## University of Technology, Graz

## MASTER THESIS

# Differential cryptanalysis with SAT solvers

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# Differential cryptanalysis with SAT solvers

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## **AFFIDAVIT**

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## **ABSTRACT**

Hash functions are ubiquitous in the modern information age. They provide preimage, second preimage and collision resistance which are needed in a wide range of applications.

In August 2006, Wang et al. showed efficient attacks against several hash function designs including MD4, MD5, HAVAL-128 and RIPEMD. With these results differential cryptanalysis has been shown useful to break collision resistance in hash functions. Over the years advanced attacks based on those differential approaches have been developed.

To find collisions like Wang et al., a cryptanalyst needs to specify a differential characteristic as starting point. This characteristic has a huge impact on the runtime. The goal is to find a differential characteristic whose differences cancel out in the output. Once such a differential characteristic was discovered, in a second step the actual values for those differences are defined yielding an actual hash collision.

Evaluating differential characteristics can be a cumbersome and tedious task. Dedicated tools can implement search heuristics. Performance shortcuts can be made by studying the hash algorithm's differential behavior.

SAT solvers inherently implement a search heuristic and should derive those shortcuts on their own. In this thesis we use SAT solvers to solve differential cryptanalysis problems. We show that SAT solvers are not able to derive those shortcuts on their own, but on the other hand we introduce tweaks which significantly improve the runtime. SAT design remains an important topic.

We wrote a library generating CNFs for differential characteristics and optionally introduced SAT design tweaks to this CNF. Those tweaks allowed a significant runtime improvement helping us to solve full-rounds hash collisions in MD4 and 24-rounds hash collisions in SHA-256. Finally we also provide a small CNF analysis library to compare encoded problems with each other.

**Keywords:** hash function, differential cryptanalysis, differential characteristic, MD4, SHA-256, collision resistance, satisfiability, SAT solver

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Thank you. どもありがとうございました。

All source codes are available at lukas-prokop.at/proj/megosat and published under terms and conditions of Free/Libre Open Source Software. This document was printed with LualFteX in the Linux Libertine typeface.

## **Contents**

1	Intr	oduction	1
	1.1	Overview	1
	1.2	Thesis Outline	2
2	Has	h algorithms	3
	2.1	Preliminaries Redux	3
		2.1.1 Merkle-Damgård designs	4
		2.1.2 Padding and length extension attacks	5
		2.1.3 Example usage	5
	2.2	MD <sub>4</sub>	6
	2.3	SHA-256	8
3	Diff	erential cryptanalysis 1	1
	3.1	Motivation	1
	3.2	Fundamentals	2
	3.3	Differential notation	4
	3.4	A simple addition example	5
	3.5	Differential characteristics in action	7
4	Sati	sfiability 1	9
			_
	4.1	Basic notation and definitions	9
	4.1		9

CONTENTS		vi

	4.2	The DIMACS de-facto standard	22					
	4.3	Terminology						
	4.4	Basic SAT solving techniques						
		4.4.1 Boolean constraint propagation (BCP)	24					
		4.4.2 Watched Literals	24					
		4.4.3 Remark	25					
	4.5	SAT solvers in use	25					
5	SAT	features	27					
	5.1	Definition	28					
	5.2	Related work	28					
	5.3	Statistical features	29					
	5.4	Suggested SAT features	30					
	5.5	Evaluation efficiency	32					
	5.6	CNF dataset	32					
	5.7	The average SAT problem	33					
	5.8	Benford's law in CNF files	34					
6	Prob	blem encoding	36					
6	<b>Prob</b> 6.1	blem encoding  Basic approach	<b>36</b> 36					
6			_					
6	6.1	Basic approach	36					
6	6.1	Basic approach	36 37					
6	6.1	Basic approach	36 37 38					
6	6.1	Basic approach	36 37 38 39					
6	6.1	Basic approach	36 37 38 39 41					
7	6.1	Basic approach	36 37 38 39 41 41					
	6.1	Basic approach	36 37 38 39 41 41					

CC	ONTEI	NTS	vii
		7.2.1 Attacking MD <sub>4</sub>	47
		7.2.2 Evaluating simplification	47
		7.2.3 Attacking SHA-256	49
		7.2.4 Modifying the guessing strategy	51
		7.2.5 Evaluating the lightweight approach	51
		7.2.6 Using preference variables	52
	7.3	Summary	53
8	Sum	amary and Future Work	54
	8.1	Related work	54
	8.2	Conclusion	54
	8.3	Future work	55
	8.4	Contributions	55
Ap	pend	lices	57
A	Har	dware setup	58
В	Test	cases	59
	B.1	MD4 testcase A	59
	B.2	MD4 testcase B	59
	B.3	MD4 testcase C	59
	B.4	SHA-256 testcase 18 rounds	60
	B.5	SHA-256 testcase 21 rounds	60
	B.6	SHA-256 testcase 23 rounds	60
	B.7	SHA-256 testcase 24 rounds	60
C	Run	times retrieved	67



## Chapter 1

## Introduction

#### 1.1 Overview

Hash functions are used as cryptographic primitives in many applications and protocols. They take an arbitrary input message and provide a hash value. Input message and hash value are considered as byte strings in a particular encoding. The hash value is of fixed length and satisfies several properties which make it useful in a variety of applications.

In this thesis, we will consider the hash algorithms MD4 and SHA-256. They use basic arithmetic functions like addition and bitwise functions such as XOR to transform an input message to a hash value. We use a bit vector as input to this implementation and all operations applied to this bit vector will be represented as clauses of a SAT problem. Additionally, we represent differential characteristics for hash collisions as SAT problem. If and only if satisfiability is given, the particular differential state is achievable using two different inputs leading to the same output. As far as SAT solvers return an actual model satisfying that state, we get an actual hash collision, which can be verified and visualized. If the internal state of the hash algorithm is too large, the attack can be computationally simplified by modelling only a subset of steps of the hash algorithm or changing the modelled differential path.

Based on experience with these kind of problems with previous heuristic search tools we aim to apply best practices to a satisfiability setting. We will discuss, which SAT techniques lead to best performance characteristics for our MD<sub>4</sub> and SHA-256 testcases.

### 1.2 Thesis Outline

This thesis is organized as follows:

- **In Chapter 1,** we briefly introduce basic subjects of this thesis. We explain our high-level goal involving hash functions and SAT solvers.
- In Chapter 2, we introduce the MD4 and SHA-256 hash functions. Certain design decisions imply certain properties which can be used in differential cryptanalysis. We discuss those decisions in this chapter after a formal definition of the function itself. Beginning with this chapter we develop a theoretical notion of our tools.
- **In Chapter** 3, we discuss approaches of differential cryptanalysis. We start with work done by Wang, et al. and followingly introduce differential notation to simplify representation of differential states. This way we can easily dump hash collisions.
- **In Chapter 4,** we discuss SAT solving techniques. We discuss how the problem needs to be encoded and give a brief overview over used SAT solvers. This includes a customized lingeling version by Armin Biere for our purposes.
- **In Chapter 5,** we define SAT features which help us to classify SAT problems. This is a small subproject we did to look at properties of resulting DI-MACS CNF files.
- **In Chapter 6,** we discuss how we represent a problem (i.e. the hash function and a differential characteristic) as SAT problem. This ultimatively allows us to solve the problem using a SAT solver.
- **In Chapter 7,** we present the result of our work. Runtimes are the main part of this chapter, but also results of Chapter 5 are presented.
- In Chapter 8, we conclude and discuss future work based on our results.



## Chapter 2

## Hash algorithms

In this chapter, we will define hash functions and their desired security properties. In the following, we look at SHA-256 and MD4 as established hash functions. MD4 unlike SHA-256 is practically broken, but has a comparably small internal state. It therefore allows a good starting point to devise our attacks. In a next step, we scaled up to SHA-256 which has an internal state size at least twice as large. In Chapter 6, we will represent them with Boolean algebra to allow to reason about states in those hash functions using SAT solvers.

## 2.1 Preliminaries Redux

## Definition 2.1 (Hash function)

A *hash function* is a mapping  $h: X \to Y$  with  $X = \{0, 1\}^*$  and  $Y = \{0, 1\}^n$  for some fixed  $n \in \mathbb{N}_{\geq 1}$ .

- Let  $x \in X$ , then h(x) is called hash value of x.
- Let  $h(x) = y \in Y$ , then x is called *preimage of y*.

Hash functions are considered as cryptographic primitives used as building blocks in cryptographic protocols. A hash function has to satisfy the following security requirements:

## **Definition 2.2** (Preimage resistance)

Given  $y \in Y$ , a hash function h is *preimage resistant* iff it is computationally infeasible to find  $x \in X$  such that h(x) = y.

### Definition 2.3 (Second-preimage resistance)

Given  $x \in X$ , a hash function h is second-preimage resistant iff it is computationally infeasible to find  $x_2 \in X$  with  $x \neq x_2$  such that  $h(x) = h(x_2)$ .  $x_2$  is called second preimage.

### Definition 2.4 (Collision resistance)

A hash function h is *collision resistant* iff it is computationally infeasible to find any two  $x \in X$  and  $x_2 \in X$  with  $x \neq x_2$  such that  $h(x) = h(x_2)$ . Tuple  $(x, x_2)$  is called *collision*.

As far as hash functions accept input strings of arbitrary length, but return a fixed size output string, existence of collisions is unavoidable [31]. However, good hash functions make it very difficult to find collisions or preimages.

Any digital data can be hashed (i.e. used as input to a hash function) by considering it in binary representation. The format or encoding is not part of the hash function's specification.

## 2.1.1 Merkle-Damgård designs

The Merkle-Damgård design is a particular design of hash functions providing the following security guarantee:

## Definition 2.5 (Collision resistance inheritance)

Let  $F_0$  be a collision resistant compression function. A hash function in Merkle-Damgård design is collision resistant if  $F_0$  is collision resistant.

This motivates thorough research of collisions in compression functions. The design was found independently by Ralph C. Merkle and Ivan B. Damgård. It was described by Merkle in his PhD thesis [17, p. 13–15] and used in popular hash functions such as MD4, MD5 and the SHA2 hash function family.

The single-pipe design works as follows:

- 1. Split the input into blocks of uniform block size. If necessary, apply padding to the last block to achieve full block size.
- 2. Compression function  $F_0$  is applied iteratively using the output  $y_{i-1}$  of the previous iteration and the next input block  $x_i$ , denoted  $y_i = F_0(y_{i-1}, x_i)$ .
- 3. An optional postprocessing function is applied.

## 2.1.2 Padding and length extension attacks

Hash functions of single-piped Merkle-Damgård design inherently suffer from length extension attacks. MD4 and SHA-256 apply padding to their input to normalize their input size to a multiple of its block size. The compression function is applied afterwards. This design is vulnerable to length extensions.

Consider some collision  $(x_0, x_1)$  with  $F_0(x_0) = y = F_0(x_1)$  where  $x_0$  and  $x_1$  have a size of one block. Let p be a suffix with size of one block. Then also  $(x_0 || p, x_1 || p)$  (where || denotes concatenation) represents a collision in single-piped Merkle-Damgård designs, because it holds that:

$$F_0(F_0(x_0), p) = F_0(F_0(x_1), p) \iff F_0(y, p) = F_0(y, p)$$

Hence  $(x_0 || p, x_1 || p)$  is a collision as well. As far as  $F_0$  is applied recursively to every block, p can be of arbitrary size and  $(x_0, x_1)$  can be of arbitrary uniform size.

Because of this vulnerability, cryptanalysts focus on finding a collision in compression functions. In our tests will only consider input of one block and padding will be neglected due to this vulnerability.

## 2.1.3 Example usage

The following list describes application examples:

**Digital signatures.** Digital signatures are schemes to guarantee data and origin integrity. They are used to verify authenticity of PDF documents, encrypted emails or software distributions. A digital signature can be verified, showing that a particular user was involved in the signature process. No third party can forge a digital signature. Because the document itself might be too large, only its hash value is attached to the hash signature.

**Storing passwords.** User account data such as passwords are commonly stored in databases. Those databases are subject to theft if network breaches take place and the passwords are known to the attackers. Hashing and salting those passwords with a hash algorithm before storing them in the database is a working countermeasure.

**Commitment schemes.** Commitment schemes like Zero-Knowledge Proofs use hash algorithms to ensure the original message is possessed by a certain party without revealing the document itself. Coin-flipping or secure computation also use hash algorithms as cryptographic building blocks.

## 2.2 MD4

MD4 is a cryptographic hash function originally described in RFC 1186 [26], updated in RFC 1320 [27] and declared obsolete by RFC 6150 [34]. It was invented by Ronald Rivest in 1990 with properties given in Table 2.1. In 1995 [5], successful full-round attacks have been found to break collision resistance. Three years later, preimage and second-preimage resistance in MD4 got broken as well. Some of those attacks are described in [28] and [20]. We derived a Python 3 implementation based on a Python 2 implementation and made it available on github [24].

block size	512 bits	namely variable block in RFC 1320 [27]
digest size	128 bits	as per Section 3.5 in RFC 1320 [27]
internal state size	128 bits	namely variables $A$ , $B$ , $C$ and $D$
word size	32 bits	as per Section 2 in RFC 1320 [27]

Table 2.1: MD4 hash algorithm properties

MD<sub>4</sub> uses three auxiliary Boolean functions:

#### **Definition 2.6**

The Boolean IF function is defined as follows: If the first argument is true, the second argument is returned. Otherwise the third argument is returned.

The Boolean MAJ function returns true if the number of arguments with Boolean value true is in the majority. The Boolean XOR function returns true if the number of arguments with Boolean value true is odd.

Using the logical operators  $\land$  (AND),  $\lor$  (OR) and  $\neg$  (NEG) we can define them as (see Section 4.1 for a thorough discussion of these operators):

$$\begin{split} \operatorname{IF}(X,Y,Z) &\coloneqq (X \wedge Y) \vee (\neg X \wedge Z) \\ \operatorname{MAJ}(X,Y,Z) &\coloneqq (X \wedge Y) \vee (X \wedge Z) \vee (Y \wedge Z) \\ \operatorname{XOR}(X,Y,Z) &\coloneqq (X \wedge \neg Y \wedge \neg Z) \vee (\neg X \wedge Y \wedge \neg Z) \\ &\vee (\neg X \wedge \neg Y \wedge Z) \vee (X \wedge Y \wedge Z) \\ &\coloneqq (X \oplus Y \oplus Z) \end{split} \tag{2.1}$$

In the following, a brief overview of MD4 is given.

**Padding and length extension.** First of all, padding is applied. A single bit 1 is appended to the input. As long as the input does not reach a length congruent 448 modulo 512, bit 0 is appended. Afterwards, length appending takes place. Append the first 64 less significant bits of the input length (without the previous modifications) represented in binary.

**Initialization.** The message is split into 512-bit blocks (i.e. 16 32-bit words). State variables  $A_i$  with  $-4 \le i < 0$  are initialized with these hexadecimal values:

$$A_{-4} = 01234567$$
  $A_{-1} = 89$ abcdef  $A_{-2} =$ fedcba98  $A_{-3} = 76543210$ 

**Round function and state variable updates.** The round function is applied in 3 rounds with 16 iterations. In every iteration, values  $A_{-1}$ ,  $A_{-2}$  and  $A_{-3}$  are taken as arguments to function F. Function F is IF in round 1, followed by MAJ for round 2 and XOR for the final round 3. The resulting value is added to  $A_{-1}$ , current message block M and constant X. Finally, the 32-bit sum will be left-rotated by p positions. Left rotation is formally defined in Definition 2.7. We define X and p:

Let i be the iteration counter between 1 and 16 and r the round between 1 and 3. Then X takes the value of the i-th column and r-th row of matrix C. p takes the value of row r and column  $i \mod 4$  of matrix P.

$$P = \begin{pmatrix} 3 & 7 & 9 & 11 \\ 3 & 5 & 9 & 13 \\ 3 & 9 & 11 & 15 \end{pmatrix}$$

This round function design is visualized in Figure 2.1.

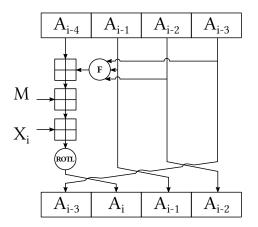


Figure 2.1: MD4 round function updating state variables

## 2.3 SHA-256

SHA-256 is a hash function from the SHA-2 family designed by the National Security Agency (NSA) and published as FIPS PUB 180-4 (originally 2001) [9]. It uses a Merkle-Damgård construction with a Davies-Meyer compression function. The best known preimage attack was found in 2011 and breaks preimage resistance for 52 rounds [11]. The best known collision attack breaks collision resistance for 31 rounds of SHA-256 [15] and pseudo-collision resistance for 46 rounds [12]. The best practical attack is a pseudo-collision for 38 steps [16].

```
block size 512 bits as per Section 1 of the standard [9] digest size 256 bits mentioned as Message Digest size [9] internal state size 256 bits as per Section 1 of the standard [9] word size 32 bits as per Section 1 of the standard [9]
```

Table 2.2: SHA-256 hash algorithm properties

## Definition 2.7 (Shifts, rotations and a notational remark)

Consider a 32-bit word X with 32 binary values  $b_i$  with  $0 \le i \le 31$ .  $b_0$  refers to the least significant bit. Shifting ( $\ll$  and  $\gg$ ) and rotation ( $\ll$  and  $\gg$ ) creates a new 32-bit word Y with 32 binary values  $a_i$ . We define the following notations:

```
Y := X \ll n \iff a_i := b_{i-n} \text{ if } 0 \leqslant i - n < 32 \text{ and } 0 \text{ otherwise}
Y := X \gg n \iff a_i := b_{i+n} \text{ if } 0 \leqslant i + n < 32 \text{ and } 0 \text{ otherwise}
Y := X \ll n \iff a_i := b_{i-n \mod 32} \text{ as used in MD4}
Y := X \gg n \iff a_i := b_{i+n \mod 32}
```

Besides MD<sub>4</sub>'s MAJ and IF, another four auxiliary functions are defined. Recognize that  $\oplus$  denotes the XOR function whereas  $\boxplus$  denotes 32-bit addition.

```
\Sigma_0(X) := (X \gg 2) \oplus (X \gg 13) \oplus (X \gg 22)

\Sigma_1(X) := (X \gg 6) \oplus (X \gg 11) \oplus (X \gg 25)

\sigma_0(X) := (X \gg 7) \oplus (X \gg 18) \oplus (X \gg 3)

\sigma_1(X) := (X \gg 17) \oplus (X \gg 19) \oplus (X \gg 10)
```

**Padding and length extension.** The padding and length extension scheme of MD<sub>4</sub> is used also in SHA-256. Append bit 1, followed by a sequence of bit 0 until the message reaches a length of 448 modulo 512 bits. Afterwards the first 64 bits of the binary representation of the original input are appended.

**Initialization.** In a similar manner to MD4, initialization of internal state variables (called "working variables" in [9, Section 6.2.2]) takes place before

running the round function. The eight state variables are initialized with the following hexadecimal values:

$$A_{-1} =$$
 6a09e667  $A_{-2} =$  bb67ae85  $A_{-3} =$  3c6ef372  $A_{-4} =$  a54ff53a  $E_{-1} =$  510e527f  $E_{-2} =$  9b05688c  $E_{-3} =$  1f83d9ab  $E_{-4} =$  5be0cd19

Furthermore SHA-256 uses 64 constant values in its round function. We initialize step constants  $K_i$  for  $0 \le i < 64$  with the following hexadecimal values (which must be read left to right and top to bottom):

4	28a2f98	71374491	b5c0fbcf	e9b5dba5	3956c25b	59f111f1
9	23f82a4	ab1c5ed5	d807aa98	12835b01	243185be	550c7dc3
7	2be5d74	80deb1fe	9bdc06a7	c19bf174	e49b69c1	efbe4786
0	fc19dc6	240ca1cc	2de92c6f	4a7484aa	5cb0a9dc	76f988da
9	83e5152	a831c66d	b00327c8	bf597fc7	c6e00bf3	d5a79147
0	6ca6351	14292967	27b70a85	2e1b2138	4d2c6dfc	53380d13
6	50a7354	766a0abb	81c2c92e	92722c85	a2bfe8a1	a81a664b
С	24b8b70	c76c51a3	d192e819	d6990624	f40e3585	106aa070
1	9a4c116	1e376c08	2748774c	34b0bcb5	391c0cb3	4ed8aa4a
5	b9cca4f	682e6ff3	748f82ee	78a5636f	84c87814	8cc70208
9	0befffa	a4506ceb	bef9a3f7	c67178f2		

**Precomputation of W.** Let  $W_i$  for  $0 \le i < 16$  be the sixteen 32-bit words of the padded input message. Then compute  $W_i$  for  $16 \le i < 64$  the following way:

$$W_i := \sigma_1(W_{i-2}) + W_{i-7} + \sigma_0(W_{i-15}) + W_{i-16}$$

**Round function.** For every block of 512 bits, the round function is applied. The eight state variables are updated iteratively for i from 0 to 63.  $W_i$  and  $K_i$  refer to the previously initialized values.

$$E_i := A_{i-4} + E_{i-4} + \Sigma_1 (E_{i-1}) + \text{IF} (E_{i-1}, E_{i-2}, E_{i-3}) + K_i + W_i$$
  
 $A_i := E_i - A_{i-4} + \Sigma_0 (A_{i-1}) + \text{MAJ} (A_{i-1}, A_{i-2}, A_{i-3})$ 

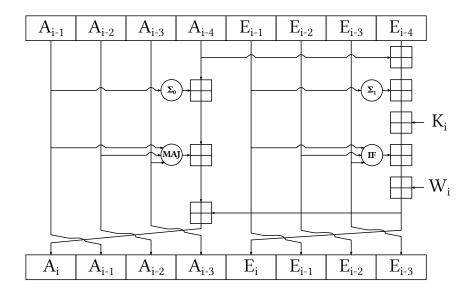


Figure 2.2: SHA-256 round function [6]



"Just because it's automatic doesn't mean it works." —Daniel J. Bernstein

## Chapter 3

## Differential cryptanalysis

In Chapter 2 we defined two hash functions. In this chapter we consider such functions from a differential perspective. Differential cryptanalysis will turn out to yield successful collision attacks on hash functions. We introduce a notation to easily represent differential characteristics.

