# University of Technology, Graz

# Master Thesis

# Differential cryptanalysis with SAT solvers

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# Differential cryptanalysis with SAT solvers

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# **AFFIDAVIT**

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# **ABSTRACT**

Hash functions are ubiquitous in the modern information age. They provide preimage, second preimage and collision resistance which are needed in a wide range of applications.

In August 2006, Wang et al. showed efficient attacks against several hash function designs including MD4, MD5, HAVAL-128 and RIPEMD. With these results differential cryptanalysis has been shown useful to break collision resistance in hash functions. Over the years advanced attacks based on those differential approaches have been developed.

To find collisions like Wang et al., a cryptanalyst needs to specify a differential characteristic. Looking at the differential behavior of the underlying operations of the hash algorithm shows how differential values propagate in the algorithm. The goal is to find a differential characteristic whose differences cancel out in the output. Once such a differential characteristic was discovered, in a second step the actual values for those differences are defined yielding an actual hash collision.

Finding a differential characteristic can be a cumbersome and tedious task. Whereas propagation can be automated using dedicated tools, finding an initial differential characteristic is a difficult task as it can be specified with arbitrary levels of granularity.

SAT solvers inherently implement both tasks. They consecutively propagate values which narrow the search space. The probability to find a satisfiable assignment increases if the narrowed search space has many satisfiable assignments. And finally the assignment reveals initial values. On the other hand, SAT solvers have no notion of differential values and therefore problem encoding becomes an important topic.

In this thesis we look at differential characteristics representing hash collisions and encode them as SAT problem. A SAT solver tells us whether this characteristic represents a valid hash state. We implemented a framework generating CNFs for these purposes and improved our CNF design to solve MD4 testcases as well as much more difficult SHA-256 testcases. Our greatest achievement was finding a MD4 full round hash collision and a SHA-256 hash collision over 27 rounds. Finally we also provide a small CNF analysis library to compare encoded problems with others.

**Keywords:** hash function, differential cryptanalysis, differential characteristic, MD4, SHA-256, collision resistance, satisfiability, SAT solver

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All source codes are available at lukas-prokop.at/proj/megosat and published under terms and conditions of Free/Libre Open Source Software. This document was printed with LualFTEX in the Linux Libertine typeface.

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# Chapter 1

# Introduction

### 1.1 Overview

Hash functions are used as cryptographic primitives in many applications and protocols. They take an arbitrary input message and provide a hash value. Input message and hash value are considered as byte strings in a particular encoding. The hash value is of fixed length and satisfies several properties which make it useful in a variety of applications.

In this thesis we will consider the hash algorithms MD4 and SHA-256. They use basic arithmetic functions like addition and bit-level functions such as XOR to transform an input to a hash value. We use a bit vector as input to this implementation and all operations applied to this bit vector will be represented as clauses of a SAT problem. Additionally we represent differential characteristics of hash collisions as SAT problem. If and only if satisfiability is given, the particular differential state is achievable using two different inputs leading to the same output. As far as SAT solvers return an actual model satisfying that state, we get an actual hash collision which can be verified and visualized. If the internal state of the hash algorithm is too large, the attack can be computationally simplified by modelling only a subset of steps of the hash algorithm or changing the modelled differential path.

Based on experience with these kind of problems with previous non-SAT-based tools we aim to apply best practices to a satisfiability setting. We will discuss which SAT techniques lead to best performance characteristics for our MD4 and SHA-256 testcases.

### 1.2 Thesis Outline

This thesis is organized as follows:

- **In Chapter 1** we briefly introduce basic subjects of this thesis. We explain our high-level goal involving hash functions and SAT solvers.
- In Chapter 2 we introduce the MD4 and SHA-256 hash functions. Certain design decisions imply certain properties which can be used in differential cryptanalysis. We discuss those decisions in this chapter after a formal definition of the function itself. Beginning with this chapter we develop a theoretical notion of our tools.
- In Chapter 3 we discuss approaches of differential cryptanalysis. We start off with work done by Wang, et al. and followingly introduce differential notation to simplify representation of differential states. This way we can easily dump hash collisions.
- **In Chapter** 4 we discuss SAT solving. We give a brief overview over used SAT solvers and discuss how we can speed up SAT solvers for cryptographic problems.
- **In Chapter** 5 we define SAT features which help us to classify SAT problems. This is a small subproject we did to look at properties of resulting DIMACS CNF files.
- **In Chapter 6** we discuss how we represent a problem (i.e. the hash function and a differential characteristic) as SAT problem. This ultimatively allows us to solve the problem using a SAT solver.
- **In Chapter 7** we show data as result of our work. Runtimes are the main part of this chapter, but also results of the SAT features project are presented.
- **In Chapter 8** we suggest future work based on our results.



# Chapter 2

# Hash algorithms

In this chapter we will define hash functions and their desired security properties. Followingly we look at SHA-256 and MD4 as established hash functions. MD4 unlike SHA-256 is practically broken but has a comparably small internal state. It therefore allows a good starting point to devise our attacks. In a next step we scaled up to SHA-256 which has an internal state size at least twice as large. In Chapter 6 we will represent them with Boolean algebra to make it possible to reason about states in those hash functions using SAT solvers.

### 2.1 Preliminaries Redux

# Definition 2.1 (Hash function)

A *hash function* is a mapping  $h: X \to Y$  with  $X = \{0,1\}^*$  and  $Y = \{0,1\}^n$  for some fixed  $n \in \mathbb{N}_{\geq 1}$ .

- Let  $x \in X$ , then h(x) is called hash value of x.
- Let  $h(x) = y \in Y$ , then x is called *preimage of y*.

Hash functions are considered as cryptographic primitives used as building blocks in cryptographic protocols. A hash function has to satisfy the following security requirements:

## Definition 2.2 (Preimage resistance)

Given  $y \in Y$ , a hash function h is *preimage resistant* iff it is computationally infeasible to find  $x \in X$  such that h(x) = y.

#### Definition 2.3 (Second-preimage resistance)

Given  $x \in X$ , a hash function h is second-preimage resistant iff it is computationally infeasible to find  $x_2 \in X$  with  $x \neq x_2$  such that  $h(x) = h(x_2)$ .  $x_2$  is called second preimage.

#### Definition 2.4 (Collision resistance)

A hash function h is *collision resistant* iff it is computationally infeasible to find any two  $x \in X$  and  $x_2 \in X$  with  $x \neq x_2$  such that  $h(x) = h(x_2)$ . Tuple  $(x, x_2)$  is called *collision*.

As far as hash functions accept input strings of arbitrary length, but return a fixed size output string, existence of collisions is unavoidable [31]. However, good hash functions make it very difficult to find collisions or preimages.

Any digital data can be hashed (i.e. used as input to a hash function) by considering it in binary representation. The format or encoding is not part of the hash function's specification.

### 2.1.1 Merkle-Damgård designs

The Merkle-Damgård design is a particular design of hash functions providing the following security guarantee:

#### Definition 2.5 (Collision resistance inheritance)

Let  $F_0$  be a collision resistant compression function. A hash function in Merkle-Damgård design is collision resistant if  $F_0$  is collision resistant.

This motivates thorough research of collisions in compression functions. The design was found independently by Ralph C. Merkle and Ivan B. Damgård. It was described by Merkle in his PhD thesis [18, p. 13–15] and followingly used in popular hash functions such as MD4, MD5 and the SHA2 hash function family. The single-pipe design works as follows:

- 1. Split the input into blocks of uniform block size. If necessary, apply padding to the last block to achieve full block size.
- 2. Compression function  $F_0$  is applied iteratively using the output  $y_{i-1}$  of the previous iteration and the next input block  $x_i$ , denoted  $y_i = F_0(y_{i-1}, x_i)$ .
- 3. An optional postprocessing function is applied.

#### 2.1.2 Padding and length extension attacks

Hash functions of single-piped Merkle-Damgård design inherently suffer from length extension attacks. MD4 and SHA-256 apply padding to their input to

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normalize their input size to a multiple of its block size. The compression function is applied afterwards. This design is vulnerable to length extensions.

Consider some collision  $(x_0, x_1)$  with  $F_0(x_0) = y = F_0(x_1)$  where  $x_0$  and  $x_1$  have a size of one block. Let p be a suffix with size of one block. Then also  $(x_0 || p, x_1 || p)$  (where || denotes concatenation) represents a collision in single-piped Merkle-Damgård designs, because it holds that:

$$F_0(F_0(x_0), p) = F_0(F_0(x_1), p) \iff F_0(y, p) = F_0(y, p)$$

Hence  $(x_0 || p, x_1 || p)$  is a collision as well. As far as  $F_0$  is applied recursively to every block, p can be of arbitrary size and  $(x_0, x_1)$  can be of arbitrary uniform size.

Because of this vulnerability, cryptanalysts only need to find a collision in compression functions. In our tests will only consider input of one block and padding will be neglected due to this vulnerability.

#### 2.1.3 Example usage

One example showing the use of hash functions as primitives are JSON Web Tokens (JWT) specified in RFC 7519 [16]. Its application allows web developers to represent claims to be transferred between two parties.

Section 8 defines implementation requirements and refers to RFC 7518 [11], which specifies cryptographic algorithms such as "HMAC SHA-256" to be implemented. It is (besides "none") the only required signature and MAC algorithm.

### 2.2 MD4

MD4 is a cryptographic hash function originally described in RFC 1186 [27], updated in RFC 1320 [28] and declared obsolete by RFC 6150 [34]. It was invented by Ronald Rivest in 1990 with properties given in Table 2.1. In 1995 [5] successful full-round attacks have been found to break collision resistance. Followingly preimage and second-preimage resistance in MD4 have been broken as well. Some of those attacks are described in [29] and [21]. We derived a Python 3 implementation based on a Python 2 implementation and made it available on github [25].

```
block size 512 bits namely variable block in RFC 1320 [28] digest size 128 bits as per Section 3.5 in RFC 1320 [28] internal state size 128 bits namely variables A, B, C and D word size 32 bits as per Section 2 in RFC 1320 [28]
```

Table 2.1: MD4 hash algorithm properties

(2.3)

MD<sub>4</sub> uses three auxiliary Boolean functions:

#### Definition 2.6

The Boolean IF function is defined as follows: If the first argument is true, the second argument is returned. Otherwise the third argument is returned.

The Boolean MAJ function returns true if the number of Boolean values true in arguments is at least 2. The Boolean XOR function returns true if the number of Boolean values true in arguments is odd.

Using the logical operators  $\land$  (AND),  $\lor$  (OR) and  $\neg$  (NEG) we can define them as (see Section 4.1 for a thorough discussion of these operators):

$$\mathsf{IF}(X,Y,Z) \coloneqq (X \land Y) \lor (\neg X \land Z) \tag{2.1}$$

$$MAJ(X,Y,Z) := (X \land Y) \lor (X \land Z) \lor (Y \land Z)$$
 (2.2)

$$XOR(X, Y, Z) := (X \land \neg Y \land \neg Z) \lor (\neg X \land Y \land \neg Z)$$
$$\lor (\neg X \land \neg Y \land Z) \lor (X \land Y \land Z)$$
$$:= (X \oplus Y \oplus Z)$$

In the following, a brief overview over MD4's design is given.

**Padding and length extension.** First of all, padding is applied. A single bit 1 is appended to the input. As long as the input does not reach a length congruent 448 modulo 512, bit 0 is appended. Followingly, length appending takes place. Represent the length of the input (without the previous modifications) in binary and take its first 64 less significant bits. Append those 64 bits to the input.

**Initialization.** The message is split into 512-bit blocks (i.e. 16 32-bit words). Four state variables  $A_i$  with  $-4 \le i < 0$  are initialized with these hexadecimal values:

$$[A_{-4}]$$
 01234567  $[A_{-1}]$  89abcdef  $[A_{-2}]$  fedcba98  $[A_{-3}]$  76543210

**Round function with state variable updates.** The round function is applied in three rounds with 16 iterations. In every iteration values  $A_{-1}$ ,  $A_{-2}$  and  $A_{-3}$  are taken as arguments to function F. Function F is IF in round 1, followed by MAJ for round 2 and XOR for the final round 3. The resulting value is added to  $A_{-1}$ , current message block M and constant X. Finally the 32-bit sum will be left-rotated by p positions. Left rotation is formally defined in Definition 2.7. The values of X and p are defined as follows:

Let i be the iteration counter between 1 and 16 and r the round between 1 and 3. Then X takes the value of the i-th column and r-th row of matrix C. p takes the value of row r and column i mod 4 of matrix P.

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$$P = \begin{pmatrix} 3 & 7 & 9 & 11 \\ 3 & 5 & 9 & 13 \\ 3 & 9 & 11 & 15 \end{pmatrix}$$

This round function design is visualized in Figure 2.1.

# 2.3 SHA-256

SHA-256 is a hash function from the SHA-2 family designed by the National Security Agency (NSA) and published in 2001 [9]. It uses a Merkle-Damgård construction with a Davies-Meyer compression function. The best known preimage attack was found in 2011 and breaks preimage resistance for 52 rounds [12]. The best known collision attack breaks collision resistance for 31 rounds of SHA-256 [17] and pseudo-collision resistance for 46 rounds [13].

```
block size 512 bits as per Section 1 of the standard [9] digest size 256 bits mentioned as Message Digest size [9] internal state size 256 bits as per Section 1 of the standard [9] word size 32 bits as per Section 1 of the standard [9]
```

TABLE 2.2: SHA-256 hash algorithm properties

### Definition 2.7 (Shifts, rotations and a notational remark)

Consider a 32-bit word X with 32 binary values  $b_i$  with  $0 \le i \le 31$ .  $b_0$  refers to the least significant bit. Shifting ( $\ll$  and  $\gg$ ) and rotation ( $\ll$  and  $\gg$ ) creates a new 32-bit word Y with 32 binary values  $a_i$ . We define the following notations:

$$Y := X \ll n \iff a_i := b_{i-n} \text{ if } 0 \leqslant i-n \leqslant 32 \text{ and } 0 \text{ otherwise}$$
  
 $Y := X \gg n \iff a_i := b_{i+n} \text{ if } 0 \leqslant i+n \leqslant 32 \text{ and } 0 \text{ otherwise}$   
 $Y := X \ll n \iff a_i := b_{i-n \mod 32} \text{ as used in MD4}$   
 $Y := X \gg n \iff a_i := b_{i+n \mod 32}$ 

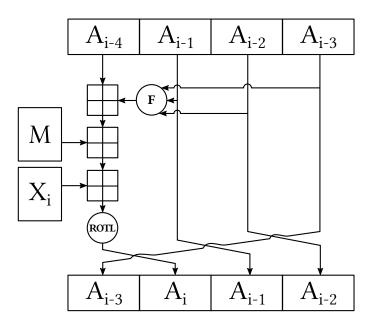


Figure 2.1: MD4 round function updating state variables



Figure 2.2: SHA-256 round function as characterized in [6]

2.3. SHA-256

Besides MD<sub>4</sub>'s MAJ and IF, another four auxiliary functions are defined. Recognize that  $\oplus$  denotes the XOR function whereas  $\boxplus$  denotes 32-bit addition.

Padding and length extension. The padding and length extension scheme of MD<sub>4</sub> is used also in SHA-256. Append bit 1 and followed by a sequence of bit 0 until the message reaches a length of 448 modulo 512 bits. Afterwards the first 64 bits of the binary representation of the original input are appended.

**Initialization.** In a similar manner to MD4, initialization of internal state variables (called "working variables" in [9, Section 6.2.2]) takes place before running the round function. The eight state variables are initialized with the following hexadecimal values:

$$A_{-1} =$$
 6a09e667  $A_{-2} =$  bb67ae85  $A_{-3} =$  3c6ef372  $A_{-4} =$  a54ff53a  $E_{-1} =$  510e527f  $E_{-2} =$  9b05688c  $E_{-3} =$  1f83d9ab  $E_{-4} =$  5be0cd19

Furthermore SHA-256 uses 64 constant values in its round function. We initialize step constants  $K_i$  for  $0 \le i < 64$  with the following hexadecimal values (which must be read left to right and top to bottom):

```
428a2f9871374491b5c0fbcfe9b5dba53956c25b59f111f1923f82a4ab1c5ed5d807aa9812835b01243185be550c7dc372be5d7480deb1fe9bdc06a7c19bf174e49b69c1efbe47860fc19dc6240ca1cc2de92c6f4a7484aa5cb0a9dc76f988da983e5152a831c66db00327c8bf597fc7c6e00bf3d5a7914706ca63511429296727b70a852e1b21384d2c6dfc53380d13650a7354766a0abb81c2c92e92722c85a2bfe8a1a81a664bc24b8b70c76c51a3d192e819d6990624f40e3585106aa07019a4c1161e376c082748774c34b0bcb5391c0cb34ed8aa4a5b9cca4f682e6ff3748f82ee78a5636f84c878148cc7020890befffaa4506cebbef9a3f7c67178f2
```

**Precomputation of W.** Let  $W_i$  for  $0 \le i < 16$  be the sixteen 32-bit words of the padded input message. Then compute  $W_i$  for  $16 \le i < 64$  the following way:

$$W_i := \sigma_1(W_{i-2}) + W_{i-7} + \sigma_0(W_{i-15}) + W_{i-16}$$

**Round function.** For every block of 512 bits, the round function is applied. The eight state variables are updated iteratively for i from 0 to 63.

$$E_i := A_{i-4} + E_{i-4} + \Sigma_1 (E_{i-1}) + \text{IF } (E_{i-1}, E_{i-2}, E_{i-3}) + K_i + W_i$$
  
 $A_i := E_i - A_{i-4} + \Sigma_0 (A_{i-1}) + \text{MAJ } (A_{i-1}, A_{i-2}, A_{i-3})$ 

 $W_i$  and  $K_i$  refer to the previously initialized values.

**Computation of intermediate hash values.** Intermediate hash values for the Davies-Meyer construction are initialized with the following values:

$$H_0^{(0)} := A_{-1}$$
  $H_1^{(0)} := A_{-2}$   $H_2^{(0)} := A_{-3}$   $H_3^{(0)} := A_{-4}$   $H_4^{(i)} := E_{-1}$   $H_5^{(i)} := E_{-2}$   $H_6^{(i)} := E_{-3}$   $H_7^{(i)} := E_{-4}$ 

Every block creates its own  $E_i$  and  $A_i$  values for  $60 \le i < 64$ . These are used to compute the next intermediate values:

$$\begin{aligned} H_0^{(j)} &\coloneqq A_{63} + H_0^{(i-1)} & H_4^{(j)} &\coloneqq E_{63} + H_4^{(i-1)} \\ H_1^{(j)} &\coloneqq A_{62} + H_1^{(i-1)} & H_5^{(j)} &\coloneqq E_{62} + H_5^{(i-1)} \\ H_2^{(j)} &\coloneqq A_{61} + H_2^{(i-1)} & H_6^{(j)} &\coloneqq E_{61} + H_6^{(i-1)} \\ H_3^{(j)} &\coloneqq A_{60} + H_3^{(i-1)} & H_7^{(j)} &\coloneqq E_{60} + H_7^{(i-1)} \end{aligned}$$

Finalization. The final hash digest of size 256 bits is provided as

$$H_0^{(N)} \, \| \, H_1^{(N)} \, \| \, H_2^{(N)} \, \| \, H_3^{(N)} \, \| \, H_4^{(N)} \, \| \, H_5^{(N)} \, \| \, H_6^{(N)} \, \| \, H_7^{(N)}$$

where N denotes the index of the last block and operator  $\parallel$  denotes concatenation. Hence  $H_0^{(N)}$  are the four least significant bytes of the digest.



"Just because it's automatic doesn't mean it works." —Daniel J. Bernstein

# Chapter 3

# Differential cryptanalysis

In Chapter 2 we defined two hash functions. In this chapter we consider such functions from a differential perspective. Differential considerations will turn out to yield successful collision attacks on hash functions. We introduce a notation to easily represent differential characteristics.

# 3.1 Motivation

In August 2004, Wang et al. published results at Crypto'04 [35] which revealed that MD4, MD5, HAVAL-128 and RIPEMD can be broken practically using differential cryptanalysis. Their work is based on preliminary work by Hans Dobbertin [5]. On an IBM P690 machine, an MD5 collision can be computed in about one hour using this approach. Collisions for HAVAL-128, MD4 and RIPEMD were found as well. Patrick Stach's md4coll.c program [33] implements Wang's approach and can find MD4 collisions in few seconds on my Thinkpad x220 setup specified in Appendix A.

Let n denote the digest size, i.e. the size of the hash value h(x) in bits. Due to the birthday paradox, a collision attack has a generic complexity of  $2^{n/2}$  whereas preimage and second preimage attacks have generic complexities of  $2^n$ . In other words it is computationally easier to find any two colliding hash values than the preimage or second preimage for a given hash value.

Following results by Wang et al., differential cryptanalysis was shown as powerful tool for cryptanalysis of hash algorithms. This thesis applies those ideas to satisfiability approaches.

