literature review.

A recent study by Bacon and Kojima (2008) suggests that both oil prices and the log transformation of oil prices are non-stationary with order $I(1)$. This suggests that both *brent_day* and *ln_brent_day* will be non-stationary with $I(1)$. Mr. David Alan Dickey himself points out how obvious it is that the log transformation of the Dow Jones Index is non-stationary of order one (Dickey, David 2005) and tests these hypotheses. I am unsure about what the literature has to say about the stationarity of the Dow Jones Index itself. The Dow Jones looks very clearly like a non-stationary variable with $I(1)$ based on the line graph, i.e. if one draws a fairly straight, positively sloped line through the data in the right location, then you can see that the variance of differences seems to be fairly constant and that the differences are centered about some mean. Thus, we also assume that *ln_djday* and *djday* are of order $I(1)$.

The stationarity of those log transformed variables for which it was possible to perform an Augmented Dickey-Fuller test without transformations was tested (Appendix B). Indeed, each of the log transformations of *totcoins*, *usd_eur*, *usd_jpy*, and *price_ave* are $I(1)$. I am done with the analysis of stationarity. I will base base modeling off of the available information, which includes information from the Dickey-Fuller and the literature about what lags may be important.

6.2 Preliminary Regressions

The first two regressions run for price estimation are in Appendix C. Initially, I attempted to keep

in all cointegrated variables and then add in lags that I thought were important. My initial model failed in every respect: there was multicollinearity, autocorrelation, heteroskedasticity, and most importantly, misspecification. The multicollinearity was clear, although not tested for; autocorrelation was indicated by failing the Augmented Durbin Watson test, which is valid for models that have lags of the dependent variable as independent variables; heteroskedasticity is indicated by rejecting the null in the Breusch-Pagen test; and both the failed Durbin Watson test and the failed Ramsey RESET test indicate misspecification of the model. The price of Bitcoin is clearly not linear, as previously discussed. The autocorrelation and homoskedasticity are also clear in Figures 30 and 31. The model does pass the F test, but of all the variables only the first and second day lags of Bitcoin price and the *address_{day}* were found to be significant.

In a vain attempt to make the model better, I decided to take out variables that were causing multicollinearity and that were not that predictive (Appendix C). The lag of exchange rates make much more sense, and the number of unique Bitcoin addresses from which purchases were made on any given day has, without a doubt, a very high correlation to the number of unique Bitcoin transactions performed on a day. Thus, I decided to keep the better proxy, the number of unique Bitcoin transactions on a given day. I believe the number of transactions would be a better proxy unless there were people spamming the network with very low payments, which would be financially costly in the Ripple system but especially so in mainstream Bitcoin exchanges. One can see from Figure 31 that the model is in no better shape than its predecessor. The very low p-values for the Durbin Watson tests suggest the regression is spurious.

I followed up these regressions by modeling the logarithmic price of Bitcoin (Appendix D).

7 Results of Best Models

The model found in figure 24 seems to have been the best model I could come up with. The model passes specification testing via the Ramsey RESET test, just barely checks in as having homoskedasticity by the Breusch-Pagen test, and has such a high probability for the Durbin Watson that it does not appear to be spurious or have autocorrelation. This should be weighed carefully because the Breusch-Pagen test only tests for linear heteroskedasticity. Interestingly, lagged exchange rates are now considered important for determining Bitcoin prices. The meaning of the signs on these coefficients is up for debate though.

If one removes the log of total Bitcoins from the regression because of its insignificance in determining prices, they will find that the probability of there being heteroskedasticity increases to the point of being significant at $\alpha = .05$ (Figure 38). Also, one should note the extremely high correlation between the one day lag and the two day lag in Bitcoin prices. Removing one of these lags results in failing of the Durbin Watson test.

8 Summary and Implications

An interesting result here is that the model goes from being a seeming pretty good model in terms of explaining having autocorrelation when the second lag of bitcoin prices is removed. I think this is because it takes away this sort of idea that Bitcoin investors and potential Bitcoin investors are not only thinking about what happened when it comes to the immediate but also to slightly before that when trying to determine what will happen to the price of Bitcoin. This is because the price volatility of Bitcoin is phenomenal. Furthermore, these regressions have very large R^2 values, and it should be determined whether or not their residuals are stationary so as to reduce the possibility that these regressions are spurious. Similar to the literature, we found that the demand for Bitcoins was more important for determining bitcoin prices. Indeed, we found that the supply of Bitcoins was not an important determinant. All results should be taken lightly because of the possibility of many omitted variables that could have biased the results.