## 3.1 Motivation

In August 2004, Wang et al. published results at Crypto'04 [35] which revealed that MD4, MD5, HAVAL-128 and RIPEMD can be broken practically using differential cryptanalysis. Their work is based on preliminary work by Hans Dobbertin [5]. On an IBM P690 machine, an MD5 collision can be computed in about one hour using this approach. Collisions for HAVAL-128, MD4 and RIPEMD were found as well. Patrick Stach's md4coll.c program [33] implements Wang's approach and can find MD4 collisions in few seconds on my Thinkpad x220 setup specified in Appendix A.

Let n denote the digest size, i.e. the size of the hash value h(x) in bits. Due to the birthday paradox, a collision attack has a generic complexity of  $2^{n/2}$  whereas preimage and second preimage attacks have generic complexities of  $2^n$ . In other words it is computationally easier to find any two colliding hash values than the preimage or second preimage for a given hash value.

Following results by Wang et al., differential cryptanalysis was shown as powerful tool for cryptanalysis of hash algorithms. This thesis applies those ideas to satisfiability approaches.

Message 1						
4d7a9c83	d6cb927a	29d5a578	57a7a5ee			
de748a3c	dcc366b3	b683a020	3b2a5d9f			
c69d71b3	f9e99198	d79f805e	a63bb2e8			
45dc8e31	97e31fe5	2794bf08	b9e8c3e9			
	Messa	age 2				
4d7a9c83	56cb927a	b9d5a578	57a7a5ee			
de748a3c	dcc366b3	b683a020	3b2a5d9f			
c69d71b3	f9e99198	d79f805e	a63bb2e8			
45dd8e31	2794bfo8	b9e8c3e9				
Hash value of Message 1 and Message 2						
5f5c1aod	71b36046	1b5435da	9bod8o7a			

Table 3.1: One of two MD4 hash collisions provided in [35]. A message represents one block of 512 bits. Values are given in hexadecimal, message words are enumerated from left to right, top to bottom. Differences are highlighted in bold for illustration purposes. For comparison the first bits of Message 1 are 11000001... and the last bits are ...10011101.

## 3.2 Fundamentals

## Definition 3.1 (Hash collision)

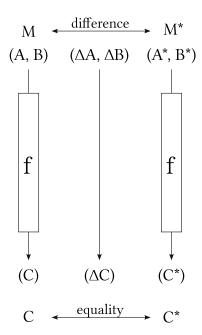
Given a hash function h, a hash collision is a pair  $(x_1, x_2)$  with  $x_1 \neq x_2$  such that  $h(x_1) = h(x_2)$ .

Pseudo-collisions are also often considered when attacking hash functions. A *pseudo-collision* is given if a hash collision can be found for a given hash function, but the initial vectors (IV) can be chosen for each message.

Hash algorithms consume input values as blocks of bits. As far as the length of the input must not conform to the block size, padding is applied. Now consider such a block of input values and another copy of it. We use those two blocks as inputs for two hash algorithm instances, but provide slight modifications in few bits. Differential cryptanalysis is based on the idea to consider those execution states and trace those differences to learn about the propagation of message differences. Compare this setup with Figure 3.1.

At the very beginning only the few defined differences are given. But as the hash algorithm progresses in computation, differences are propagated to more and more bits. Most likely the final value will differ in many bits, because of a desirable hash algorithm property called *avalanche effect*. A small difference in the input should lead to a significant difference in the output (i.e. visually recognizable).

Visualizing those differences helps the cryptanalyst to find modifications yielding a small number of differences in the evaluation state. Empirical results in



**Figure 3.1:** Common attack setting for a collision attack: Hash function f is applied to two inputs M and  $M^*$  which differ by some predefined bits.  $\Delta M$  describes the difference between these values. A hash collision is given if and only if output values C and  $C^*$  show the same value. In differential cryptanalysis we observe the differences between two instances applying function f to inputs M and  $M^*$ .

differential cryptanalysis indicate that sparse characteristics are desirable, because it is easier to cancel out few differences in the output compared to many differences. The cryptanalyst consecutively modifies the input values to eventually receive a collision in the output value (i.e.  $\Delta C = 0 \iff C = C^*$ ).

## **Definition 3.2**

The differential state during a computation is called *differential characteristic* (also *differential path*).

### Theorem 3.1

Assuming the number of differences in a differential characteristic is small, this characteristic is expected to result in a hash collision with higher probability.

## 3.3 Differential notation

Differential notation helps us to visualize differential characteristics by defining so-called *generalized bit conditions*. It was introduced by Christophe de Cannière and Christian Rechberger in 2006 [2, Section 3.2], inspired by *signed differences* by Wang et al. and is shown in Table 3.2.

$(x_i, x_i^*)$	(0,0)	(1,0)	(0,1)	(1, 1)	$(x_i, x_i^*)$	(0,0)	(1,0)	(0,1)	(1, 1)
?	✓	$\checkmark$	$\checkmark$	$\checkmark$	3	✓	$\checkmark$		
_	✓			✓	5	✓		$\checkmark$	
X		$\checkmark$	$\checkmark$		7	✓	$\checkmark$	$\checkmark$	
0	✓				A		$\checkmark$		$\checkmark$
u		$\checkmark$			В	✓	$\checkmark$		✓
n			$\checkmark$		С			$\checkmark$	✓
1				✓	D	✓		$\checkmark$	✓
#					E		✓	✓	✓

Table 3.2: Differential notation as introduced in [2]. The left-most column specifies a symbol called "bit condition" and right-side columns indicate which bit configurations are possible for two given bits  $x_i$  and  $x_i^*$ .

Consider two hash algorithm instances. Let  $x_i$  be some bit from the first instance and let  $x_i^*$  be the corresponding bit from the second instance. Differences are computed using a XOR and commonly denoted as  $\Delta x = x_i \oplus x_i^*$ . Bit conditions allow us to encode possible relations between bits  $x_i$  and  $x_i^*$ .

For example, let us take a look at the original Wang et al. hash collision in MD4 provided in Table 3.1. We extract all values with differences and represent them using differential notation. This gives us Table 3.3.

bit	hexadecimal	binary representation / differential notation
$\overline{x_0}$	d6cb927a	11010110110010111001001001111010
$x_1$	29d5a578	001010011101010110100101011111000
$x_2$	45dc8e31	01000101110111001000111000110001
$\overline{x_0^*}$	56cb927a	01010110110010111001001001111010
$x_1^*$	b9d5a578	101110011101010110100101011111000
$x_2^*$	45dd8e31	01000101110111011000111000110001
$\Delta x$		u1010110110010111001001001111010
		n01n10011101010110100101011111000
		010001011101110n1000111000110001

TABLE 3.3: The three words different between Message 1 and Message 2 of the original MD4 hash collision by Wang et al. The last three lines show how differences can be written down using bit conditions. As far as 4 symbols are not from the set {0, 1} it holds that the messages differ by 4 bits.

The following properties hold for bit conditions:

- If  $x_i = x_i^*$  holds and some value is known,  $\{0, 1\}$  contains its bit condition.
- If  $x_i \neq x_i^*$  holds and some value is known,  $\{u, n\}$  contains its bit condition.
- If  $x_i = x_i^*$  holds and the values are unknown, its bit condition is -.
- If  $x_i \neq x_i^*$  holds and the values are unknown, its bit condition is x.

Applying this notation to hash collisions means that arbitrary bit conditions (except for #) can be specified for the input values. In one of the intermediate iterations, we enforce a difference using one of the bit conditions  $\{u, n, x\}$ . This excludes trivial solutions with no differences from the set of possible solutions. And the final values need to lack differences thus are represented using a dash  $\neg$ .

$\Delta x$	conjunctive normal form	$\Delta x$	conjunctive normal form
#	$(x) \wedge (\neg x)$	1	$(x) \wedge (x^*)$
0	$(\neg x) \wedge (\neg x^*)$	_	$\neg(x \oplus x^*)$
u	$(x) \wedge (\neg x^*)$	Α	(x)
3	$(\neg x^*)$	В	$(x \vee \neg x^*)$
n	$(\neg x) \wedge (x^*)$	С	$(x^*)$
5	$(\neg x)$	D	$(\neg x \lor x^*)$
Χ	$(x \oplus x^*)$	Ε	$(x \vee x^*)$
7	$(\neg x \lor \neg x^*)$	?	

Table 3.4: All bit conditions represented as CNF using two Boolean variables x and  $x^*$  to represent two bits.

## 3.4 A simple addition example

Using this notation, we can now reason about the behavior of functions on differential values. We start with 1-bit addition as basic exercise to the reader. Consider a matrix with two input rows and one output row. The values of the first two rows are added such that the bit difference at the third row is created.

**Figure 3.2:** A simple 1-bit addition example: On the left the differential characteristic is given. Two dashes, by definition, denote a missing difference in both arguments. The result of the addition must never show a difference. This yields eight possible bit configurations where two values close to each other denote  $(M, M^*)$  of Figure 3.1. Due to the behavior of addition, we know that configurations 2, 3, 5 and 8 (from left to right) are invalid.

Figure 3.2 illustrates this example. Remember that symbols such as – and 0 underlie semantics defined in Table 3.2. It is also interesting to see how propagation of values can work. In Figure 3.3 we see how an underspecified value? can be strengthened once we have checked which values can be taken. Recognize that the system is constrained by the function in use and the definition of the differential symbols.

**Figure 3.3:** Like Figure 3.2, but any difference value for the result bit is possible. As such we consider any possible bit configuration, but eventually recognize that only four bit configurations are consistent with the behavior of addition. Because all resulting configurations show no bit difference in the output bit, we can strengthen? by replacing it with -. This illustrates how knowledge about differential states can be propagated.

Finally, we can extend our testcases to 4 bits and retrieve testcases such as Figures 3.4 and 3.5.

A:	0011	A:	x	A:	x	A:	x
B:	0101	B:	x	B:	x	B:	x
S:	1000	S:	????	S:	???-	S:	x???
	A:	0011	A:	x	A:		
	B:	0101	B:	x	B:	x	
	S:	0000	S:	???x	S:	x-??	

**Figure 3.4:** Testcases for 4-bit addition: The upper line shows valid differential characteristics for 4-bit addition whereas the lower line show invalid ones for 4-bit addition. The rows are conventionally named using capital letters.

A:		A:	7C-3	A:	0uCD
S:	0000	S:	-3u?	S:	ADC7
	A:	x	A:	XXXX	
	S:	0000	S:	0000	

**Figure 3.5:** Differential characteristics for the SHA-2 Sigma function. The upper line shows valid states. The lower line shows invalid ones.

## 3.5 Differential characteristics in action

In the previous section, we illustrated how propagation with differential values works and how differential characteristics are written down. It is always important to keep in mind which function the characteristic illustrates, because this is not documented with the characteristic.

Now consider MD<sub>4</sub> as defined in Section 2.2. MD<sub>4</sub> takes some input message (in our case limited to size of one block), the state variables are initialized and iteratively new  $A_i$  are computed.

Similarly, SHA-256 takes a message block M and initializes eight variables with an initial vector (IV). The remaining  $W_i$  are computed and iteratively, values  $A_i$  and  $E_i$  are computed.

Those values are structured in differential characteristics illustrated in Figure 3.6. Those layouts are used to specify our hash collisions we want to evaluate. Table 3.5 also gives an application of the layout.

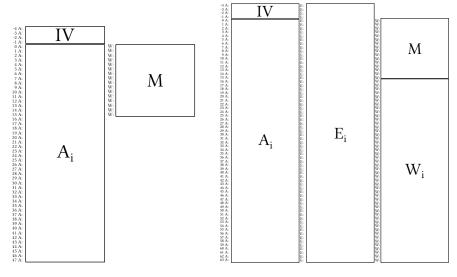


Figure 3.6: Layout of MD4 (left) and SHA-256 (right) differential characteristics

_						_	_			
i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$		i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001				-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110				-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101011011100111111110				-2	A:	100110001011101011011110011111110		
-1	A:	111011111100110110101011110001001				-1	A:	1110111111100110110101011110001001		
0	A:	01101011110101001110010000010010	W:	01001101011110101001110010000011		0	A:	01101011110101001110010000010010	W:	01001101011110101001110010000011
1	A:	01110110010011111111011100u110001	W:	u1010110110010111001001001111010		1	A:	01110110010011111111011100u110001	W:	u1010110110010111001001001111010
2	A:	101010110100000001110u01n1110010	W:	n01n10011101010110100101011111000		2	A:	101010110100000001110u01n1110010	W:	n01n10011101010110100101011111000
3	A:	101011u1001111010101001001010001	W:	01010111101001111010010111101110		3	A:	101011u1001111010101001001010001	W:	01010111101001111010010111101110
4	A:	001011000110001101010101111110010	W:	11011110011101001000101000111100		4	A:	001011000110001101010101111110010	W:	11011110011101001000101000111100
5	A:	000110100110001010u1101000000001	W:	11011100110000110110011010110011		5	A:	000110100110001010u1101000000001	W:	11011100110000110110011010110011
6	A:	0001101100unuu110001000001111010	W:	777777777777777777777777777777777		6	A:	0001101100unuu110001000001111010	W:	10110110100000111010000000100000
7	A:	00101011100000010unn011001010000	W:	00111011001010100101110110011111		7	A:	00101011100000010unn011001010000	W:	00111011001010100101110110011111
8	A:	77777777777777777777777777777777	W:	11000110100111010111000110110011		8	A:	011100110010001u11111111110110000	W:	11000110100111010111000110110011
9	A:	777777777777777777777777777777777	W:	11111001111010011001000110011000		9	A:	101011n01unnu0001111100110011111	W:	11111001111010011001000110011000
10	A:	10n0010010000101?????????????110	W:	110101111100111111100000000010111110		10	A:	10n00100100001010100000010101110	W:	110101111001111110000000001011110
11	A:	u100011010110110?????????????111	W:	101001100011101110110010111101000		11	A:	u10001101011011001001010111111111	W:	101001100011101110110010111101000
12	A:	001011u00u101011?????????????011	W:	010001011101110n1000111000110001		12	A:	001011u00u101011111111100011111011	W:	010001011101110n1000111000110001
13	A:	10un1n0100110001?????????????101	W:	100101111110001100011111111100101		13	A:	10un1n01001100010100000111100101	W:	100101111110001100011111111100101
14	A:	0000101001010001110	W:	001001111001010010111111100001000		14	A:	00001010010100011000100011010110	W:	001001111001010010111111100001000
15	A:	0001111010101u01100	W:	10111001111010001100001111101001		15	A:	0001111010101u010110011011010100	W:	10111001111010001100001111101001
16	A:	n00n0un011010010111				16	A:	n00n0un0110100101001101101011111		
17	A:	0001111100111010110				17	A:	000111110011101000010010000011110	1	
18	A:	0101011100001101100			l i	18	A:	01010111000011010000000010010100	l	
19	A:	u1n1000000010111100				19	A:	u1n10000000101111001101011000100		
20	A:	n1un1001111111011101000000110100			l i	20	A:	n1un10011111111011101000000110100	l	
21	A:	111100111011000001011111111010100			⇒	21	A:	111100111011000001011111111010100		
22	A:	01011101110011010011001100111010				22	A:	01011101110011010011001100111010		
23	A:	01010000111011101100011110001111				23	A:	01010000111011101100011110001111		
24	A:	00000010000100100011011100011010				24	A:	00000010000100100011011100011010		
25	A:	10110000100101100001010011101010				25	A:	10110000100101100001010011101010	1	
26	A:	00001010100010010111011101000001				26	A:	00001010100010010111011101000001		
27	A:	00000110111011110101101010110011				27	A:	00000110111011110101101010110011		
28	A:	10110110010111010110110000100101				28	A:	10110110010111010110110000100101		
29	A:	10100010000011010100100001101001				29	A:	10100010000011010100100001101001		
30	A:	00101001110101111100011101100011				30	A:	00101001110101111100011101100011		
31	A:	111111001001001011010111110110110				31	A:	111111001001001011010111110110110		
32	A:	01001111110100100110100000101111				32	A:	01001111110100100110100000101111		
33	A:	00111000001111010110111011100100				33	A:	00111000001111010110111011100100		
34	A:	00100000011101011110100000010101				34	A:	00100000011101011110100000010101		
35	A:	n0100000001100110000010001110010				35	A:	n0100000001100110000010001110010		
36	A:	n00001111110101111011111001011001				36	A:	n00001111110101111101111001011001		
37	A:	11001000000110100100001100001100				37	A:	11001000000110100100001100001100		
38	A:	10110000011001111110100110101100				38	A:	10110000011001111110100110101100		
39	A:	00010010000010100001101100011100				39	A:	00010010000010100001101100011100		
40	A:	11000000010010000111000110000101				40	A:	11000000010010000111000110000101		
41	A:	00000110100001101111010100100110				41	A:	00000110100001101111010100100110		
42	A:	01001110110111011111111010000110				42	A:	010011101101110111111111010000110		
43	A:	01010000011000111101000001101101				43	A:	01010000011000111101000001101101		
44	A:	11111000000101101111011100001100				44	A:	11111000000101101111011100001100		
45	A:	10001010110110110010110000000100				45	A:	10001010110110110010110000000100		
46	A:	100000101001100101100011011100				46	A:	1000001010011001011100011011100		
47	A:	10000001111001011011010010111101				47	A:	100000011110010110110100101111101		

Table 3.5: One of the original MD4 collisions by Wang et al, with a few bits underspecified (left) and propagated values (right). The question marks indicate that any bit configuration for the two bits are possible. Dashes indicate that the bits have the same configuration in both instances, but the value itself is unknown. However, it turns out the description with missing values in iteration 6 (message) and iterations 8–19 is complete enough such that missing values can be deduced by other values and the description of the algorithm. A collision is given in the last 4 rounds, because no differences are left as they cancel out after round 36.



"What idiot called them logic errors rather than bool shit?" —Unknown

## Chapter 4

## Satisfiability

Boolean algebra allows us to describe functions over two-valued variables. Satisfiability is the question for an assignment such that a function evaluates to true. Satisfiability problems are solved by SAT solvers. We discuss the basic theory behind satisfiability. Because any computation can be represented as satisfiability problem, we are able to verify whether an algorithm can reach a certain state. In Chapter 6, we will represent a differential cryptanalysis problem such that it is solvable iff the corresponding SAT problem is satisfiable.

## 4.1 Basic notation and definitions

## Definition 4.1 (Boolean function)

A Boolean function is a mapping  $h: X \to Y$  with  $X = \{0,1\}^n$  for  $n \in \mathbb{N}_{\geq 1}$  and  $Y = \{0,1\}$ .

## Definition 4.2 (Assignment)

A *k*-assignment is an element of  $\{0,1\}^k$ .

Let f be some k-ary Boolean function. An assignment for function f is any k-assignment.

### Definition 4.3 (Truth table)

Let f be some k-ary Boolean function. The *truth table of Boolean function* f assigns truth value 0 or 1 to any assignment of f.

$x_1$	$x_2$	$f(x_1,x_2)$	$x_1$	$x_2$	$f(x_1,x_2)$	$\boldsymbol{x}$	$\int f(x)$	
1	1	1	1	1	1	1	0	
1	0	0	1	0	1	0	1	
0	1	0	0	1	1	(6	(c) NOT	
0	0	0	0	0	0	`	,	
	(A	) AND		(E	s) OR			

TABLE 4.1: Truth tables for AND, OR and NOT

Boolean functions are characterized by their corresponding truth table.

Table 4.1 shows example truth tables for the Boolean AND, OR and NOT functions. A different definition of the three functions is given the following way:

#### **Definition 4.4**

Let AND, OR and NOT be three Boolean functions.

- AND maps  $X = \{0, 1\}^2$  to 1 if all values of X are 1. OR maps  $X = \{0, 1\}^2$  to 1 if any value of X is 1.
- NOT maps  $X = \{0, 1\}^1$  to 1 if the single value of X is 0.