Message 1									
see									
l9f									
a63bb2e8									
b9e8c3e9									
45dc8e31 97e31fe5 2794bfo8 b9e8c3e9  Message 2									
see									
l9f									
e8									
ge9									
Hash value of Message 1 and Message 2									
7a									

Table 3.1: One of two MD4 hash collisions provided in [35]. A message represents one block of 512 bits. Values are given in hexadecimal, message words are enumerated from left to right, top to bottom. Differences are highlighted in bold for illustration purposes. For comparison the first bits of Message 1 are 11000001... and the last bits are ...10011101.

# 3.2 Fundamentals

# Definition 3.1 (Hash collision)

Given a hash function h, a hash collision is a pair  $(x_1, x_2)$  with  $x_1 \neq x_2$  such that  $h(x_1) = h(x_2)$ .

Pseudo-collisions are also often considered when attacking hash functions. A *pseudo collision* is given if a hash collision can be found for a given hash function, but the initial vectors (IV) can be chosen arbitrarily.

Hash algorithms consume input values as blocks of bits. As far as the length of the input must not conform to the block size, padding is applied. Now consider such a block of input values and another copy of it. We use those two blocks as inputs for two hash algorithm instances, but provide slight modifications in few bits. Differential cryptanalysis is based on the idea to consider those execution states and tracing those difference to learn about the propagation of message differences. Compare this setup with Figure 3.1.

At the very beginning only the few defined differences are given. But as the hash algorithm progresses in computation, differences are propagated to more and more bits. Most likely the final value will differ in many bits, because of a desirable hash algorithm property called *avalanche effect*. A small difference in the input should lead to a significant difference in the output (i.e. visually recognizable).

Visualizing those differences helps the cryptanalyst to find modifications yielding a small number of differences in the evaluation state. The propagation of



**Figure 3.1:** Common attack setting for a collision attack: Hash function f is applied to two inputs M and  $M^*$  which differ by some predefined bits.  $\Delta M$  describes the difference between these values. A hash collision is given if and only if output values C and  $C^*$  show the same value. In differential cryptanalysis we observe the differences between two instances applying function f to inputs M and  $M^*$ .

differences in a particular hash algorithm is called *differential path*. Empirical results in differential cryptanalysis indicate that spare paths are desirable, because it is easier to cancel out few differences in the output compared to many differences. The cryptanalyst consecutively modifies the input values to eventually receive a collision in the output value.

#### **Definition 3.2**

The propagation of differences in a particular function is called *differential* path. The complete differential state during a computation is called *differential* characteristic.

#### Theorem 3.1

Assuming the number of differences in a differential path is small, this path is expected to result in a hash collision with higher probability.

bit	binary	hexadecimal representation / differential notation
$=$ $x_0$	d6cb927a	11010110110010111001001001111010
$x_1$	29d5a578	001010011101010110100101011111000
$x_2$	45dc8e31	01000101110111001000111000110001
$-\frac{1}{x_0^*}$	56cb927a	01010110110010111001001001111010
$x_1^*$	b9d5a578	101110011101010110100101011111000
$x_2^*$	45dd8e31	01000101110111011000111000110001
$\Delta x$		u1010110110010111001001001111010
		n01n10011101010110100101011111000
		010001011101110n1000111000110001

Table 3.2: The three words different between Message 1 and Message 2 of the original MD4 hash collision by Wang et al. The last three lines show how differences can be written down using bit conditions. As far as 4 symbols are not from the set {0, 1} it holds that the messages differ by 4 bits.

# 3.3 Differential notation

Differential notation helps us to visualize differential characteristics by defining so-called *generalized bit conditions*. It was introduced by Christian Rechberger and Christophe de Cannière in 2006 [2, Section 3.2], inspired by *signed differences* by Wang et al. and is shown in Table 3.3.

Consider two hash algorithm instances. Let  $x_i$  be some bit from the first instance and let  $x_i^*$  be the corresponding bit from the second instance. Differences are computed using a XOR and commonly denoted as  $\Delta x = x_i \oplus x_i^*$ . Bit conditions allow us to encode possible relations between bits  $x_i$  and  $x_i^*$ .

For example, let us take a look at the original Wang et al. hash collision in MD4 provided in Table 3.1. We extract all values with differences and represent them using differential notation. This gives us Table 3.2.

The following properties hold for bit conditions:

- If  $x_i = x_i^*$  holds and some value is known,  $\{0, 1\}$  contains its bit condition.
- If  $x_i \neq x_i^*$  holds and some value is known,  $\{u, n\}$  contains its bit condition.
- If  $x_i = x_i^*$  holds and the values are unknown, its bit condition is -.
- If  $x_i \neq x_i^*$  holds and the values are unknown, its bit condition is x.

Applying this notation to hash collisions means that arbitrary bit conditions (expect for #) can be specified for the input values. In one of the intermediate iterations, we enforce a difference using one of the bit conditions  $\{u, n, x\}$ . This excludes trivial solutions with no differences from the set of possible solutions. And the final values need to lack differences thus are represented using a dash  $\neg$ .

$(x_i, x_i^*)$	(0,0)	(1,0)	(0,1)	(1, 1)	$(x_i, x_i^*)$	(0,0)	(1,0)	(0,1)	(1, 1)
?	<b>✓</b>	<b>✓</b>	<b>✓</b>	$\checkmark$	3	<b>✓</b>	$\checkmark$		
_	✓			✓	5	✓		$\checkmark$	
X		$\checkmark$	$\checkmark$		7	✓	$\checkmark$	$\checkmark$	
0	✓				Α		$\checkmark$		✓
u		$\checkmark$			В	✓	$\checkmark$		✓
n			$\checkmark$		С			$\checkmark$	✓
1				✓	D	✓		$\checkmark$	✓
#					E		$\checkmark$	$\checkmark$	✓

Table 3.3: Differential notation as introduced in [2]. The left-most column specifies a symbol called "bit condition" and right-side columns indicate which bit configurations are possible for two given bits  $x_i$  and  $x_i^*$ .

$\Delta x$	conjunctive normal form	$\Delta x$	conjunctive normal form
#	$(x) \wedge (\neg x)$	1	$(x) \wedge (x^*)$
0	$(\neg x) \wedge (\neg x^*)$	_	$\neg(x \oplus x^*)$
u	$(x) \wedge (\neg x^*)$	Α	(x)
3	$(\neg x^*)$	В	$(x \vee \neg x^*)$
n	$(\neg x) \wedge (x^*)$	С	$(x^*)$
5	$(\neg x)$	D	$(\neg x \lor x^*)$
Χ	$(x \oplus x^*)$	Е	$(x \vee x^*)$
7	$(\neg x \vee \neg x^*)$	?	

Table 3.4: All bit conditions represented as CNF using two Boolean variables x and  $x^*$  to represent two bits.

# 3.4 A simple addition example

Using this notation, we can now reason about the behavior of functions on differential values. We start with 1-bit addition as most basic exercise to the reader. Consider a matrix with two input rows and one output row. The values of the first two rows are added such that the bit difference at the third row is created.

Figure 3.5 illustrates this example. Remember that symbols such as – and 0 underlie semantics defined in Table 3.3. It is also interesting to see how propagation of values can work. In Figure 3.6 we see how an underspecified value? can be strengthened once we have checked which values can be taken. Recognize that the system is constrained by the function in use and the definition of the differential symbols.

Finally we can extend our testcases to 4 bits and retrieve testcases such as Table 3.7 and 3.8.

# 3.5 Differential characteristics in action

In the previous section we illustrated how propagation with differential values works and how differential characteristics are written down. It is always important to keep in mind which function the characteristic illustrates, because this is not documented with the characteristic.

Now consider MD4 as defined in Section 2.2. MD4 takes some input message (in our case limited to size of one block), the state variables are initialized and iteratively new  $A_i$  are computed.

Similarly, SHA-256 takes a message block M and initializes eight variables with an initial vector (IV). The remaining  $W_i$  are computed and iteratively, values  $A_i$  and  $E_i$  are computed.

Those values are structured in differential characteristics illustrated in Figure 3.2. Those layouts are used to specify our hash collisions we want to evaluate. Table 3.9 is also gives an application of the layout.

Table 3.5: A simple 1-bit addition example: On the left the differential characteristic is given. Two dashes, by definition, denote a missing difference in both arguments. The result of the addition most neither show a difference. This yields eight possible bit configurations where two values close to each other denote  $(M, M^*)$  of Figure 3.1. Due to the behavior of addition, we know that configurations 2, 3, 5 and 8 (from left to right) are invalid.

Table 3.6: Like Figure 3.5, but any difference value for the result bit is possible. As such we consider any possible bit configuration, but eventually recognize that only four bit configurations are consistent with the behavior of addition. Because all resulting configurations show no bit difference in the output bit, we can strengthen? by replacing it with -. This illustrates how knowledge about differential states can be propagated.

A:	0011	A:	x	A:	x	A:	x
B:	0101	B:	x	В:	x	В:	x
S:	1000	S:	????	S:	???-	S:	x???
	A:	0011	A:	x	A:		
	B:	0101	B:	x	B:	x	
	S:	0000	S:	???x	S:	x-??	

Table 3.7: Testcases for 4-bit addition: The upper line shows valid differential characteristics for 4-bit addition whereas the lower line show invalid ones for 4-bit addition. The rows are conventionally named using capital letters.

A:		A:	7C-3	A:	0uCD
S:	0000	S:	-3u?	S:	ADC7
	A:	x	A:	xxxx	
	S:	0000	S:	0000	

Table 3.8: Differential characteristics for the SHA-2 Sigma function. The upper line shows valid states. The lower line shows invalid ones.

_						_				
1	_	$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$		i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001				-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110				-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101011011110011111110				-2	A:	100110001011101011011100111111110		
-1	A:	111011111100110110101011110001001				-1	A:	1110111111100110110101011110001001		
0	A:	01101011110101001110010000010010	W:	01001101011110101001110010000011		0	A:	011010111101010011110010000010010	W:	01001101011110101001110010000011
1	A:	01110110010011111111011100u110001	W:	u1010110110010111001001001111010		1	A:	01110110010011111111011100u110001	W:	u1010110110010111001001001111010
2	A:	1010101101000000001110u01n1110010	W:	n01n10011101010110100101011111000		2	A:	101010110100000001110u01n1110010	W:	n01n10011101010110100101011111000
3	A:	101011u1001111010101001001010001	W:	01010111101001111010010111101110		3	A:	101011u1001111010101001001010001	W:	01010111101001111010010111101110
4	A:	001011000110001101010101111110010	W:	11011110011101001000101000111100		4	A:	001011000110001101010101111110010	W:	11011110011101001000101000111100
5	A:	000110100110001010u1101000000001	W:	11011100110000110110011010110011		5	A:	000110100110001010u1101000000001	W:	11011100110000110110011010110011
6	A:	0001101100unuu110001000001111010	W:	???????????????????????????????		6	A:	0001101100unuu110001000001111010	W:	10110110100000111010000000100000
7	A:	00101011100000010unn011001010000	W:	00111011001010100101110110011111		7	A:	00101011100000010unn011001010000	W:	00111011001010100101110110011111
8	A:	??????????????????????????????	W:	11000110100111010111000110110011		8	A:	011100110010001u111111111110110000	W:	11000110100111010111000110110011
9	A:	??????????????????????????????	W:	11111001111010011001000110011000		9	A:	101011n01unnu0001111100110011111	W:	11111001111010011001000110011000
10	A:	10n0010010000101????????????110	W:	110101111001111110000000001011110		10	A:	10n00100100001010100000010101110	W:	11010111110011111110000000010111110
11	A:	u100011010110110?????????????111	W:	101001100011101110110010111101000		11	A:	u10001101011011001001010111111111	W:	10100110001110111011001011101000
12	A:	001011u00u101011????????????011	W:	010001011101110n1000111000110001		12	A:	001011u00u10101111111110001111011	W:	010001011101110n1000111000110001
13	A:	10un1n0100110001????????????101	W:	100101111110001100011111111100101		13	A:	10un1n01001100010100000111100101	W:	10010111111100011000111111111100101
14	A:	0000101001010001110	W:	001001111001010010111111100001000		14	A:	00001010010100011000100011010110	W:	001001111001010010111111100001000
15	A:	0001111010101u01100	W:	10111001111010001100001111101001		15	A:	0001111010101u010110011011010100	W:	10111001111010001100001111101001
16	A:	n00n0un011010010111				16	A:	n00n0un01101001010011011010111111		
17	A:	0001111100111010110				17	A:	00011111001110100001001000011110		
18	A:	0101011100001101100				18	A:	01010111000011010000000010010100		
19	A:	u1n1000000010111100				19	A:	u1n10000000101111001101011000100		
20	A:	n1un1001111111011101000000110100				20	A:	n1un10011111111011101000000110100		
21	A:	111100111011000001011111111010100			$\Rightarrow$	21	A:	111100111011000001011111111010100		
22	A:	01011101110011010011001100111010				22	A:	01011101110011010011001100111010		
23	A:	01010000111011101100011110001111				23	A:	01010000111011101100011110001111		
24	A:	00000010000100100011011100011010				24	A:	00000010000100100011011100011010		
25	A:	10110000100101100001010011101010				25	A:	10110000100101100001010011101010		
26	A:	00001010100010010111011101000001				26	A:	00001010100010010111011101000001		
27	A:	00000110111011110101101010110011				27	A:	00000110111011110101101010110011		
28	A:	10110110010111010110110000100101				28	A:	10110110010111010110110000100101		
29	A:	10100010000011010100100001101001				29	A:	10100010000011010100100001101001		
30	A:	00101001110101111100011101100011				30	A:	00101001110101111100011101100011		
31	A:	111111001001001011010111110110110				31	A:	111111001001001011010111110110110		
32	A:	01001111110100100110100000101111				32	A:	01001111110100100110100000101111		
33	A:	00111000001111010110111011100100				33	A:	00111000001111010110111011100100		
34	A:	00100000011101011110100000010101				34	A:	00100000011101011110100000010101		
35	A:	n0100000001100110000010001110010				35	A:	n0100000001100110000010001110010		
36	A:	n00001111110101111011111001011001				36	A:	n0000111111010111101111001011001		
37	A:	11001000000110100100001100001100				37	A:	11001000000110100100001100001100		
38	A:	10110000011001111110100110101100				38	A:	10110000011001111110100110101100		
39	A:	00010010000010100001101100011100				39	A:	00010010000010100001101100011100		
40	A:	11000000010010000111000110000101				40	A:	11000000010010000111000110000101		
41	A:	00000110100001101111010100100110				41	A:	00000110100001101111010100100110		
42	A:	010011101101110111111111010000110				42	A:	010011101101110111111111010000110		
43	A:	01010000011000111101000001101101				43	A:	01010000011000111101000001101101	l	
44	A:	11111000000101101111011100001100				44	A:	11111000000101101111011100001100		
45	A:	10001010110110110010110000000100				45	A:	10001010110110110010110000000100		
46	A:	1000001010011001011100011011100				46	A:	1000001010011001011100011011100	1	
47	A:	10000001111001011011010010111101				47	A:	100000011110010110110100101111101		

Table 3.9: One of the original MD4 collisions by Wang et al, with a few bits underspecified (left) and propagated values (right). The question marks indicate that any bit configuration for the two bits are possible. Dashes indicate that the bits have the same configuration in both instances, but the value itself is unknown. However, it turns out the description with missing values in iteration 6 (message) and iterations 8–19 is complete enough such that missing values can be deduced by other values the description of the algorithm. Therefore the collision They propagates through the intermediate values until the differences cancel out after round 36.

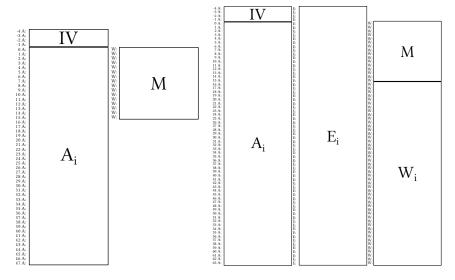


Figure 3.2: Layout of MD4 and SHA-256 differential characteristics



"What idiot called them logic errors rather than bool shit?" —Unknown

# Chapter 4

# Satisfiability

Boolean algebra allows us to describe functions over two-valued variables. Satisfiability is the question for an assignment such that a function evaluates to true. Satisfiability problems are solved by SAT solvers. We discuss the basic theory behind satisfiability. Because any computation can be represented as satisfiability problem, we are able to verify intermediate states of algorithms. In Chapter 6 we will represent a differential cryptanalysis problem such that it is solvable iff the corresponding SAT problem is satisfiable.

# 4.1 Basic notation and definitions

### Definition 4.1 (Boolean function)

A Boolean function is a mapping  $h: X \to Y$  with  $X = \{0,1\}^n$  for  $n \in \mathbb{N}_{\geq 1}$  and  $Y = \{0,1\}$ .

# Definition 4.2 (Assignment)

A *k*-assignment is an element of  $\{0,1\}^k$ .

Let f be some k-ary Boolean function. An assignment for function f is any k-assignment.

### Definition 4.3 (Truth table)

Let f be some k-ary Boolean function. The *truth table of Boolean function* f assigns truth value 0 or 1 to any assignment of f.

$x_1$	$x_2$	$f(x_1,x_2)$	$x_1$	$x_2$	$f(x_1,x_2)$	v	f(v)
1	1	1	1	1	1	1	0
1	0	0	1	0	1	0	1
0	1	0	0	1	1	(	c) NOT
0	0	0	0	0	0	,	•
	) AND		(E	s) OR			

TABLE 4.1: Truth tables for AND, OR and NOT

Boolean functions are characterized by their corresponding truth table.

Table 4.1 shows example truth tables for the Boolean AND, OR and NOT functions. A different definition of the three functions is given the following way:

#### **Definition 4.4**

Let AND, OR and NOT be three Boolean functions.

- AND maps  $X=\{0,1\}^2$  to 1 if all values of X are 1. OR maps  $X=\{0,1\}^2$  to 1 if any value of X is 1. NOT maps  $X=\{0,1\}^1$  to 1 if the single value of X is 0.

All functions return 0 in the other case.

Those functions are denoted  $a_0 \wedge a_1$ ,  $a_0 \vee a_1$  and  $\neg a_0$  respectively, for input parameters  $a_0$  and  $a_1$ .

It is interesting to observe, that any Boolean function can be represented using only these three operators. This can be proven by complete induction over the number of arguments k of the function.

Let k = 1. Then we consider any possible 2-assignment for one input variable  $x_1$  and one value of  $f(x_1)$ . Then four truth tables are possible listed in Table 4.2. The description shows the corresponding definition of f using AND, OR and NOT only.

Now let g be some k-ary function. Let  $(a_0, a_1, ..., a_k)$  be the k input arguments to g and  $x_1 := g(a_0, a_1, \dots, a_k)$ . Then we can again look at Table 4.2 to discover that 4 cases are possible: 2 cases where the return value of our new (k + 1)-ary function depends on value  $x_1$  and 2 cases where the return value is constant.

This completes our proof.

Boolean functions have an important property which is described in the following definition:

#### **Definition 4.5**

A Boolean function f is *satisfiable* iff there exists at least one input  $x \in X$  such that f(x) = 1. Every input  $x \in X$  satisfying this property is called *model*.

$x_1$	$f(x_1)$	$x_1$	$f(x_1)$	$x_1$	$f(x_1)$	$x_1$	$f(x_1)$
1	1	1	1	1	0	1	0
0	1	0	0	0	1	0	0
(A) j	$f: x \mapsto 1$	(B) f	$x: x \mapsto x$	(c) <i>f</i>	$: x \mapsto \neg x$	(D) j	$f: x \mapsto 0$

Table 4.2: Unary f and its four possible cases

The corresponding tool to determine satisfiability is defined as follows:

### **Definition 4.6**

A *SAT solver* is a tool to determine satisfiability (SAT or UNSAT) of a Boolean function. If satisfiability is given, it returns some model.

# 4.1.1 Computational considerations

The generic complexity of SAT determination is given by  $2^n$  for n Boolean variables.

Let n be the number of variables of a Boolean function. No known algorithm exists to determine satisfiability in polynomial runtime. This means no algorithm solves the SAT problem with runtime behavior which depends polynomially on the growth of n.

This is known as the famous  $\mathscr{P} \neq \mathscr{N} \mathscr{P}$  problem.

However, SAT solver can take advantage of the problem's description. For example consider function f in Display 4.1.

$$f(x_0, x_1, x_2) = x_0 \land (\neg x_1 \lor x_2) \tag{4.1}$$

Instead of trying all possible 8 cases for 3 Boolean variables, we can immediately see that  $x_0$  is required to be 1. So we don't need to test  $x_0 = 0$  and can skip 4 cases. This particular strategy is called *unit propagation*.

#### 4.1.2 SAT competitions

SAT research is heavily concerned with finding good heuristics to find some model for a given SAT problem as fast as possible. Biyearly SAT competitions take place to challenge SAT solvers in a set of benchmarks. The committee evaluates the most successful SAT solvers defined by solving the most problems within a given time frame.

