

1 Intro

I need to prove that haskell types and terms that I expose wouldn't break the system. It means two things:

1. Types preserve the same set of invariants
2. Terms have the same interface: any combination of **APPLY** that can be used to original(ignore types) term must be usable with generated; and primitives(numbers, strings, ... and their ops) are the same.

2 Preserving type invariants

Conversion for types:

$$TT[AgdaType](Context) = HaskellType$$

$$TT[A\ args\ \dots](\Gamma) = a\ TT[args\ \dots](\Gamma), \quad (A \mapsto a) \in \Gamma$$

$$TT[CT\ args\ \dots](\Gamma) = CT\ TT[args\ \dots](\Gamma), \quad CT \text{ is a } \text{COMPILED_TYPE}, \text{ EXPORT or a primitive postulate}$$

$$TT[(A : Kind) \rightarrow T](\Gamma) = \forall a. TT[T](\Gamma \cup (A \mapsto a)), \quad Kind \text{ is a combination of } Set \text{ and arrows}$$

$$TT[(x : T_1) \rightarrow T_2](\Gamma) = TT[T_1](\Gamma) \rightarrow TT[T_2](\Gamma), \quad x \notin freevars(T_2)$$

$$TT[(x : T_1, T_2)](\Gamma) = (TT[T_1](\Gamma), TT[T_2](\Gamma)), \quad x \notin freevars(T_2)$$

$$TT[_](\Gamma) = \perp$$

Two things to watch for:

- **newtype** wrappers in the first case
- The third case

Every other case is exactly the same.

TODO:

3 Preserving term interface

Conversion for terms:

$$Wrap[AgdaType](MAlonzoTerm) = MyTerm$$

$$Unwrap[AgdaType](MyTerm) = MAlonzoTerm$$

Both are only valid when $TT[AgdaType](\emptyset) \neq \perp$

$$Wrap[A\ args\ \dots](term) = \text{unsafeCoerce } term$$

$$Wrap[(A : Kind) \rightarrow T](term) = Wrap[T](term\ ())$$

$$Wrap[(x : T_1) \rightarrow T_2](term) = \lambda x. Wrap[T_2](term\ Unwrap[T_1](x))$$

$$Wrap[(x : T_1, T_2)]((term_1, term_2)) = (Wrap[T_1](term_1), Wrap[T_2](term_2))$$

$$Wrap[_](term) = \perp$$

$$Unwrap[A\ args\ \dots](term) = \text{unsafeCoerce } term$$

$$Unwrap[(A : Kind) \rightarrow T](term) = Unwrap[T](\lambda_. term)$$

$$Unwrap[(x : T_1) \rightarrow T_2](term) = \lambda x. Unwrap[T_2](term\ Wrap[T_1](x))$$

$$Unwrap[(x : T_1, T_2)]((term_1, term_2)) = (Unwrap[T_1](term_1), Unwrap[T_2](term_2))$$

$$Unwrap[_](term) = \perp$$

unsafeCoerce is legal because it's either:

- The same term(when its type is a type variable)
- A newtype around MAlonzo generated type
- A primitive