All functions return 0 in the other case. Those functions are denoted  $a_0 \wedge a_1$ ,  $a_0 \lor a_1$  and  $\neg a_0$  respectively, for input parameters  $a_0$  and  $a_1$ .

It is interesting to observe, that any Boolean function can be represented using only these three operators. This can be proven by complete induction over the number of arguments *k* of the function.

Let k = 1. Then we consider any possible 2-assignment for one input variable  $x_1$  and one value of  $f(x_1)$ . Then four truth tables are possible listed in Table 4.2. The description shows the corresponding definition of f using AND, OR and NOT only.

Now let *g* be some *k*-ary function. Let  $(a_0, a_1, ..., a_k)$  be the *k* input arguments to g and  $x_1 := g(a_0, a_1, \dots, a_k)$ . Then we can again look at Table 4.2 to discover that 4 cases are possible: 2 cases where the return value of our new (k + 1)-ary function depends on value  $x_1$  and 2 cases where the return value is constant.

This completes our proof.

Table 4.2: Unary f and its four possible cases

Boolean functions have an important property which is described in the following definition:

## **Definition 4.5**

A Boolean function f is *satisfiable* iff there exists at least one input  $x \in X$  such that f(x) = 1. Every input  $x \in X$  satisfying this property is called *model*.

The corresponding tool to determine satisfiability is defined as follows:

#### **Definition 4.6**

A *SAT solver* is a tool to determine satisfiability (SAT or UNSAT) of a Boolean function. If satisfiability is given, it returns some model.

## 4.1.1 Computational considerations

The generic complexity of SAT determination is given by  $2^n$  for n Boolean variables.

Let n be the number of variables of a Boolean function. No known algorithm exists to determine satisfiability in polynomial runtime. This means no algorithm solves the SAT problem with runtime behavior which depends polynomially on the growth of n. However, SAT solvers can take advantage of the problem's description. For example, consider function f:

$$f(x_0, x_1, x_2) = x_0 \land (\neg x_1 \lor x_2) \tag{4.1}$$

Instead of trying all possible 8 cases for 3 Boolean variables, we can immediately see that  $x_0$  is required to be 1. So we don't need to test  $x_0 = 0$  and can skip 4 cases. This particular strategy is called *unit propagation*.

#### 4.1.2 SAT competitions

SAT research is heavily concerned with finding fast heuristics determining (un)satisfiability. Biyearly, SAT competitions [30] take place to challenge SAT solvers in a set of benchmarks. The committee evaluates the most successful SAT solvers defined by solving the most problems within a given time frame.

In 2014, lingeling by Armin Biere has won first prize in the Application benchmarks track and second prize in the Hard Combinatorial benchmarks track for SAT and UNSAT instances, respectively. Its parallelized sibling plingeling and Cube & Conquer sibling treengeling have won prizes in parallel settings. And in the most recent 2016 competition lingeling has won bronze in the Main track for SAT+UNSAT instances.

In Chapter 7, we will discuss runtime results shown by (but not limited to) those SAT solvers.

## 4.2 The DIMACS de-facto standard

### **Definition 4.7**

A SAT problem is given in *Conjunctive Normal Form* (CNF) if the problem is defined as conjunction of disjunctions of literals.

A *conjunction* is a sequence of Boolean functions combined using a logical AND. A *disjunction* is a sequence of Boolean functions combined using a logical OR. A *literal* is a Boolean variable (*positive*) or its negation (*negative*).

A simple example for a SAT problem in CNF is the exclusive OR (XOR). It takes two Boolean values a and b as arguments and returns true if and only if the two arguments differ:

$$(a \lor b) \land (\neg a \lor \neg b) \tag{4.2}$$

It consists of one conjunction (denoted  $\land$ ) of two disjunctions (denoted  $\lor$ ) of literals (denoted a and b where prefix  $\neg$  represents negation). This structure constitutes a CNF.

Analogously we define a *Disjunctive Normal Form* (DNF) as disjunction of conjunctions of literals. The negation of a CNF is in DNF, because literals are negated and conjunctions become disjunctions, vice versa.

## Theorem 4.1

Every Boolean function can be represented as CNF.

Theorem 4.1 is easy to prove. Consider the truth table of an arbitrary Boolean function f with k input arguments and j rows of output value false. We represent f as CNF.

Consider Boolean variables  $b_{i,l}$  with  $0 \le i \le j$  and  $0 \le l \le k$ . For every row i of the truth table with assignment  $(r_i)$ , add one disjunction to the CNF. This disjunction contains  $b_{i,l}$  if  $r_{i,l}$  is false. The disjunction contains  $b_{i,l}$  if  $r_{i,l}$  is true.

As far as f is an arbitrary k-ary Boolean function, we have proven that any Boolean function can be represented as CNF.

SAT problems are usually represented in the DIMACS de-facto standard. Consider a SAT problem in CNF with *nbclauses* clauses and enumerate all variables from 1 to *nbvars*. A DIMACS file is an ASCII text file. Lines starting with "c" are skipped (comment lines). The first remaining line has to begin with "p cnf" followed by *nbclauses* and *nbvars* separated by spaces (header line). All following non-comment lines are space-separated indices of Boolean variables optionally prefixed by a hyphen. Then one line represents one clause and must be terminated with a zero character after a space. All lines are conjuncted to form a CNF.

Variations of the DIMACS de-facto standard also allow multiline clauses (the

zero character constitutes the end of a clause) or arbitrary whitespace instead of spaces. Another variant terminates DIMACS files once it encounters a single percent sign on a line. The syntactical details are individually published on a per competition basis.

LISTING 4.1: CNF of the XOR in Display (4.2)

```
p cnf 2 2
a b
-a -b
```

## 4.3 Terminology

Given a conjunctive structure of disjunctions, we can define terms related to this structure. Those terms will be used in the SAT features we present in Section 5.4.

### **Definition 4.8**

A *clause* is a disjunction of literals. A k-clause is a clause consisting of exactly k literals. A *unit clause* is a 1-clause.

A *Horn clause* is a clause with at most one positive literal. A *definite clause* is a clause with exactly one positive literal. A *goal clause* is a clause with no positive literal.

### **Definition 4.9**

Given a literal, its *negated literal* is the literal with its sign negated. A literal is *positive*, if its sign is positive. A literal is *negative* if its sign is negative.

An *existential literal* is a literal which occurs exactly once and its negation does not occur. A *used variable* is a variable which occurs at least once in the CNF.

The *literal frequency* is the number of occurences of a literal in the CNF divided by the number of clauses declared. Equivalently *variable frequency* defines the number of variable occurences divided by the number of clauses declared.

### **Definition 4.10**

The *clause length of a clause* is the number of literals contained. A clause is called *tautological* if a literal and its negated literal occurs in it.

A few basic properties hold in terms of satisfiability. For example, existential literals are interesting, because they can be set to true and make one clause immediately satisfied without influencing other clauses.

## 4.4 Basic SAT solving techniques

### **Definition 4.11**

Given two CNFs *A* and *B*, they are called *equisatisfiable* iff *A* is satisfiable iff *B*.

## 4.4.1 Boolean constraint propagation (BCP)

One of the most basic techniques to SAT solving is *Boolean Constraint Propagation*, also called *unit propagation*. It is so fundamental that SATzilla, introduced in Section 5.2, applies it immediately before looking at SAT features.

Let l be the literal of a unit clause in a CNF. Remove any clause containing l and replace any occurences of -l from the CNF. It is easy to see, that the resulting CNF is equisatisfiable, because due to the unit clause l must be true. So any clause containing l is satisfied and -l yields false, where ( $A \lor$  false) is equivalent to (A) for any Boolean function A.

#### 4.4.2 Watched Literals

Watched Literals are another fundamental concept in SAT solving. It is very expensive to check satisfiability of all clauses for every assigned value of a literal. Watched Literals is a neat technique to reduce the number of checks.

In each clause two unassigned literals are declared to be "watched". Structurally it is implemented the other way around: A clauses watch list is maintained per literal. Now as long as at least two literals are unassigned, the clause cannot become false (recognize that a clause is false iff all literals are false). Therefore the clause does not need to be visited as long as at least one unassigned literal exist. This implies the following decision procedure:

- If all but one literal is false, propagate the remaining literal to be true.
- If all literals are false, report UNSAT.
- If any literal becomes true, watched literals do not change.
- Else replace the literal on the watch list with a remaining unassigned literal.

This empirical approach was established with the Chaff and zChaff SAT solvers [19] and has proven useful in various variants.

## 4.4.3 Remark

The previous two techniques illustrate basic approaches, but actual SAT solving research requires decades of development to tune individual SAT solvers. Memory models and concurrency strategies lead to fundamentally different runtime behaviors of SAT solvers.

As such, an initial idea to initiate an individual SAT solver specifically designed for solving problems in differential cryptanalysis was dropped, because development time is expected too long for a master thesis to be fruitful. As such we focused on popular and established SAT solvers of the SAT community.

## 4.5 SAT solvers in use

In this thesis we considered several SAT solvers. They have been selected either by their popularity or their good results at previous SAT competitions:

- MiniSat 2.2.0
- CryptoMiniSat versions 4.5.3 and 5
- treengeling, lingeling and plingeling, in versions:
  - lingeling ats1
  - lingeling ats101
  - lingeling ats102
  - lingeling ats104
  - lingeling baz
- glucose version 4.0 and glucose syrup version 4.0

This means the hash collision attacks we implemented have run with these SAT solvers. The results are discussed in Chapter 7 and a more comprehensive list is provided in Appendix C.

MiniSat is known as "Swiss army knife of SAT solving" meaning that it includes many well-established techniques that can be built upon. SAT competitions 2009, 2011, 2013 and 2014 included a special MiniSat "hack track" where participants are asked to modify MiniSat to prove the best performance with as little change to the MiniSat codebase as possible. Even though is not one of the fastest SAT solvers today, it provides a nice codebase to experiment with.

CryptoMiniSat is a derivative of MiniSat, which was originally modified for cryptographic problems. It features XOR clauses meaning that binary clauses of

structure  $a \oplus b$  could be added and will be resolved using Gaussian elimination. Please recognize that our encoding introduced in Section 6.2 uses equivalence to model assignment and as such only clauses of structure  $r = a \oplus b$  emerge rendering this feature impractical to use.

Glucose was the gold winner 2011 in the SAT+UNSAT application track. Modifications of glucose also ranked high throughout the years of SAT competition. Glucose is a sequential SAT solver whereas glucose syrup is its parallelized version.

Lingeling is SAT solver developed by Armin Biere. Lingeling has been the winner of several tracks in the SAT competitions 2011 to 2016. For example, it has won gold in the SAT+UNSAT application track in 2014. Lingeling has two siblings: plingeling and treengeling. plingeling is a parallelized version of lingeling. As such it executes in multiple threads and shares units and equivalences between those instances. treengeling is a Cube & Conquer solver meaning it partitions the problem into many subproblems and solves them individually.

Lingeling releases ats101, ats102 and ats104 are non-public, experimental releases of lingeling. They have been developed in private communication with Armin Biere. Our main goal was to achieve a separation between two sets of variables. First, all variables of the first need to be assigned in the best possible way. Afterwards, the second set of variables is considered. Specifically variables modelling the differences between the two hash algorithm instances should constitute the first set as discussed in Chapter 6.

Lingeling ats101 implements the strategy to guess difference variables first (with Boolean value false) and usual heuristics apply for all other variables. Our intermediate results with incomplete CNF files showed a high number of restarts. Therefore ats102 disables backjumping and therefore skips decisions for important variables. Finally ats104 is not expected to distinguish from ats102. It only provides further debugging information.

The SAT solvers have generally been run without any special options and several times, except for

- MiniSat was run with pre=once as it is generally recommended to run with the builtin preprocessor.
- Lingeling has been generally run with phase=0 per default and phase=-1
  to prefer false as initial assignment to literals. However, lingeling ats101
  implements this with a more forceful strategy.

Preprocessing is a difficult topic on its own. Sometimes preprocessing can provide a speedup, before actually solving the problem, but mostly SAT solvers implement preprocessing strategies themselves and run them repeatedly when solving the problem. Chapter 7 presents runtime results for that issue.



"To be usable effectively [...] these features must be related to instance hardness and relatively cheap to compute"

—SATzilla

## **Chapter 5**

## **SAT** features

At the very beginning I was very intrigued by the question "What is an 'average' SAT problem?". Answers to this question can help to optimize SAT solver memory layouts. Specifically for this thesis I wanted to find out whether our problems distinguish from "average" problems in any way such that we can use this distinction for runtime optimization.

I came up with 8 questions related to basic properties of SAT problems we will discuss in depth in this section. We will characterize an average SAT problem at Section 5.7:

- 1. Given an arbitrary literal. What is the percentage it is positive?
- 2. What is the clauses / variables ratio?
- 3. How many literals occur only once either positive or negative?
- 4. What is the average and longest clause length among CNF benchmarks?
- 5. How many Horn clauses exist in a CNF?
- 6. Are there any tautological clauses?
- 7. Are there any CNF files with more than one connected variable component?
- 8. How many variables of a CNF are covered by unit clauses?

We will now define the terms used in those questions.

## 5.1 Definition

## Definition 5.1 (SAT feature)

A *SAT feature* is a statistical value (named *feature value*) retrievable from some given SAT problem.

The most basic example of a SAT feature is the number of variables and clauses of a given SAT problem. This SAT feature is stored in the CNF header of a SAT problem encoded in the DIMACS format.

The general goal is to write a tool which evaluates several SAT features at the same time and retrieve them for comparison with other problems. Therefore it should be computationally easy to evaluate SAT features of a given SAT problem. A suggested computational limit is given with polynomial complexity in terms of number of variables and number of clauses for memory as well as runtime for evaluation algorithms. Sticking to this convention implies that evaluation of satisfiability must not be necessary to evaluate a SAT feature under the assumption that  $\mathcal{P} \neq \mathcal{NP}$ . Hence the number of valid models cannot be a SAT feature as far as satisfiability needs to be determined. But no actual hard computational limit is defined.

## 5.2 Related work

The most similar resource I found looking at SAT features was the SATzilla project [22, 36] in 2012. The authors systematically defined 138 SAT features categorized in 12 groups. Some features are only evaluated conditionally. The features themselves are not defined formally, but an implementation is provided bundled with example data. The following list provides an excerpt of the features:

nvarsOrig number of variables defined in the CNF header

**nvars** number of active variables

reducedVars nvarsOrig - nvars, divided by nvars

vars-clauses-ratio nvars divided by number of active clauses

**POSNEG-RATIO-CLAUSE-mean** mean of  $2 \cdot ||0.5 - pos/length||$  where pos is the number of positive literals and length clause length of a specific clause

**POSNEG-RATIO-CLAUSE-entropy** like POSNEG-RATIO-CLAUSE-mean but entropy

TRINARY+ number of clauses with clause length 1, 2 or 3 divided by number of active clauses

**HORNY-VAR-min** minimum number of times a variable occurs in a Horn clause

**cluster-coeff-mean** let neighbors of a clause be all clauses containing any literal negated and let clauses  $c_1$  and  $c_2$  be conflicting if  $c_1$  contains literal l and  $c_2$  contains -l, then return the mean of 2 times the number of conflicting neighbors of a clause c divided by the number of unordered pairs of neighbors, returned iff computable within 20 seconds for all clauses

Please recognize that active clauses are the unsatisfied clauses after BCP has been applied. Equivalently active variables are remaining variables after application of BCP.

Many SAT solvers collect feature values to improve algorithm selection, restart strategies and estimate problem sizes. Recent trends to apply Machine Learning to SAT solving imply feature evaluation. SAT features and the resulting satisfiability runtime are used as training data for Machine Learning. One example using SAT features for algorithm selection is ASlib [1].

The SAT solvers of Section 4.5 we use also compute features they use when computing a solution. For example, CryptoMiniSat 4.5.3 prints the following lines

```
c [features] numVars 56118, numClauses 358991, var_cl_ratio 0.156,
binary 0.019, trinary 0.520, horn 0.387, horn_mean 0.000, horn_std
0.000, horn_min 0.000, horn_max 0.000, horn_spread 0.000,
vcg_var_mean 0.000, vcg_var_std 0.902, vcg_var_min 0.000,
vcg_var_max 0.000, vcg_var_spread -0.000, vcg_cls_mean 0.000,
```

Even though we will partially use equivalent features (like Horn clauses), many are actually related to the current state of evaluation like decisions per conflicts. We consider this as a property of the evaluation and not the SAT problem itself.

### 5.3 Statistical features

For our SAT features we need to define some basic statistical terminology. Let  $x_1, x_2, ..., x_n$  be a finite sequence of numbers  $(n \in \mathbb{N})$ .

**Arithmetic mean** (or short: mean) is defined as

$$\overline{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

**Standard deviation** (or short: sd) with mean  $\overline{x}$  is defined as

$$\sigma(x) = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \overline{x})}$$

**Median** with  $x_1 \le x_2 \le ... \le x_n$  (i.e. sorted ascendingly) is defined as

$$m = \begin{cases} x_{\text{mid}} & \text{if } n \text{ odd} \\ \frac{x_{\text{mid}} + x_{\text{mid}+1}}{2} & \text{if } n \text{ even} \end{cases} \text{ with mid} = \frac{n}{2}$$

and often considered more "robust" than the arithmetic mean.

**Entropy** is defined according to Claude Shannon's information theory:

$$H(x) = -\sum_{i=1}^{n} x_i \cdot \log_2(x_i)$$

where  $0 \cdot log_2(0) := 0$ .

Furthermore *count* refers to the number of elements n, *largest* refers to the maximum element  $\max_{1 \le i \le n} (x_i)$  and *smallest* refers to the minimum element  $\min_{1 \le i \le n} (x_i)$ .

### 5.4 Suggested SAT features

We wrote a tool called cnf-analysis. The evaluated features are partially inspired by SATzilla and lingeling. The latter prints basic statistics for every CNF it evaluates.

A summary of our suggested SAT features is given:

#### clause variables sd mean

mean of sd of variables in a clause

#### clauses\_length\_(largest, smallest, mean, median, sd)

statistics related to the clause length

### connected\_(literal, variable)\_components\_count

two literals (variables) are connected if they occur in some clause together, count the number of connected components

#### definite\_clauses\_count

number of definite clauses in the CNF

### existential\_literals\_count

number of existential literals in the CNF

### existential\_positive\_literals\_count

number of positive, existential literals in the CNF

### (false, true)\_trivial

is the CNF satisfied if all variables are claimed to be false (true)?

#### goal\_clauses\_count

number of goal clauses in the CNF

#### literals count

number of literals in the CNF (i.e. sum of clause lengths)

### literals\_frequency\_k\_to\_k + 5

let  $n_l$  be the literal frequency of literal l, count the number of  $n_l$  satisfying  $\frac{k}{100} \le n_l < \frac{k+5}{100}$  where k is a variable in  $\{0, 5, 10, \dots, 90, 95\}$  and k = 95 counts  $\frac{k}{100} \le n_l \le \frac{k+5}{100}$ .

### literals\_frequency\_(largest, smallest, mean, median, sd)\_entropy

statistics related to literal frequencies

#### literals\_occurence\_one\_count

number of literals with occurence 1

**nbclauses**, **nbvars** number of clauses (variables) as defined in the CNF header

### negative\_literals\_in\_clause\_(smallest, largest, mean)

statistics related to number of negative literals in clauses

### (positive, negative)\_unit\_clause\_count

number of unit clauses with a positive (negative) literal

#### positive literals count

number of positive literals in CNF

#### positive literals in clause (largest, smallest, mean, median, sd)

statistics related to number of positive literals in clauses

#### positive\_negative\_literals\_in\_clause\_ratio\_(mean, entropy)

let  $r_c$  be the number of positive literals divided by clause length of clause c, mean and related of all  $r_c$ 

#### positive negative literals in clause ratio mean

mean of all  $r_c$ 

### tautological\_literals\_count

number of clauses which contain a tautological literal

### two\_literals\_clause\_count

number of clauses with two literals

### variables\_frequency\_k\_to\_k + 5

same as literals\_frequency\_k\_to\_k + 5 but for variables

### variables\_frequency\_(largest, smallest, mean, median, sd, entropy)

same as literals frequency but for variables

### variables\_used\_count

number of variables with occurence greater o

### 5.5 Evaluation efficiency

The resource requirements of those features have been classified:

**Type 1** read the files as bytestring, a DIMACS CNF parser is not necessary, constant memory is used

Type 2 features understand what a clause is, but still need constant memory

Type 3 subquadratic runtime and linear memory

Type 4 unrestricted

Memory and runtime is always considered in comparison with the filesize.

This classification should support future considerations regarding feature evaluation tools. The suggested SAT features above have been explicitly selected to avoid Type 4 implementations to limit the time to compute features. Furthermore tools evaluating only a subset of features (like Type 2 features) with better performance characteristics.