SAT 2016 is currently ongoing, but in 2014 lingeling by Armin Biere has won first prize in the Application benchmarks track and second prize in the Hard

Combinatorial benchmarks track for SAT and UNSAT instances respectively. Its parallelized sibling plingeling and Cube & Conquer sibling treengeling have won prizes in parallel settings.

In Chapter 7 we will look at runtime results shown by (but not limited to) those SAT solvers.

# 4.2 The DIMACS de-facto standard

#### **Definition 4.7**

A *conjunction* is a sequence of Boolean functions combined using a logical OR. A *disjunction* is a sequence of Boolean functions combined using a logical AND. A *literal* is a Boolean variable (*positive*) or its negation (*negative*).

A SAT problem is given in *Conjunctive Normal Form* (CNF) if the problem is defined as conjunction of disjunctions of literals.

A simple example for a SAT problem in CNF is the exclusive OR (XOR). It takes two Boolean values a and b as arguments and returns true if and only if the two arguments differ.

$$(a \lor b) \land (\neg a \lor \neg b) \tag{4.2}$$

Display 4.2 shows one conjunction (denoted  $\land$ ) of two disjunctions (denoted  $\lor$ ) of literals (denoted a and b where prefix  $\neg$  represents negation). This structure constitutes a CNF.

Analogously we define a *Disjunctive Normal Form* (DNF) as disjunction of conjunctions of literals. The negation of a CNF is in DNF, because literals are negated and conjunctions become disjunctions, vice versa.

#### Theorem 4.1

Every Boolean function can be represented as CNF.

Theorem 4.1 is easy to prove. Consider the truth table of an arbitrary Boolean function f with k input arguments and j rows of output value false. We represent f as CNF.

Consider Boolean variables  $b_{i,l}$  with  $0 \le i \le j$  and  $0 \le l \le k$ . For every row i of the truth table with assignment  $(r_i)$ , add one disjunction to the CNF. This disjunction contains  $b_{i,l}$  if  $r_{i,l}$  is false. The disjunction contains  $b_{i,l}$  if  $r_{i,l}$  is true.

As far as f is an arbitrary k-ary Boolean function, we have proven that any function can be represented as CNF.

SAT problems are usually represented in the DIMACS de-facto standard. Consider a SAT problem in CNF with *nbclauses* clauses and enumerate all variables

from 1 to *nbvars*. A DIMACS file is an ASCII text file. Lines starting with "c" are skipped (comment lines). The first remaining line has to begin with "p cnf" followed by *nbclauses* and *nbvars* separated by spaces (header line). All following non-comment lines are space-separated indices of Boolean variables optionally prefixed by a minus symbol. Then one line represents one clause and must be terminated with a zero symbol after a space. All lines are conjuncted to form a CNF.

Variations of the DIMACS de-facto standard also allow multiline clauses (the zero symbol constitutes the end of a clause) or arbitrary whitespace instead of spaces. Another variant terminates DIMACS files once it encounters a single percent sign on a line. The syntactical details are individually published on a per competition basis.

LISTING 4.1: Display 4.2 represented in DIMACS format

```
p cnf 2 2
a b
-a -b
```

# 4.3 Terminology

Given a conjunctive structure of disjunctions, we can define terms related to this structure. Those terms will be used in the SAT features we suggest in Section 5.4.

#### **Definition 4.8**

A *clause* is a disjunction of literals. A *k-clause* is a clause consisting of exactly k literals. A *unit clause* is a 1-clause. A *Horn clause* is a clause with at most one positive literal. A *definite clause* is a clause with exactly one positive literal. A *goal clause* is a clause with no positive literal.

## **Definition 4.9**

Given a literal, its *negated literal* is the literal with its sign negated. A literal is *positive*, if its sign is positive. A literal is *negative* if its sign is negative. An *existential literal* is a literal which occurs exactly once and its negation does not occur. A *used variable* is a variable which occurs at least once in the CNF.

The *literal frequency* is the number of occurences of a literal in the CNF divided by the number of clauses declared. Equivalently *variable frequency* defines the number of variable occurences divided by the number of clauses declared.

#### **Definition 4.10**

The *clause length of a clause* is the number of literals contained. A clause is called *tautological* if a literal and its negated literal occurs in it.

A few basic properties hold in terms of satisfiability. For example existential literals are interesting, because they can be set to true and make one clause immediately satisfied without influencing other clauses.

# 4.4 Basic SAT solving techniques

#### **Definition 4.11**

Given two CNFs A and B, they are called *equisatisfiable* if and only if A is satisfiable if and only if B.

### 4.4.1 Boolean constraint propagation (BCP)

One of the most basic techniques to SAT solving is *Boolean Constraint Propagation*, also called *unit propagation*. It is so fundamental that SATzilla, introduced in Section 5.2, applies it immediately before looking at SAT features.

Let l be the literal of a unit clause in a CNF. Remove any clause containing l and replace any occurences of -l from the CNF. It is easy to see, that the resulting CNF is equisatisfiable, because due to the unit clause l must be true. So any clause containing l is satisfied and -l yields false, where  $A \vee \bot$  is equivalent to A for any Boolean function A.

#### 4.4.2 Watched literals

Watched Literals are another fundamental concept in SAT solving. It is very expensive to check satisfiability of all clauses for every assigned value of a literal. Watched Literals is a neat technique to reduce the number of checks.

In each clause two unassigned literals are declared to be "watched". Structurally it is implemented the other way around: A clauses watch list is maintained per literal. Now as long as at least two literals are unassigned, the clause cannot become false (recognize that a clause is false if all literals are false). Therefore the clause does not need to be visited as long as at least unassigned literals exist. This implies the following decision procedure:

- If all but one literal is false, propagate the remaining literal to be true.
- If all literals are false, report UNSAT.
- If any literal becomes true, watched literals do not change.
- Else replace the literal on the watch list with a remaining unassigned literal.

This empirical approach was established with the Chaff and zChaff SAT solvers [20] and has proven useful in various variants.

### 4.4.3 Remark

The previous two techniques shall illustrate basic approaches, but actual SAT solving research requires decades of development to tune individual SAT solvers. Memory models and concurrency strategies lead to fundamentally different runtime behaviors of SAT solvers.

As such an initial idea to initiate an individual SAT solver specifically designed for solving problems in differential cryptanalysis was dropped, because development time is expected too long for a master thesis to be fruitful. As such we focused on popular and established SAT solvers of the SAT community.

### 4.5 SAT solvers in use

In this thesis we consider the several SAT solvers. They have been selected either by their popularity or their good results at previous SAT competitions:

- · MiniSat 2.2.0
- CryptoMiniSat in versions 4.5.3 and 5
- treengeling, lingeling and plingeling, in versions:
  - lingeling ats1
  - lingeling ats101
  - lingeling ats102
  - lingeling ats104
  - lingeling baz
- glucose 4.0
- glucose syrup 4.0

Specifically this means the hash collision attacks we looked have run with these SAT solvers. The results are discussed in Section 7 and provided in Appendix C.

MiniSat is known as "Swiss army knife of SAT solving" meaning that it includes many well-established techniques that can be built upon. SAT competitions 2009, 2011, 2013 and 2014 included a special MiniSat hack track where participants are asked to modify MiniSat to prove the best performance with as little change to the

MiniSat codebase as possible. Even though is not one of the fastest SAT solvers today, it provides a nice codebase to experiment with.

CryptoMiniSat is a derivative of MiniSat, which was originally modified for cryptographic problems. It famously features XOR clauses meaning that binary clauses of structure  $a \oplus b$  could be added and will be resolved using Gaussian elimination. Temporarily development has been given up but most recently it was added again. Please recognize that our encoding introduced in Section 6.2 uses equivalence to model assignment and as such only clauses of structure  $r = a \oplus b$  emerge rendering this feature impractical to use.

glucose was the gold winner 2011 in the SAT+UNSAT application track. Modifications of glucose also ranked high throughout the years of SAT competition. glucose is a sequential SAT solver whereas glucose syrup is its parallelized version.

lingeling is SAT solver developed by Armin Biere. Lingeling has been the winner of several tracks in the SAT competitions 2011 to 2016. For example it has won gold in the SAT+UNSAT application track in 2014. lingeling has two siblings: plingeling and treengeling. plingeling is a parallelized version of lingeling. As such it executes in multiple threads and shares units and equivalences between those instances. treengeling is a Cube & Conquer solver meaning it partitions the problem into many subproblems and solves them individually.

lingeling releases ats101, ats102 and ats104 are non-public releases of lingeling. They have been developed in private communication with Armin Biere. Our main goal was to achieve a separation between two sets of variables. First all variables of the first need to be assigned in the best possible way. Afterwards the second set of variables is considered. Specifically variables modelling the differences between the two hash algorithm instances should constitute the first set.

ats101 implements that difference variables are guessed with false first and usual heuristics apply for all other variables. Our intermediate results with incomplete CNF files showed a high number of restarts. Therefore ats102 disables backjumping and therefore skips decisions for important variables. Finally ats104 is not expected to distinguish from ats102. It only provides further debugging information.

The SAT solvers have generally been run without any special options, except

- MiniSat was run with pre=once as it is generally recommended to run with the builtin preprocessor.
- Lingeling has been generally run with phase=-1 to prefer false as initial assignment to literals. However, lingeling ats101 implements this with a more forceful strategy.

Testcases with lingeling have all been run 5 times with various seeds (for

reference, the default seed is o). Only the mean runtime value is displayed in the results in Chapter 7.

Preprocessing is a difficult topic on its own. Sometimes preprocessing can provide a speedup, before actually solving the problem, but mostly SAT solvers implement preprocessing strategies themselves and run them repeatedly when solving the problem.



"To be usable effectively [...] these features must be related to instance hardness and relatively cheap to compute"

—SATzilla

## **Chapter 5**

## **SAT** features

At the very beginning I was very intrigued by the question "What is an 'average' SAT problem?". Answers to this question can help to optimize SAT solver memory layouts. Specifically for this thesis I wanted to find out whether our problems distinguish from "average" problems in any way such that we can use this distinction for runtime optimization.

I came up with 8 questions related to basic properties of SAT problems we will discuss in depth in this section. We will characterize an average SAT problem at Section 5.7:

- 1. Given an arbitrary literal. What is the percentage it is positive?
- 2. What is the clauses / variables ratio?
- 3. How many literals occur only once either positive or negative?
- 4. What is the average and longest clause length among CNF benchmarks?
- 5. How many Horn clauses exist in a CNF?
- 6. Are there any tautological clauses?
- 7. Are there any CNF files with more than one connected variable component?
- 8. How many variables of a CNF are covered by unit clauses?

We will now define the terms used in those questions.

### 5.1 Definition

### Definition 5.1 (SAT feature)

A *SAT feature* is a statistical value (named *feature value*) retrievable from some given SAT problem.

The most basic example of a SAT feature is the number of variables and clauses of a given SAT problem. This SAT feature is stored in the CNF header of a SAT problem encoded in the DIMACS format.

The general goal is to write a tool which evaluates several SAT features at the same time and retrieve them for comparison with other problems. Therefore it should be computationally easy to evaluate SAT features of a given SAT problem. A suggested computational limit is given with polynomial complexity in terms of number of variables and number of clauses for memory as well as runtime for evaluation algorithms. Sticking to this convention implies that evaluation of satisfiability must not be necessary to evaluate a SAT feature under the assumption that  $\mathcal{P} \neq \mathcal{NP}$ . Hence the number of valid models cannot be a SAT feature as far as satisfiability needs to be determined. But no actual hard computational limit is defined.

### 5.2 Related work

The most similar resource I found looking at SAT features was the SATzilla project [23, 36] in 2012. The authors systematically defined 138 SAT features categorized in 12 groups. Some features are only evaluated conditionally. The features themselves are not defined formally, but an implementation is provided bundled with example data. The following list provides an excerpt of the features:

nvarsOrig number of variables defined in the CNF header

**nvars** number of active variables

reducedVars nvarsOrig - nvars, divided by nvars

vars-clauses-ratio nvars divided by number of active clauses

**POSNEG-RATIO-CLAUSE-mean** mean of  $2 \cdot ||0.5 - pos/length||$  where pos is the number of positive literals and length clause length of a specific clause

**POSNEG-RATIO-CLAUSE-entropy** like POSNEG-RATIO-CLAUSE-mean but entropy

**TRINARY+** number of clauses with clause length 1, 2 or 3 divided by number of active clauses

**HORNY-VAR-min** minimum number of times a variable occurs in a Horn clause

**cluster-coeff-mean** let neighbors of a clause be all clauses containing any literal negated and let clauses  $c_1$  and  $c_2$  be conflicting if  $c_1$  contains literal l and  $c_2$  contains -l, then return the mean of 2 times the number of conflicting neighbors of a clause c divided by the number of unordered pairs of neighbors, returned iff computable within 20 seconds for all clauses

Please recognize that active clauses are the unsatisfied clauses after BCP has been applied. Equivalently active variables are remaining variables after application of BCP.

Many SAT solvers collect feature values to improve algorithm selection, restart strategies and estimate problem sizes. Recent trends to apply Machine Learning to SAT solving imply feature evaluation. SAT features and the resulting satisfiability runtime are used as training data for Machine Learning. One example using SAT features for algorithm selection is ASlib [1].

The SAT solvers of Section 4.5 we use also compute features they use when computing a solution. For example CryptoMiniSat 4.5.3 prints the following lines

```
c [features] numVars 56118, numClauses 358991, var_cl_ratio 0.156,
binary 0.019, trinary 0.520, horn 0.387, horn_mean 0.000, horn_std
0.000, horn_min 0.000, horn_max 0.000, horn_spread 0.000,
vcg_var_mean 0.000, vcg_var_std 0.902, vcg_var_min 0.000,
vcg_var_max 0.000, vcg_var_spread -0.000, vcg_cls_mean 0.000,
```

Even though we will partially use equivalent features (like Horn clauses), many are actually related to the current state of evaluation like decisions per conflicts. We consider this as a property of the evaluation and not the SAT problem itself.

### 5.3 Statistical features

For our SAT features we need to define some basic statistical terminology. Let  $x_1, x_2, ..., x_n$  be a finite sequence of numbers  $(n \in \mathbb{N})$ .

Arithmetic mean (or short: mean) is defined as

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

**Standard deviation** (or short: sd) with mean  $\overline{x}$  is defined as

$$\sigma(x) = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \overline{x})}$$

**Median** with  $x_1 \le x_2 \le ... \le x_n$  (i.e. sorted ascendingly) is defined as

$$m = \begin{cases} x_{\text{mid}} & \text{if } n \text{ odd} \\ \frac{x_{\text{mid}} + x_{\text{mid}+1}}{2} & \text{if } n \text{ even} \end{cases} \text{ with mid} = \frac{n}{2}$$

and often considered more "robust" than the arithmetic mean.

**Entropy** is defined according to Claude Shannon's information theory:

$$H(x) = -\sum_{i=1}^{n} x_i \cdot \log_2(x_i)$$

where  $0 \cdot log_2(0) := 0$ .

Furthermore *count* refers to the number of elements n, *largest* refers to the maximum element  $\max_{1 \le i \le n} (x_i)$  and *smallest* refers to the minimum element  $\min_{1 \le i \le n} (x_i)$ .

### 5.4 Suggested SAT features

We wrote a tool called cnf-analysis. The evaluated features are partially inspired by SATzilla and lingeling. The latter prints basic statistics for every CNF it evaluates.

A summary of our suggested SAT features is given:

### clause\_variables\_sd\_mean

mean of sd of variables in a clause

#### clauses\_length\_(largest, smallest, mean, median, sd)

statistics related to the clause length

### connected\_(literal, variable)\_components\_count

two literals (variables) are connected if they occur in some clause together, count the number of connected components

#### definite\_clauses\_count

number of definite clauses in the CNF

### existential\_literals\_count

number of existential literals in the CNF

### existential\_positive\_literals\_count

number of positive, existential literals in the CNF

### (false, true)\_trivial

is the CNF satisfied if all variables are claimed to be false (true)?

### goal\_clauses\_count

number of goal clauses in the CNF

#### literals\_count

number of literals in the CNF (i.e. sum of clause lengths)

### literals\_frequency\_k\_to\_k + 5

let  $n_l$  be the literal frequency of literal l, count the number of  $n_l$  satisfying  $\frac{k}{100} \le n_l < \frac{k+5}{100}$  where k is a variable in  $\{0, 5, 10, \dots, 90, 95\}$  and k = 95 counts  $\frac{k}{100} \le n_l \le \frac{k+5}{100}$ .

### literals\_frequency\_(largest, smallest, mean, median, sd)\_entropy

statistics related to literal frequencies

#### literals\_occurence\_one\_count

number of literals with occurence 1

**nbclauses**, **nbvars** number of clauses (variables) as defined in the CNF header

### negative\_literals\_in\_clause\_(smallest, largest, mean)

statistics related to number of negative literals in clauses

### (positive, negative)\_unit\_clause\_count

number of unit clauses with a positive (negative) literal

### positive\_literals\_count

number of positive literals in CNF

### positive\_literals\_in\_clause\_(largest, smallest, mean, median, sd)

statistics related to number of positive literals in clauses

### positive\_negative\_literals\_in\_clause\_ratio\_(mean, entropy)

let  $r_c$  be the number of positive literals divided by clause length of clause c, mean and related of all  $r_c$ 

### positive negative literals in clause ratio mean

mean of all  $r_c$ 

### tautological\_literals\_count

number of clauses which contain a tautological literal

### two\_literals\_clause\_count

number of clauses with two literals

### variables\_frequency\_k\_to\_k + 5

same as literals\_frequency\_k\_to\_k + 5 but for variables

### variables\_frequency\_(largest, smallest, mean, median, sd, entropy)

same as literals\_frequency but for variables

#### variables\_used\_count

number of variables with occurence greater o

### 5.5 Evaluation efficiency

The resource requirements of those features have been classified:

**Type 1** read the files as bytestring, a DIMACS CNF parser is not necessary, constant memory is used

Type 2 features understand what a clause is, but still need constant memory

**Type 3** subquadratic runtime and linear memory

Type 4 unrestricted

Memory and runtime is always considered in comparison with the filesize.

This classification should support future considerations regarding feature evaluation tools. The suggested SAT features above have been explicitly selected to avoid Type 4 implementations to limit the time to compute features. Furthermore tools evaluating only a subset of features (like Type 2 features) with better performance characteristics.

The Python implementation triggered MemoryErrors on a computer with 4 GB RAM for a 770 MB CNF file. Followingly a much more efficient Go implementation was implemented which requires much less memory and is much faster. bench\_573.smt2.cnf took 1 second in Go instead of 2 minutes in Python. However, the data evaluated is less accurate compared to Python, because Python unlike Go provides a nice implementation of statistical tools in the standard library. Go algorithms were written on our own.

In the following section, we define the dataset we consider.

### 5.6 CNF dataset

To evaluate CNF features of a representative set of CNF files, it was necessary to identify equivalent CNF files in the best possible way. Therefore we defined

a hashing algorithm standardizing the CNF input provided to a SHA1 instance. Every CNF file is identifiable by its "cnfhash 2.0.0" hash value.

In the next step a complete set of CNF files of previous SAT competitions was collected. The following CNF file collections have been considered:

• SAT Race 2008

• SATo9 Competition

• SAT-Race 2010

• SAT11 Competition

• SAT Challenge 2012

• SAT Competition 2013

• SAT Competition 2014

• SAT-Race 2015

• SAT Competition 2016

• SATlib

The benchmarks are mostly contributed by the participants of the associated conferences. Others are reused from previous years. Individual projects allow to generate CNF files for specific problems in a selectable problem size; such as CNFgen [14] by Massimo Lauria.

Some files turned out to be problematic. In SATlib, 3 gzipped files couldn't be decompressed and several files contain empty clauses. Empty clauses are assumed to immediately falsify the CNF and are therefore pointless. I removed trailing zeros in CNFs. Variants of the DIMACS standard also expect lines with a percent symbol to terminate the CNF. Besides those minor issues documented as part of the cnf-analysis project, 175 gigabytes of CNF files have been evaluated with a total of 68,069 CNF files (62,251 unique CNF files).

### 5.7 The average SAT problem

#### Proposition 5.1

The set of public benchmarks in SAT competitions between 2008 and 2015 represent average SAT problems

It is important to point out that public benchmark files are specifically chosen to be evaluated before a conference is held. Hence they are expected to terminate within a given time frame and are therefore not oversized. On the one hand this ensures that the problems are feasible, but on the other hand they might be a biased selection. At this point no better data set is available and therefore we proceeded with this dataset.

