

**Problem 0(a)**

**Theorem 1** ( $|A| = 0 \implies |\mathcal{P}(A)| = 1$ ). *The power set of the empty set has one element.*

*Proof.* Constructing the power set of  $\emptyset$  (i.e., the empty set), the definition of the power set gives  $\mathcal{P}(\emptyset)$  equal to  $\{\emptyset\}$ . We see that there is one element in  $\mathcal{P}(\emptyset)$ . ■