The Python implementation triggered MemoryErrors on a computer with 4 GB RAM for a 770 MB CNF file. Followingly a much more efficient Go implementation was implemented which requires much less memory and is much faster. bench\_573.smt2.cnf took 1 second in Go instead of 2 minutes in Python. However, the data evaluated is less accurate compared to Python, because Python unlike Go provides a nice implementation of statistical tools in the standard library. Go algorithms were written on our own.

In the following section, we define the dataset we consider.

### 5.6 CNF dataset

To evaluate CNF features of a representative set of CNF files, it was necessary to identify equivalent CNF files in the best possible way. Therefore we defined

a hashing algorithm standardizing the CNF input provided to a SHA1 instance. Every CNF file is identifiable by its "cnfhash 2.0.0" hash value.

In the next step a complete set of CNF files of previous SAT competitions was collected. The following CNF file collections have been considered:

• SAT Race 2008

• SAToo Competition

• SAT-Race 2010

• SAT11 Competition

• SAT Challenge 2012

• SAT Competition 2013

• SAT Competition 2014

• SAT-Race 2015

• SAT Competition 2016

• SATlib

The benchmarks are mostly contributed by the participants of the associated conferences. Others are reused from previous years. Individual projects allow to generate CNF files for specific problems in a selectable problem size; such as CNFgen [13] by Massimo Lauria.

Some files turned out to be problematic. In SATlib, 3 gzipped files couldn't be decompressed and several files contain empty clauses. Empty clauses are assumed to immediately falsify the CNF and are therefore pointless. I removed trailing zeros in CNFs. Variants of the DIMACS standard also expect lines with a percent symbol to terminate the CNF. Besides those minor issues documented as part of the cnf-analysis project, 175 gigabytes of CNF files have been evaluated with a total of 68,069 CNF files (62,251 unique CNF files).

### 5.7 The average SAT problem

#### Claim 5.1

The set of public benchmarks in SAT competitions between 2008 and 2015 represent average SAT problems

It is important to point out that public benchmark files are specifically chosen to be evaluated before a conference is held. Hence they are expected to terminate within a given time frame and are therefore not oversized. On the one hand this ensures that the problems are feasible, but on the other hand they might be a biased selection. At this point no better data set is available and therefore we proceeded with this dataset.

According to my results, an average SAT problem consists of:

• 83,542 clauses in average ranging from 21 to 53,616,734 (median = 430,  $\sigma$  = 848388)

- The longest clause we found had 61,473 literals, but the longest clause of an average CNF covers 20 literals.
- The number of total literals in a CNF ranges from 60 up to 150,609,758.
- The clause-variables ratio lies between 1.22 and 27,720 with mean = 9.54 and  $\sigma$  = 139.
- The average length of a clause is expected to be 3. The largest clause length mean we found was 19.58 compared to 2.83 as the smallest clause length mean.
- Surprisingly, in average a CNF file has 205 connected literal components and 53 connected variable components. However both corresponding medians are 1 meaning that at least have of the problems still have only one component.
- In average 32,787 clauses are definite clauses and 35,094 clauses are goal clauses.
- In average a literal occurs in 1.4 % of the clauses of the CNF.
- 47 % of literals in a clause are positive.
- The arithmetic mean tells 124 unit clauses per CNF file can be expected, but the median tells it is mostly o.
- The largest variable found was 13,842,706 and 13,829,558 variables were used at most.
- Exactly one CNF file was true-trivial (namely dubois/dubois100.cnf of SATlib) whereas 13 CNF files were false-trivial (of SAT competition 2014 and SAT-Race 2015).

### 5.8 Benford's law in CNF files

Given this huge set of CNF files and therefore integers, we evaluated whether Benford's law holds.

A paper by Theodore P. Hill [8] characterizes Benford's Law as the following conjecture:

#### Theorem 5.1

Consider arbitrary data from tables, listings or other sources in publications, newspaper and so on and so forth, the digit 1 occurs in about 30 % of the time. The first digit is 1 about 30 percent of the time and 9 only about 4.6 percent of the time.

We evaluated that the leading digits 1 to 9 occur with probabilities 28.76 %, 19.09 %, 13.56 %, 10.97 %, 7.48 %, 5.76 %, 5.12 %, 4.79 % and 4.46 % respectively. We concluded that:

Considering a deviation of 1.34% for digit 1 (expected 30.1, actual 28.76) and 0.12% for digit 9 (expected 4.58, actual 4.46), we claimed the CNF files considered satisfy Benford's law.



"There is concensus that encoding techniques usually have a dramatic impact on the efficiency of the SAT solver"

—Magnus Björk

# **Chapter 6**

# **Problem encoding**

We already discussed how SAT solvers work and which input they take. We also sketched how hash algorithm properties got broken using differential cryptanalysis. In this section we combine those subjects and describe how we designed an attack setting.

We designed a basic prototype with the STP SMT solver. Followingly we wanted to tweak the CNF used by the SAT solver and wrote our own library *algotocnf* to generate CNFs for differential purposes; as illustrated in Section 3. There we distinguished 5 different tweaks. We evaluate the performance of those tweaks in Chapter 7.

Every section represents a major approach whereas subsections represent derivatives of this approach with minor tweaks.

### 6.1 Basic approach

Our first approach started with Simple Theorem Prover (STP) [7] initially written by Vijay Ganesh and David L. Dill. It is currently maintained by Mate Soos.

STP is an SMT solver which allows to declare bitvectors. A bitvector is an array of Boolean variables providing high-level constructs such as additions or right-shift through an interface. Writing all clauses individually to model a hash algorithm is too cumbersome to be done in practice and STP simplifies this process. STP is recommendable as a tool to model arithmetic and bitwise functions.

First we wrote an implementation using the CVC language to model the MD4 hash algorithm. We provide a bitvector to the hash algorithm instance. When applying the corresponding arithmetic operations we generate expressions such as ASSERT(y = 0bin00000101); to model the assignment of a constant. Here the desired constant is assigned variable y, because of equivalence. y is required to have the constant after this expression as value. Whereas we generate the ASSERT statement, it is STP's task to generate the CNF formula and solve it with a SAT solver.

We take two hash algorithm instances and an additional bitvector diff for every pair of bitvectors (bv1, bv2) where bv2 represents the corresponding bitvector of the second hash algorithm instance to bv1. We claim ASSERT(diff = BVXOR(bv1, bv2)) to ensure that diff represents the difference between bv1 and bv2. Given the bitconditions for a bitvector from a differential characteristic, we require diff to enforce those particular differences. This corresponds to the idea of differential cryptanalysis introduces in Chapter 3.

It is now trivial to consider a differential characteristic such as Testcase B.1 and generate the corresponding CVC input for STP. STP solves this particular problem within a second. Testcase B.2 already provides a more complex example taking 40 minutes to solve. We used minisat as SAT solver in the backend, even though STP allows to exchange it for CryptoMiniSat which is a more modern and versatile SAT solver.

Even though STP allows to come to useful results pretty quickly, it seems cumbersome to model all hash algorithms in the CVC language. STP provides a python interface meaning that pure Python implementations of hash algorithms can be taken with little modifications to model the hash algorithm itself. We add code to declare the difference bitvectors diff and finally add the constraints resulting from the differential characteristic.

This interface switch introduces no significant performance difference.

As a next step, we wanted to improve the evaluation performance to tackle more difficult problems. We considered this design as a working prototype of a basic approach to be improved upon.

STP was not fruitful for our next goal, because we wanted to tweak the SAT design generated for the SAT solver and needed good control over the SAT encoding which we expected to have a major influence on the performance.

### 6.2 algotocnf

We implemented our own library *algotocnf* to achieve greater flexibility in SAT design.

#### 6.2.1 Two instances and its difference

Similar to STP, algotocnf generates a CNF for a given hash algorithm implementation. Besides modelling bitvectors, it also implements differential bitvectors which inherently handle the difference bitvectors diff which contain difference variables. It can also directly operate with differential characteristics. Similarly to STP, it implements arithmetic and bitwise operations.

We think *algotocnf* mainly differs from other SMT tools like STP because of its implementation of differential logic.

To model our CNF *algotocnf* implements the following strategy:

- 1. Take a differential characteristic and the hash algorithm as input.
- 2. Every bit is therefore represented as a Boolean variable. If you apply addition, operator overloading in python will ensure that clauses are generated to describe the addition consisting of XORs and MAJs. Every operation is modelled as assignment. Hence an operation operating on a few Boolean variables is equivalent to a single variable which represents the result. Equivalently other operations related to integers are implemented as well.
- 3. Constants used in the implementation are automatically converted to bitvectors with unit clauses.
- 4. After running the hash algorithm with bitvectors per instance, all constraints related to the hash algorithm are added.
- 5. Followingly the differential characteristic is read. Values such as  $A_i$  represent intermediate states of bitvectors. Therefore the corresponding bitvectors are looked up and equivalences with temporary bitvectors are added. Those temporary bitvectors are initialized with all constraints resulting from the bit conditions of this bitvector. In conclusion all constraints resulting from the differential characteristic are added.
- 6. Finally the SAT solver is called. The CNF was mostly solved on a cluster specified in Appendix A.
- 7. Afterwards the program is run again to create the exactly same problem instance and the solver's solution replaces symbolic values with actual Boolean values. The resulting differential characteristic is parsed backed and printed out as differential characteristic where expectedly many bit conditions have been strengthened.

When adding clauses resulting from the differential characteristic as constraints, the question arises how those bit conditions are encoded. Essentially, we

have only Boolean values available, but bit conditions tell constraints such as "a difference is given, but the actual value is unknown".

It seemed trivial to add a *difference variable* for every pair of Boolean values representing a bit in the two instances. Furthermore the difference variable  $\Delta x$  is connected by a XOR with the variables of the pair (x, x').

$$\Delta x = x \oplus x'$$

Therefore it should be trivial for a preprocessor to simplify the formula appropriately or actually we don't expect runtime differences for the larger amount of variables.

And finally we expect the CNF to inherit a property of hash functions. Inputs are provided into the hash algorithm and strongly intermingled with other values. This should result in a high diffusion and almost every variable is expected to share a clause with another variable.

The difference variables design corresponds to diff bit vectors in the STP and therefore designs the difference described in Chapter 3. The design decisions of this encoding are fundamental to the resulting runtime discussed in Chapter 7.

### 6.2.2 Adding the differential description

Using the approach in the previous section, we were able to find actual MD<sub>4</sub> collisions using a SAT solver (please refer to Section 7.2.1). A SHA<sub>256</sub> implementation followed which obviously lead to worse runtime results, because the internal state of SHA-<sub>256</sub> is much larger (by a factor of at least 2). Can we further improve the runtime of the SAT solver?

Because we work with bitvectors and apply high-level operations like MAJ or addition, we can additionally implement how differences in those operations propagate. Magnus Daum's thesis on "Cryptanalysis of Hash Functions of the MD4-Family" [4, Table 4.4] discusses how differences propagate in Boolean functions. Trivially, XORs propagate differences the way they are  $^1$ . Another example is MAJ: Let a,b and c be difference variables and MAJ is applied to both corresponding hash algorithm instances. r is the difference variable of the result. Then its differential behavior states that

$$(0,1,1) \implies 1 \qquad (0,0,0) \implies 0$$

where (IN)  $\implies$  OUT denotes an input-output relation. Because of this behavior we add clauses to explicit describe this behavior:

$$(\neg a \land b \land c) \implies r \iff a \lor \neg b \lor \neg c \lor r$$

<sup>&</sup>lt;sup>1</sup>A difference in the arguments of two XOR instances remains the same difference after applying XOR to each instance

We also model the second behavior:

$$(\neg a \land \neg b \land \neg c) \implies \neg r \iff a \lor b \lor c \lor \neg r$$

This approach explicitly models differentiable behavior, which should be deducible by the SAT solver itself based on the clauses we added before. However, this lead to a major speedup which can be observed in the runtime results of Chapter 7.

### 6.2.3 Evaluating difference variables first

#### Claim 6.1

Deriving difference values first, followed by actual bit values for the two instances, leads to a speedup.

This proposed principle is fundamental to differential cryptanalysis. A previous tool at our department implements propagation of hash algorithm values without a SAT solver and this strategy is essential to good performance. This strategy was introduced in the very early days of differential cryptanalysis and was also used by Wang et al. [35] to find their hash collisions.

So basically in terms of SAT solvers we want to guess values for difference variables first and once all have been assigned, we try to find actual values for the two hash algorithm instances.

It is important to point out that DIMACS does not specify a way to annotate Boolean variables. As such that SAT solver cannot distinguish between difference variables and variables of the instances. Therefore implementing this approach requires a custom SAT solver which is given with lingeling ats101.

Another claim is important for this approach:

#### Claim 6.2

Guessing difference values false first, followed by true, should solve hash collision problems faster.

This claim is justified by the desire to find as little differences as possible in a hash collision to increase the probability of values cancelling each other out in the later rounds.

### 6.2.4 A lightweight approach

In this tweak we made a step back and considered the ideas of the previous section but neglected the differential description. This approach was interesting to recognize the effect introduced by adding the differential description.

### 6.2.5 Influencing the evaluation order

To take the idea to influence the evaluation order to the next level, we enforced the evaluation order even stronger by applying the following SAT design:

Let  $\Delta x$  be the difference variable of pair (x, x'). We introduce a new Boolean

variable  $x^*$  called *preference variable*. We add clause

$$x^* = (\Delta x \wedge x)$$

and explicitly tell the SAT solver to guess on  $x^*$  before guessing on  $\Delta x$ , x or x'.

The SAT solver will assign x'=0 first, because of the evaluation order. So either  $\Delta x$  or x must be false.  $\Delta x$  is assigned false, because as difference variable it has a higher priority over x. Equivalently for x'=1 we have  $\Delta x$  needs to be true. So we actually achieve an early guess on the difference variable.



# Chapter 7

### Results

In Chapter 4, we discussed Boolean algebra; in particular we looked at satisfiability which is practically covered by SAT solvers. SAT solvers take Boolean functions in Conjunctive Normal Form and determine satisfiability. In Chapter 3, we looked at how we can analyze algorithms by looking at the progression of differences between algorithm instances. In particular, we looked at hash algorithms introduced in Chapter 2.

With this background, we designed an attack setting in Chapter 6 which enables us to verify and also find a hash collision given a differential characteristic as starting point. Our goal is to find hash collisions in practical time which we define by 1 day (86,400 seconds). Therefore, we designed several approaches to improve our runtime results.

In this section, we will evaluate those approaches. Furthermore, we briefly discuss claims we made about average SAT problems. In Section 5, we looked at SAT features which to some extent characterize a SAT problem.

### 7.1 Evaluating SAT features

In Chapter 5, we posed 8 questions. In the following, we want to answer them with the data provided by the cnf-analysis project.

**Given an arbitrary literal. What is the percentage it is positive?** We look at every clause and determine the ratio of positive to the total number of liter-

- als. We determine the mean per CNF file and the mean among all CNF files and retrieve a value of 0.48 meaning that 48 % of the literals are positive.
- What is the clauses / variables ratio? In average a CNF file has 12,219 variables and 89,541 clauses. Its clauses-variables ratio is 7.328.
- **How many literals occur only once either positive or negative?** In average there are 36 existential literals per CNF file, but its standard deviation of 967 is very large.
- What is the average and longest clause length among CNF benchmarks? The average clause length is 3.04 with a standard deviation of 0.99 and the longest clause length found was 61,473. Long clauses are typically outliers excluding specific assignments.
- **How many Horn clauses exist in a CNF?** In average 29,994 goal clauses and 31,315 definite clauses exist with an average number of 83,649 clauses in a CNF file.
- **Are there any tautological clauses?** In one file, 1679 tautological literals have been found. However, its mean is 0.07 with a standard deviation of 9.63 meaning that tautological clauses are very rare.
- Are there any CNF files with more than one connected variable component? Indeed, an average CNF file contains 67.07 connected variable components. However, its median is 1 implying that at least half of the CNF files have only 1 connected variable component.
- How many variables of a CNF are covered by unit clauses? In average 124 variables are covered by unit clauses. This is an insignificant number compared to 12,219 variables in an average CNF.

The clauses/variables ratio was thoroughly studied by the SAT community [23]. A strong correlation between the instance's hardness and the ratio of number of clauses to number of variables exists [32] though it is important to point out that this result holds for randomly generated SAT instances, which our testcases are not classified as.

Existential literals are interesting to discover, because they allow to remove a clause immediately. Consider a clause with literals  $(l_1, l_2, ..., l_n)$ . If a guarantee exists such that the variable of any literal  $l_i$  does not occur in any other clause, we can claim  $l_i$  true rendering the clause satisfied.

Tautological clauses trivially also render clauses satisfied.

Connected variable components are interesting, because they split the SAT problem into several small independent subproblems which can be solved in

parallel. Consider two sets of variables A and B. Now consider some clauses using only variables of A and some clauses using only variables of B. The overall CNF is satisfiable iff both clause sets are satisfiable. The overall CNF is falsifiable iff any clause set is falsifiable. Hence, if we know the connected variable components, we could easily create two parallel SAT solver instances and solve the problems independently. 4,607 out of 62,251 CNF files contained more than one connected variable component.

These features represent very fundamental properties of the SAT problem. But for us the question arises whether we can distinguish our cryptoproblems from average problems?

- We looked at 36 files classified as cryptographic problems. They are considered cryptographic, because their file or folder name indicated they are related to hash functions or general cryptographic applications like AES. The specific selection can be identified by the crypto tag annotated to these CNF files as part of the cnf-analysis project.
- In average these problems have 116,398 clauses and 27,407 variables. The average clauses-variables ratio is 5.58.
- The 36 cryptographic SAT instances give a standard deviation of 0.7 for clause length meaning that most clause lengths are close to the mean 3.4.
- The number of definite clauses is twice its value for general problems (62,457 versus 31,315) and the number of goal clauses is 26 % of its value for general problems (7,761 versus 29,994).
- The number of connected variable components is 2,236 in average ( $\sigma = 10,060$ ), but the median is 1 again.

No other value has been found to be significantly different from average problems (or its difference follows immediately by the non-uniform clause length).

The number of connected variable components seems interesting in cryptographic problem, because it might indicate diffusion in cryptographic problems. Diffusion means that variables strongly interact with many different variables due to the repetitive structure of cryptographic primitives. And finally the other differences can be explained by a certain SAT design which reoccurs in these testcases, because 36 is an exceptionally small number compared to 62,251 unique CNF problems. It is expected the cryptographic problems were designed by a small set of authors.

Comparing our average problem with cryptographic problems did not draw any useful conclusions. Particularly a more thorough discussion of the SAT designs might be more valuable than our high-level features. We now specifically look at a SAT design we are familiar with: Do average SAT problems distinguish from *our* CNF testcases?

• For all MD4 testcases we have the same number of variables, because the internal state of the hash algorithm instances are always the same size. However, adding the differential description as described in Section 6.2.2 increases the number of clauses by about 47 % ( $\sigma=0.0005$ ) for MD4 instances and by about 43 % ( $\sigma=0.0008$ ) for SHA-256 instances. For SHA-256 problems, this is illustrated in Table 7.5. The preference variable introduced in Section 6.2.5 increases the number of variables by about 80 % and the number of clauses by factor 2.

Compared to 83,542 clauses and 12,219 variables for our average SAT problem, we consider our testcases to be noticeably large. However, it is important to point out that the problem size does not necessarily correlate with the hardness of the SAT problem.

- The variables of clauses of average SAT problems have a standard deviation of 3,337 in average ( $\sigma$  =1,261, median =3,643). Our average SAT problem has a standard deviation of 1,004 in average ( $\sigma$  =13,992, median = 22). Hence variables which got created at every point during the CNF generation are shared within one clause. The general statement, that variable enumeration is arbitrary and therefore this standard deviation has no meaning holds, but we need to consider that practically speaking variables created close to each other share close variable indices. Under these assumptions a large  $\sigma$  indicates variables are reused. We assume this is another indicator for high diffusion in cryptographic algorithms. Values are intermingled over and over throughout the repetitive structure of hash algorithms.
- Connected variables components are 129 for MD4 problems and 2 for SHA-256 problems. For SHA-256 problems, a unit clause is given as existential literal and for MD4 problems, all components except one are of size 3. We did not investigate further, because this number is constant with an increasing problem size and all other variables are strongly correlated due to a high diffusion.
- An average literal frequency of  $3.5 \cdot 10^{-5}$  for our testcases is much lower than 0.014 for average problems. We explain this with the larger problem size. Literal frequency is divided by the number of clauses of the CNF and is therefore smaller, the larger the problem is.

In general we were not able to identify features allowing us to solve differential cryptanalysis problems more efficiently compared to general-purpose SAT problems. We concluded writing your own SAT solver dedicated to solving differential cryptanalysis problems is not worth the effort.

### 7.2 Finding hash collisions

In this section, we look at our runtime results of testcases provided in Appendix B. We make various claims and substantiate them with runtime results. Runtimes are always provided in seconds. Therefore smaller runtimes are better.  $\top$  denotes a timeout (solving took more than 1 day) and — denotes unavailable data.