According to my results, an average SAT problem consists of:

• 83,542 clauses in average ranging from 21 to 53,616,734 (median = 430,  $\sigma$  = 848388)

- The longest clause we found had 61,473 literals, but the longest clause of an average CNF covers 20 literals.
- The number of total literals in a CNF ranges from 60 up to 150,609,758.
- The clause-variables ratio lies between 1.22 and 27,720 with mean = 9.54 and  $\sigma$  = 139.
- The average length of a clause is expected to be 3. The largest clause length mean we found was 19.58 compared to 2.83 as the smallest clause length mean.
- Surprisingly, in average a CNF file has 205 connected literal components and 53 connected variable components. However both corresponding medians are 1 meaning that at least have of the problems still have only one component.
- In average 32,787 clauses are definite clauses and 35,094 clauses are goal clauses.
- In average a literal occurs in 1.4 % of the clauses of the CNF.
- 47 % of literals in a clause are positive.
- The arithmetic mean tells 124 unit clauses per CNF file can be expected, but the median tells it is mostly o.
- The largest variable found was 13,842,706 and 13,829,558 variables were used at most.
- Exactly one CNF file was true-trivial (namely dubois/dubois100.cnf of SATlib) whereas 13 CNF files were false-trivial (of SAT competition 2014 and SAT-Race 2015).

### 5.8 Benford's law in CNF files

Given this huge set of CNF files and therefore integers, we evaluated whether Benford's law holds.

A paper by Theodore P. Hill [8] characterizes Benford's Law as the following conjecture:

#### Theorem 5.1

Consider arbitrary data from tables, listings or other sources in publications, newspaper and so on and so forth, the digit 1 occurs in about 30 % of the time. The first digit is 1 about 30 percent of the time and 9 only about 4.6 percent of the time.

We evaluated that the leading digits 1 to 9 occur with probabilities 28.76 %, 19.09 %, 13.56 %, 10.97 %, 7.48 %, 5.76 %, 5.12 %, 4.79 % and 4.46 % respectively. We concluded that:

Considering a deviation of 1.34% for digit 1 (expected 30.1, actual 28.76) and 0.12% for digit 9 (expected 4.58, actual 4.46), we claimed the CNF files considered satisfy Benford's law.



"There is concensus that encoding techniques usually have a dramatic impact on the efficiency of the SAT solver"

—Magnus Björk

## **Chapter 6**

## **Problem encoding**

We already discussed how SAT solvers work and which input they take. We also sketched how hash algorithm properties got broken using differential cryptanalysis. In this section we combine those subjects and describe how we designed an attack setting.

We designed a basic prototype with the STP SMT solver. Followingly we wanted to tweak the CNF used by the SAT solver and wrote our own library *algotocnf* to generate CNFs for differential purposes; as illustrated in Section 3. There we distinguished 5 different tweaks. We evaluate the performance of those tweaks in Chapter 7.

Every section represents a major approach whereas subsections represent derivatives of this approach with minor tweaks.

### 6.1 Basic approach

Our first approach started with Simple Theorem Prover (STP) [7] initially written by Vijay Ganesh and David L. Dill. It is currently maintained by Mate Soos.

STP is an SMT solver which allows to declare bitvectors. A bitvector is an array of Boolean variables providing high-level constructs such as additions or right-shift through an interface. Writing all clauses individually to model a hash algorithm is too cumbersome to be done in practice and STP simplifies this process. STP is recommendable as a tool to model arithmetic and bitwise functions.

First we wrote an implementation using the CVC language to model the MD4 hash algorithm. We provide a bitvector to the hash algorithm instance. When applying the corresponding arithmetic operations we generate expressions such as ASSERT(y = 0bin00000101); to model the assignment of a constant. Here the desired constant is assigned variable y, because of equivalence. y is required to have the constant after this expression as value. Whereas we generate the ASSERT statement, it is STP's task to generate the CNF formula and solve it with a SAT solver.

We take two hash algorithm instances and an additional bitvector diff for every pair of bitvectors (bv1, bv2) where bv2 represents the corresponding bitvector of the second hash algorithm instance to bv1. We claim ASSERT(diff = BVXOR(bv1, bv2)) to ensure that diff represents the difference between bv1 and bv2. Given the bitconditions for a bitvector from a differential characteristic, we require diff to enforce those particular differences. This corresponds to the idea of differential cryptanalysis introduces in Chapter 3.

It is now trivial to consider a differential characteristic such as Testcase B.1 and generate the corresponding CVC input for STP. STP solves this particular problem within a second. Testcase B.2 already provides a more complex example taking 40 minutes to solve. We used minisat as SAT solver in the backend, even though STP allows to exchange it for CryptoMiniSat which is a more modern and versatile SAT solver.

Even though STP allows to come to useful results pretty quickly, it seems cumbersome to model all hash algorithms in the CVC language. STP provides a python interface meaning that pure Python implementations of hash algorithms can be taken with little modifications to model the hash algorithm itself. We add code to declare the difference bitvectors diff and finally add the constraints resulting from the differential characteristic.

This interface switch introduces no significant performance difference.

As a next step, we wanted to improve the evaluation performance to tackle more difficult problems. We considered this design as a working prototype of a basic approach to be improved upon.

STP was not fruitful for our next goal, because we wanted to tweak the SAT design generated for the SAT solver and needed good control over the SAT encoding which we expected to have a major influence on the performance.

### 6.2 algotocnf

We implemented our own library *algotocnf* to achieve greater flexibility in SAT design.

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#### 6.2.1 Two instances and its difference

Similar to STP, algotocnf generates a CNF for a given hash algorithm implementation. Besides modelling bitvectors, it also implements differential bitvectors which inherently handle the difference bitvectors diff which contain difference variables. It can also directly operate with differential characteristics. Similarly to STP, it implements arithmetic and bitwise operations.

We think *algotocnf* mainly differs from other SMT tools like STP because of its implementation of differential logic.

To model our CNF *algotocnf* implements the following strategy:

- 1. Take a differential characteristic and the hash algorithm as input.
- 2. Every bit is therefore represented as a Boolean variable. If you apply addition, operator overloading in python will ensure that clauses are generated to describe the addition consisting of XORs and MAJs. Every operation is modelled as assignment. Hence an operation operating on a few Boolean variables is equivalent to a single variable which represents the result. Equivalently other operations related to integers are implemented as well.
- 3. Constants used in the implementation are automatically converted to bitvectors with unit clauses.
- 4. After running the hash algorithm with bitvectors per instance, all constraints related to the hash algorithm are added.
- 5. Followingly the differential characteristic is read. Values such as  $A_i$  represent intermediate states of bitvectors. Therefore the corresponding bitvectors are looked up and equivalences with temporary bitvectors are added. Those temporary bitvectors are initialized with all constraints resulting from the bit conditions of this bitvector. In conclusion all constraints resulting from the differential characteristic are added.
- 6. Finally the SAT solver is called. The CNF was mostly solved on a cluster specified in Appendix A.
- 7. Afterwards the program is run again to create the exactly same problem instance and the solver's solution replaces symbolic values with actual Boolean values. The resulting differential characteristic is parsed backed and printed out as differential characteristic where expectedly many bit conditions have been strengthened.

When adding clauses resulting from the differential characteristic as constraints, the question arises how those bit conditions are encoded. Essentially, we

have only Boolean values available, but bit conditions tell constraints such as "a difference is given, but the actual value is unknown".

It seemed trivial to add a *difference variable* for every pair of Boolean values representing a bit in the two instances. Furthermore the difference variable  $\Delta x$  is connected by a XOR with the variables of the pair (x, x').

$$\Delta x = x \oplus x'$$

Therefore it should be trivial for a preprocessor to simplify the formula appropriately or actually we don't expect runtime differences for the larger amount of variables.

And finally we expect the CNF to inherit a property of hash functions. Inputs are provided into the hash algorithm and strongly intermingled with other values. This should result in a high diffusion and almost every variable is expected to share a clause with another variable.

The difference variables design corresponds to diff bit vectors in the STP and therefore designs the difference described in Chapter 3. The design decisions of this encoding are fundamental to the resulting runtime discussed in Chapter 7.

### 6.2.2 Adding the differential description

Using the approach in the previous section, we were able to find actual MD4 collisions using a SAT solver (please refer to Section 7.2.1). A SHA256 implementation followed which obviously lead to worse runtime results, because the internal state of SHA-256 is much larger (by a factor of at least 2). Can we further improve the runtime of the SAT solver?

Because we work with bitvectors and apply high-level operations like MAJ or addition, we can additionally implement how differences in those operations propagate. Magnus Daum's thesis on "Cryptanalysis of Hash Functions of the MD4-Family" [4, Table 4.4] discusses how differences propagate in Boolean functions. Trivially, XORs propagate differences the way they are  $^1$ . Another example is MAJ: Let a, b and c be difference variables and MAJ is applied to both corresponding hash algorithm instances. r is the difference variable of the result. Then its differential behavior states that

$$(0,1,1) \Longrightarrow 1 \quad (0,0,0) \Longrightarrow 0$$

where (IN)  $\implies$  OUT denotes an input-output relation. Because of this behavior we add clauses to explicit describe this behavior:

$$(\neg a \land b \land c) \implies r \iff a \lor \neg b \lor \neg c \lor r$$

<sup>&</sup>lt;sup>1</sup>A difference in the arguments of two XOR instances remains the same difference after applying XOR to each instance

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We also model the second behavior:

$$(\neg a \land \neg b \land \neg c) \implies \neg r \iff a \lor b \lor c \lor \neg r$$

This approach explicitly models differentiable behavior, which should be deducible by the SAT solver itself based on the clauses we added before. However, this lead to a major speedup which can be observed in the runtime results of Chapter 7.

### 6.2.3 Evaluating difference variables first

### Proposition 6.1

Deriving difference values first, followed by actual bit values for the two instances, leads to a speedup.

This proposed principle is fundamental to differential cryptanalysis. A previous tool at our department implements propagation of hash algorithm values without a SAT solver and this strategy is essential to good performance. This strategy was introduced in the very early days of differential cryptanalysis and was also used by Wang et al. [35] to find their hash collisions.

So basically in terms of SAT solvers we want to guess values for difference variables first and once all have been assigned, we try to find actual values for the two hash algorithm instances.

It is important to point out that DIMACS does not specify a way to annotate Boolean variables. As such that SAT solver cannot distinguish between difference variables and variables of the instances. Therefore implementing this approach requires a custom SAT solver which is given with lingeling ats101.

Another proposition is important for this approach:

### Proposition 6.2

Guessing difference values false first, followed by true, should solve hash collision problems faster.

This proposition is justified by the desire to find as little differences as possible in a hash collision to increase the probability of values cancelling each other out in the later rounds.

### 6.2.4 A light-weight approach

In this tweak we made a step back and considered the ideas of the previous section but neglected the differential description. This approach was interesting to recognize the effect introduced by adding the differential description.

### 6.2.5 Influencing the evaluation order

We took to idea to influence the evaluation order to the next level, by applying the following design:

Let  $\Delta x$  be the difference variable of pair (x, x'). We introduce a new Boolean variable  $x^*$ . We add clause

$$x^* = (\Delta x \wedge x)$$

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and explicitly tell the SAT solver to guess on  $x^*$  before guessing on  $\Delta x$ , x or x'.

The SAT solver will assign x'=0 first, because of the evaluation order. So either  $\Delta x$  or x must be false.  $\Delta x$  is assigned false, because as difference variable it has a higher priority over x. Equivalently for x'=1 we have  $\Delta x$  needs to be true. So we actually achieve an early guess on the difference variable.

This another approach evaluates in the results chapter.



## Chapter 7

## Results

In Chapter 4 we discussed Boolean algebra; in particular we looked at satisfiability which is practically covered by SAT solvers. SAT solvers take Boolean functions in Conjunctive Normal Form and determine satisfiability. In Chapter 3 we looked at how we can analyze algorithms by looking at the progression of differences between algorithm instances. In particular we looked at hash algorithms introduced in Chapter 2.

With this background we designed a attack setting in Chapter 6 which enables us to verify and also find a hash collision given a differential characteristic given as starting point. Our goal is to find hash collisions in as little time as possible. Therefore we introduced several approaches in Section 6.2.

In this section we will evaluate those approaches. Furthermore we briefly discuss claims we made about average SAT problems. In Section 5 we looked at SAT features which to some extent characterize a SAT problem.

### 7.1 Evaluating SAT features

In the introduction of Chapter 5 we posed 8 questions. In the following, we want to answer them with the data provided by the cnf-analysis project.

**Given an arbitrary literal. What is the percentage it is positive?** We look at every clause and determine the ratio of positive to the total number of literals. We determine the mean per CNF file and the mean among all CNF files and retrieve a value of 0.48 meaning that 48 % of the literals are positive.

- What is the clauses / variables ratio? In average a CNF file has 12,219 variables and 89,541 clauses. Its clauses-variables ratio is 7.328.
- How many literals occur only once either positive or negative? In average there are 36 existential literals per CNF file, but its standard deviation of 967 is very high.
- What is the average and longest clause length among CNF benchmarks? The average clause length is 3.04 with a standard deviation of 0.99 and the longest clause length found was 61,473. Long clauses are typically outliers excluding specific assignments.
- How many Horn clauses exist in a CNF? In average 29,994 goal clauses and 31,315 definite clauses exist with an average number of 83649 clauses in a CNF file.
- **Are there any tautological clauses?** In a file, 1679 tautological literals have been found. However, its mean is 0.07 with a standard deviation of 9.63 meaning that tautological clauses are very rare.
- Are there any CNF files with more than one connected variable component? Indeed, an average CNF file contains 67.07 connected variable components. However, its median is 1 anyway implying that at least half of the CNF files have only 1 connected variable component.
- How many variables of a CNF are covered by unit clauses? In average 124 variables are covered by unit clauses. This is an insignificant number compared to 12,219 variables in an average CNF.

The clauses/variables ratio was thoroughly studied by the SAT community [24]. A strong correlation between the instance's hardness and the ratio of number of clauses to number variables exists [32] though it is important to point out that this result holds for randomly generated SAT instances, which our benchmarks are not classified as.

Existential literals are interesting to discover, because they allow to remove a clause immediately. Consider a clause with literals  $(l_1, l_2, \dots, l_n)$ . If a guarantee exists such that the variable of any literal  $l_i$  does not occur in any other clause, we can claim  $l_i$  true rendering the clause satisfied.

Tautological clauses obviously also render clauses satisfied.

Connected variable components are interesting, because they split the SAT problem into several small subproblems which can be independently. Consider two sets of variables A and B. Now consider some clauses using only variables of A and some clauses using only variables of B. The overall CNF is satisfiable iff both clause sets are satisfiable. The overall CNF is falsifiable iff any clause set is

falsifiable. Hence if we know the connected variable components, we could easily create two parallel SAT solver instances and solve the problems independently. 4,607 out of 62,251 CNF files contained more than 1 connected variable component.

These properties represent very fundamental properties of the SAT problem. But for us the question arises whether we can distinguish our cryptoproblems from average problems?

- We looked at 36 files classified as cryptographic problems. They are considered cryptographic, because their file or folder name indicated they are related to hash functions or general cryptographic applications like AES. The specific selection can be identified by the crypto tag annotated to these CNF files as part of the cnf-analysis project.
- 62,533 clauses and 8,279 variables in average yield a variables-clauses ratio of 7.55.
- The 36 cryptographic SAT instances give a standard deviation of o for clause length meaning that all clauses had the same length.
- Whereas the number of connected variable components has a mean of 52.73 ( $\sigma = 1225$ , median = 1) for general problems, Our cryptographic problems considered had a mean of 1 ( $\sigma = 0$ , median = 1).
- The number of definite clauses is half its value for general problems (16,687 versus 32,787) and the number of goal clauses is 16 % of its value for general problems (5,767 versus 35,094).

No other value has been found to be significantly different from average problems (or its difference follows immediately by the non-uniform clause length). The number of connected variable components seems interesting because it might indicate diffusion in cryptographic problems. Diffusion means that variables strongly interact with many different variables due to the repetitive structure of cryptographic primitives. And finally the other differences can be explained by a certain SAT design which reoccurs in this benchmarks, because 36 is an exceptionally small number compared to 62,251 unique CNF problems.

Comparing our average problem with cryptographic problems did not draw any useful conclusions. Particularly a more thorough discussion of the SAT designs might be more valuable than our high-level features. We now specificall look at a SAT design we are familiar with: Do average SAT problems distinguish from *our* CNF benchmarks?

• For all MD4 testcases we have the same number of variables, because the internal state of the hash algorithm instances are always the same size. However, adding the differential description described in Section 6.2.2 increases

the number of clauses by about 47 % ( $\sigma=0.0005$ ) for MD4 instances and by about 43 % ( $\sigma=0.0008$ ) for SHA-256 instances. The additional variable introduced in Section 6.2.5 increases the number of variables by about 80 % and the number of clauses by factor 2.

MD <sub>4</sub> C	253,984 / 48,704	MD <sub>4</sub> C diff-desc	373,920 / 48,704
$MD_4 B$	254,210 / 48,704	MD4 B diff-desc	374,146 / 48,704
$MD_4 A$	254,656 / 48,704	MD <sub>4</sub> A diff-desc	374,592 / 48,704
SHA-256 18	590,953 / 107,839	SHA-256 18 diff-desc	846,487 / 107,839
SHA-256 21	636,838 / 116,800	SHA-256 21 diff-desc	911,629 / 116,800
SHA-256 23	667,438 / 122,774	SHA-256 23 diff-desc	955,067 / 122,774
SHA-256 24	682,722 / 125,761	SHA-256 24 diff-desc	976,770 / 125,761

Table 7.1: Our testcases and their number of clauses / variables

Compared to 83,542 clauses and 12,219 variables for our average SAT problem, we consider our benchmark to be noticeably large. It is important to point out that the problem size does not necessarily correlate with the hardness of the SAT problem.

- The variables of clauses of average SAT problems have a standard deviation of 3,337 in average ( $\sigma$  =1,261, median =3,643). Our average SAT problem has a standard deviation of 1,004 in average ( $\sigma$  =13,992, median = 22). Hence variables which got created at very points during the CNF generation are shared within one clause. The general statement, that variable enumeration is arbitrary and therefore this standard deviation has no meaning, holds but we need to consider that practically speaking variables created close to each other share close variable indices. Under these assumptions a large  $\sigma$  indicates variables are reused. We assume this is another indicator for high diffusion in cryptographic algorithms. Values are intermingled over and over throughout the repetitive structure of hash algorithms.
- Connected variables components are 129 for MD4 problems and 2 for SHA-256 problems. We couldn't explain where those components come from and the component size would help us to identify their source. We did not investigate further, because this number is constant with an increasing problem size.
- An average literal frequency of  $3.5 \cdot 10^{-5}$  for our benchmarks is much lower than 0.014 for average problems. We explain this with the larger problem size. Literal frequency is divided by the number of clauses of the CNF and is therefore smaller the larger the problem is.

In general we were not able to identify features which allows us to solve differential cryptanalysis problems more efficiently compared to general-purpose SAT problems. We concluded writing your own SAT solver dedicated to solving differential cryptanalysis problems is not worth the effort.

### 7.2 Finding hash collisions

In this section we look at our benchmark results of Testcases provided in Appendix B. We make various propositions and substantiate them with runtime results. Runtimes are always provided in seconds and  $\top$  denotes a timeout (solving takes more than 1 day).

### 7.2.1 Attacking MD4

#### Proposition 7.1

Testcase B.1 in the encoding described in Section 6.2.1 can be solved within one minute by all considered SAT solvers.

In our attack setting we started off with Testcase B.1. It serves rather as a toy example to verify correctness of our implementation than as an actual runtime benchmark. Be aware that invalid implementations either result in unsatisfiability for satisfiable testcases or runtime results are unexpected because the SAT solver could not take advantage of our SAT design implementations. This particular testcase can be solved easily with all major SAT solvers as can be seen in Table 7.2.

We end up with the result, that the hash collision given in Table B.3 can be solved by a limited set of modern SAT solvers. Of course the cryptanalyst needs to figure out good starting points for the hash collision and encode them in the differential characteristic, but this task is still considered practical, because this task can be easily automated.

solver	version	propagations	decisions	restarts	runtime
MiniSat	2.2.0	3,813,726	250,759	_	3
CryptoMiniSat	4.5.3	140,000	2,441,566	539	26
	5	_	2,428,824	637	37
Lingeling	ats1	6,586,770	436,621	980	23
plingeling	ats1	452,630,440	3,275,498	_	88
Glucose	4.0	14,727,839	990,491	272	8
Glucose Syrup	4.0	_	629,363	201	14

Table 7.2: Testcase B.1 can be solved within 1 minute by all SAT solvers

### 7.2.2 Evaluating simplification

As a next approach, we looked at CNF simplifiers. Those simplifiers consume a CNF file and transform the CNF file to an equisatisfiable CNF file.

### Proposition 7.2

Simplification reduces the problem size (number of variables and clauses).