9 Future Work

Future work on this project will involve a more indepth study of solving endogeneity problems. I could try performing more complex error correction models within the VAR framework, or more interestingly, work with simultaneous equations. Either way, I would still like to take another look at this problem when I have collected data from Ripple and gotten data on the price volatility of Bitcoin. I would also like to learn how to test for stationarity when there is gaps in the data. In addition to this, one thing I am particularly interested in is using machine learning for prediction.

References

- Aslan, O. and Korap, L. (2007). Testing Theory of Money for the Turkish Economy. *BDDK*
https://www.bddk.org.tr/WebSitesi/turkce/Raporlar/BDDK_Dergi/4212Makale-5.pdf
- Bacon, R. and Kojima, M. (2008). Coping with Oil Price Volatility. *ESMAP* 05/008 http://www.esmap.org/sites/esmap.org/files/8142008101202_coping_oil_price.pdf
- Barber, B.M. and T. Odean (2008). All That Glitters: The Effect of Attention and News on the Buying Behavior of Individual and Institutional Investors. *Review of Financial Studies* 21(2): 785 – 818.
- Brand, C., Gerdesmeier, and D., Roffia (2002). Estimating the Trend of M3 Income Velocity Underlying the Reference Value for Monetary Growth. *European Central Bank* 3 1 – 61
<https://www.ecb.europa.eu/pub/pdf/scpops/ecbocp3.pdf>
- Buchholz, M., Delaney, J., Warren, J. and Parker, J. (2012). Bits and Bets, Information, Price Volatility, and Demand for Bitcoin. *Economics* 312, <http://www.Bitcointrading.com/pdf/bitsandbets.pdf>
- David, D. (2005). Stationary Issues in Time Series Modeling. *Sugi* 30: 192 – 30. <http://www2.sas.com/proceedings/sugi30/192-30.pdf>
- Dimitrova, D. (2005). The Relationship between Exchange Rates and Stock Prices; Studied in a Multivariate Model. *Issues in Political Economy* 14: 1 – 25.
- Gervais, Simon, Ron Kaniel, and Dan H. Mingelgrin. (2001). The high-volume return premium. *Journal of Finance* 56: 877919.
- Grullon, G., Kanatas, G. and Weston, J.P. (2004). Advertising, breadth of ownership, and liquidity. *Review of Financial Studies* 17: 43961.
- Kristoufek, L. (2013). BitCoin meets Google Trends and Wikipedia: Quantifying the relationship between phenomena of the Internet era. *Scientific Reports* 3 (3415): 1 – 7.
- Nakamoto, S. (2008). Bitcoin: A Peer-to-Peer Electronic Cash System. *The Cryptography Mailing List*, 1 – 9.

MacDonell, Alec (2014). Popping the Bitcoin Bubble: An application of log-periodic power law modeling to digital currency to digital currency. *University of Notre Dame* [http : //economics.nd.edu/assets/134206/macdonell.pdf](http://economics.nd.edu/assets/134206/macdonell.pdf)

Moore, T. and N. Christin (2013). Beware the Middleman: Empirical Analysis of BitCoin-Exchange Risk. *Financial Cryptography and Data Security* 7859: 25 – 33.

Schwartz, D., Youngs, N., and Britto, A. (2014), The Ripple Protocol Consensus Algorithm. *Ripple Labs Inc.* [https : //ripple.com/files/ripple_consensus_whitepaper.pdf](https://ripple.com/files/ripple_consensus_whitepaper.pdf)

Appendix A: Preliminary Analysis

Variable	Obs	Mean	Std. Dev.	Min	Max
price_ave	1587	160.2033	249.8758	.05	1132.26
totcoins	1585	9480720	2861734	3627950	1.36e+07
dj_day	1092	13812.72	2034.512	9985.81	17912.62
brent_day	1086	106.0654	11.20424	70.61	128.14
usd_jpy	1587	89.63665	11.15878	75.79	121.47
usd_eur	1587	.7499775	.0301359	.6738	.8265
bcdde	1584	4839413	8921822	25227	1.73e+08
address_day	1585	55929.46	58017.73	284	245004
trans_day	1585	33592.71	27467.2	268	102010