We considered MD4 testcases A, B and C (listed in Table 7.1) and generated the corresponding CNF files. The SAT solvers mentioned in Section 4.5 were used to evaluate whether the problem is solvable within the time limit.

algorithm	testcase	rounds	diff. characteristic	clauses	variables
$MD_4$	A	48	Appendix B.1	254,656	48,704
$MD_4$	В	48	Appendix B.2	254,210	48,704
$MD_4$	C	48	Appendix B.3	253,984	48,704

Table 7.1: MD4 testcases considered

### 7.2.1 Attacking MD4

### Claim 7.1

Testcase A in the encoding described in Section 6.2.1 can be solved within one minute by all considered SAT solvers.

In our attack setting we started off with Testcase A. It serves rather as a toy example to verify correctness of our implementation than as an actual benchmark. Be aware that invalid implementations either result in unsatisfiability for satisfiable testcases or runtime results are unexpected because the SAT solver could not take advantage of our SAT design improvements. This particular testcase can be solved easily with all major SAT solvers as can be seen in Table 7.2.

We end up with the result, that the hash collision given in Testcase C can be solved by the majority of modern SAT solvers. Of course the cryptanalyst needs to figure out good starting points for the hash collision and encode them in the differential characteristic, but this task is still considered practical, because this task can be easily automated.

### 7.2.2 Evaluating simplification

As a next approach, we looked at CNF simplifiers. Those simplifiers consume a CNF file and transform the CNF file to an equisatisfiable CNF file. Those simplified CNF files might be subject to performance improvements.

solver	version	propagations	decisions	restarts	runtime
MiniSat	2.2.0	3,813,726	250,759	_	3
CryptoMiniSat	4.5.3	140,000	2,441,566	539	26
	5	32,163,801	2,178,965	598	29
Lingeling	ats1	6,586,770	436,621	980	23
Plingeling	ats1	452,630,440	3,275,498	_	88
Treengeling	ats1	18,629,811	1,640,289	_	64
Glucose	4.0	14,727,839	990,491	272	8
Glucose Syrup	4.0	37,021,496	629,363	201	14

Table 7.2: Testcase A can be solved within 1 minute by all SAT solvers

#### Claim 7.2

Simplification reduces the problem size (number of variables and clauses).

Consider for example Testcase C (Appendix B.3) in the basic encoding introduced in Section 6.2.1. Then simplification will reduce the problem size down to 42.9 % or more of its original size (as illustrated in Table 7.3). We verified these data for all simplified files and got similar results. Therefore the claim holds considering the problem size gets reduced to approximately half of its size.

simplification	variables	percent of none	clauses	percent of none
none	48,704	100 %	253,984	100 %
cmsat	24,503	50.31 %	111,931	44.07 %
lingeling	48,704	100 %	106,626	41.98 %
minisat	20,895	42.90~%	118,236	46.55 %
satelite	27,495	56.45 %	153,262	60.34 %

Table 7.3: Problem sizes of Testcase C in the encoding of Section 6.2.1 after simplification. lingeling maintains the same number of variables according to the CNF header.

### Claim 7.3

Simplification as preprocessing step does not significantly improve the runtime of SAT solvers.

We look at Testcase C which is a more difficult MD<sub>4</sub> problem compared to Testcase A. Simplification runtime results depend on the SAT solver, which applies certain simplifications while trying to solve the CNF, and the simplifier used. A small number of variables or clauses does not necessarily lead to better performance. But an equisatisfiable encoding of the same problem is worth considering.

Table 7.4 lists runtimes depending on the simplification used.

**none** refers to the unsimplified CNF

cmsat refers to simplification applied with Cryptominisat version 5:
 ./cryptominisat5 -p1 file.cnf simplified.cnf

 $\label{lingeling} \textbf{lingeling} \ \ \textbf{refers to simplification with lingeling version ats 1:}$ 

./lingeling -s file.cnf -o simplified.cnf

minisat also simplifies CNF file with the following command line:

./minisat file.cnf -dimacs=simplified.cnf

**satelite** is specifically designed to simplify CNF files: ./satelite file.cnf simplified.cnf

It is worth pointing out that simplification time is not part of the runtime listed. Simplification can take very long. Especially simplifications with lingeling have sometimes taken several hours without result.

In conclusion, simplification leads to a slight improvement of the runtime, but in general we cannot recommend simplifying every CNF file before running it. Because technically speaking, SAT solvers internally apply simplification algorithms on their own.

solver	version	none	cmsat	lingeling	minisat	satelite
MiniSat	2.2.0	4,519	7,649	1,337	1,476	1,293
CryptoMiniSat	5	1,064	973	1,201	4,470	3,920
Lingeling	ats1	1,492	906	356	860	1,297
Treengeling	ats1	1,281	13,401	20,903	13,790	10,840
Plingeling	ats1	2,310	1,232	955	1,384	2,030

TABLE 7.4: Runtimes of Testcase C after CNF files have been simplified

#### 7.2.3 Attacking SHA-256

While the basic approach works well for MD4, hash algorithm SHA-256 encompasses a much larger state making the problem significantly more difficult for the SAT solver. Consider Testcases 18, 21, 23 and 24. Those testcases describe round-reduced hash collisions on SHA-256 (the testcase number gives the number of rounds). Our next approach is called differential description as originally described in Section 6.2.2.

### Claim 7.4

A differential description encoding (Section 6.2.2) improves the runtime compared to a missing differential description.

testcase	clauses / variables	testcase	clauses / variables
18:	590,953 / 107,839	18 diff-desc:	846,487 / 107,839
21:	636,838 / 116,800	21 diff-desc:	911,629 / 116,800
23:	667,438 / 122,774	23 diff-desc:	955,067 / 122,774
24:	682,722 / 125,761	24 diff-desc:	976,770 / 125,761

Table 7.5: Problem sizes of our SHA-256 testcases (clauses / variables)

To testing differential description, we looked at MD4's Testcase C and compared it with out SHA-256 testcases. Those testcases are described in detail in Appendices B.4, B.5 and B.6.

Recall that differential description explicitly encodes how differences in arithmetic and bitwise operations propagate in the CNF. We discussed XOR and MAJ in Section 6.2.2.

The data corresponds to even larger testcases, namely a 27-rounds variant we looked at, but did not list. This 27-rounds testcase could not be solved in many cases within our time limit and is therefore excluded from our lists.

We evaluated runtimes with and without differential description. In Table 7.6 we randomly picked SAT solvers and we can clearly see a significant improvement of the runtimes.

We continued by trying to influence the guessing strategy to reflect differential cryptanalysis, which generally use the assumption that difference variables are assigned first. This strategy requires customization of the SAT solver and therefore we only considered lingeling, which was adapted for our purposes.

	CryptoM	1iniSat 5	lingeling-ats1		
testcase	w/o dd	w/ dd	w/o dd	w/ dd	
MD <sub>4</sub> , C	1,064	231	798	53	
SHA-256, 18	37	37	31	160	
SHA-256, 21	T	7,855	28,621	5,513	
SHA-256, 23	T	26,212	76,196	1,450	
SHA-256, 24	T	37,194	78,017	1,235	

Table 7.6: Runtimes for various testcases with or without differential description with CryptoMiniSat and lingeling. Testcase C has been added for reference.

### 7.2.4 Modifying the guessing strategy

In differential cryptanalysis the general assumption is made that differences should be guessed first. Once they are assigned, we can look at the Boolean values in the two hash algorithm instances. To model this behavior, we looked at options provided by SAT solvers.

#### Claim 7.5

Lingeling option --phase=-1 improves its runtime for our testcases.

Option --phase=-1 of lingeling is described as "default phase" set to -1 (negative), 0 (Jeroslow-Wang strategy [10]) or 1 (positive). Per default a strategy engineered by Jeroslow-Wang [10] is used, but considering Claim 6.2 at page 41 we expect --phase=-1 to provide better runtime results.

Indeed our results consistently indicate a small improvement. This can be recognized in Table 7.7.

	testcase	1	8	21		23		24	
	phase	О	-1	0	-1	0	-1	0	-1
•	runtime	31	22	28,621	19,717	76,196	71,677	85,774	70,259

Table 7.7: lingeling-ats1 results for SHA-256 comparing --phase=-1 with --phase=0

### 7.2.5 Evaluating the lightweight approach

Though the results of --phase=-1 was recognizable, we wanted to push it further. We got in contact with Armin Biere who provided us an extended lingeling implementation which understands the notion of difference variables as a set of variables which needs to be assigned first.

### Claim 7.6

Evaluating difference variables first and with Boolean value false improves the runtime.

The lightweight approach mentioned in Section 6.2.4 evaluates difference variables first with Boolean value false, but neglects the differential description. This approach is justified by the assumption that a low number of differences, leading to a sparse differential path, is more likely to cancel out differences ending in a hash collision.

Table 7.8 reveals a nice improvement (the runtime becomes 0.85~%) of its original runtime in average.

testcase	C	18	21	23	24
basic approach (ats1)	798	31	28,621	76,196	85,774
diff-first-false (ats101)	652	29	27,599	59,312	66,052

Table 7.8: lingeling-ats101 and lingeling-ats1 results comparing a difference variables (with Boolean value false) first approach with the basic approach

### 7.2.6 Using preference variables

Our last approach uses *preference variables* mentioned in Section 6.2.5. Under the assumption that preference variables  $x^*$  and difference variables  $\Delta x$  are assigned first, an additional clauses provides a decision tree which assigns difference variables first and once they are all set, values for the two hash algorithm instances are assigned.

#### Claim 7.7

Adding preference variables lead to a performance improvement.

Section 6.2.5 introduces preference variables which enforce the idea that difference variables are evaluated first. Preference variables only add additional clauses, but do not provide a runtime improvement per se. The larger number of variables and clauses make the problem potentially harder.

However, evaluating them with false first makes sure that a low number of differences is propagated. Otherwise the SAT solver would spend much time in fruitless branches and the number of restarts would be comparably high.

Given an assigned difference variable, differential description ensures that the value is propagated quickly to other parts of the equation system. This justifies why our encoding with preference variables should be compared to an instance with differential description and difference variables first.

Table 7.9 shows a significant runtime improvement.

testcase	A	В	C
CNF with differential description	11	133	155
additionally with preference variables	8	50	62

Table 7.9: lingeling-ats101 testcases comparing an approach with differential description with additional preference variables

### 7.3 Summary

In this section we looked at various improvements to improve the runtime, namely

- 1. CNF simplification
- 2. differential description
- 3. Lingeling's --phase=-1 option
- 4. Difference variables first with Boolean false
- 5. Preference variables

We evaluated these approaches with several SAT solvers and found significiant runtime improvements. We successfully found hash collisions for MD4 and SHA-256.

# **Chapter 8**

# **Summary and Future Work**

### 8.1 Related work

In my bachelor thesis [25] we tried to integrate a SAT solver into our department's existing tool which encodes propagation explicitly. This approach was not very successful as restarts between hash algorithm rounds implied that intermediate results by the SAT solver got lost. This was our motivation for this master thesis: We represent all details in CNF.

Research was already done by Ilya Mironov and Lintao Zhang [18] to apply SAT solvers to differential cryptanalysis specifically to find hash collision in MD4. However whereas their basic approach seems to correspond to our approach described in Section 6.2.1, our implementation uses additional SAT design tweaks to improve our results. Also because 10 years have gone since publication, SAT technology has progressed and modern SAT solvers on modern hardware provide better results.

### 8.2 Conclusion

We successfully found full-round hash collisions for MD<sub>4</sub> using SAT solvers mentioned in Section 4.5. We applied tweaks to the lingeling SAT solver to improve our runtime results further and found 24-round hash collisions for SHA-256. Our attack starting points for MD<sub>4</sub> — Testcases B.1, B.2 and B.3 — were found by Yusuke Naito, Yu Sasaki, Noboru Kunihiro and Kazuo Ohta [29]. Our starting points for SHA-256 — Testcases B.4, B.5, B.6 and B.7 — were found by Ivica Nikolić and Alex Biryukov [21].

### 8.3 Future work

Future work might want to consider our design decisions made in chapter 6.

In general, it would be interesting to generate our testcase for a broader set of differential characteristics. Probably we can come up with empirical results showing a relation between the size of unspecified areas in the differential characteristics and the evaluated runtime.

Furthermore, many SAT-related effort could be put to thoroughly discuss why differential description provides such a dramatic performance improvement. This necessarily means the SAT solver is generally not capable of deriving the useful clauses, differential description provides. The resulting numbers of restarts could also be subject of further research.

As far as cnf-analysis is concerned, the project aims to extend to a larger set of SAT features. Furthermore benchmarks should be aggregated from more sources, but Armin Biere pointed out in private conversation that not all benchmarks of SAT competitions become publicly available. This avoids machine learning hacks where submitted SAT solvers perform exceptionally well on known benchmarks. Our main contribution is a search interface to search for SAT features given the cnfhash of a CNF file. We hope to get in touch with new SAT feature ideas and SAT benchmark files.

### 8.4 Contributions

To strengthen Reproducible Research, the source code and data resulting from this thesis is available online. It allows the reader to run the experiments again and verify our claims. We did our best to describe our hardware setup as accurately as possible. At the following website, any results part of this project are collected:

```
http://lukas-prokop.at/proj/megosat/
```

Several subprojects are part of this master thesis:

#### algotocnf

A python library implementing the encoding described in Chapter 6.

Python3 library and program: https://github.com/prokls/algotocnf

### cnf-hash

A standardized way to produce a unique hash for CNF files

Go implementation: https://github.com/prokls/cnf-hash-go

Python3 implementation: https://github.com/prokls/cnf-hash-py

**Testsuite:** https://github.com/prokls/cnf-hash-tests2

### cnf-analysis

Evaluate SAT features for a given CNF file.

**Go implementation:** https://github.com/prokls/cnf-analysis-go **Python3 implementation:** https://github.com/prokls/cnf-analysis-py

**Testsuite:** https://github.com/prokls/cnf-analysis-tests

# Appendices

# Appendix A

# Hardware setup

We introduce two hardwarde setups used in this master thesis. Thinkpad x220 was used to simplify CNF files and evaluate SAT features. The cluster was used for running SAT solvers and retrieving runtime results.

Model type	Thinkpad Lenovo x220 tablet, 4299-2P6
Processor	Intel i5-2520M, 2.50 GHz, dual-core, Hyperthreaded
RAM	16 GB (extension to common retail setup)
L1–L3 cache sizes	32 KB / 256 KB / 3,072 KB

Table A.1: Thinkpad x220 Tablet specification [14]

Clu	Cluster node nehalem192go specification [3]			
Processor	Intel Xeon X5690, 3.47 GHz, 6 cores, Hyperthreaded			
RAM	192 GB			
L1-L3 cache sizes	32 KB / 256 KB / 12,288 KB			
$\overline{C}$	Cluster node nehalem72go specification			
Processor	Intel Xeon X5550, 2.67 GHz, 4 cores, Hyperthreaded			
RAM	72 GB			
L1-L3 cache sizes	32 KB / 256 KB / 8,192 KB			
	Cluster node xeon64g* specification			
Processor	Intel Xeon E5430, 2.66 GHz, 4 cores, Hyperthreaded			
RAM	72 GB			
L1-L3 cache sizes	32 KB / 6144 KB			

Table A.2: One node nehalem192go, one node nehalem72go and four nodes xeon64g\* were used for evaluating runtimes

## Appendix B

### **Testcases**

### B.1 MD4 testcase A

Please compare with Figure B.1.

We can clearly see that all difference variables are defined. Either they are true (bit condition x) or false (bit condition –), but no variable has an undeciable state like?. At the top we can see bit conditions 0 and 1 encoding the MD4 initial vector defined by the hash algorithm. The differences x introduce the hash collision and with round 47 being set of – only, the output is forced to be equal between both hash algorithm instances. This testcase is a trivial version of the differential characteristic described in [29].

### B.2 MD4 testcase B

Please compare with Figure B.2.

In this testcase we have less knowledge about the state than in testcase A because many values are encoded with? meaning that neither their difference nor their actual values are known. However, of course some x exists to introduce a hash collision and the last round only consists of dashes to assert no difference in the output. So unlike testcase A, the SAT solver needs to figure out the difference variables in rounds o-11 increasing its overall runtime in all SAT solver implementations.

### B.3 MD4 testcase C

Please compare with Figure B.3.

This testcases introduces a hash collision which is expected to cancel out at round

32. At the same time no information is provided about the intermediate state of the hash algorithm in rounds 0-20.

### B.4 SHA-256 testcase 18 rounds

Please compare with Figure B.4.

All SHA-256 testcases got derived from a paper by Ivica Nikolić and Alex Biryukov [21]. Recall that message input of one block only fills Wo to W15. W16 or later are generated based on the previous message words. This differential characteristic depicts a hash collision introduced in round 3. When solving this differential characteristic differences will especially occur in the most-significant bit of words with unspecified difference. Differences cancel out after round 7.

### B.5 SHA-256 testcase 21 rounds

*Please compare with Figure B.5.* 

Unlike Testcase B.4 word A5 is underspecified with question marks. This certainly makes the problem harder for a SAT solver. At the same time differences of the message words W9 and W10 are specified. This makes the problem easier. At the same time the whole collision covers 21 rounds, unlike Testcase B.4 with 18 rounds.

### B.6 SHA-256 testcase 23 rounds

Please compare with Figure B.6.

Message word W9 specifies no difference, but the collision is extended to 23 rounds.

### B.7 SHA-256 testcase 24 rounds

Please compare with Figure B.7.

No measures were taken to simplify the problem for the SAT solver, but the hash collision needs to be found for 24 rounds, which makes the problem hard for the SAT solver because of its increased state size.

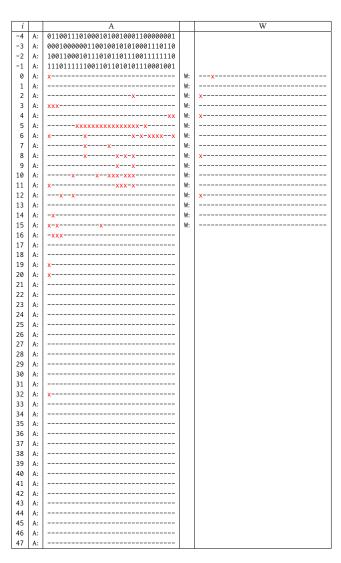


Figure B.1: Differential characteristic of MD4 testcase A

-4 A: 010e11101e0e10e10e010e0e10e0e0e0e1 -3 A: 0e010e0e0e011b011e011011 -1 A: 1116111111e0110111111e0e10111011e1 -1 A: 1116111111e01e0111e0e0110e1 0 A: ????????????????????????????? 2 A: ???????????????????????? 3 A: ??????????????????????? 4 A: ?????????????????????  5 A: ????????????????????????  6 A: ???????????????????????  7 A: ???????????????????????  8 A: ????????????????????????  8 A: ????????????????????????  10 A: ???????????????????????  11 A: ??????????????????????????  12 A: ????????????????????????  13 A: ?????????????????????????  14 A: ???????????????  15 A: ?????????????  16 A: ??????????????????????????  17 A: ?	i		A		W
-3   A.	-	۸.			VV
-2					
-1	1				
0					
1       A.       ????????????????????????????????????					
2 A. ???????????????????????????????????					x
3       A.       ????????????????????????????????????					
4       A.       ??????????????????????????????       W.       X					x
5       A.:       ????????????????????????????????????					
6 A: ???????????????????????????????????	1				x
7       A.       ?????????????????????????       W.         8       A.       ????????????????????????       W.         9       A.       ??????????????????????????       W.         10       A.       ?????????????????????????       W.         11       A.       ?????????????       W.         12       A.       ????????????       W.         13       A.       ????????????       W.         14       A.       ?????????????       W.         15       A.       ??????????????       W.         16       A.       ???       W.         17       A.       ?       W.         20       A.       X       X         21       A.       X       X         22       A.       X       X         23       A.       X       X         24       A.       X       X         25       A.       X       X         30       A.       X       X         31       A.       X       X         33       A.       X       X         34       A.       X       X					
8       A:       ??????????????????????????????       W:       X	1				
9   A: ??????????????????????????????????		A:			
10       A:       ???????????????????????????????       W:         11       A:       ?????????????????????????????       W:       X         12       A:       ?????????????       W:       X         13       A:       ?????????????       W:       X         14       A:       ??????????????       W:       X         15       A:       ??????????????       W:       X         16       A:       ????       X       X         19       A:       ?       X       X         20       A:       X       X       X         25       A:       X       X       X         25       A:       X       X       X       X         28       A:       X <td< td=""><td></td><td>A:</td><td></td><td></td><td>x</td></td<>		A:			x
11       A:       ??????????????????????????????????       W:	9	A:	????????????????????????????????	W:	
12       A:       ?????????????       W:       X	10	A:	???????????????????????????????	W:	
13       A:       ?????????????       W:         14       A:       ????????????       W:         15       A:       ????????????       W:         16       A:       ???         17       A:       ?         18       A:       ?         20       A:       X         21       A:          22       A:          23       A:          26       A:          27       A:          28       A:          30       A:          31       A:          32       A:          33       A:          34       A:          35       A:          38       A:          39       A:          40       A:          41       A:          43       A:          45       A:          46       A:	11	A:	????????????????????????????????	W:	
14       A:       ?????????????       W:         15       A:       ????????????       W:         16       A:       ???       P.         17       A:       ?	12	A:	????????????	W:	x
15 A: ????????????? W:   W:	13	A:	????????????	W:	
16       A:       ???x         17       A:       ?	14	A:	????????????	W:	
17       A:       ?	15	A:	????????????	W:	
18       A:       ?	16	A:	???x		
19       A:       ?	17	A:	?		
20       A:       X	18	A:	?		
21       A:         22       A:         23       A:         24       A:         25       A:         26       A:         27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:	19	A:	?		
22       A:         23       A:         24       A:         25       A:         26       A:         27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:	20	A:	x		
22       A:         23       A:         24       A:         25       A:         26       A:         27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:	21	A:			
24       A:         25       A:         26       A:         27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:	1				
24       A:         25       A:         26       A:         27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:	23	A:			
25 A:					
26 A:					
27       A:         28       A:         29       A:         30       A:         31       A:         32       A:         33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:					
28 A:					
29 A:					
30       A:					
31     A:       32     A:       33     A:       34     A:       35     A:       36     A:       37     A:       38     A:       40     A:       41     A:       42     A:       43     A:       44     A:       45     A:       46     A:	1 .				
32 A: x	1				
33       A:         34       A:         35       A:         36       A:         37       A:         38       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:			·		
34       A:         35       A:         36       A:         37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:			^		
35 A:					
36       A:         37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:					
37       A:         38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:					
38       A:         39       A:         40       A:         41       A:         42       A:         43       A:         44       A:         45       A:         46       A:					
39     A:       40     A:       41     A:       42     A:       43     A:       44     A:       45     A:       46     A:	1 '				
40       A:	1				
41 A:					
42 A:	1				
43       A:         44       A:         45       A:         46       A:					
44 A:					
45 A:					
46 A:					
47 A:	47	A:			