Consider for example Testcase B.4 in the basic encoding introduced in Section 6.2.1. Then simplification will reduce the problem size down by 57–77 % of its original size (compare with Table 7.3). We verified these data for all simplified files and got similar results. Therefore the proposition holds considering the problem size gets reduced to approximately half of its size.

simplification	variables	/	clauses	(variables left / clauses left)
none	590953	/	107839	(100 % / 100 %)
satelite	457972	/	69670	(77.50 % / 64.61 %)
cmsat	342139	/	61789	(57.90 % / 57.30 %)
lingeling	344544	/	107839	(58.30 % / 100.00 %)
minisat	391134	/	61845	(66.19 % / 57.35 %)

Table 7.3: Problem sizes of Testcase B.4 in the encoding of Section 6.2.1 after simplification

### **Proposition 7.3**

Simplification as preprocessing step does not significantly improve the runtime of SAT solvers.

We look at Testcase B.3 which is a more difficult MD4 problem compared to Testcase B.1. Simplification runtime results depend on the SAT solver, which applies certain simplifications while trying to solve the CNF, and the simplifier used. Table 7.4 lists runtimes depending on the simplification used.

**none** refers to the unsimplified CNF

cmsat refers to simplification applied with Cryptominisat version 5: ./cryptominisat5
 -p1 file.cnf simplified.cnf

lingeling refers to simplification with lingeling version ats1: ./lingeling -s
 file.cnf -o simplified.cnf

minisat also simplifies CNF file with the following command line: ./minisat
 file.cnf -dimacs=simplified.cnf

satelite is specifically designed to simplify CNF files: ./satelite file.cnf
 simplified.cnf

It is worth pointing out that simplification time is not part of the listed runtime. Simplification can take very long. Especially simplifications with lingeling have sometimes taken several hours without result.

In conclusion, simplification leads to a slight improvement of the runtime, but in general we cannot recommend simplifying every CNF file before running it.

solver	version	none	cmsat	lingeling	minisat	satelite
MiniSat	2.2.0	4,519	7,649	_	1,476	1,293
CryptoMiniSat	4.5.3	_	_	_	_	_
	5	1,064	973	_	4,470	3,920
Lingeling	ats1	1,492	906	_	86o	1,297
Treengeling	ats1	1,281	13,401	_	13,790	10,840
plingeling	ats1	2,310	1,232	_	1,384	2,030
Glucose	4.0	_	_	_	_	_
Glucose Syrup	4.0	_	_	_	_	_

TABLE 7.4: Runtimes of Testcase B.3 after CNF files have been simplified

### 7.2.3 Improvements with differential description

Our next goal was to scale up to a more difficult problem. We considered SHA-256 which has a much larger internal state (at least by factor 2). So finding a hash collision is more difficult and we considered further strategies.

### **Proposition 7.4**

A differential description encoding (Section 6.2.2) improves the runtime compared to a missing differential description.

Consider testcase C for MD4 (Appendix B.1) and testcases testcases 18, 21 and 23 (Appendices B.4, B.5 and B.6) for SHA-256. We evaluate the runtimes with or without differential description.

Recall that differential description explicitly encode in the CNF how differences in arithmetic and bitwise operations propagate. We discussed XOR and MAJ in Section 6.2.2.

The data corresponds to even larger testcases, namely a 27-rounds variant we looked at, but did not list. This 27-rounds testcase could not be solved in many cases within our time limit and is therefore excluded from our lists.

In Table 7.5 we randomly picked SAT solvers and we can clearly see a significant improvement of the runtimes.

We continued by trying the influence the guessing strategy.

	CryptoM	1iniSat 5	lingelin	ıg-ats1
testcase	w/o dd	w/ dd	w/o dd	w/ dd
MD <sub>4</sub> , C	1,064	231	798	_
SHA-256, 18	37	37	31	160
SHA-256, 21	_	7,855	28,621	5,513
SHA-256, 23	_	26,212	76,196	1,450

Table 7.5: Runtimes for various testcases with or without differential description with CryptoMiniSat and lingeling

### 7.2.4 Modifying the guessing strategy

### Proposition 7.5

Using phase=-1 improves the runtime of lingeling for our testcases.

Option phase=-1 of lingeling is described as default phase set to -1 (negative), 0 (Jeroslow-Wang strategy [10]) or 1 (positive). Per default a strategy engineered by Jeroslow-Wang [10] is used, but considering Proposition 6.2 at page 46 we expect phase=-1 to provide better runtime results.

Indeed our results consistently indicate a small improvement. This can be recognized in Table 7.6.

testcase	1	8	2	1	23		24	
phase	0	1	0	1	0	1	0	1
runtime	31	22	28,621	19,717	76,196	71,677	85774	70,259

Table 7.6: lingeling-ats1 results for SHA-256 comparing phase=-1 with phase=0

As pointed out in Section 6.2.3, a best practice law of differential cryptanalysis states that difference variables should be assigned first. Afterwards propagation of actual values for the two instances can take place.

To enforce such a strategy, we tried several approaches:

- 1. Armin Biere provided us with a custom release of lingeling which enforces that a special set of variables is evaluated first. It is important that the CNF is still solved with usual SAT solver heuristics, because enforcing assignment of one variable after another leads to an increase in backtracking steps and restarts. Hence, we consider this release as a nice tradeoff. Difference variables are assigned "as early as possible, as late as necessary".
- 2. Given this custom SAT solver we considered a SAT design which requires the SAT solver to prefer a certain. This particular design with a special

Boolean variable is explained in Section 6.2.5.

### 7.3 Related work

In my bachelor thesis [26] we tried to integrate a SAT solver into our department's existing tool which encodes propagation explicitly. This approach was not very successful as restarts between hash algorithm rounds implied that intermediate results by the SAT solver get lost.

Research was already done by Ilya Mironov and Lintao Zhang [19] to apply SAT solvers to differential cryptanalysis specifically to find hash collision in MD4. However whereas their basic approach seems to correspond to our approach described in Section 6.2.1, our implementation uses additional SAT design tweaks to improve our results. Also because 10 years have gone since publication, SAT technology has progressed and modern SAT solvers on modern hardware provide better results.

TODO justify: differential description improves runtime

### 7.4 Conclusion

We successfully found full-round hash collisions for MD4 using SAT solvers mentioned in Section 4.5. We applied tweaks to the lingeling SAT solver to improve our runtime results further and found 24-round hash collisions for SHA-256. Our attack starting points for MD4 — Testcases B.1, B.2 and B.3 — were found by Yusuke Naito, Yu Sasaki, Noboru Kunihiro and Kazuo Ohta [30]. Our starting points for SHA-256 — Testcases B.4, B.5, B.6 and B.7 — were found by Ivica Nikolić and Alex Biryukov [22].

### 7.5 Contributions

To strengthen Reproducible Research, the source code and data resulting from this thesis is available online. It allows the reader to run the experiments again and verify our claims. We did our best to describe our hardware setup as accurately as possible. At the following website, any results part of this project are collected:

http://lukas-prokop.at/proj/megosat/

Several subprojects are part of this master thesis:

### algotocnf

A python library implementing the encoding described in Chapter 6.

Python3 library and program: https://github.com/prokls/algotocnf

### cnf-hash

A standardized way to produce a unique hash for CNF files

**Go implementation:** https://github.com/prokls/cnf-hash-go **Python3 implementation:** https://github.com/prokls/cnf-hash-py

**Testsuite:** https://github.com/prokls/cnf-hash-tests2

### cnf-analysis

Evaluate SAT features for a given CNF file.

**Go implementation:** https://github.com/prokls/cnf-analysis-go **Python3 implementation:** https://github.com/prokls/cnf-analysis-py

**Testsuite:** https://github.com/prokls/cnf-analysis-tests

## **Chapter 8**

# **Summary and Future Work**

### 8.1 Summary of results

In this thesis we looked at

### 8.2 Future work

# Appendices

## Appendix A

# Hardware setup

In the following we introduce two hardware setups which were used to run our testcases. The first setup is referred to as "Thinkpad x220" throughout the document whereas the second setup is referred to as "Cluster".

Type model	Thinkpad Lenovo x220 tablet, 4299-2P6
Processor	Intel i5-2520M, 2.50 GHz, dual-core, Hyperthreaded
RAM	16 GB (extension to common retail setup)
Memory	160 GB SSD
L3 cache size	3072 KB

Table A.1: Thinkpad x220 Tablet specification [15]

Processor	Intel Xeon X5690, 3.47 GHz, 6 cores, Hyperthreaded
RAM	192 GB
L3 cache size	12288 KB

TABLE A.2: Cluster node nehalem192go specification [3]

TODO: other cluster cores

### Appendix B

### **Testcases**

#### B.1 MD4 testcase A

Please compare with Figure B.1.

We can clearly see that all difference variables are defined. Either they are true (bit condition x) or false (bit condition –), but no variable has an undeciable state like? At the top we can see bit conditions 0 and 1 encoding the MD4 initial vector defined by the hash algorithm. The differences x introduce the hash collision and with round 47 being set of – only, the output is forced to be equal between both hash algorithm instances. This testcase is a trivial version of the differential characteristic described in [30].

#### B.2 MD4 testcase B

*Please compare with Figure B.2.* 

In this testcase we have less knowledge about the state than in testcase A because many values are encoded with? meaning that neither their difference nor their actual values are known. However, of course some x exists to introduce a hash collision and the last round only consists of dashes to assert no difference in the output. So unlike testcase A, the SAT solver needs to figure out the difference variables in rounds o-11 increasing its overall runtime in all SAT solver implementations.

### B.3 MD4 testcase C

Please compare with Figure B.3.

This testcases introduces a hash collision which is expected to cancel out at round

32. At the same time no information is provided about the intermediate state of the hash algorithm in rounds 0-20.

#### B.4 SHA-256 testcase 18 rounds

Please compare with Figure B.4.

All SHA-256 testcases got derived from a paper by Ivica Nikolić and Alex Biryukov [22]. Recall that message input of one block only fills Wo to W15. W16 or later are generated based on the previous message words. This differential characteristic depicts a hash collision introduced in round 3. When solving this differential characteristic differences will especially occur in the most-significant bit of words with unspecified difference. Differences cancel out after round 7.

#### B.5 SHA-256 testcase 21 rounds

Please compare with Figure B.5.

Unlike Testcase B.4 word A5 is underspecified with question marks. This certainly makes the problem harder for a SAT solver. At the same time differences of the message words W9 and W10 are specified. This makes the problem easier. At the same time the whole collision covers 21 rounds, unlike Testcase B.4 with 18 rounds.

#### B.6 SHA-256 testcase 23 rounds

Please compare with Figure B.6.

Message word W9 specifies no difference, but the collision is extended to 23 rounds.

#### B.7 SHA-256 testcase 24 rounds

Please compare with Figure B.7.

No measures were taken to simplify the problem for the SAT solver, but the hash collision needs to be found for 24 rounds, which makes the problem hard for the SAT solver because of its increased state size.

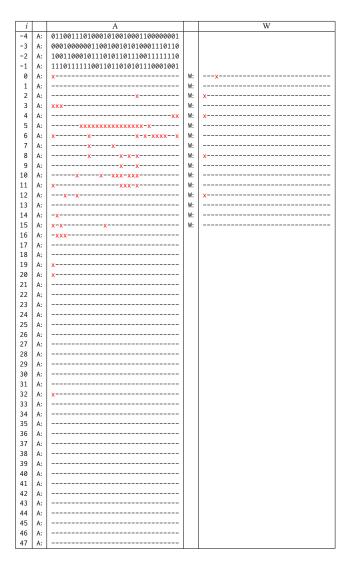


Figure B.1: Differential characteristic of MD4 testcase A

i		A		W
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	1001100010111010110111100111111110		
-1	A:	1110111111100110110101011110001001		
0	A:	???????????????????????????????	W:	x
1	A:	77777777777777777777777777777777	W:	
2	A:	???????????????????????????????	W:	x
3	A:	77777777777777777777777777777777	W:	
4	A:	77777777777777777777777777777777	W:	x
5	A:	77777777777777777777777777777777	W:	
6	A:	777777777777777777777777777777777	W:	
7	A:	77777777777777777777777777777777	W:	
8	A:	77777777777777777777777777777777	W:	¥
9	A:	77777777777777777777777777777777	W:	
10	A:	777777777777777777777777777777777777	W:	
11	A:	77777777777777777777777777777777	W:	
12	A:	????????????	W:	×
13	A:	????????????	W:	
14	A:	?????????????	W:	
15	A:	?????????????	W:	
		???x	۳.	
16	A:	?		
17 18	A:	?		
	A:	[ ·		
19	A:	?		
20	A:	x		
21	A:			
22	A:			
23	A:			
24	A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30	A:			
31	A:			
32	A:	x		
33	A:			
34	A:			
35	A:			
36	A:			
37	A:			
38	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:			
	_		_	l

Figure B.2: Differential characteristic of MD4 testcase B  $\,$ 

i		A		W
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	1001100010111010110111100111111110		
-1	A:	1110111111100110110101011110001001		
0	A:	777777777777777777777777777777777	W:	v
1	A:	7777777777777777777777777777777	W:	
2	A:	77777777777777777777777777777777	W:	¥
3	A:	7777777777777777777777777777777	W:	
4	A:	7777777777777777777777777777777	W:	¥
5	A:	7777777777777777777777777777777	W:	
6	A:	77777777777777777777777777777777	W:	
7	A:	7777777777777777777777777777777	W:	
8	A:	7777777777777777777777777777777	W:	¥
9	A:	7777777777777777777777777777777	W:	
10	A:	7777777777777777777777777777777	W:	
11	A:	7777777777777777777777777777777	W:	
12	A:	7777777777777777777777777777777	W:	x
13	A:	7777777777777777777777777777777	W:	
14	A:	7777777777777777777777777777777	W:	
15	A:	7777777777777777777777777777777	W:	
16	A:	7777777777777777777777777777777		
17	A:	7777777777777777777777777777777		
18	A:	77777777777777777777777777777777		
19	A:	7777777777777777777777777777777		
20	A:	7777777777777777777777777777777		
21	A:			
22	A:			
23	A:			
24	A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30	A:			
31	A:			
32	A:	x		
33	A:			
34	A:			
35	A:			
36	A:			
37	A:			
38	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:			

**Figure B.3:** Differential characteristic of MD<sub>4</sub> testcase C

i		A		Е		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:	x	E:	???????????????????????????????	W:	??????????????????????????????
4	A:		E:	???????????????????????????????	W:	??????????????????????????????
5	A:		E:	???????????????????????????????	W:	??????????????????????????????
6	A:		E:	???????????????????????????????	W:	??????????????????????????????
7	A:		E:	???????????????????????????????	W:	??????????????????????????????
8	A:		E:		W:	??????????????????????????????
9	A:		E:		W:	
10	A:		E:		W:	
11	A:		E:		W:	???????????????????????????????
12	A:		E:		W:	
13	A:		E:		W:	
14	A:		E:		W:	
15	A:		E:		W:	
16	A:		E:		W:	
17	A:		E:		W:	

Figure B.4: SHA256 hash collision over 18 rounds

i		A		E		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:	x???????????????????????????????	E:	???????????????????????????????	W:	??????????????????????????????
6	A:		E:	???????????????????????????????	W:	??????????????????????????????
7	A:		E:	???????????????????????????????	W:	??????????????????????????????
8	A:		E:	???????????????????????????????	W:	??????????????????????????????
9	A:		E:	???????????????????????????????	W:	
10	A:		E:		W:	
11	A:		E:		W:	
12	A:		E:		W:	
13	A:		E:		W:	??????????????????????????????
14	A:		E:		W:	
15	A:		E:		W:	
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	

**Figure B.5:** SHA-256 hash collision over 21 rounds

i		A		E		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:		E:		W:	
6	A:		E:		W:	
7	A:	x??????????????????????????????	E:	???????????????????????????????	W:	??????????????????????????????
8	A:		E:	???????????????????????????????	W:	??????????????????????????????
9	A:		E:	???????????????????????????????	W:	
10	A:		E:	???????????????????????????????	W:	??????????????????????????????
11	A:		E:	???????????????????????????????	W:	
12	A:		E:		W:	
13	A:		E:		W:	
14	A:		E:		W:	
15	A:		E:		W:	??????????????????????????????
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	
21	A:		E:		W:	
22	A:		E:		W:	

Figure B.6: SHA-256 hash collision over 23 rounds

-				l r		W
1		A		E		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:		E:		W:	
6	A:		E:		W:	
7	A:	x??????????????????????????????	E:	???????????????????????????????	W:	??????????????????????????????
8	A:		E:	???????????????????????????????	W:	???????????????????????????????
9	A:		E:	???????????????????????????????	W:	
10	A:		E:	???????????????????????????????	W:	??????????????????????????????
11	A:		E:	???????????????????????????????	W:	
12	A:		E:		W:	
13	A:		E:		W:	
14	A:		E:		W:	
15	A:		E:		W:	??????????????????????????????
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	
21	A:		E:		W:	
22	A:		E:		W:	
23	A:		E:		W:	
23	A:		E:		W:	

**Figure B.7:** SHA-256 hash collision over 24 rounds

### **Appendix C**

### Runtimes retrieved

#### TODO

FAILED means unexpected exit code or missing results. TIMEOUT mean did not terminate within 1 day. SUCCESS means SAT within 1 day.

```
Results cover 50 CNFs

cmsat5 83 occurences

minisat 169 occurences

lingeling-ats1o4 267 occurences

minisat-core 85 occurences

glucose-syrup 84 occurences

lingeling-ats1o1 145 occurences

treengeling-ats1o1 84 occurences

lingeling-ats1o2 250 occurences

plingeling-ats1o1 85 occurences

cmsat4 84 occurences

glucose 84 occurences

FAILED=303 TIMEOUT=722 SUCCESS=1395
```