Figure 1: Summary Statistics

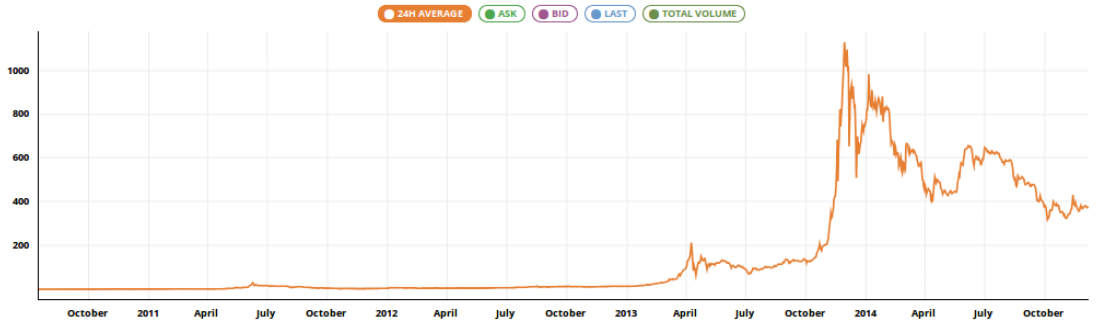


Figure 2: Bitcoin value in US Dollars



Figure 3: Brent Oil Prices in US Dollars



Figure 4: DOW Jones Index US Dollars

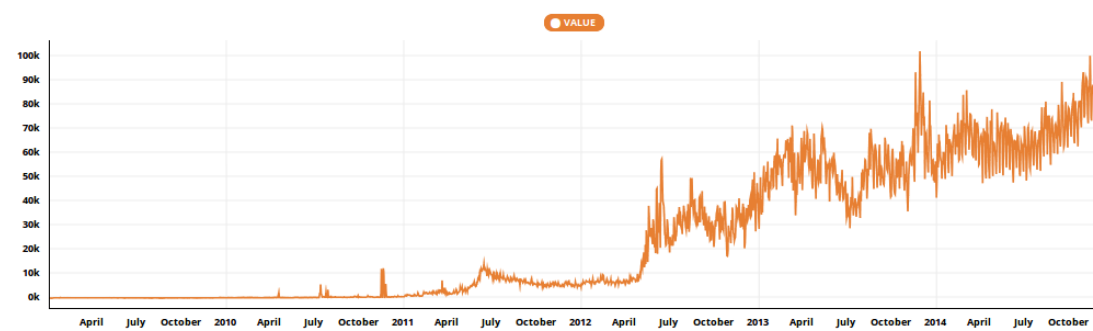


Figure 5: Number of Unique Bitcoin Transactions per Day

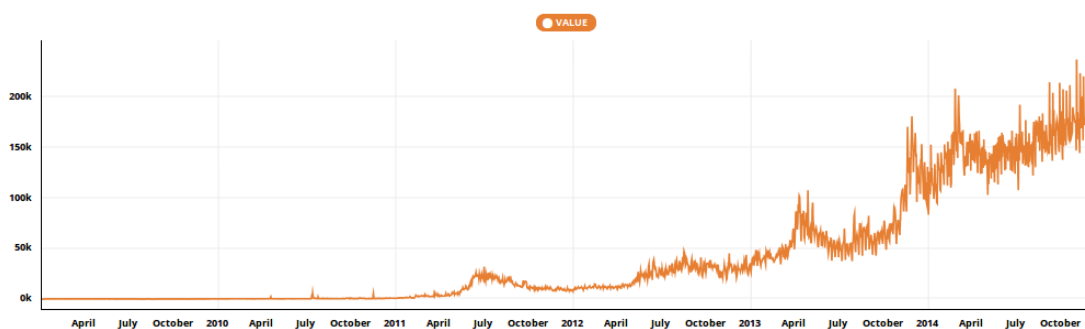


Figure 6: Number of Unique Bitcoin Addresses Involved In Transactions per Day

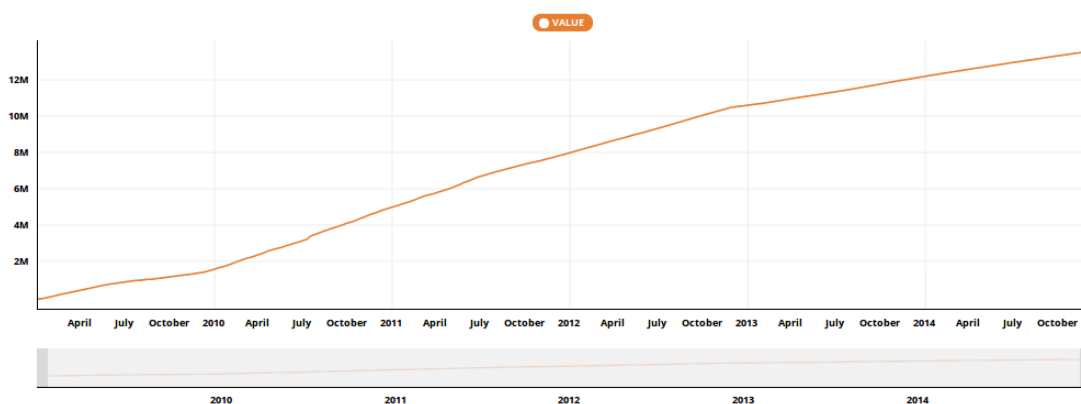


Figure 7: Total Bitcoins



Figure 8: USD-EUR Exchange Rate in US Dollars



Figure 9: USD-JPY Exchange Rate in Japanese Yen

Appendix B: Stationarity

Variable	VIF	1/VIF
ln_price_ave		
L1.	13.64	0.073298
ln_trans_day	9.56	0.104618
ln_usd_jpy		
L2.	3.05	0.328190
ln_usd_eur		
L1.	1.43	0.697013
Mean VIF	6.92	

Figure 10: Decreased Multicollinearity


```
. regress ln_price_ave L2.ln_usd_jpy L.ln_usd_eur ln_trans_day L.ln_price_ave L2.l
> n_price_ave
```

Source	SS	df	MS	Number of obs =	1583
Model	11617.813	5	2323.5626	F(5, 1577) =	.
Residual	5.86219907	1577	.003717311	Prob > F =	0.0000
				R-squared =	0.9995
				Adj R-squared =	0.9995
Total	11623.6752	1582	7.34745588	Root MSE =	.06097

ln_price_ave	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