**Figure B.2:** Differential characteristic of MD<sub>4</sub> testcase B

i		A		W
-4	A:	01100111010001010010001100000001		**
-3	A:	00010000001100100101010001110110		
-2	A:	1001100010111010110111100111111110		
-1	A:	1110111111100110110101011110001001		
9	A:	77777777777777777777777777777777	W:	<u>x</u>
1	A:	77777777777777777777777777777777	W:	
2	A:	77777777777777777777777777777777	W:	¥
3	A:	7777777777777777777777777777777	W:	···
4	A:	7777777777777777777777777777777	W:	x
5	A:	7777777777777777777777777777777	W:	
6	A:	7777777777777777777777777777777	W:	
7	A:	7777777777777777777777777777777	W:	
8	A:	7777777777777777777777777777777	W:	x
9	A:	7777777777777777777777777777777	W:	
10	A:	77777777777777777777777777777777	W:	
11	A:	77777777777777777777777777777777	W:	
12	A:	77777777777777777777777777777777	W:	x
13	A:	77777777777777777777777777777777	W:	
14	A:	227777777777777777777777777777777	W:	
15	A:	???????????????????????????????	W:	
16	A:	77777777777777777777777777777777		
17	A:	77777777777777777777777777777777		
18	A:	???????????????????????????????		
19	A:	???????????????????????????????		
20	A:	???????????????????????????????		
21	A:			
22	A:			
23	A:			
24	A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30	A:			
31	A:			
32	A:	x		
33	A:			
34	A:			
35	A:			
36	A:			
37	A:			
38	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:		<u> </u>	

**Figure B.3:** Differential characteristic of MD<sub>4</sub> testcase C

i		A		E		W	
-4	A:		E:				
-3	A:		E:				
-2	A:		E:				
-1	A:		E:				
0	A:		E:		W:		
1	A:		E:		W:		
2	A:		E:		W:		
3	A:	x	E:	???????????????????????????????	W:	??????????????????????????????	
4	A:		E:	???????????????????????????????	W:	??????????????????????????????	
5	A:		E:	???????????????????????????????	W:	??????????????????????????????	
6	A:		E:	???????????????????????????????	W:	??????????????????????????????	
7	A:		E:	???????????????????????????????	W:	???????????????????????????????	
8	A:		E:		W:	??????????????????????????????	
9	A:		E:		W:		
10	A:		E:		W:		
11	A:		E:		W:	??????????????????????????????	
12	A:		E:		W:		
13	A:		E:		W:		
14	A:		E:		W:		
15	A:		E:		W:		
16	A:		E:		W:		
17	A:		E:		W:		

Figure B.4: SHA256 hash collision over 18 rounds

i		A		E		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:	x?????????????????????????????	E:	???????????????????????????????	W:	?????????????????????????????
6	A:		E:	???????????????????????????????	W:	7?????????????????????????????
7	A:		E:	???????????????????????????????	W:	?????????????????????????????
8	A:		E:	???????????????????????????????	W:	??????????????????????????????
9	A:		E:	???????????????????????????????	W:	
10	A:		E:		W:	
11	A:		E:		W:	
12	A:		E:		W:	
13	A:		E:		W:	??????????????????????????????
14	A:		E:		W:	
15	A:		E:		W:	
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	

Figure B.5: SHA-256 hash collision over 21 rounds

i		A		E		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:		E:		W:	
6	A:		E:		W:	
7	A:	x???????????????????????????????	E:	777777777777777777777777777777777	W:	??????????????????????????????
8	A:		E:	77777777777777777777777777777777	W:	??????????????????????????????
9	A:		E:	777777777777777777777777777777777	W:	
10	A:		E:	????????????????????????????????	W:	???????????????????????????????
11	A:		E:	77777777777777777777777777777777	W:	
12	A:		E:		W:	
13	A:		E:		W:	
14	A:		E:		W:	
15	A:		E:		W:	??????????????????????????????
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	
21	A:		E:		W:	
22	A:		E:		W:	

Figure B.6: SHA-256 hash collision over 23 rounds

i		A		Е		W
-4	A:		E:			
-3	A:		E:			
-2	A:		E:			
-1	A:		E:			
0	A:		E:		W:	
1	A:		E:		W:	
2	A:		E:		W:	
3	A:		E:		W:	
4	A:		E:		W:	
5	A:		E:		W:	
6	A:		E:		W:	
7	A:	x?????????????????????????????	E:	???????????????????????????????	W:	??????????????????????????????
8	A:		E:	77777777777777777777777777777777	W:	7777777777777777777777777777777
9	A:		E:	77777777777777777777777777777777	W:	
10	A:		E:	77777777777777777777777777777777	W:	7777777777777777777777777777777
11	A:		E:	77777777777777777777777777777777	W:	
12	A:		E:		W:	
13	A:		E:		W:	
14	A:		E:		W:	
15	A:		E:		W:	???????????????????????????????
16	A:		E:		W:	
17	A:		E:		W:	
18	A:		E:		W:	
19	A:		E:		W:	
20	A:		E:		W:	
21	A:		E:		W:	
22	A:		E:		W:	
23	A:		E:		W:	

Figure B.7: SHA-256 hash collision over 24 rounds

## Appendix C

## Runtimes retrieved

## **TODO**

FAILED means unexpected exit code or missing results. TIMEOUT mean did not terminate within 1 day. SUCCESS means SAT within 1 day.

```
Results cover 50 CNFs

cmsat5 83 occurences
minisat 169 occurences
lingeling-ats1o4 267 occurences
minisat-core 85 occurences
glucose-syrup 84 occurences
lingeling-ats1o1 145 occurences
treengeling-ats1o1 84 occurences
lingeling-ats1o2 250 occurences
plingeling-ats1o1 85 occurences
cmsat4 84 occurences
glucose 84 occurences
FAILED=303 TIMEOUT=722 SUCCESS=1395
```

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	d
cmsat4	algotocnf_1.cnf	none	no	48704 / 253984		
cmsat4	algotocnf_1.cnf	cmsat	no	24503 / 111931		
cmsat4	algotocnf_1.cnf	minisat	no	20895 / 118236		
cmsat4	algotocnf_1.cnf	satelite	no	27495 / 153262		
cmsat4	algotocnf_18-t9.cnf	none	no	107839 / 590953	140000	
cmsat4	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	0	
cmsat4	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544	90000	
cmsat4	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	120000	
cmsat4	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	0	
cmsat4	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 846487	140000	
cmsat4	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	120000	
cmsat4	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	0	
cmsat4	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	0	
cmsat4	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	140000	
cmsat4	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	860000	3
cmsat4	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	520000	1
cmsat4	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	530000	2
cmsat4	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	800000	2
cmsat4	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	780000	2
cmsat4	algotocnf_2.cnf	none	no	48704 / 254210		
cmsat4	algotocnf_2.cnf	cmsat	no	24323 / 111661		
cmsat4	algotocnf_2.cnf	minisat	no	20895 / 118688		
cmsat4	algotocnf_2.cnf	satelite	no	27775 / 154276		
cmsat4	algotocnf_21-t9.cnf	none	no	116800 / 636838		
cmsat4	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308		
cmsat4	algotocnf_21-t9.cnf	minisat	no	65572 / 414470		
cmsat4	algotocnf_21-t9.cnf	satelite	no	74562 / 486714		
cmsat4	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	1540000	7
cmsat4	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	1510000	Ć
cmsat4	algotocnf_21-t9_diff-desc.cnf	lingeling	no	116800 / 404126	1290000	Ć
cmsat4	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	1560000	8
cmsat4	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	1540000	Ć
cmsat4	algotocnf_23-t9.cnf	none	no	122774 / 667438		
cmsat4	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775		
cmsat4	algotocnf_23-t9.cnf	minisat	no	67979 / 429734		
cmsat <sub>4</sub>	algotocnf_23-t9.cnf	satelite	no	77835 / 506217		

SAT solver	CNF file	simplified	phase	vars/clauses	pr
cmsat4	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	
cmsat4	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	
cmsat4	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	
cmsat4	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	
cmsat4	algotocnf_24-t9.cnf	none	no	125761 / 682722	
cmsat4	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	
cmsat4	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	
cmsat4	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	
cmsat4	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770	
cmsat4	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	
cmsat4	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	
cmsat4	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	
cmsat4	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349	
cmsat4	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
cmsat4	algotocnf_27-t10-diff.cnf	lingeling	no	134722 / 0	
cmsat4	algotocnf_27-t10-diff.cnf	minisat	no	o / o	
cmsat4	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722 / o	
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
cmsat4	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	
cmsat4	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542	
cmsat4	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	
cmsat4	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	
cmsat4	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309	
cmsat4	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589	
cmsat4	algotocnf_27-t10.cnf	none	no	134722 / 728030	
cmsat4	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
cmsat4	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
cmsat4	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
cmsat4	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335	
cmsat4	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations
cmsat <sub>4</sub>	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	propagations
cmsat4	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
cmsat4	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146	950000
cmsat4	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	550000
cmsat4	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546	490000
cmsat4	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	720000
cmsat4	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	700000
cmsat4	algotocnf_3.cnf	none	no	48704 / 254656	70000
cmsat4	algotocnf_3.cnf	cmsat	no	23893 / 111403	70000
cmsat4	algotocnf_3.cnf	lingeling	no	48704 / 100941	0
cmsat4	algotocnf_3.cnf	minisat	no	20895 / 119580	60000
cmsat4	algotocnf_3.cnf	satelite	no	28647 / 156910	60000
cmsat4	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	0
cmsat <sub>5</sub>	algotocnf_1.cnf			48704 / 374592	U
-	algotocnf_1.cnf	none	no		
cmsat5	algotocnf_1.cnf	cmsat minisat	no	24503 / 111931 20895 / 118236	
cmsat5	algotocnf_1.cnf	satelite	no		
cmsat5			no	27495 / 153262	
cmsat5	algotocnf_18-t9.cnf	none	no	107839 / 590953	
cmsat5	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	
cmsat5	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544	
cmsat5	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	
cmsat5	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	
cmsat5	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 846487	
cmsat5	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	
cmsat5	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	
cmsat5	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	
cmsat5	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	
cmsat5	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	
cmsat5	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	
cmsat5	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	
cmsat5	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	
cmsat5	algotocnf_2.cnf	none	no	48704 / 254210	
cmsat5	algotocnf_2.cnf	cmsat	no	24323 / 111661	
cmsat <sub>5</sub>	algotocnf_2.cnf	minisat	no	20895 / 118688	
cmsat5	algotocnf_2.cnf	satelite	no	27775 / 154276	

cmsat5         algotocnf_21-t9.cnf         none         no         116800 / 636838           cmsat5         algotocnf_21-t9.cnf         cmsat         no         63555 / 358308           cmsat5         algotocnf_21-t9.cnf         minisat         no         63572 / 414470           cmsat5         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat5         algotocnf_21-t9.diff-desc.cnf         none         no         116800 / 911629           cmsat5         algotocnf_21-t9.diff-desc.cnf         lingeling         no         116800 / 404126           cmsat5         algotocnf_21-t9.diff-desc.cnf         minisat         no         59528 / 318049           cmsat5         algotocnf_21-t9.diff-desc.cnf         minisat         no         61680 / 720755           cmsat5         algotocnf_23-t9.cnf	SAT solver	CNF file	simplified	phase	vars/clauses	propagation
cmsat5         algotocnf_21-to.cnf         cmsat         no         63555 / 358308           cmsat5         algotocnf_21-to.cnf         minisat         no         65572 / 414470           cmsat5         algotocnf_21-to.cnf         satelite         no         74562 / 486714           cmsat5         algotocnf_21-to.diff-desc.cnf         none         no         116800 / 911629           cmsat5         algotocnf_21-to.diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-to.diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-to.diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-to.diff-desc.cnf         minisat         no         51650 / 534965           cmsat5         algotocnf_21-to.diff-desc.cnf         minisat         no         90236 / 720755           cmsat5         algotocnf_23-to.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-to.cnf         cmsat         no         67999 / 429734           cmsat5         algotocnf_23-to.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-to.diff-desc.cnf         cmsat         <						I I G 32 2
cmsat5         algotocnf_21-to.cnf         minisat         no         65572 / 414470           cmsat5         algotocnf_21-to.cnf         satelite         no         74562 / 486714           cmsat5         algotocnf_21-to.diff-desc.cnf         none         no         116800 / 3011629           cmsat5         algotocnf_21-to.diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-to.diff-desc.cnf         lingeling         no         116800 / 404126           cmsat5         algotocnf_21-to.diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_21-to.diff-desc.cnf         satelite         no         90236 / 720755           cmsat5         algotocnf_23-to.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-to.cnf         cmsat         no         67979 / 429734           cmsat5         algotocnf_23-to.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-to.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-to.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-to.diff-desc.cnf         satelite </td <td>-</td> <td>_</td> <td></td> <td></td> <td></td> <td></td>	-	_				
cmsat5         algotocnf_21-t9.cnf         satelite         no         74562 / 486714           cmsat5         algotocnf_21-t9_diff-desc.cnf         none         no         116800 / 911629           cmsat5         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_23-t9_cnf         minisat         no         90236 / 720755           cmsat5         algotocnf_23-t9_cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-t9_cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9_cnf         satelite         no         76510 / 307118           cmsat5         algotocnf_23-t9_cdiff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9_cdiff-desc.cnf         satelite			minisat	no		
cmsat5         algotocnf_21-19_diff-desc.cnf         none         no         116800 / 911629           cmsat5         algotocnf_21-19_diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-19_diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-19_diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-19_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_23-19_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_23-19_cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-19_cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-19_cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-19_cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-19_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-19_diff-desc.cnf         satelite         no         57510 / 307118           cmsat5         algotocnf_24-19_cnf         none	-					
cmsat5         algotocnf_21-t9_diff-desc.cnf         cmsat         no         59528 / 318049           cmsat5         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126           cmsat5         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755           cmsat5         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         65579 / 377228           cmsat5         algotocnf_23-t9_cnf         cmsat	-			no		
cmsat5         algotocnf_21-t9_diff-desc.cnf         lingeling         no         116800 / 404126           cmsat5         algotocnf_21-t9_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755           cmsat5         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-t9.cnf         minisat         no         64880 / 369775           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         77835 / 506217           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.cnf         cmsat	-					
cmsat5         algotocnf_21-19_diff-desc.cnf         minisat         no         81650 / 534965           cmsat5         algotocnf_21-19_diff-desc.cnf         satelite         no         90236 / 720755           cmsat5         algotocnf_23-19_cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-19_cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-19_cnf         satelite         no         67979 / 429734           cmsat5         algotocnf_23-19_cnf         satelite         no         677835 / 506217           cmsat5         algotocnf_23-19_diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-19_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-19_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-19_diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_23-19_diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_24-19_cnf         minisat         no         65579 / 377228           cmsat5         algotocnf_24-19_cnf         satelite <td>-</td> <td></td> <td>lingeling</td> <td>no</td> <td></td> <td></td>	-		lingeling	no		
cmsat5         algotocnf_21-t9_diff-desc.cnf         satelite         no         90236 / 720755           cmsat5         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9.diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         minisat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         minisat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         65579 / 377228           cmsat5         algotocnf_24-t9.cnf         satelite         no         69023 / 436292           cmsat5         algotocnf_24-t9.diff-desc.cnf         cmsa	-			no	<del></del>	
cmsat5         algotocnf_23-t9.cnf         none         no         122774 / 667438           cmsat5         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9.diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         minisat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_24-t9.diff-desc.cnf         none         no         125761 / 682722           cmsat5         algotocnf_24-t9.cnf         mone         no         65579 / 377228           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9.diff-desc.cnf         cmsat         no	-		satelite	no		
cmsat5         algotocnf_23-t9.cnf         cmsat         no         64880 / 369775           cmsat5         algotocnf_23-t9.cnf         minisat         no         67979 / 429734           cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9.diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-t9.diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9.diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_24-t9.diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_24-t9.cnf         none         no         125761 / 682722           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9.cnf         satelite         no         79486 / 515977           cmsat5         algotocnf_24-t9.diff-desc.cnf         cmsat         no         56447 / 302014           cmsat5         algotocnf_24-t9.diff-desc.cnf         cmsat         no		algotocnf_23-t9.cnf	none	no	122774 / 667438	
cmsat5         algotocnf_23-t9.cnf         satelite         no         77835 / 506217           cmsat5         algotocnf_23-t9_diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-t9_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_23-t9_diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_23-t9_ciff         none         no         125761 / 682722           cmsat5         algotocnf_24-t9.cnf         cmsat         no         65579 / 377228           cmsat5         algotocnf_24-t9.cnf         cmsat         no         69023 / 436292           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9_ciff         satelite         no         79486 / 515977           cmsat5         algotocnf_24-t9_diff-desc.cnf         cmsat         no         56447 / 302014           cmsat5         algotocnf_24-t9_diff-desc.cnf         cmsat         no         56447 / 302014           cmsat5         algotocnf_27-t10-diff.cnf         cmsat <t< td=""><td>cmsat<sub>5</sub></td><td>algotocnf_23-t9.cnf</td><td>cmsat</td><td>no</td><td></td><td></td></t<>	cmsat <sub>5</sub>	algotocnf_23-t9.cnf	cmsat	no		
cmsat5         algotocnf_23-t9_diff-desc.cnf         none         no         122774 / 955067           cmsat5         algotocnf_23-t9_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         93504 / 740545           cmsat5         algotocnf_24-t9_cnf         none         no         125761 / 682722           cmsat5         algotocnf_24-t9.cnf         mone         no         65579 / 377228           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9.cnf         satelite         no         79486 / 515977           cmsat5         algotocnf_24-t9_diff-desc.cnf         none         no         125761 / 976770           cmsat5         algotocnf_24-t9_diff-desc.cnf         cmsat         no         56447 / 302014           cmsat5         algotocnf_24-t9_diff-desc.cnf         minisat         no         85312 / 558731           cmsat5         algotocnf_27-t10-diff.cnf         none         no         134722 / 728349           cmsat5         algotocnf_27-t10-diff.cnf         cmsat	cmsat5	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	
cmsat5         algotocnf_23-t9_diff-desc.cnf         cmsat         no         57510 / 307118           cmsat5         algotocnf_23-t9_diff-desc.cnf         minisat         no         84080 / 550727           cmsat5         algotocnf_23-t9_diff-desc.cnf         satelite         no         93504 / 740545           cmsat5         algotocnf_24-t9.cnf         none         no         125761 / 682722           cmsat5         algotocnf_24-t9.cnf         cmsat         no         65579 / 377228           cmsat5         algotocnf_24-t9.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9_diff-desc.cnf         minisat         no         69023 / 436292           cmsat5         algotocnf_24-t9_diff-desc.cnf         satelite         no         79486 / 515977           cmsat5         algotocnf_24-t9_diff-desc.cnf         cmsat         no         125761 / 976770           cmsat5         algotocnf_24-t9_diff-desc.cnf         cmsat         no         56447 / 302014           cmsat5         algotocnf_24-t9_diff-desc.cnf         minisat         no         85312 / 558731           cmsat5         algotocnf_27-t10-diff.cnf         none         no         95154 / 750557           cmsat5         algotocnf_27-t10-diff.cnf	cmsat5	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	
cmsat5 algotocnf_23-t9_diff-desc.cnf minisat no 84080 / 550727 cmsat5 algotocnf_23-t9_diff-desc.cnf satelite no 93504 / 740545 cmsat5 algotocnf_24-t9.cnf none no 125761 / 682722 cmsat5 algotocnf_24-t9.cnf cmsat no 65579 / 377228 cmsat5 algotocnf_24-t9.cnf minisat no 69023 / 436292 cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977 cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	
cmsat5 algotocnf_23-t9_diff-desc.cnf satelite no 93504 / 740545 cmsat5 algotocnf_24-t9.cnf none no 125761 / 682722 cmsat5 algotocnf_24-t9.cnf cmsat no 65579 / 377228 cmsat5 algotocnf_24-t9.cnf minisat no 69023 / 436292 cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977 cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_24-t9_diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	
cmsat5 algotocnf_24-t9.cnf none no 125761 / 682722 cmsat5 algotocnf_24-t9.cnf cmsat no 65579 / 377228 cmsat5 algotocnf_24-t9.cnf minisat no 69023 / 436292 cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977 cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	
cmsat5 algotocnf_24-t9.cnf cmsat no 65579 / 377228 cmsat5 algotocnf_24-t9.cnf minisat no 69023 / 436292 cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977 cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	
cmsat5 algotocnf_24-t9.cnf minisat no 69023 / 436292 cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977 cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_24-t9.cnf	none	no	125761 / 682722	
cmsat5 algotocnf_24-t9.cnf satelite no 79486 / 515977  cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770  cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014  cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731  cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557  cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349  cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0  cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0  cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0  cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0  cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0	cmsat5	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	
cmsat5 algotocnf_24-t9_diff-desc.cnf none no 125761 / 976770 cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat5			no	69023 / 436292	
cmsat5 algotocnf_24-t9_diff-desc.cnf cmsat no 56447 / 302014 cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731 cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat5	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	
cmsat5 algotocnf_24-t9_diff-desc.cnf minisat no 85312 / 558731  cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557  cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349  cmsat5 algotocnf_27-t10-diff.cnf cmsat no o / o  cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / o  cmsat5 algotocnf_27-t10-diff.cnf minisat no o / o  cmsat5 algotocnf_27-t10-diff.cnf satelite no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o / o	cmsat <sub>5</sub>		none	no	125761 / 976770	
cmsat5 algotocnf_24-t9_diff-desc.cnf satelite no 95154 / 750557 cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349 cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat <sub>5</sub>			no		
cmsat5 algotocnf_27-t10-diff.cnf none no 134722 / 728349  cmsat5 algotocnf_27-t10-diff.cnf cmsat no o / o  cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / o  cmsat5 algotocnf_27-t10-diff.cnf minisat no o / o  cmsat5 algotocnf_27-t10-diff.cnf satelite no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no o / o  cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o / o	cmsat <sub>5</sub>			no	85312 / 558731	
cmsat5 algotocnf_27-t10-diff.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat <sub>5</sub>	=	satelite	no	95154 / 750557	
cmsat5 algotocnf_27-t10-diff.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff.cnf satelite no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat <sub>5</sub>	_	none	no		
cmsat5 algotocnf_27-t10-diff.cnf minisat no o/o cmsat5 algotocnf_27-t10-diff.cnf satelite no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o/o	cmsat <sub>5</sub>			no	o / o	
cmsat5algotocnf_27-t10-diff.cnfsatelitenoo / ocmsat5algotocnf_27-t10-diff_diff-desc.cnfcmsatnoo / ocmsat5algotocnf_27-t10-diff_diff-desc.cnflingelingno134722 / ocmsat5algotocnf_27-t10-diff_diff-desc.cnfminisatnoo / ocmsat5algotocnf_27-t10-diff_diff-desc.cnfsatelitenoo / o	cmsat <sub>5</sub>			no		
cmsat5 algotocnf_27-t10-diff_diff-desc.cnf cmsat no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o/o	cmsat5			no		
cmsat5 algotocnf_27-t10-diff_diff-desc.cnf lingeling no 134722 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no 0 / 0 cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no 0 / 0	cmsat5		satelite	no		
cmsat5 algotocnf_27-t10-diff_diff-desc.cnf minisat no o/o cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o/o	cmsat5			no	o / o	
cmsat5 algotocnf_27-t10-diff_diff-desc.cnf satelite no o/o	cmsat5			no	·	
	cmsat5			no		
cmsat5   algotocnf_27-t10-simplified.cnf none no 134722 / 728542	cmsat <sub>5</sub>		satelite	no		
	cmsat5	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542	