cmsat4         algotocnf_1.cnf         none         no         48704 / 253984           cmsat4         algotocnf_1.cnf         cmsat         no         24503 / 111931           cmsat4         algotocnf_1.cnf         minisat         no         22695 / 118236           cmsat4         algotocnf_1.enf         satelite         no         27495 / 153262           cmsat4         algotocnf_1.end         none         no         107839 / 590953         140000           cmsat4         algotocnf_1.end         cmsat         no         61786 / 321193         o           cmsat4         algotocnf_1.end         cmsat         no         61786 / 391134         120000           cmsat4         algotocnf_1.end         satelite         no         69670 / 457972         o           cmsat4         algotocnf_1.end         satelite         no         69670 / 457972         o           cmsat4         algotocnf_1.ender.end         none         no         107839 / 40466         o           cmsat4         algotocnf_1.ender.end         minisat         no         57114 / 30348         120000           cmsat4         algotocnf_2.endif-desc.enf         minisat         no         78055 / 511431         o           cmsat4 <th>SAT solver</th> <th>CNF file</th> <th>simplified</th> <th>phase</th> <th>vars/clauses</th> <th>propagation</th>	SAT solver	CNF file	simplified	phase	vars/clauses	propagation
cmsat4         algotocnf_1.cnf         minisat         no         20895 / 118236           cmsat4         algotocnf_1.cnf         satelite         no         27495 / 153262           cmsat4         algotocnf_18-to.cnf         none         no         107839 / 590953         140000           cmsat4         algotocnf_18-to.cnf         cmsat         no         61789 / 342139         o           cmsat4         algotocnf_18-to.cnf         lingeling         no         107839 / 344544         90000           cmsat4         algotocnf_18-to.cnf         satelite         no         69670 / 457972         o           cmsat4         algotocnf_18-to_diff-desc.cnf         none         no         57114 / 39348         120000           cmsat4         algotocnf_18-to_diff-desc.cnf         cmsat         no         57114 / 39348         120000           cmsat4         algotocnf_18-to_diff-desc.cnf         cmsat         no         78055 / 511431         o           cmsat4         algotocnf_18-to_diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_1-diff-desc.cnf         cmsat         no         15402 / 37342         520000           cmsat4         algotocnf_1-diff-desc.cnf         cmsat </td <td>cmsat4</td> <td>algotocnf_1.cnf</td> <td>none</td> <td>no</td> <td>48704 / 253984</td> <td></td>	cmsat4	algotocnf_1.cnf	none	no	48704 / 253984	
cmsat4         algotocnf_1.cnf         satelite         no         27495 / 153262           cmsat4         algotocnf_1.end         none         no         107839 / 590953         140000           cmsat4         algotocnf_1.end         cmsat         no         61789 / 342139         o           cmsat4         algotocnf_1.end         cmsat         no         61789 / 342139         o           cmsat4         algotocnf_1.end         lingeling         no         107839 / 344544         90000           cmsat4         algotocnf_1.end         satelite         no         69670 / 457972         o           cmsat4         algotocnf_1.end         desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_1.end         desc.cnf         cmsat         none         no         57114 / 393489         120000           cmsat4         algotocnf_1.end         desc.cnf         mone         none         107839 / 846487         140000           cmsat4         algotocnf_1.end         desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_1.end         desc.cnf         satelite         no         85386 / 692408         140000	cmsat4	algotocnf_1.cnf	cmsat	no	24503 / 111931	
cmsat4         algotocnf_18-to.cnf         none         no         107839 / 590953         140000           cmsat4         algotocnf_18-to.cnf         cmsat         no         61789 / 342139         0           cmsat4         algotocnf_18-to.cnf         lingeling         no         107839 / 344544         90000           cmsat4         algotocnf_18-to.cnf         minisat         no         61845 / 391134         120000           cmsat4         algotocnf_18-to.cnf         satelite         no         69670 / 457972         o           cmsat4         algotocnf_18-to.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-to.diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-to.diff-desc.cnf         lingeling         no         107839 / 404666         o           cmsat4         algotocnf_18-to.diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_1.diff-desc.cnf         minisat         no         85386 / 692408         140000           cmsat4         algotocnf_1.diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4	cmsat4	algotocnf_1.cnf	minisat	no	20895 / 118236	
cmsat4         algotocnf_18-t9.cnf         cmsat         no         61789 / 342139         o           cmsat4         algotocnf_18-t9.cnf         lingeling         no         107839 / 344544         90000           cmsat4         algotocnf_18-t9.cnf         satelite         no         61845 / 391134         120000           cmsat4         algotocnf_18-t9.cnf         satelite         no         69670 / 457972         o           cmsat4         algotocnf_18-t9.diff-desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-t9.diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-t9.diff-desc.cnf         cmsat         no         78055 / 511431         o           cmsat4         algotocnf_18-t9.diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_18-t9.diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_1.diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1.diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat	cmsat4	algotocnf_1.cnf	satelite	no	27495 / 153262	
cmsat4         algotocnf_18-t9.cnf         lingeling         no         107839 / 344544         90000           cmsat4         algotocnf_18-t9.cnf         minisat         no         61845 / 391134         120000           cmsat4         algotocnf_18-t9.cnf         satelite         no         69670 / 457972         0           cmsat4         algotocnf_18-t9.diff-desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-t9.diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-t9.diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_18-t9.diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_18-t9.diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_1.diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1.diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_2.diff-desc.cnf         minisat         no         25107 / 158393         800000	cmsat4	algotocnf_18-t9.cnf	none	no	107839 / 590953	140000
cmsat4         algotocnf_18-to.cnf         minisat         no         61845 / 391134         120000           cmsat4         algotocnf_18-to.cnf         satelite         no         69670 / 457972         0           cmsat4         algotocnf_18-to.cnf         satelite         no         69670 / 457972         0           cmsat4         algotocnf_18-to.diff-desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-to.diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-to.diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-to.diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_1-diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_1-diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1-diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1-diff-desc.cnf         minisat         no         25107 / 154393         80000 <th< td=""><td>cmsat4</td><td>algotocnf_18-t9.cnf</td><td>cmsat</td><td>no</td><td>61789 / 342139</td><td>0</td></th<>	cmsat4	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	0
cmsat4         algotocnf_18-t9_diff-desc.cnf         satelite         no         69670 / 457972         0           cmsat4         algotocnf_18-t9_diff-desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-t9_diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-t9_diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-t9_diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_18-t9_diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_1_diff-desc.cnf         mone         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2_cmf         minisat         no         25107 / 158393         800000	cmsat4	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544	90000
cmsat4         algotocnf_18-to_diff-desc.cnf         none         no         107839 / 846487         140000           cmsat4         algotocnf_18-to_diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-to_diff-desc.cnf         lingeling         no         107839 / 404666         o           cmsat4         algotocnf_18-to_diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_18-to_diff-desc.cnf         satelite         no         85386 / 692408         140000           cmsat4         algotocnf_18-to_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1 diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1 diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_2 diff-desc.cnf         minisat         no         15402 / 73142         520000           cmsat4         algotocnf_2 diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2 cnf         satelite         no         30950 / 226602         780000	cmsat4	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	120000
cmsat4         algotocnf_18-t9_diff-desc.cnf         cmsat         no         57114 / 303489         120000           cmsat4         algotocnf_18-t9_diff-desc.cnf         lingeling         no         107839 / 404666         o           cmsat4         algotocnf_18-t9_diff-desc.cnf         minisat         no         78055 / 511431         o           cmsat4         algotocnf_18-t9_diff-desc.cnf         satelite         no         85386 / 692408         140000           cmsat4         algotocnf_18-t9_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         cmsat         no         48704 / 254210         10           cmsat4         algotocnf_2.cnf         minisat         no         24323 / 111661         11660 <td< td=""><td>cmsat4</td><td>algotocnf_18-t9.cnf</td><td>satelite</td><td>no</td><td>69670 / 457972</td><td>0</td></td<>	cmsat4	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	0
cmsat4         algotocnf_18-t9_diff-desc.cnf         lingeling         no         107839 / 404666         0           cmsat4         algotocnf_18-t9_diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_18-t9_diff-desc.cnf         satelite         no         85386 / 692408         140000           cmsat4         algotocnf_1_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2_cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_2_cnf         cmsat         no         2430 / 111661         11660           cmsat4         algotocnf_2_cnf         cmsat         no         24323 / 111661         11660           c	cmsat4	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 846487	140000
cmsat4         algotocnf_18-t9_diff-desc.cnf         minisat         no         78055 / 511431         0           cmsat4         algotocnf_18-t9_diff-desc.cnf         satelite         no         85386 / 692408         140000           cmsat4         algotocnf_1_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2_cnf         mone         no         48704 / 254210         780000           cmsat4         algotocnf_2_cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2_cnf         minisat         no         20895 / 18688         780000           cmsat4         algotocnf_2_cnf         satelite         no         277775 / 154276         780000           cmsat4 <td>cmsat4</td> <td>algotocnf_18-t9_diff-desc.cnf</td> <td>cmsat</td> <td>no</td> <td>57114 / 303489</td> <td>120000</td>	cmsat4	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	120000
cmsat4         algotocnf_18-t9_diff-desc.cnf         satelite         no         85386 / 692408         140000           cmsat4         algotocnf_1_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2.cnf         minisat         no         249323 / 118688         780000           cmsat4         algotocnf_2.cnf         satelite         no         277775 / 154276         780000           cmsat4         algotocnf_21-t9.cnf         none         no         116800 / 636838         780000           cmsat4	cmsat4	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	0
cmsat4         algotocnf_1_diff-desc.cnf         none         no         48704 / 373920         860000           cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688         780000           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276         780000           cmsat4         algotocnf_2.tncnf         cmsat         no         63555 / 358308         780000         780000         780000         780000	cmsat4	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	0
cmsat4         algotocnf_1_diff-desc.cnf         cmsat         no         15402 / 73142         520000           cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2.cnf         cmsat         no         20895 / 118688         780000           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276         780000           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276         780000           cmsat4         algotocnf_2.cnf         cmsat         no         63555 / 358308         78000           cmsat4         algotocnf_2.tof         cmsat         no         65572 / 414470         78000           cmsat4         algotocnf_2.tof	cmsat4	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	140000
cmsat4         algotocnf_1_diff-desc.cnf         lingeling         no         48704 / 101182         530000           cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         780000           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688         780000           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276         780000           cmsat4         algotocnf_2.cnf         none         no         116800 / 636838         780000           cmsat4         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308         780000           cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470         780000           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714         774562 / 486714         774562 / 486714         7745602 / 48671	cmsat4	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	860000
cmsat4         algotocnf_1_diff-desc.cnf         minisat         no         25107 / 158393         800000           cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         none         no         24323 / 111661         24323 / 111661           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276           cmsat4         algotocnf_2.tng.cnf         none         no         116800 / 636838           cmsat4         algotocnf_21-tg.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_21-tg.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-tg.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-tg.diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-tg.diff-desc.cnf         cmsat         no         59528 / 318049         1510000	cmsat4	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	520000
cmsat4         algotocnf_1_diff-desc.cnf         satelite         no         30950 / 226602         780000           cmsat4         algotocnf_2.cnf         none         no         48704 / 254210         780000           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661         24323 / 111661           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 18688         227775 / 154276           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276         22775 / 154276           cmsat4         algotocnf_2.cnf         none         no         116800 / 636838         38           cmsat4         algotocnf_2.cnf         cmsat         no         63555 / 358308         38           cmsat4         algotocnf_2.cnf         minisat         no         65572 / 414470         38           cmsat4         algotocnf_2.l-ty.cnf         satelite         no         74562 / 486714         38           cmsat4         algotocnf_2.l-ty.diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_2.l-ty.diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotoc	cmsat4	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	530000
cmsat4         algotocnf_2.cnf         none         no         48704 / 254210           cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276           cmsat4         algotocnf_21-t9.cnf         none         no         116800 / 636838           cmsat4         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9.diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         a	cmsat4	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	800000
cmsat4         algotocnf_2.cnf         cmsat         no         24323 / 111661           cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276           cmsat4         algotocnf_2.1-t9.cnf         none         no         116800 / 636838           cmsat4         algotocnf_2.1-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_2.1-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_2.1-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         none         no         122774 / 667438 <th< td=""><td>cmsat4</td><td>algotocnf_1_diff-desc.cnf</td><td>satelite</td><td>no</td><td>30950 / 226602</td><td>780000</td></th<>	cmsat4	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	780000
cmsat4         algotocnf_2.cnf         minisat         no         20895 / 118688           cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276           cmsat4         algotocnf_2.1-t9.cnf         none         no         116800 / 636838           cmsat4         algotocnf_2.1-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_2.1-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_2.1-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_2.1-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_2.3-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_2.3-t9.cnf         cmsat         no         64880 / 369775           cmsat4	cmsat4	algotocnf_2.cnf	none	no	48704 / 254210	
cmsat4         algotocnf_2.cnf         satelite         no         27775 / 154276           cmsat4         algotocnf_21-t9.cnf         none         no         116800 / 636838           cmsat4         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775     <	cmsat4	algotocnf_2.cnf	cmsat	no	24323 / 111661	
cmsat4         algotocnf_21-t9.cnf         none         no         116800 / 636838           cmsat4         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	_	minisat	no	20895 / 118688	
cmsat4         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308           cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	_	satelite	no	27775 / 154276	
cmsat4         algotocnf_21-t9.cnf         minisat         no         65572 / 414470           cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	algotocnf_21-t9.cnf	none	no	116800 / 636838	
cmsat4         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4		cmsat	no	63555 / 358308	
cmsat4         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629         1540000           cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	
cmsat4         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049         1510000           cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	
cmsat4         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126         1290000           cmsat4         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965         1560000           cmsat4         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755         1540000           cmsat4         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4		none	no	116800 / 911629	1540000
cmsat4       algotocnf_21-t9_diff-desc.cnf       minisat       no       81650 / 534965       1560000         cmsat4       algotocnf_21-t9_diff-desc.cnf       satelite       no       90236 / 720755       1540000         cmsat4       algotocnf_23-t9.cnf       none       no       122774 / 667438         cmsat4       algotocnf_23-t9.cnf       cmsat       no       64880 / 369775         cmsat4       algotocnf_23-t9.cnf       minisat       no       67979 / 429734	cmsat4			no	59528 / 318049	1510000
cmsat4       algotocnf_21-t9_diff-desc.cnf       satelite       no       90236 / 720755       1540000         cmsat4       algotocnf_23-t9.cnf       none       no       122774 / 667438         cmsat4       algotocnf_23-t9.cnf       cmsat       no       64880 / 369775         cmsat4       algotocnf_23-t9.cnf       minisat       no       67979 / 429734	cmsat4			no	116800 / 404126	1290000
cmsat4       algotocnf_23-t9.cnf       none       no       122774 / 667438         cmsat4       algotocnf_23-t9.cnf       cmsat       no       64880 / 369775         cmsat4       algotocnf_23-t9.cnf       minisat       no       67979 / 429734	cmsat4			no	81650 / 534965	1560000
cmsat4         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat4         algotocnf_23-t9.cnf         minisat         no         67979 / 429734	cmsat4	=	satelite	no	90236 / 720755	1540000
cmsat4 algotocnf_23-t9.cnf minisat no 67979 / 429734	cmsat4		none	no	122774 / 667438	
	cmsat4		cmsat	no	64880 / 369775	
cmsat4 algotocnf_23-t9.cnf satelite no 77835 / 506217	cmsat4			no	67979 / 429734	
	cmsat <sub>4</sub>	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	

SAT solver	CNF file	simplified	phase	vars/clauses	propagati
cmsat <sub>4</sub>	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	1 1 0
cmsat4	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	
cmsat4	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	
cmsat4	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	
cmsat4	algotocnf_24-t9.cnf	none	no	125761 / 682722	
cmsat4	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	
cmsat4	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	
cmsat4	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	
cmsat4	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770	
cmsat4	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	
cmsat4	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	
cmsat4	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	
cmsat4	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349	0
cmsat4	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	o
cmsat4	algotocnf_27-t10-diff.cnf	lingeling	no	134722 / 0	o
cmsat4	algotocnf_27-t10-diff.cnf	minisat	no	o / o	o
cmsat4	algotocnf_27-t10-diff.cnf	satelite	no	o / o	O
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	0
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722 / o	O
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	o
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	O
cmsat4	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542	
cmsat4	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	
cmsat4	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	
cmsat4	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589	
cmsat4	algotocnf_27-t10.cnf	none	no	134722 / 728030	
cmsat4	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
cmsat4	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
cmsat4	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
cmsat4	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335	
cmsat4	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	

SAT solver	CNF file	simplified	phase	vars/clauses	propagati
cmsat <sub>4</sub>	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	
cmsat4	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
cmsat4	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146	950000
cmsat4	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	550000
cmsat4	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546	490000
cmsat4	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	720000
cmsat4	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	700000
cmsat4	algotocnf_3.cnf	none	no	48704 / 254656	70000
cmsat4	algotocnf_3.cnf	cmsat	no	23893 / 111403	70000
cmsat4	algotocnf_3.cnf	lingeling	no	48704 / 100941	0
cmsat4	algotocnf_3.cnf	minisat	no	20895 / 119580	60000
cmsat4	algotocnf_3.cnf	satelite	no	28647 / 156910	60000
cmsat4	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	0
cmsat5	algotocnf_1.cnf	none	no	48704 / 253984	
cmsat5	algotocnf_1.cnf	cmsat	no	24503 / 111931	
cmsat5	algotocnf_1.cnf	minisat	no	20895 / 118236	
cmsat5	algotocnf_1.cnf	satelite	no	27495 / 153262	
cmsat5	algotocnf_18-t9.cnf	none	no	107839 / 590953	
cmsat5	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	
cmsat5	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544	
cmsat5	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	
cmsat5	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	
cmsat5	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 846487	
cmsat5	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	
cmsat5	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	
cmsat5	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	
cmsat5	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	
cmsat5	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	
cmsat5	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	
cmsat5	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	
cmsat5	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	
cmsat5	algotocnf_2.cnf	none	no	48704 / 254210	
cmsat <sub>5</sub>	algotocnf_2.cnf	cmsat	no	24323 / 111661	
cmsat <sub>5</sub>	algotocnf_2.cnf	minisat	no	20895 / 118688	
cmsat5	algotocnf_2.cnf	satelite	no	27775 / 154276	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	d
cmsat5	algotocnf_21-t9.cnf	none	no	116800 / 636838	propagations	
cmsat5	algotocnf 21-t9.cnf	cmsat	no	63555 / 358308		
cmsat5	algotocnf 21-t9.cnf	minisat	no	65572 / 414470		
cmsat5	algotocnf_21-t9.cnf	satelite	no	74562 / 486714		
cmsat5	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629		_
cmsat5	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049		4
cmsat5	algotocnf_21-t9_diff-desc.cnf	lingeling		116800 / 404126		4
-	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965		4
cmsat5		satelite	no			1
cmsat5	algotocnf_21-t9_diff-desc.cnf		no	90236 / 720755		
cmsat5	algotocnf_23-t9.cnf	none	no	122774 / 667438		
cmsat5	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775		
cmsat5	algotocnf_23-t9.cnf	minisat	no	67979 / 429734		
cmsat5	algotocnf_23-t9.cnf	satelite	no	77835 / 506217		
cmsat5	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067		3
cmsat5	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118		5
cmsat5	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727		4
cmsat5	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545		2
cmsat5	algotocnf_24-t9.cnf	none	no	125761 / 682722		
cmsat5	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228		
cmsat5	algotocnf_24-t9.cnf	minisat	no	69023 / 436292		
cmsat5	algotocnf_24-t9.cnf	satelite	no	79486 / 515977		
cmsat5	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770		5
cmsat5	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014		7
cmsat5	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731		4
cmsat5	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557		3
cmsat5	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349		
cmsat5	algotocnf_27-t10-diff.cnf	cmsat	no	o / o		
cmsat5	algotocnf_27-t10-diff.cnf	lingeling	no	134722 / o		
cmsat5	algotocnf_27-t10-diff.cnf	minisat	no	o / o		
cmsat5	algotocnf_27-t10-diff.cnf	satelite	no	o / o		
cmsat <sub>5</sub>	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o		
cmsat5	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722 / 0		
cmsat5	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o		
cmsat5	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o		
cmsat <sub>5</sub>	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542		

SAT solver	CNF file	simplified	phase	vars/clauses
cmsat <sub>5</sub>	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680
cmsat5	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404
cmsat5	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998
cmsat5	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847
cmsat5	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443
cmsat5	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309
cmsat5	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589
cmsat5	algotocnf_27-t10.cnf	none	no	134722 / 728030
cmsat5	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276
cmsat5	algotocnf_27-t10.cnf	minisat	no	73897 / 465248
cmsat5	algotocnf_27-t10.cnf	satelite	no	85274 / 549734
cmsat5	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335
cmsat5	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219
cmsat5	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480
cmsat5	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675
cmsat5	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146
cmsat5	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870
cmsat5	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546
cmsat5	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436
cmsat5	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577
cmsat5	algotocnf_3.cnf	none	no	48704 / 254656
cmsat5	algotocnf_3.cnf	cmsat	no	23893 / 111403
cmsat5	algotocnf_3.cnf	lingeling	no	48704 / 100941
cmsat5	algotocnf_3.cnf	minisat	no	20895 / 119580
cmsat5	algotocnf_3.cnf	satelite	no	28647 / 156910
cmsat5	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592
glucose	algotocnf_1.cnf	none	no	48704 / 225124
glucose	algotocnf_1.cnf	cmsat	no	24503 / 111931
glucose	algotocnf_1.cnf	minisat	no	20895 / 118236
glucose	algotocnf_1.cnf	satelite	no	27495 / 153262
glucose	algotocnf_18-t9.cnf	none	no	107839 / 582936
glucose	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139
glucose	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544
glucose	algotocnf_18-t9.cnf	minisat	no	61845 / 391134
glucose	algotocnf_18-t9.cnf	satelite	no	69670 / 457972

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	decisi
glucose	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	10471476	6444
glucose	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	20143829	12469
glucose	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	7239871	7647
glucose	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	15403560	9340
glucose	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	30131933	15390
glucose	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	1231386505	47264
glucose	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	1038552689	32670
glucose	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	1251948097	59378
glucose	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	785694216	29540
glucose	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	751454677	28310
glucose	algotocnf_2.cnf	none	no	48704 / 224220		
glucose	algotocnf_2.cnf	cmsat	no	24323 / 111661		
glucose	algotocnf_2.cnf	minisat	no	20895 / 118688		
glucose	algotocnf_2.cnf	satelite	no	27775 / 154276		
glucose	algotocnf_21-t9.cnf	none	no	116800 / 627112		
glucose	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308		
glucose	algotocnf_21-t9.cnf	minisat	no	65572 / 414470		
glucose	algotocnf_21-t9.cnf	satelite	no	74562 / 486714		
glucose	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072		
glucose	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	2790904343	82667
glucose	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	1838242760	74906
glucose	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	3062139546	87991
glucose	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	3468599865	98765.
glucose	algotocnf_23-t9.cnf	none	no	122774 / 656628		
glucose	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775		
glucose	algotocnf_23-t9.cnf	minisat	no	67979 / 429734		
glucose	algotocnf_23-t9.cnf	satelite	no	77835 / 506217		
glucose	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 936270		
glucose	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118		
glucose	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727		
glucose	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545		
glucose	algotocnf_24-t9.cnf	none	no	125761 / 671432		
glucose	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228		
glucose	algotocnf_24-t9.cnf	minisat	no	69023 / 436292		
glucose	algotocnf_24-t9.cnf	satelite	no	79486 / 515977		

SAT solver	CNF file	simplified	phase	vars/clauses
glucose	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 957493
glucose	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014
glucose	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731
glucose	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557
glucose	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320
glucose	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
glucose	algotocnf_27-t10-diff.cnf	lingeling	no	o / o
glucose	algotocnf_27-t10-diff.cnf	minisat	no	o / o
glucose	algotocnf_27-t10-diff.cnf	satelite	no	o / o
glucose	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
glucose	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
glucose	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
glucose	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
glucose	algotocnf_27-t10-simplified.cnf	none	no	134722 / 715830
glucose	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680
glucose	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404
glucose	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1020826
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589
glucose	algotocnf_27-t10.cnf	none	no	134722 / 717878
glucose	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276
glucose	algotocnf_27-t10.cnf	minisat	no	73897 / 465248
glucose	algotocnf_27-t10.cnf	satelite	no	85274 / 549734
glucose	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1022874
glucose	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219
glucose	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480
glucose	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675
glucose	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788
glucose	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870
glucose	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546
glucose	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436
glucose	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577
glucose	algotocnf_3.cnf	none	no	48704 / 222436