ln_usd_jpy L2.	.071636	.0220801	3.24	0.001	.0283266	.1149454
ln_usd_eur L1.	-.1463623	.045723	-3.20	0.001	-.2360467	-.056678
ln_trans_day	.0136244	.0029439	4.63	0.000	.0078501	.0193987
ln_price_ave L1.	1.164519	.0245544	47.43	0.000	1.116356	1.212682
L2.	-.1753258	.0243649	-7.20	0.000	-.2231169	-.1275347
_cons	-.460025	.1140711	-4.03	0.000	-.683772	-.2362781

```
. durbina
```

Number of gaps in sample: 1

Durbin's alternative test for autocorrelation

lags(p)	chi2	df	Prob > chi2
1	0.207	1	0.6494

H0: no serial correlation

```
. hettest
```

Breusch-Pagan / Cook-Weisberg test for heteroskedasticity

H0: Constant variance

Variables: fitted values of ln_price_ave

chi2(1) = 3.89

Prob > chi2 = 0.0487

```
. ovttest
```

Ramsey RESET test using powers of the fitted values of ln_price_ave

H0: model has no omitted variables

F(3, 1574) = 0.63

Prob > F = 0.5934

```
. vif
```

Variable	VIF	1/VIF
ln_price_ave L1.	1888.70	0.000529
L2.	1863.63	0.000537
ln_trans_day	9.57	0.104481
ln_usd_jpy L2.	3.05	0.327852
ln_usd_eur L1.	1.44	0.694444

Variable	VIF	1/VIF
ln_price_ave		
L1.	1888.70	0.000529
L2.	1863.63	0.000537
ln_trans_day	9.57	0.104481
ln_usd_jpy		
L2.	3.05	0.327852
ln_usd_eur		
L1.	1.44	0.696078
Mean VIF	753.28	

Figure 12: Multicollinearity of Model