SAT solver	CNF file	simplified	phase	vars/clauses	prop
cmsat <sub>5</sub>	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	
cmsat5	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	
cmsat <sub>5</sub>	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998	
cmsat <sub>5</sub>	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847	
cmsat <sub>5</sub>	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443	
cmsat <sub>5</sub>	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309	
cmsat <sub>5</sub>	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589	
cmsat <sub>5</sub>	algotocnf_27-t10.cnf	none	no	134722 / 728030	
cmsat <sub>5</sub>	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
cmsat5	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
cmsat <sub>5</sub>	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
cmsat <sub>5</sub>	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335	
cmsat <sub>5</sub>	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	
cmsat <sub>5</sub>	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	
cmsat <sub>5</sub>	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
cmsat5	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146	
cmsat5	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	
cmsat5	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546	
cmsat5	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	
cmsat5	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	
cmsat5	algotocnf_3.cnf	none	no	48704 / 254656	
cmsat5	algotocnf_3.cnf	cmsat	no	23893 / 111403	
cmsat5	algotocnf_3.cnf	lingeling	no	48704 / 100941	
cmsat5	algotocnf_3.cnf	minisat	no	20895 / 119580	
cmsat5	algotocnf_3.cnf	satelite	no	28647 / 156910	
cmsat5	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	
glucose	algotocnf_1.cnf	none	no	48704 / 225124	
glucose	algotocnf_1.cnf	cmsat	no	24503 / 111931	
glucose	algotocnf_1.cnf	minisat	no	20895 / 118236	
glucose	algotocnf_1.cnf	satelite	no	27495 / 153262	
glucose	algotocnf_18-t9.cnf	none	no	107839 / 582936	147
glucose	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	262
glucose	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	14
glucose	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	383
glucose	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	360

SAT solver	CNF file	simplified	phase	vars/clauses	propagations d
glucose	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	10471476
glucose	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	20143829
glucose	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	7239871
glucose	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	15403560
glucose	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	30131933
glucose	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	1231386505
glucose	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	1038552689
glucose	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	1251948097
glucose	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	785694216 2
glucose	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	751454677
glucose	algotocnf_2.cnf	none	no	48704 / 224220	
glucose	algotocnf_2.cnf	cmsat	no	24323 / 111661	
glucose	algotocnf_2.cnf	minisat	no	20895 / 118688	
glucose	algotocnf_2.cnf	satelite	no	27775 / 154276	
glucose	algotocnf_21-t9.cnf	none	no	116800 / 627112	
glucose	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	
glucose	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	
glucose	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	
glucose	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	
glucose	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	2790904343
glucose	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	1838242760
glucose	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	3062139546
glucose	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	3468599865
glucose	algotocnf_23-t9.cnf	none	no	122774 / 656628	
glucose	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	
glucose	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	
glucose	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	
glucose	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 936270	
glucose	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	
glucose	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	
glucose	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	
glucose	algotocnf_24-t9.cnf	none	no	125761 / 671432	
glucose	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	
glucose	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	
glucose	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	

SAT solver	CNF file	simplified	phase	vars/clauses	prop
glucose	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 957493	PTOP
glucose	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	
glucose	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	
glucose	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	
glucose	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	1
glucose	algotocnf_27-t10-diff.cnf	cmsat	no	0 / 0	-,
glucose	algotocnf_27-t10-diff.cnf	lingeling	no	0 / 0	
glucose	algotocnf_27-t10-diff.cnf	minisat	no	0 / 0	
glucose	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
glucose	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	0 / 0	
glucose	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	
glucose	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
glucose	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	0 / 0	
glucose	algotocnf_27-t10-simplified.cnf	none	no	134722 / 715830	
glucose	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	
glucose	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	
glucose	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998	
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1020826	
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443	
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309	
glucose	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589	
glucose	algotocnf_27-t10.cnf	none	no	134722 / 717878	
glucose	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
glucose	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
glucose	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
glucose	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1022874	
glucose	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	
glucose	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	
glucose	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
glucose	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	112
glucose	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	939
glucose	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	993
glucose	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	714
glucose	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	599
glucose	algotocnf_3.cnf	none	no	48704 / 222436	19
5.40036	2150100III_J.0III	110110	110	40/04/222430	19

SAT solver	CNF file	simplified	phase	vars/clauses	propagations
glucose	algotocnf_3.cnf	cmsat	no	23893 / 111403	23157475
glucose	algotocnf_3.cnf	lingeling	no	44000 / 100941	9187396
glucose	algotocnf_3.cnf	minisat	no	20895 / 119580	16616478
glucose	algotocnf_3.cnf	satelite	no	28647 / 156910	15878157
glucose	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	9899755
glucose-syrup	algotocnf_1.cnf	none	no	48704 / 225124	
glucose-syrup	algotocnf_1.cnf	cmsat	no	24503 / 111931	
glucose-syrup	algotocnf_1.cnf	minisat	no	20895 / 118236	
glucose-syrup	algotocnf_1.cnf	satelite	no	27495 / 153262	
glucose-syrup	algotocnf_18-t9.cnf	none	no	107839 / 582936	
glucose-syrup	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	
glucose-syrup	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	
glucose-syrup	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	
glucose-syrup	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	
glucose-syrup	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	
glucose-syrup	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	
glucose-syrup	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	
glucose-syrup	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	
glucose-syrup	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	
glucose-syrup	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	
glucose-syrup	algotocnf_2.cnf	none	no	48704 / 224220	
glucose-syrup	algotocnf_2.cnf	cmsat	no	24323 / 111661	
glucose-syrup	algotocnf_2.cnf	minisat	no	20895 / 118688	
glucose-syrup	algotocnf_2.cnf	satelite	no	27775 / 154276	
glucose-syrup	algotocnf_21-t9.cnf	none	no	116800 / 627112	
glucose-syrup	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	
glucose-syrup	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	
glucose-syrup	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	

SAT solver	CNF file	simplified	phase	vars/clauses	pr
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	P
glucose-syrup	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	
glucose-syrup	algotocnf_23-t9.cnf	none	no	122774 / 656628	
glucose-syrup	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	
glucose-syrup	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	
glucose-syrup	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 936270	
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	
glucose-syrup	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	
glucose-syrup	algotocnf_24-t9.cnf	none	no	125761 / 671432	
glucose-syrup	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	
glucose-syrup	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	
glucose-syrup	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 957493	
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	
glucose-syrup	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	
glucose-syrup	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	
glucose-syrup	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
glucose-syrup	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	
glucose-syrup	algotocnf_27-t10-diff.cnf	minisat	no	o / o	
glucose-syrup	algotocnf_27-t10-diff.cnf	satelite	no	o / o	
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	
glucose-syrup	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	
glucose-syrup	algotocnf_27-t10-simplified.cnf	none	no	134722 / 715830	
glucose-syrup	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680	
glucose-syrup	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404	
glucose-syrup	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998	
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1020826	
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302443	
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	89667 / 586309	
glucose-syrup	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589	

SAT solver	CNF file	simplified	phase	vars/clauses	propagatio
glucose-syrup	algotocnf_27-t10.cnf	none	no	134722 / 717878	Propugation
glucose-syrup	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	
glucose-syrup	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	
glucose-syrup	algotocnf_27-t10.cnf	satelite	no	85274 / 549734	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1022874	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	
glucose-syrup	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	
glucose-syrup	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	
glucose-syrup	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	
glucose-syrup	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	
glucose-syrup	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	
glucose-syrup	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	
glucose-syrup	algotocnf_3.cnf	none	no	48704 / 222436	
glucose-syrup	algotocnf_3.cnf	cmsat	no	23893 / 111403	
glucose-syrup	algotocnf_3.cnf	lingeling	no	44000 / 100941	
glucose-syrup	algotocnf_3.cnf	minisat	no	20895 / 119580	
glucose-syrup	algotocnf_3.cnf	satelite	no	28647 / 156910	
glucose-syrup	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	
lingeling-ats101	algotocnf_1.cnf	cmsat	no	24503 / 111931	830112341
lingeling-ats101	algotocnf_1.cnf	cmsat	yes	24503 / 111931	820517590
lingeling-ats101	algotocnf_1.cnf	minisat	no	20895 / 118236	575783290
lingeling-ats101	algotocnf_1.cnf	minisat	yes	20895 / 118236	333100908
lingeling-ats101	algotocnf_1.cnf	satelite	no	27495 / 153262	855959855
lingeling-ats101	algotocnf_1.cnf	satelite	yes	27495 / 153262	455268862
lingeling-ats101	algotocnf_18-t9.cnf	none	no	107839 / 590953	6579999
lingeling-ats101	algotocnf_18-t9.cnf	none	yes	107839 / 590953	6637382
lingeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	19838315
lingeling-ats101	algotocnf_18-t9.cnf	cmsat	yes	61789 / 342139	20128556
lingeling-ats101	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	4891154
lingeling-ats101	algotocnf_18-t9.cnf	lingeling	yes	102616 / 344544	3026807
lingeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	6037622
lingeling-ats101	algotocnf_18-t9.cnf	minisat	yes	61845 / 391134	8386925
lingeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	4521332
lingeling-ats101	algotocnf_18-t9.cnf	satelite	yes	69670 / 457972	6584687
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SAT solver	CNF file	simplified	phase	vars/clauses	prop
lingeling-ats101	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	no	196473 / 1197423	669
lingeling-ats101	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	yes	196473 / 1197423	655
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	none	yes	107839 / 846487	72
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	49
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	yes	57114 / 303489	30
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	40
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	yes	99452 / 404666	24
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	9
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	yes	78055 / 511431	27
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	44
lingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	yes	85386 / 692408	12
lingeling-ats101	algotocnf_18-t9_diff-desc_ocnf.cnf	none	no	107839 / 846487	668
lingeling-ats101	algotocnf_18-t9_diff-desc_ocnf.cnf	none	yes	107839 / 846487	684
lingeling-ats101	algotocnf_18-t9_ocnf.cnf	none	no	107839 / 590953	617
lingeling-ats101	algotocnf_18-t9_ocnf.cnf	none	yes	107839 / 590953	542
lingeling-ats101	algotocnf_1_diff-desc-sc_ocnf.cnf	none	no	85760 / 522144	7¢
lingeling-ats101	algotocnf_1_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522144	61
lingeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	29
lingeling-ats101	algotocnf_1_diff-desc.cnf	none	yes	48704 / 373920	63
lingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	60
lingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	yes	15402 / 73142	83
lingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	56
lingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	yes	40554 / 101182	29
lingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	72
lingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	yes	25107 / 158393	59
lingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	44
lingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	yes	30950 / 226602	6c
lingeling-ats101	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920	95
lingeling-ats101	algotocnf_1_diff-desc_ocnf.cnf	none	yes	48704 / 373920	22
lingeling-ats101	algotocnf_1_ocnf.cnf	none	no	48704 / 253984	24
lingeling-ats101	algotocnf_1_ocnf.cnf	none	yes	48704 / 253984	15
lingeling-ats101	algotocnf_2.cnf	none	no	48704 / 254210	96
lingeling-ats101	algotocnf_2.cnf	none	yes	48704 / 254210	10
lingeling-ats101	algotocnf_2.cnf	cmsat	no	24323 / 111661	19
lingeling-ats101	algotocnf_2.cnf	cmsat	yes	24323 / 111661	26
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SAT solver	CNF file	simplified	phase	vars/clauses	prop
lingeling-ats101	algotocnf_2.cnf	minisat	no	20895 / 118688	25.
lingeling-ats101	algotocnf_2.cnf	minisat	yes	20895 / 118688	13
lingeling-ats101	algotocnf_2.cnf	satelite	no	27775 / 154276	36
lingeling-ats101	algotocnf_2.cnf	satelite	yes	27775 / 154276	58
lingeling-ats101	algotocnf_21-t9.cnf	none	no	116800 / 636838	656
lingeling-ats101	algotocnf_21-t9.cnf	none	yes	116800 / 636838	122
lingeling-ats101	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	808
lingeling-ats101	algotocnf_21-t9.cnf	cmsat	yes	63555 / 358308	516
lingeling-ats101	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	755
lingeling-ats101	algotocnf_21-t9.cnf	minisat	yes	65572 / 414470	376
lingeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	941
lingeling-ats101	algotocnf_21-t9.cnf	satelite	yes	74562 / 486714	503
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	379
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	yes	116800 / 911629	89
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	19
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	yes	59528 / 318049	71
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	171
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	yes	81650 / 534965	108
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	81
lingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	yes	90236 / 720755	46
lingeling-ats101	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629	478
lingeling-ats101	algotocnf_21-t9_diff-desc_ocnf.cnf	none	yes	116800 / 911629	505
lingeling-ats101	algotocnf_23-t9.cnf	none	no	122774 / 667438	114
lingeling-ats101	algotocnf_23-t9.cnf	none	yes	122774 / 667438	925
lingeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	949
lingeling-ats101	algotocnf_23-t9.cnf	cmsat	yes	64880 / 369775	145
lingeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	775
lingeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	966
lingeling-ats101	algotocnf_23-t9.cnf	satelite	yes	77835 / 506217	100
lingeling-ats101	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343	355
lingeling-ats101	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	yes	222613 / 1350343	412
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	94
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	yes	122774 / 955067	69
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	70
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	yes	57510 / 307118	122

SAT solver	CNF file	simplified	phase	vars/clauses	prop
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	49
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	yes	84080 / 550727	135
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	297
lingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	yes	93504 / 740545	112
lingeling-ats101	algotocnf_23-t9_diff-desc_ocnf.cnf	none	no	122774 / 955067	393
lingeling-ats101	algotocnf_23-t9_diff-desc_ocnf.cnf	none	yes	122774 / 955067	403
lingeling-ats101	algotocnf_23-t9_ocnf.cnf	none	no	122774 / 667438	517
lingeling-ats101	algotocnf_23-t9_ocnf.cnf	none	yes	122774 / 667438	500
lingeling-ats101	algotocnf_24-t9.cnf	none	no	125761 / 682722	819
lingeling-ats101	algotocnf_24-t9.cnf	none	yes	125761 / 682722	111
lingeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	150
lingeling-ats101	algotocnf_24-t9.cnf	cmsat	yes	65579 / 377228	138
lingeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	107
lingeling-ats101	algotocnf_24-t9.cnf	minisat	yes	69023 / 436292	101
lingeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	148
lingeling-ats101	algotocnf_24-t9.cnf	satelite	yes	79486 / 515977	826
lingeling-ats101	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914	344
lingeling-ats101	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	yes	227841 / 1380914	395
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770	448
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	yes	125761 / 976770	78
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	48.
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	yes	56447 / 302014	89
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731	123
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	yes	85312 / 558731	99
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557	106
lingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	yes	95154 / 750557	36
lingeling-ats101	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	125761 / 976770	391
lingeling-ats101	algotocnf_24-t9_diff-desc_ocnf.cnf	none	yes	125761 / 976770	340
lingeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349	1
lingeling-ats101	algotocnf_27-t10-diff.cnf	none	yes	134722 / 728349	1
lingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	
lingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	yes	o / o	
lingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	
lingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	yes	o / o	
lingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	o / o	

SAT solver	CNF file	simplified	phase	vars/claus
lingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	o / o
lingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 104
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	yes	134722 / 104
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	yes	o / o
lingeling-ats101	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats101	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	yes	134722 / 104
lingeling-ats101	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722 / 728
lingeling-ats101	algotocnf_27-t10-diff_ocnf.cnf	none	yes	134722 / 728
lingeling-ats101	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728
lingeling-ats101	algotocnf_27-t10-simplified.cnf	none	yes	134722 / 728
lingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392
lingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	yes	67175 / 392
lingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460
lingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	yes	72909 / 460
lingeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544
lingeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	yes	84442 / 544
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	no	243525 / 147
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	yes	243525 / 147
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 104
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	yes	134722 / 104
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	yes	100735 / 789
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats101	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	yes	134722 / 104
lingeling-ats101	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722 / 728
lingeling-ats101	algotocnf_27-t10-simplified_ocnf.cnf	none	yes	134722 / 728

