Storing messages with neural multipartite cliques

L

number of neurons per cluster l number of clusters c number of erased clusters c_e number of messages : m number of activities per cluster : a density : d edge : (i,j)

probability for i and j to be active in their respective clusters for one message : $\frac{a}{l}$

probability of the edge not being added in the network for one message : $1-\left(\frac{a}{l}\right)^2$

$$d = 1 - \left(1 - \left(\frac{a}{l}\right)^2\right)^m$$

gap with density in simulations: under 1 percent

probability for a vertex v to achieve the maximum score, that is to mean $a(c-c_e):d^{a(c-c_e)}$

probability for a vertex v not to achieve the maximum : $1 - d^{a(c-c_e)}$ probability for none of the vertices of one erased cluster, excepting the correct ones, to achieve the maximum : $(1 - d^{a(c-c_e)})^{l-a}$

probability for none of the vertices in any erased cluster, excepting the correct ones, to achieve the maximum in their respective cluster: $(1 - d^{a(c-c_e)})^{c_e(l-a)}$ Whence error rate is:

$$P_{err} = 1 - (1 - d^{a(c-c_e)})^{c_e(l-a)}$$

The simulations agree with the analytical result.

For one iteration (for erasures, not for errors), winner takes all is the same as a-winners take all.

For multiple iterations a-winner take all is an improvement.

"a-Winners take all" better than "winner takes all" with errors instead of erasures.

For errors: only better than only 1 activity per cluster if multiple iterations of the a-winners take all rule. For one iteration, it is less efficient.

Spéculations en Français :

Peut-être un intérêt pour cluter based associative memories build from unreliable storage : si une arête porte moins d'info, on peut peut-être en supprimer plus (mais rajout ?!)

Marche un petit peu, mais pas forcément significatif : à tester plus en détail.

Marche mieux pour des bruits importants

$$P(n_{v_c} = n_0) = \binom{ac_k}{n_0} (1 - \psi)^{n_0} \psi^{ac_k - n_0}$$

$$P_+ = \psi(1 - d) + (1 - \psi)d$$

$$P(n_v = x) = \binom{ac_k}{x} P_+^x (1 - P_+)^{ac_k - x}$$

$$P(\text{no other vertex activated in this cluster}) = \sum_{n_0=1}^{ac_k} P(n_{v_c} \geqslant n_0)^a \left[\sum_{x=0}^{n_0-1} P(n_v = x) \right]^{l-a}$$

$$P(\text{no other vertex activated in any cluster}) = \left(\sum_{n_0=1}^{ac_k} P(n_{v_c} \geqslant n_0)^a \left[\sum_{x=0}^{n_0-1} P(n_v = x)\right]^{l-a}\right)^{c_e}$$

Sans tenir compte du choix au hasard si plus sont activés.

References

[LPGRG14] François Leduc-Primeau, Vincent Gripon, Michael Rabbat, and Warren Gross. Cluster-based associative memories built from unreliable storage. In *ICASSP*, May 2014. To appear.