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	deci
glucose	algotocnf_3.cnf	cmsat	no	23893 / 111403	23157475	127
glucose	algotocnf_3.cnf	lingeling	no	44000 / 100941	9187396	73
glucose	algotocnf_3.cnf	minisat	no	20895 / 119580	16616478	104
glucose	algotocnf_3.cnf	satelite	no	28647 / 156910	15878157	100
glucose	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	9899755	53
glucose-syrup	algotocnf_1.cnf	none	no	48704 / 225124		1739
glucose-syrup	algotocnf_1.cnf	cmsat	no	24503 / 111931		1289
glucose-syrup	algotocnf_1.cnf	minisat	no	20895 / 118236		1306
glucose-syrup	algotocnf_1.cnf	satelite	no	27495 / 153262		1303
glucose-syrup	algotocnf_18-t9.cnf	none	no	107839 / 582936		629
glucose-syrup	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139		645
glucose-syrup	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544		49'
glucose-syrup	algotocnf_18-t9.cnf	minisat	no	61845 / 391134		72
glucose-syrup	algotocnf_18-t9.cnf	satelite	no	69670 / 457972		680
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263		74
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489		201
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666		48
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431		534
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408		59'
glucose-syrup	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692		281
glucose-syrup	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142		856
glucose-syrup	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182		120
glucose-syrup	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393		764
glucose-syrup	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602		133
glucose-syrup	algotocnf_2.cnf	none	no	48704 / 224220		1743
glucose-syrup	algotocnf_2.cnf	cmsat	no	24323 / 111661		1497
glucose-syrup	algotocnf_2.cnf	minisat	no	20895 / 118688		1414
glucose-syrup	algotocnf_2.cnf	satelite	no	27775 / 154276		1717
glucose-syrup	algotocnf_21-t9.cnf	none	no	116800 / 627112		822
glucose-syrup	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308		872
glucose-syrup	algotocnf_21-t9.cnf	minisat	no	65572 / 414470		788
glucose-syrup	algotocnf_21-t9.cnf	satelite	no	74562 / 486714		806
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072		485
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049		246
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126		305

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SAT solver	CNF file	simplified	phase	vars/clauses
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755
glucose-syrup	algotocnf_23-t9.cnf	none	no	122774 / 656628
glucose-syrup	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775
glucose-syrup	algotocnf_23-t9.cnf	minisat	no	67979 / 429734
glucose-syrup	algotocnf_23-t9.cnf	satelite	no	77835 / 506217
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 936270
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545
glucose-syrup	algotocnf_24-t9.cnf	none	no	125761 / 671432
glucose-syrup	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228
glucose-syrup	algotocnf_24-t9.cnf	minisat	no	69023 / 436292
glucose-syrup	algotocnf_24-t9.cnf	satelite	no	79486 / 515977
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 957493
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557
glucose-syrup	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320
glucose-syrup	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
glucose-syrup	algotocnf_27-t10-diff.cnf	lingeling	no	o / o
glucose-syrup	algotocnf_27-t10-diff.cnf	minisat	no	o / o
glucose-syrup	algotocnf_27-t10-diff.cnf	satelite	no	o / o
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
glucose-syrup	algotocnf_27-t10-simplified.cnf	none	no	134722 / 715830
glucose-syrup	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680
glucose-syrup	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404
glucose-syrup	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1020826
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589
glucose-syrup	algotocnf_24-t9.cnf algotocnf_24-t9.cnf algotocnf_24-t9.cnf algotocnf_24-t9_diff-desc.cnf algotocnf_24-t9_diff-desc.cnf algotocnf_24-t9_diff-desc.cnf algotocnf_24-t9_diff-desc.cnf algotocnf_24-t9_diff-desc.cnf algotocnf_27-t10-diff.cnf algotocnf_27-t10-diff.cnf algotocnf_27-t10-diff.cnf algotocnf_27-t10-diff.cnf algotocnf_27-t10-diff.cnf algotocnf_27-t10-diff_diff-desc.cnf algotocnf_27-t10-diff_diff-desc.cnf algotocnf_27-t10-diff_diff-desc.cnf algotocnf_27-t10-diff_diff-desc.cnf algotocnf_27-t10-simplified.cnf algotocnf_27-t10-simplified.cnf algotocnf_27-t10-simplified_cnf algotocnf_27-t10-simplified_diff-desc.cnf algotocnf_27-t10-simplified_diff-desc.cnf algotocnf_27-t10-simplified_diff-desc.cnf algotocnf_27-t10-simplified_diff-desc.cnf algotocnf_27-t10-simplified_diff-desc.cnf	cmsat minisat satelite none cmsat minisat satelite none cmsat lingeling minisat satelite cmsat lingeling minisat satelite cmsat lingeling minisat satelite none cmsat minisat satelite none cmsat minisat satelite none cmsat minisat	no n	65579 / 37722 69023 / 43629 79486 / 51597 125761 / 95749 56447 / 30201 85312 / 55873 95154 / 75055 134722 / 8320 0 / 0 0 / 0 0 / 0 0 / 0 0 / 0 0 / 0 0 / 0 134722 / 71583 67175 / 39268 72909 / 46040 84442 / 54499 134722 / 10208 56223 / 30244 89667 / 58630

SAT solver	CNF file	simplified	phase	vars/clauses	propagations
glucose-syrup	algotocnf_27-t10.cnf	none	no	134722 / 717878	
glucose-syrup	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
glucose-syrup	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
glucose-syrup	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1022874	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
glucose-syrup	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	
glucose-syrup	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	
glucose-syrup	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	
glucose-syrup	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	
glucose-syrup	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	
glucose-syrup	algotocnf_3.cnf	none	no	48704 / 222436	
glucose-syrup	algotocnf_3.cnf	cmsat	no	23893 / 111403	
glucose-syrup	algotocnf_3.cnf	lingeling	no	44000 / 100941	
glucose-syrup	algotocnf_3.cnf	minisat	no	20895 / 119580	
glucose-syrup	algotocnf_3.cnf	satelite	no	28647 / 156910	
glucose-syrup	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	
lingeling-ats101	algotocnf_1.cnf	cmsat	no	24503 / 111931	830112341
lingeling-ats101	algotocnf_1.cnf	cmsat	yes	24503 / 111931	820517590
lingeling-ats101	algotocnf_1.cnf	minisat	no	20895 / 118236	575783290
lingeling-ats101	algotocnf_1.cnf	minisat	yes	20895 / 118236	333100908
lingeling-ats101	algotocnf_1.cnf	satelite	no	27495 / 153262	855959855
lingeling-ats101	algotocnf_1.cnf	satelite	yes	27495 / 153262	455268862
lingeling-ats101	algotocnf_18-t9.cnf	none	no	107839 / 590953	6579999
lingeling-ats101	algotocnf_18-t9.cnf	none	yes	107839 / 590953	6637382
lingeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	19838315
lingeling-ats101	algotocnf_18-t9.cnf	cmsat	yes	61789 / 342139	20128556
lingeling-ats101	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	4891154
lingeling-ats101	algotocnf_18-t9.cnf	lingeling	yes	102616 / 344544	3026807
lingeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	6037622
lingeling-ats101	algotocnf_18-t9.cnf	minisat	yes	61845 / 391134	8386925
lingeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	4521332
lingeling-ats101	algotocnf_18-t9.cnf	satelite	yes	69670 / 457972	6584687

SAT solver	CNF file	simplified	phase	vars/clauses
lingeling-ats101	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	no	196473 / 1197423
lingeling-ats101	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	yes	196473 / 1197423
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	none	yes	107839 / 846487
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	yes	57114 / 303489
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	yes	99452 / 404666
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	yes	78055 / 511431
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	yes	85386 / 692408
lingeling-ats101	algotocnf_18-t9_diff-desc_ocnf.cnf	none	no	107839 / 846487
lingeling-ats101	algotocnf_18-t9_diff-desc_ocnf.cnf	none	yes	107839 / 846487
lingeling-ats101	algotocnf_18-t9_ocnf.cnf	none	no	107839 / 590953
lingeling-ats101	algotocnf_18-t9_ocnf.cnf	none	yes	107839 / 590953
lingeling-ats101	algotocnf_1_diff-desc-sc_ocnf.cnf	none	no	85760 / 522144
lingeling-ats101	algotocnf_1_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522144
lingeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920
lingeling-ats101	algotocnf_1_diff-desc.cnf	none	yes	48704 / 373920
lingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142
lingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	yes	15402 / 73142
lingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182
lingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	yes	40554 / 101182
lingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393
lingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	yes	25107 / 158393
lingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602
lingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	yes	30950 / 226602
lingeling-ats101	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920
lingeling-ats101	algotocnf_1_diff-desc_ocnf.cnf	none	yes	48704 / 373920
lingeling-ats101	algotocnf_1_ocnf.cnf	none	no	48704 / 253984
lingeling-ats101	algotocnf_1_ocnf.cnf	none	yes	48704 / 253984
lingeling-ats101	algotocnf_2.cnf	none	no	48704 / 254210
lingeling-ats101	algotocnf_2.cnf	none	yes	48704 / 254210
lingeling-ats101	algotocnf_2.cnf	cmsat	no	24323 / 111661
lingeling-ats101	algotocnf_2.cnf	cmsat	yes	24323 / 111661

SAT solver	CNF file	simplified	phase	vars/clauses	propagat
lingeling-ats101	algotocnf_2.cnf	minisat	no	20895 / 118688	2541176
lingeling-ats101	algotocnf_2.cnf	minisat	yes	20895 / 118688	1376618
lingeling-ats101	algotocnf_2.cnf	satelite	no	27775 / 154276	3691672
lingeling-ats101	algotocnf_2.cnf	satelite	yes	27775 / 154276	5825908
lingeling-ats101	algotocnf_21-t9.cnf	none	no	116800 / 636838	65674937
lingeling-ats101	algotocnf_21-t9.cnf	none	yes	116800 / 636838	12248160
lingeling-ats101	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	80810652
lingeling-ats101	algotocnf_21-t9.cnf	cmsat	yes	63555 / 358308	51696309
lingeling-ats101	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	75552790
lingeling-ats101	algotocnf_21-t9.cnf	minisat	yes	65572 / 414470	37660918
lingeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	9417657
lingeling-ats101	algotocnf_21-t9.cnf	satelite	yes	74562 / 486714	50330239
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	3799761
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	yes	116800 / 911629	8977998
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	1939016
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	yes	59528 / 318049	7115202
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	1719807
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	yes	81650 / 534965	1086561
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	8199245
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	yes	90236 / 720755	4633920
lingeling-ats101	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629	47871721
lingeling-ats101	algotocnf_21-t9_diff-desc_ocnf.cnf	none	yes	116800 / 911629	50571983
lingeling-ats101	algotocnf_23-t9.cnf	none	no	122774 / 667438	11406748
lingeling-ats101	algotocnf_23-t9.cnf	none	yes	122774 / 667438	92551973
lingeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	94924448
lingeling-ats101	algotocnf_23-t9.cnf	cmsat	yes	64880 / 369775	14551473
lingeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	77557115
lingeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	9669970:
lingeling-ats101	algotocnf_23-t9.cnf	satelite	yes	77835 / 506217	10029572
lingeling-ats101	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343	35575573
lingeling-ats101	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	yes	222613 / 1350343	41256543
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	9459499
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	yes	122774 / 955067	6955287
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	7067769
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	yes	57510 / 307118	1221950

SAT solver	CNF file	simplified	phase	vars/clauses
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	yes	84080 / 550727
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	yes	93504 / 740545
lingeling-ats101	algotocnf_23-t9_diff-desc_ocnf.cnf	none	no	122774 / 955067
lingeling-ats101	algotocnf_23-t9_diff-desc_ocnf.cnf	none	yes	122774 / 955067
lingeling-ats101	algotocnf_23-t9_ocnf.cnf	none	no	122774 / 667438
lingeling-ats101	algotocnf_23-t9_ocnf.cnf	none	yes	122774 / 667438
lingeling-ats101	algotocnf_24-t9.cnf	none	no	125761 / 682722
lingeling-ats101	algotocnf_24-t9.cnf	none	yes	125761 / 682722
lingeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228
lingeling-ats101	algotocnf_24-t9.cnf	cmsat	yes	65579 / 377228
lingeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023 / 436292
lingeling-ats101	algotocnf_24-t9.cnf	minisat	yes	69023 / 436292
lingeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486 / 515977
lingeling-ats101	algotocnf_24-t9.cnf	satelite	yes	79486 / 515977
lingeling-ats101	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914
lingeling-ats101	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	yes	227841 / 1380914
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	yes	125761 / 976770
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	yes	56447 / 302014
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	yes	85312 / 558731
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	yes	95154 / 750557
lingeling-ats101	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	125761 / 976770
lingeling-ats101	algotocnf_24-t9_diff-desc_ocnf.cnf	none	yes	125761 / 976770
lingeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349
lingeling-ats101	algotocnf_27-t10-diff.cnf	none	yes	134722 / 728349
lingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	o / o

SAT solver	CNF file	simplified	phase	vars/clauses
lingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 1041654
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	yes	134722 / 1041654
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722 / 1041654
lingeling-ats101	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	yes	134722 / 1041654
lingeling-ats101	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722 / 728349
lingeling-ats101	algotocnf_27-t10-diff_ocnf.cnf	none	yes	134722 / 728349
lingeling-ats101	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542
lingeling-ats101	algotocnf_27-t10-simplified.cnf	none	yes	134722 / 728542
lingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680
lingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	yes	67175 / 392680
lingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404
lingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	yes	72909 / 460404
lingeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998
lingeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	yes	84442 / 544998
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	no	243525 / 1472595
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	yes	243525 / 1472595
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	yes	134722 / 1041847
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	yes	100735 / 789589
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722 / 1041847
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	yes	134722 / 1041847
lingeling-ats101	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722 / 728542
lingeling-ats101	algotocnf_27-t10-simplified_ocnf.cnf	none	yes	134722 / 728542

SAT solver	CNF file	simplified	phase	vars/clauses
lingeling-ats101	algotocnf_27-t10.cnf	none	no	134722 / 728030
lingeling-ats101	algotocnf_27-t10.cnf	none	yes	134722 / 728030
lingeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276
lingeling-ats101	algotocnf_27-t10.cnf	cmsat	yes	72044 / 411276
lingeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897 / 465248
lingeling-ats101	algotocnf_27-t10.cnf	minisat	yes	73897 / 465248
lingeling-ats101	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525 / 1472083
lingeling-ats101	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	yes	243525 / 1472083
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	yes	134722 / 1041335
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	yes	57956 / 311219
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	yes	105733 / 857675
lingeling-ats101	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722 / 1041335
lingeling-ats101	algotocnf_27-t10_diff-desc_ocnf.cnf	none	yes	134722 / 1041335
lingeling-ats101	algotocnf_27-t10_ocnf.cnf	none	no	134722 / 728030
lingeling-ats101	algotocnf_27-t10_ocnf.cnf	none	yes	134722 / 728030
lingeling-ats101	algotocnf_2_diff-desc-sc_ocnf.cnf	none	no	85760 / 522370
lingeling-ats101	algotocnf_2_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522370
lingeling-ats101	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146
lingeling-ats101	algotocnf_2_diff-desc.cnf	none	yes	48704 / 374146
lingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870
lingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	yes	15342 / 72870
lingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546
lingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	yes	40767 / 106546
lingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436
lingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	yes	23531 / 149436
lingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577
lingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	yes	29428 / 204577
lingeling-ats101	algotocnf_2_diff-desc_ocnf.cnf	none	no	48704 / 374146
lingeling-ats101	algotocnf_2_diff-desc_ocnf.cnf	none	yes	48704 / 374146
lingeling-ats101	algotocnf_2_ocnf.cnf	none	no	48704 / 254210
lingeling-ats101	algotocnf_2_ocnf.cnf	none	yes	48704 / 254210

SAT solver	CNF file	simplified	phase	vars/clauses	propagat
lingeling-ats101	algotocnf_3.cnf	none	no	48704 / 254656	1384778
lingeling-ats101	algotocnf_3.cnf	none	yes	48704 / 254656	1300597
lingeling-ats101	algotocnf_3.cnf	cmsat	no	23893 / 111403	2581772
lingeling-ats101	algotocnf_3.cnf	cmsat	yes	23893 / 111403	2729812
lingeling-ats101	algotocnf_3.cnf	lingeling	no	44000 / 100941	107507
lingeling-ats101	algotocnf_3.cnf	lingeling	yes	44000 / 100941	998189
lingeling-ats101	algotocnf_3.cnf	minisat	no	20895 / 119580	117457
lingeling-ats101	algotocnf_3.cnf	minisat	yes	20895 / 119580	1024653
lingeling-ats101	algotocnf_3.cnf	satelite	no	28647 / 156910	179127
lingeling-ats101	algotocnf_3.cnf	satelite	yes	28647 / 156910	1577494
lingeling-ats101	algotocnf_3_diff-desc-sc_ocnf.cnf	none	no	85760 / 522816	314777
lingeling-ats101	algotocnf_3_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522816	377633
lingeling-ats101	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	521025
lingeling-ats101	algotocnf_3_diff-desc.cnf	none	yes	48704 / 374592	344378
lingeling-ats101	algotocnf_3_diff-desc_ocnf.cnf	none	no	48704 / 374592	629567
lingeling-ats101	algotocnf_3_diff-desc_ocnf.cnf	none	yes	48704 / 374592	556136
lingeling-ats101	algotocnf_3_ocnf.cnf	none	no	48704 / 254656	1378843
lingeling-ats101	algotocnf_3_ocnf.cnf	none	yes	48704 / 254656	1224756
lingeling-ats102	algotocnf_18-t9_diff-desc_ocnf.cnf	none	no	107839 / 846487	2919960
lingeling-ats102	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920	1385390
lingeling-ats102	algotocnf_1_ocnf.cnf	none	no	48704 / 253984	2233118
lingeling-ats102	algotocnf_21-t9.cnf	none	no	116800 / 636838	65674937
lingeling-ats102	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	9417657
lingeling-ats102	algotocnf_21-t9_diff-desc-sc_ocnf.cnf	none	no	212157 / 1289169	13886232
lingeling-ats102	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	20645562
lingeling-ats102	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	2367713
lingeling-ats102	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629	35242124
lingeling-ats102	algotocnf_21-t9_ocnf.cnf	none	no	116800 / 636838	1268850
lingeling-ats102	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	11185442
lingeling-ats102	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343	13598362
lingeling-ats102	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	29754850
lingeling-ats102	algotocnf_24-t9.cnf	none	no	125761 / 682722	81971060
lingeling-ats102	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	13872340
lingeling-ats102	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	10756062
lingeling-ats102	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914	15199857

SAT solver	CNF file	simplified	phase	vars/
lingeling-ats102	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447
lingeling-ats102	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	50447 125761
lingeling-ats102	algotocni_24-t9_ocnf.cnf	none	no	125761
lingeling-ats102	algotocni_24-t9_ocni.cni algotocnf_27-t10-diff.cnf	none	no	
lingeling-ats102	algotocni_27-t10-diff.cnf	cmsat		134722
0 0			no	· ·
lingeling-ats102	algotocnf_27-t10-diff.cnf	lingeling	no	Q
lingeling-ats102	algotocnf_27-t10-diff.cnf	satelite	no	
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	C
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	d
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	d
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	d
lingeling-ats102	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10-simplified.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10-simplified.cnf	cmsat	no	67175
lingeling-ats102	algotocnf_27-t10-simplified.cnf	minisat	no	72909
lingeling-ats102	algotocnf_27-t10-simplified.cnf	satelite	no	84442
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	no	243525
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10.cnf	cmsat	no	72044
lingeling-ats102	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733
lingeling-ats102	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_27-t10_ocnf.cnf	none	no	134722
lingeling-ats102	algotocnf_2_diff-desc_ocnf.cnf	none	no	48704
lingeling-ats102	algotocnf_2_ocnf.cnf	none	no	48704
lingeling-ats102	algotocnf_3_ocnf.cnf	none	no	48704
lingeling-ats104	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	no	196473

SAT solver	CNF file	simplified	phase	vars/clauses	prop
lingeling-ats104	algotocnf_18-t9_ocnf.cnf	none	no	107839 / 590953	49
lingeling-ats104	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920	119
lingeling-ats104	algotocnf_1_ocnf.cnf	none	no	48704 / 253984	20
lingeling-ats104	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	808
lingeling-ats104	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	941
lingeling-ats104	algotocnf_21-t9_diff-desc-sc_ocnf.cnf	none	no	212157 / 1289169	159
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	379
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	76
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	206
lingeling-ats104	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629	249
lingeling-ats104	algotocnf_21-t9_ocnf.cnf	none	no	116800 / 636838	14:
lingeling-ats104	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	104
lingeling-ats104	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343	963
lingeling-ats104	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	254
lingeling-ats104	algotocnf_23-t9_diff-desc_ocnf.cnf	none	no	122774 / 955067	251
lingeling-ats104	algotocnf_23-t9_ocnf.cnf	none	no	122774 / 667438	89
lingeling-ats104	algotocnf_24-t9.cnf	none	no	125761 / 682722	819
lingeling-ats104	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	150
lingeling-ats104	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	107
lingeling-ats104	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914	116
lingeling-ats104	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	135
lingeling-ats104	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	125761 / 976770	344
lingeling-ats104	algotocnf_24-t9_ocnf.cnf	none	no	125761 / 682722	36
lingeling-ats104	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349	1
lingeling-ats104	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff_diff-desc-sc_ocnf.cnf	none	no	243525 / 1472402	2
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 1041654	1
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	
lingeling-ats104	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722 / 1041654	1
lingeling-ats104	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722 / 728349	1

SAT solver	CNF file	simplified	phase	vars/
lingeling-ats104	algotocnf_27-t10-simplified.cnf	none	no	
lingeling-ats104	algotocnf_27-t10-simplified.cnf	minisat	no	134722
lingeling-ats104	algotocnf_27-t10-simplified.cnf	satelite		72909 84442
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf		no	84442
	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	243525
lingeling-ats104		none	no	134722
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722
lingeling-ats104	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722
lingeling-ats104	algotocnf_27-t10.cnf	none	no	134722
lingeling-ats104	algotocnf_27-t10.cnf	cmsat	no	72044
lingeling-ats104	algotocnf_27-t10.cnf	minisat	no	73897
lingeling-ats104	algotocnf_27-t10.cnf	satelite	no	85274
lingeling-ats104	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733
lingeling-ats104	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722
lingeling-ats104	algotocnf_27-t10_ocnf.cnf	none	no	134722
lingeling-ats104	algotocnf_3_ocnf.cnf	none	no	48704
minisat	algotocnf_1.cnf	none	no	48704
minisat	algotocnf_1.cnf	none	no	
minisat	algotocnf_1.cnf	cmsat	no	
minisat	algotocnf_1.cnf	cmsat	no	24503
minisat	algotocnf_1.cnf	minisat	no	20895
minisat	algotocnf_1.cnf	minisat	no	
minisat	algotocnf_1.cnf	satelite	no	
minisat	algotocnf_1.cnf	satelite	no	27495
minisat	algotocnf_18-t9.cnf	none	no	107839
minisat	algotocnf_18-t9.cnf	none	no	
minisat	algotocnf_18-t9.cnf	cmsat	no	61789
minisat	algotocnf_18-t9.cnf	cmsat	no	
minisat	algotocnf_18-t9.cnf	lingeling	no	
minisat	algotocnf_18-t9.cnf	lingeling	no	102616
minisat	algotocnf_18-t9.cnf	minisat	no	61845
minisat	algotocnf_18-t9.cnf	minisat	no	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	decis
minisat	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	17335955	8932
minisat	algotocnf_18-t9.cnf	satelite	no			
minisat	algotocnf_18-t9_diff-desc.cnf	none	no			
minisat	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	18671534	8573
minisat	algotocnf_18-t9_diff-desc.cnf	cmsat	no			
minisat	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	21547194	1001
minisat	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	7408845	6092
minisat	algotocnf_18-t9_diff-desc.cnf	lingeling	no			
minisat	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	6527792	3836
minisat	algotocnf_18-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_18-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	7396646	4010
minisat	algotocnf_1_diff-desc.cnf	none	no			
minisat	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	145509993	4711
minisat	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	221480273	6830
minisat	algotocnf_1_diff-desc.cnf	cmsat	no			
minisat	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	407709713	18029
minisat	algotocnf_1_diff-desc.cnf	lingeling	no			
minisat	algotocnf_1_diff-desc.cnf	minisat	no			
minisat	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	166787763	5399
minisat	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	267008243	8016
minisat	algotocnf_1_diff-desc.cnf	satelite	no			
minisat	algotocnf_2.cnf	none	no			
minisat	algotocnf_2.cnf	none	no	48704 / 224220	201587749	9459
minisat	algotocnf_2.cnf	cmsat	no	24323 / 111661	2750894175	90426
minisat	algotocnf_2.cnf	cmsat	no			
minisat	algotocnf_2.cnf	minisat	no			
minisat	algotocnf_2.cnf	minisat	no	20895 / 118688	491695491	21320
minisat	algotocnf_2.cnf	satelite	no	27775 / 154276	1522804488	65886
minisat	algotocnf_2.cnf	satelite	no			
minisat	algotocnf_21-t9.cnf	none	no			
minisat	algotocnf_21-t9.cnf	none	no			
minisat	algotocnf_21-t9.cnf	cmsat	no			
minisat	algotocnf_21-t9.cnf	cmsat	no			
minisat	algotocnf_21-t9.cnf	minisat	no			

SAT solver	CNF file	simplified	phase	vars/clauses	propagation
minisat	algotocnf_21-t9.cnf	minisat	no		
minisat	algotocnf_21-t9.cnf	satelite	no		
minisat	algotocnf_21-t9.cnf	satelite	no		
minisat	algotocnf_21-t9_diff-desc.cnf	none	no		
minisat	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	9147981007
minisat	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	577921212
minisat	algotocnf_21-t9_diff-desc.cnf	cmsat	no		
minisat	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	1058635766
minisat	algotocnf_21-t9_diff-desc.cnf	lingeling	no		
minisat	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	3082155154
minisat	algotocnf_21-t9_diff-desc.cnf	minisat	no		
minisat	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	4261434766
minisat	algotocnf_21-t9_diff-desc.cnf	satelite	no		
minisat	algotocnf_23-t9.cnf	none	no		
minisat	algotocnf_23-t9.cnf	none	no		
minisat	algotocnf_23-t9.cnf	cmsat	no		
minisat	algotocnf_23-t9.cnf	cmsat	no		
minisat	algotocnf_23-t9.cnf	minisat	no		
minisat	algotocnf_23-t9.cnf	minisat	no		
minisat	algotocnf_23-t9.cnf	satelite	no		
minisat	algotocnf_23-t9.cnf	satelite	no		
minisat	algotocnf_23-t9_diff-desc.cnf	none	no		
minisat	algotocnf_23-t9_diff-desc.cnf	none	no		
minisat	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	3433286956
minisat	algotocnf_23-t9_diff-desc.cnf	cmsat	no		
minisat	algotocnf_23-t9_diff-desc.cnf	minisat	no		
minisat	algotocnf_23-t9_diff-desc.cnf	minisat	no		
minisat	algotocnf_23-t9_diff-desc.cnf	satelite	no		
minisat	algotocnf_23-t9_diff-desc.cnf	satelite	no		
minisat	algotocnf_24-t9.cnf	none	no		
minisat	algotocnf_24-t9.cnf	none	no		
minisat	algotocnf_24-t9.cnf	cmsat	no		
minisat	algotocnf_24-t9.cnf	cmsat	no		
minisat	algotocnf_24-t9.cnf	minisat	no		
minisat	algotocnf_24-t9.cnf	minisat	no		

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	de
minisat	algotocnf_24-t9.cnf	satelite	no			
minisat	algotocnf_24-t9.cnf	satelite	no			
minisat	algotocnf_24-t9_diff-desc.cnf	none	no			
minisat	algotocnf_24-t9_diff-desc.cnf	none	no			
minisat	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	3471709121	54
minisat	algotocnf_24-t9_diff-desc.cnf	cmsat	no			
minisat	algotocnf_24-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_24-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_24-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_24-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	134722	
minisat	algotocnf_27-t10-diff.cnf	none	no			
minisat	algotocnf_27-t10-diff.cnf	cmsat	no			
minisat	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	0	
minisat	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	0	
minisat	algotocnf_27-t10-diff.cnf	lingeling	no			
minisat	algotocnf_27-t10-diff.cnf	minisat	no			
minisat	algotocnf_27-t10-diff.cnf	minisat	no	o / o	0	
minisat	algotocnf_27-t10-diff.cnf	satelite	no			
minisat	algotocnf_27-t10-diff.cnf	satelite	no	o / o	0	
minisat	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 8320	134722	
minisat	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no			
minisat	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	0	
minisat	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no			
minisat	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	0	
minisat	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	0	
minisat	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no			
minisat	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no			
minisat	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	0	
minisat	algotocnf_27-t10-simplified.cnf	none	no			
minisat	algotocnf_27-t10-simplified.cnf	none	no			
minisat	algotocnf_27-t10-simplified.cnf	cmsat	no			
minisat	algotocnf_27-t10-simplified.cnf	cmsat	no			
minisat	algotocnf_27-t10-simplified.cnf	minisat	no			
minisat	algotocnf_27-t10-simplified.cnf	minisat	no			

SAT solver	CNF file	simplified	phase	vars/clauses	p
minisat	algotocnf_27-t10-simplified.cnf	satelite	no		
minisat	algotocnf_27-t10-simplified.cnf	satelite	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10.cnf	none	no		
minisat	algotocnf_27-t10.cnf	none	no		
minisat	algotocnf_27-t10.cnf	cmsat	no		
minisat	algotocnf_27-t10.cnf	cmsat	no		
minisat	algotocnf_27-t10.cnf	minisat	no		
minisat	algotocnf_27-t10.cnf	minisat	no		
minisat	algotocnf_27-t10.cnf	satelite	no		
minisat	algotocnf_27-t10.cnf	satelite	no		
minisat	algotocnf_27-t10_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10_diff-desc.cnf	satelite	no		
minisat	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	
minisat	algotocnf_2_diff-desc.cnf	none	no		
minisat	algotocnf_2_diff-desc.cnf	cmsat	no		
minisat	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	
minisat	algotocnf_2_diff-desc.cnf	lingeling	no		
minisat	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	
minisat	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	
minisat	algotocnf_2_diff-desc.cnf	minisat	no		
minisat	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	decis
minisat	algotocnf_2_diff-desc.cnf	satelite	no			
minisat	algotocnf_3.cnf	none	no	48704 / 222436	13991247	8535
minisat	algotocnf_3.cnf	none	no			
minisat	algotocnf_3.cnf	cmsat	no	23893 / 111403	15330537	8946
minisat	algotocnf_3.cnf	cmsat	no			
minisat	algotocnf_3.cnf	lingeling	no			
minisat	algotocnf_3.cnf	lingeling	no	44000 / 100941	3922854	3284
minisat	algotocnf_3.cnf	minisat	no	20895 / 119580	11055439	7059
minisat	algotocnf_3.cnf	minisat	no			
minisat	algotocnf_3.cnf	satelite	no			
minisat	algotocnf_3.cnf	satelite	no	28647 / 156910	15840699	1019
minisat	algotocnf_3_diff-desc.cnf	none	no			
minisat	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	8355604	4517
minisat-core	algotocnf_1.cnf	none	no	48704 / 225124	12249636981	19487
minisat-core	algotocnf_1.cnf	cmsat	no	24503 / 111931	1345904991	45407
minisat-core	algotocnf_1.cnf	minisat	no	20895 / 118236	1001195109	41539
minisat-core	algotocnf_1.cnf	satelite	no	27495 / 153262	2852530112	91754
minisat-core	algotocnf_18-t9.cnf	none	no	107839 / 582936	197561807	5771
minisat-core	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	3714952	3362
minisat-core	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	27126157	3729
minisat-core	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	11474979	6664
minisat-core	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	48139459	2806
minisat-core	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	134492463	5454
minisat-core	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	22660129	1033
minisat-core	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	4783352	1249
minisat-core	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	6527792	3836
minisat-core	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	68801966	3555
minisat-core	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	556973568	10855
minisat-core	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	565587287	15477
minisat-core	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	130669677	6453
minisat-core	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	166787763	5399
minisat-core	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	218192599	7694
minisat-core	algotocnf_2.cnf	none	no	48704 / 224220	4474027487	81273
minisat-core	algotocnf_2.cnf	cmsat	no	24323 / 111661	3271551070	10951
minisat-core	algotocnf_2.cnf	minisat	no	20895 / 118688	491695491	21320

SAT solver	CNF file	simplified	phase	vars/clauses	propag
minisat-core	algotocnf_2.cnf	satelite	no	27775 / 154276	13561
minisat-core	algotocnf_21-t9.cnf	none	no		
minisat-core	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	97208
minisat-core	algotocnf_21-t9.cnf	minisat	no		
minisat-core	algotocnf_21-t9.cnf	satelite	no		
minisat-core	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	61849
minisat-core	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	30333
minisat-core	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	23091
minisat-core	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	30821
minisat-core	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	20288
minisat-core	algotocnf_23-t9.cnf	none	no		
minisat-core	algotocnf_23-t9.cnf	cmsat	no		
minisat-core	algotocnf_23-t9.cnf	minisat	no		
minisat-core	algotocnf_23-t9.cnf	satelite	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	none	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	66867
minisat-core	algotocnf_23-t9_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_24-t9.cnf	none	no		
minisat-core	algotocnf_24-t9.cnf	cmsat	no		
minisat-core	algotocnf_24-t9.cnf	minisat	no		
minisat-core	algotocnf_24-t9.cnf	satelite	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	none	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	33082
minisat-core	algotocnf_24-t9_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	134
minisat-core	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
minisat-core	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	
minisat-core	algotocnf_27-t10-diff.cnf	minisat	no	o / o	
minisat-core	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 8320	134
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
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SAT solver	CNF file	simplified	phase	vars/clauses	propa
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	
minisat-core	algotocnf_27-t10-simplified.cnf	none	no		
minisat-core	algotocnf_27-t10-simplified.cnf	cmsat	no		
minisat-core	algotocnf_27-t10-simplified.cnf	minisat	no		
minisat-core	algotocnf_27-t10-simplified.cnf	satelite	no		
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	none	no		
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no		
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_27-t10.cnf	none	no		
minisat-core	algotocnf_27-t10.cnf	cmsat	no		
minisat-core	algotocnf_27-t10.cnf	minisat	no		
minisat-core	algotocnf_27-t10.cnf	satelite	no		
minisat-core	algotocnf_27-t10_diff-desc.cnf	none	no		
minisat-core	algotocnf_27-t10_diff-desc.cnf	cmsat	no		
minisat-core	algotocnf_27-t10_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_27-t10_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	6426
minisat-core	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	1001
minisat-core	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	1283
minisat-core	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	1695
minisat-core	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	2143
minisat-core	algotocnf_3.cnf	none	no	48704 / 222436	1346
minisat-core	algotocnf_3.cnf	cmsat	no	23893 / 111403	162
minisat-core	algotocnf_3.cnf	lingeling	no	44000 / 100941	497
minisat-core	algotocnf_3.cnf	minisat	no	20895 / 119580	110
minisat-core	algotocnf_3.cnf	satelite	no	28647 / 156910	814
minisat-core	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	820
plingeling-ats101	algotocnf_1.cnf	cmsat	no	24503 / 111931	8548
plingeling-ats101	algotocnf_1.cnf	minisat	no	20895 / 118236	8304
plingeling-ats101	algotocnf_1.cnf	satelite	no	27495 / 153262	12438
plingeling-ats101	algotocnf_18-t9.cnf	none	no	107839 / 590953	5891
plingeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	3575
plingeling-ats101	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544	1992
plingeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	303
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SAT solver	CNF file	simplified	phase	vars/clauses	propag
plingeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	39631
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	94961
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	74562
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	5270
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	37528
plingeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	42891
plingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	35481
plingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	31808
plingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	19652
plingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	24912
plingeling-ats101	algotocnf_2.cnf	none	no	48704 / 254210	112788
plingeling-ats101	algotocnf_2.cnf	cmsat	no	24323 / 111661	81450
plingeling-ats101	algotocnf_2.cnf	minisat	no	20895 / 118688	31248
plingeling-ats101	algotocnf_2.cnf	satelite	no	27775 / 154276	68889
plingeling-ats101	algotocnf_21-t9.cnf	none	no	116800 / 636838	130188
plingeling-ats101	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	172558
plingeling-ats101	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	191274
plingeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	132702
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	185148
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	144502
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	217187
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	238047
plingeling-ats101	algotocnf_23-t9.cnf	none	no	122774 / 667438	231925
plingeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	251983
plingeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	261991
plingeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	228831
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	558888
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	254882
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	397121
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	531778
plingeling-ats101	algotocnf_24-t9.cnf	none	no	125761 / 682722	768191
plingeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	274278
plingeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	251062
plingeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	295147
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770	438780

SAT solver	CNF file	simplified	phase	vars/clauses	prop
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	3183
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	3305
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	2932
plingeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349	10'
plingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
plingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	134722 / 0	
plingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	o / o	
plingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 1041654	16
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722 / 0	
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	
plingeling-ats101	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542	2742
plingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	32543
plingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	2559:
plingeling-ats101	eling-ats101 algotocnf_27-t10-simplified.cnf		no	84442 / 544998	3270
plingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847	29200
plingeling-ats101	$algotocnf\_27\hbox{-}t10\hbox{-}simplified\_diff-desc.cnf}$	satelite	no	100735 / 789589	2987
plingeling-ats101	algotocnf_27-t10.cnf	none	no	134722 / 728030	29330
plingeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	2922
plingeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	23830
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335	28599
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	31179
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	3257
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	2846
plingeling-ats101	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146	474
plingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	203
plingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546	214
plingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	107'
plingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	166
plingeling-ats101	algotocnf_3.cnf	none	no	48704 / 254656	452
plingeling-ats101	algotocnf_3.cnf	cmsat	no	23893 / 111403	126′
plingeling-ats101	algotocnf_3.cnf	lingeling	no	48704 / 100941	531
plingeling-ats101	algotocnf_3.cnf	minisat	no	20895 / 119580	472

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SAT solver	CNF file	simplified	phase	vars/clauses	pro
plingeling-ats101	algotocnf_3.cnf	satelite	no	28647 / 156910	6
plingeling-ats101	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	2
treengeling-ats101	algotocnf_1.cnf	cmsat	no	24503.0 / 111931.0	1
treengeling-ats101	algotocnf_1.cnf	minisat	no	20895.0 / 118236.0	1
treengeling-ats101	algotocnf_1.cnf	satelite	no	27495.0 / 153262.0	1
treengeling-ats101	algotocnf_18-t9.cnf	none	no	107839.0 / 590953.0	
treengeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789.0 / 342139.0	
treengeling-ats101	algotocnf_18-t9.cnf	lingeling	no	107839.0 / 344544.0	
treengeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845.0 / 391134.0	
treengeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670.0 / 457972.0	
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114.0 / 303489.0	1
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839.0 / 404666.0	
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055.0 / 511431.0	2
treengeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704.0 / 373920.0	3
treengeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402.0 / 73142.0	5
treengeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107.0 / 158393.0	1
treengeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950.0 / 226602.0	5
treengeling-ats101	algotocnf_2.cnf	none	no	48704.0 / 254210.0	1
treengeling-ats101	algotocnf_2.cnf	cmsat	no	24323.0 / 111661.0	2
treengeling-ats101	algotocnf_2.cnf	minisat	no	20895.0 / 118688.0	
treengeling-ats101	algotocnf_2.cnf	satelite	no	27775.0 / 154276.0	1
treengeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562.0 / 486714.0	48
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800.0 / 911629.0	7
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528.0 / 318049.0	4
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650.0 / 534965.0	21
treengeling-ats101	algotocnf_23-t9.cnf	none	no	122774.0 / 667438.0	43
treengeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880.0 / 369775.0	42
treengeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979.0 / 429734.0	43
treengeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835.0 / 506217.0	34
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774.0 / 955067.0	20
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510.0 / 307118.0	6
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080.0 / 550727.0	11
treengeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579.0 / 377228.0	39
treengeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023.0 / 436292.0	42
treengeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486.0 / 515977.0	50
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SAT solver	CNF file	simplified	phase	vars/clauses
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761.0 / 976770.0
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447.0 / 302014.0
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312.0 / 558731.0
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154.0 / 750557.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722.0 / 728349.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	134722.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175.0 / 392680.0
treengeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909.0 / 460404.0
treengeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	no	84442.0 / 544998.0
treengeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735.0 / 789589.0
treengeling-ats101	algotocnf_27-t10.cnf	none	no	134722.0 / 728030.0
treengeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044.0 / 411276.0
treengeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897.0 / 465248.0
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722.0 / 1041335.0
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956.0 / 311219.0
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850.0 / 619480.0
treengeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342.0 / 72870.0
treengeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	48704.0 / 106546.0
treengeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531.0 / 149436.0
treengeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428.0 / 204577.0
treengeling-ats101	algotocnf_3.cnf	none	no	48704.0 / 254656.0
treengeling-ats101	algotocnf_3.cnf	cmsat	no	23893.0 / 111403.0
treengeling-ats101	algotocnf_3.cnf	lingeling	no	48704.0 / 100941.0
treengeling-ats101	algotocnf_3.cnf	minisat	no	20895.0 / 119580.0
treengeling-ats101	algotocnf_3.cnf	satelite	no	28647.0 / 156910.0

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