SAT solver	CNF file	simplified	phase	vars/clauses	pro
lingeling-ats101	algotocnf_27-t10.cnf	none	no	134722 / 728030	19
lingeling-ats101	algotocnf_27-t10.cnf	none	yes	134722 / 728030	23
lingeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276	28
lingeling-ats101	algotocnf_27-t10.cnf	cmsat	yes	72044 / 411276	19
lingeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897 / 465248	22
lingeling-ats101	algotocnf_27-t10.cnf	minisat	yes	73897 / 465248	14
lingeling-ats101	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525 / 1472083	28
lingeling-ats101	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	yes	243525 / 1472083	29
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335	16
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	yes	134722 / 1041335	15
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219	17
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	yes	57956 / 311219	19
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480	17
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675	15
lingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	yes	105733 / 857675	150
lingeling-ats101	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722 / 1041335	40
lingeling-ats101	algotocnf_27-t10_diff-desc_ocnf.cnf	none	yes	134722 / 1041335	34
lingeling-ats101	algotocnf_27-t10_ocnf.cnf	none	no	134722 / 728030	43
lingeling-ats101	algotocnf_27-t10_ocnf.cnf	none	yes	134722 / 728030	45
lingeling-ats101	algotocnf_2_diff-desc-sc_ocnf.cnf	none	no	85760 / 522370	4
lingeling-ats101	algotocnf_2_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522370	2
lingeling-ats101	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146	2
lingeling-ats101	algotocnf_2_diff-desc.cnf	none	yes	48704 / 374146	7
lingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	8
lingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	yes	15342 / 72870	1
lingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	5
lingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	yes	40767 / 106546	9
lingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	1
lingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	yes	23531 / 149436	5
lingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	8
lingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	yes	29428 / 204577	1
lingeling-ats101	algotocnf_2_diff-desc_ocnf.cnf	none	no	48704 / 374146	1
lingeling-ats101	algotocnf_2_diff-desc_ocnf.cnf	none	yes	48704 / 374146	2
lingeling-ats101	algotocnf_2_ocnf.cnf	none	no	48704 / 254210	20
lingeling-ats101	algotocnf_2_ocnf.cnf	none	yes	48704 / 254210	1

SAT solver	CNF file	simplified	phase	vars/clauses	prop
lingeling-ats101	algotocnf_3.cnf	none	no	48704 / 254656	13
lingeling-ats101	algotocnf_3.cnf	none	yes	48704 / 254656	13
lingeling-ats101	algotocnf_3.cnf	cmsat	no	23893 / 111403	25
lingeling-ats101	algotocnf_3.cnf	cmsat	yes	23893 / 111403	27
lingeling-ats101	algotocnf_3.cnf	lingeling	no	44000 / 100941	10
lingeling-ats101	algotocnf_3.cnf	lingeling	yes	44000 / 100941	9
lingeling-ats101	algotocnf_3.cnf	minisat	no	20895 / 119580	11
lingeling-ats101	algotocnf_3.cnf	minisat	yes	20895 / 119580	10
lingeling-ats101	algotocnf_3.cnf	satelite	no	28647 / 156910	17
lingeling-ats101	algotocnf_3.cnf	satelite	yes	28647 / 156910	15
lingeling-ats101	algotocnf_3_diff-desc-sc_ocnf.cnf	none	no	85760 / 522816	3
lingeling-ats101	algotocnf_3_diff-desc-sc_ocnf.cnf	none	yes	85760 / 522816	3
lingeling-ats101	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	5
lingeling-ats101	algotocnf_3_diff-desc.cnf	none	yes	48704 / 374592	3
lingeling-ats101	algotocnf_3_diff-desc_ocnf.cnf	none	no	48704 / 374592	6:
lingeling-ats101	algotocnf_3_diff-desc_ocnf.cnf	none	yes	48704 / 374592	5:
lingeling-ats101	algotocnf_3_ocnf.cnf	none	no	48704 / 254656	13
lingeling-ats101	algotocnf_3_ocnf.cnf	none	yes	48704 / 254656	12
lingeling-ats102	algotocnf_18-t9_diff-desc_ocnf.cnf	none	no	107839 / 846487	29
lingeling-ats102	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920	138
lingeling-ats102	algotocnf_1_ocnf.cnf	none	no	48704 / 253984	22
lingeling-ats102	algotocnf_21-t9.cnf	none	no	116800 / 636838	656
lingeling-ats102	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	941
lingeling-ats102	algotocnf_21-t9_diff-desc-sc_ocnf.cnf	none	no	212157 / 1289169	138
lingeling-ats102	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	206
lingeling-ats102	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	236
lingeling-ats102	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629	352
lingeling-ats102	algotocnf_21-t9_ocnf.cnf	none	no	116800 / 636838	12
lingeling-ats102	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	111
lingeling-ats102	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343	135
lingeling-ats102	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	297
lingeling-ats102	algotocnf_24-t9.cnf	none	no	125761 / 682722	819
lingeling-ats102	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	138
lingeling-ats102	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	107
lingeling-ats102	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914	151

0.455	over all		•	, ,
SAT solver	CNF file	simplified	phase	vars/claus
lingeling-ats102	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302
lingeling-ats102	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	125761 / 976
lingeling-ats102	algotocnf_24-t9_ocnf.cnf	none	no	125761 / 682
lingeling-ats102	algotocnf_27-t10-diff.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
lingeling-ats102	algotocnf_27-t10-diff.cnf	lingeling	no	o / o
lingeling-ats102	algotocnf_27-t10-diff.cnf	satelite	no	o / o
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 104
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
lingeling-ats102	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
lingeling-ats102	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats102	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392
lingeling-ats102	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460
lingeling-ats102	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	no	243525 / 147
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	56223 / 302
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789
lingeling-ats102	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats102	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_27-t10.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_27-t10.cnf	cmsat	no	72044 / 411
lingeling-ats102	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525 / 147
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 104
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311
lingeling-ats102	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857
lingeling-ats102	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats102	algotocnf_27-t10_ocnf.cnf	none	no	134722 / 728
lingeling-ats102	algotocnf_2_diff-desc_ocnf.cnf	none	no	48704 / 374
lingeling-ats102	algotocnf_2_ocnf.cnf	none	no	48704 / 254
lingeling-ats102	algotocnf_3_ocnf.cnf	none	no	48704 / 254
lingeling-ats104	algotocnf_18-t9_diff-desc-sc_ocnf.cnf	none	no	196473 / 119

SAT solver	CNF file	simplified	phase	vars/clauses
lingeling-ats104	algotocnf_18-t9_ocnf.cnf	none	no	107839 / 590953
lingeling-ats104	algotocnf_1_diff-desc_ocnf.cnf	none	no	48704 / 373920
lingeling-ats104	algotocnf_1_ocnf.cnf	none	no	48704 / 253984
lingeling-ats104	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308
lingeling-ats104	algotocnf_21-t9.cnf	satelite	no	74562 / 486714
lingeling-ats104	algotocnf_21-t9_diff-desc-sc_ocnf.cnf	none	no	212157 / 1289169
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049
lingeling-ats104	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126
lingeling-ats104	algotocnf_21-t9_diff-desc_ocnf.cnf	none	no	116800 / 911629
lingeling-ats104	algotocnf_21-t9_ocnf.cnf	none	no	116800 / 636838
lingeling-ats104	algotocnf_23-t9.cnf	satelite	no	77835 / 506217
lingeling-ats104	algotocnf_23-t9_diff-desc-sc_ocnf.cnf	none	no	222613 / 1350343
lingeling-ats104	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545
lingeling-ats104	algotocnf_23-t9_diff-desc_ocnf.cnf	none	no	122774 / 955067
lingeling-ats104	algotocnf_23-t9_ocnf.cnf	none	no	122774 / 667438
lingeling-ats104	algotocnf_24-t9.cnf	none	no	125761 / 682722
lingeling-ats104	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228
lingeling-ats104	algotocnf_24-t9.cnf	minisat	no	69023 / 436292
lingeling-ats104	algotocnf_24-t9_diff-desc-sc_ocnf.cnf	none	no	227841 / 1380914
lingeling-ats104	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014
lingeling-ats104	algotocnf_24-t9_diff-desc_ocnf.cnf	none	no	125761 / 976770
lingeling-ats104	algotocnf_24-t9_ocnf.cnf	none	no	125761 / 682722
lingeling-ats104	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349
lingeling-ats104	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
lingeling-ats104	algotocnf_27-t10-diff.cnf	lingeling	no	o / o
lingeling-ats104	algotocnf_27-t10-diff.cnf	satelite	no	o / o
lingeling-ats104	algotocnf_27-t10-diff_diff-desc-sc_ocnf.cnf	none	no	243525 / 1472402
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 1041654
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
lingeling-ats104	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
lingeling-ats104	algotocnf_27-t10-diff_diff-desc_ocnf.cnf	none	no	134722 / 1041654
lingeling-ats104	algotocnf_27-t10-diff_ocnf.cnf	none	no	134722 / 728349

SAT solver	CNF file	simplified	phase	vars/claus
lingeling-ats104	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728
lingeling-ats104	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460
lingeling-ats104	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc-sc_ocnf.cnf	none	no	243525 / 147
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 104
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789
lingeling-ats104	algotocnf_27-t10-simplified_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats104	algotocnf_27-t10-simplified_ocnf.cnf	none	no	134722 / 728
lingeling-ats104	algotocnf_27-t10.cnf	none	no	134722 / 728
lingeling-ats104	algotocnf_27-t10.cnf	cmsat	no	72044 / 411
lingeling-ats104	algotocnf_27-t10.cnf	minisat	no	73897 / 465
lingeling-ats104	algotocnf_27-t10.cnf	satelite	no	85274 / 549
lingeling-ats104	algotocnf_27-t10_diff-desc-sc_ocnf.cnf	none	no	243525 / 147
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619
lingeling-ats104	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857
lingeling-ats104	algotocnf_27-t10_diff-desc_ocnf.cnf	none	no	134722 / 104
lingeling-ats104	algotocnf_27-t10_ocnf.cnf	none	no	134722 / 728
lingeling-ats104	algotocnf_3_ocnf.cnf	none	no	48704 / 254
minisat	algotocnf_1.cnf	none	no	48704 / 225
minisat	algotocnf_1.cnf	none	no	
minisat	algotocnf_1.cnf	cmsat	no	
minisat	algotocnf_1.cnf	cmsat	no	24503 / 111
minisat	algotocnf_1.cnf	minisat	no	20895 / 118
minisat	algotocnf_1.cnf	minisat	no	
minisat	algotocnf_1.cnf	satelite	no	
minisat	algotocnf_1.cnf	satelite	no	27495 / 153
minisat	algotocnf_18-t9.cnf	none	no	107839 / 582
minisat	algotocnf_18-t9.cnf	none	no	
minisat	algotocnf_18-t9.cnf	cmsat	no	61789 / 342
minisat	algotocnf_18-t9.cnf	cmsat	no	
minisat	algotocnf_18-t9.cnf	lingeling	no	
minisat	algotocnf_18-t9.cnf	lingeling	no	102616 / 344
minisat	algotocnf_18-t9.cnf	minisat	no	61845 / 391
minisat	algotocnf_18-t9.cnf	minisat	no	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	d
minisat	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	17335955	
minisat	algotocnf_18-t9.cnf	satelite	no			
minisat	algotocnf_18-t9_diff-desc.cnf	none	no			
minisat	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	18671534	
minisat	algotocnf_18-t9_diff-desc.cnf	cmsat	no			
minisat	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	21547194	
minisat	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	7408845	
minisat	algotocnf_18-t9_diff-desc.cnf	lingeling	no			
minisat	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	6527792	
minisat	algotocnf_18-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_18-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	7396646	
minisat	algotocnf_1_diff-desc.cnf	none	no			
minisat	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	145509993	
minisat	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	221480273	
minisat	algotocnf_1_diff-desc.cnf	cmsat	no			
minisat	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	407709713	3
minisat	algotocnf_1_diff-desc.cnf	lingeling	no			
minisat	algotocnf_1_diff-desc.cnf	minisat	no			
minisat	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	166787763	
minisat	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	267008243	
minisat	algotocnf_1_diff-desc.cnf	satelite	no			
minisat	algotocnf_2.cnf	none	no			
minisat	algotocnf_2.cnf	none	no	48704 / 224220	201587749	
minisat	algotocnf_2.cnf	cmsat	no	24323 / 111661	2750894175	9
minisat	algotocnf_2.cnf	cmsat	no			
minisat	algotocnf_2.cnf	minisat	no			
minisat	algotocnf_2.cnf	minisat	no	20895 / 118688	491695491	2
minisat	algotocnf_2.cnf	satelite	no	27775 / 154276	1522804488	Ć
minisat	algotocnf_2.cnf	satelite	no			
minisat	algotocnf_21-t9.cnf	none	no			
minisat	algotocnf_21-t9.cnf	none	no			
minisat	algotocnf_21-t9.cnf	cmsat	no			
minisat	algotocnf_21-t9.cnf	cmsat	no			
minisat	algotocnf_21-t9.cnf	minisat	no			

SAT solver	CNF file	simplified	phase	vars/clauses	propagations	d
minisat	algotocnf_21-t9.cnf	minisat	no			
minisat	algotocnf_21-t9.cnf	satelite	no			
minisat	algotocnf_21-t9.cnf	satelite	no			
minisat	algotocnf_21-t9_diff-desc.cnf	none	no			
minisat	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	9147981007	1
minisat	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	577921212	1
minisat	algotocnf_21-t9_diff-desc.cnf	cmsat	no			
minisat	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	1058635766	2
minisat	algotocnf_21-t9_diff-desc.cnf	lingeling	no			
minisat	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	3082155154	4
minisat	algotocnf_21-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	4261434766	D.
minisat	algotocnf_21-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_23-t9.cnf	none	no			
minisat	algotocnf_23-t9.cnf	none	no			
minisat	algotocnf_23-t9.cnf	cmsat	no			
minisat	algotocnf_23-t9.cnf	cmsat	no			
minisat	algotocnf_23-t9.cnf	minisat	no			
minisat	algotocnf_23-t9.cnf	minisat	no			
minisat	algotocnf_23-t9.cnf	satelite	no			
minisat	algotocnf_23-t9.cnf	satelite	no			
minisat	algotocnf_23-t9_diff-desc.cnf	none	no			
minisat	algotocnf_23-t9_diff-desc.cnf	none	no			
minisat	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	3433286956	
minisat	algotocnf_23-t9_diff-desc.cnf	cmsat	no			
minisat	algotocnf_23-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_23-t9_diff-desc.cnf	minisat	no			
minisat	algotocnf_23-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_23-t9_diff-desc.cnf	satelite	no			
minisat	algotocnf_24-t9.cnf	none	no			
minisat	algotocnf_24-t9.cnf	none	no			
minisat	algotocnf_24-t9.cnf	cmsat	no			
minisat	algotocnf_24-t9.cnf	cmsat	no			
minisat	algotocnf_24-t9.cnf	minisat	no			
minisat	algotocnf_24-t9.cnf	minisat	no			

SAT solver	CNF file	simplified	phase	vars/clauses	propagations
minisat	algotocnf_24-t9.cnf	satelite	no		
minisat	algotocnf_24-t9.cnf	satelite	no		
minisat	algotocnf_24-t9_diff-desc.cnf	none	no		
minisat	algotocnf_24-t9_diff-desc.cnf	none	no		
minisat	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	3471709121
minisat	algotocnf_24-t9_diff-desc.cnf	cmsat	no		
minisat	algotocnf_24-t9_diff-desc.cnf	minisat	no		
minisat	algotocnf_24-t9_diff-desc.cnf	minisat	no		
minisat	algotocnf_24-t9_diff-desc.cnf	satelite	no		
minisat	algotocnf_24-t9_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	134722
minisat	algotocnf_27-t10-diff.cnf	none	no		
minisat	algotocnf_27-t10-diff.cnf	cmsat	no		
minisat	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	0
minisat	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	0
minisat	algotocnf_27-t10-diff.cnf	lingeling	no		
minisat	algotocnf_27-t10-diff.cnf	minisat	no		
minisat	algotocnf_27-t10-diff.cnf	minisat	no	o / o	0
minisat	algotocnf_27-t10-diff.cnf	satelite	no		
minisat	algotocnf_27-t10-diff.cnf	satelite	no	o / o	0
minisat	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 8320	134722
minisat	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	0
minisat	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no		
minisat	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	0
minisat	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	0
minisat	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o	0
minisat	algotocnf_27-t10-simplified.cnf	none	no		
minisat	algotocnf_27-t10-simplified.cnf	none	no		
minisat	algotocnf_27-t10-simplified.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified.cnf	minisat	no		
minisat	algotocnf_27-t10-simplified.cnf	minisat	no		

SAT solver	CNF file	simplified	phase	vars/clauses	propag
minisat	algotocnf_27-t10-simplified.cnf	satelite	no	vars/clauses	propag
minisat	algotocnf_27-t10-simplified.cnf	satelite	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	minisat			
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no		
minisat		mmsat satelite	no		
	algotocnf_27-t10-simplified_diff-desc.cnf		no		
minisat	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10.cnf	none	no		
minisat	algotocnf_27-t10.cnf	none	no		
minisat	algotocnf_27-t10.cnf	cmsat	no		
minisat	algotocnf_27-t10.cnf	cmsat	no		
minisat	algotocnf_27-t10.cnf	minisat	no		
minisat	algotocnf_27-t10.cnf	minisat	no		
minisat	algotocnf_27-t10.cnf	satelite	no		
minisat	algotocnf_27-t10.cnf	satelite	no		
minisat	algotocnf_27-t10_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10_diff-desc.cnf	none	no		
minisat	algotocnf_27-t10_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	cmsat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	minisat	no		
minisat	algotocnf_27-t10_diff-desc.cnf	satelite	no		
minisat	algotocnf_27-t10_diff-desc.cnf	satelite	no		
minisat	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788	4414
minisat	algotocnf_2_diff-desc.cnf	none	no		
minisat	algotocnf_2_diff-desc.cnf	cmsat	no		
minisat	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870	99844
minisat	algotocnf_2_diff-desc.cnf	lingeling	no		
minisat	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546	11876
minisat	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436	16959
minisat	algotocnf_2_diff-desc.cnf	minisat	no	1,10	, 3,
minisat	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577	11840
				, 1	

SAT solver	CNF file	simplified	phase	vars/clauses	propagations of
minisat	algotocnf_2_diff-desc.cnf	satelite	no		1 1 0
minisat	algotocnf_3.cnf	none	no	48704 / 222436	13991247
minisat	algotocnf_3.cnf	none	no		
minisat	algotocnf_3.cnf	cmsat	no	23893 / 111403	15330537
minisat	algotocnf_3.cnf	cmsat	no		
minisat	algotocnf_3.cnf	lingeling	no		
minisat	algotocnf_3.cnf	lingeling	no	44000 / 100941	3922854
minisat	algotocnf_3.cnf	minisat	no	20895 / 119580	11055439
minisat	algotocnf_3.cnf	minisat	no		
minisat	algotocnf_3.cnf	satelite	no		
minisat	algotocnf_3.cnf	satelite	no	28647 / 156910	15840699
minisat	algotocnf_3_diff-desc.cnf	none	no		
minisat	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004	8355604
minisat-core	algotocnf_1.cnf	none	no	48704 / 225124	12249636981
minisat-core	algotocnf_1.cnf	cmsat	no	24503 / 111931	1345904991
minisat-core	algotocnf_1.cnf	minisat	no	20895 / 118236	1001195109
minisat-core	algotocnf_1.cnf	satelite	no	27495 / 153262	2852530112
minisat-core	algotocnf_18-t9.cnf	none	no	107839 / 582936	197561807
minisat-core	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139	3714952
minisat-core	algotocnf_18-t9.cnf	lingeling	no	102616 / 344544	27126157
minisat-core	algotocnf_18-t9.cnf	minisat	no	61845 / 391134	11474979
minisat-core	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	48139459
minisat-core	algotocnf_18-t9_diff-desc.cnf	none	no	107839 / 831263	134492463
minisat-core	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	22660129
minisat-core	algotocnf_18-t9_diff-desc.cnf	lingeling	no	99452 / 404666	4783352
minisat-core	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	6527792
minisat-core	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	68801966
minisat-core	algotocnf_1_diff-desc.cnf	none	no	48704 / 330692	556973568
minisat-core	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	565587287
minisat-core	algotocnf_1_diff-desc.cnf	lingeling	no	40554 / 101182	130669677
minisat-core	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	166787763
minisat-core	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	218192599
minisat-core	algotocnf_2.cnf	none	no	48704 / 224220	4474027487
minisat-core	algotocnf_2.cnf	cmsat	no	24323 / 111661	3271551070
minisat-core	algotocnf_2.cnf	minisat	no	20895 / 118688	491695491

SAT solver	CNF file	simplified	phase	vars/clauses	propagation
minisat-core	algotocnf_2.cnf	satelite	no	27775 / 154276	1356174519
minisat-core	algotocnf_21-t9.cnf	none	no		
minisat-core	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	972084600
minisat-core	algotocnf_21-t9.cnf	minisat	no		
minisat-core	algotocnf_21-t9.cnf	satelite	no		
minisat-core	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 894072	6184915141
minisat-core	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	3033335128
minisat-core	algotocnf_21-t9_diff-desc.cnf	lingeling	no	104860 / 404126	2309115640
minisat-core	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	3082155154
minisat-core	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	2028870107
minisat-core	algotocnf_23-t9.cnf	none	no		
minisat-core	algotocnf_23-t9.cnf	cmsat	no		
minisat-core	algotocnf_23-t9.cnf	minisat	no		
minisat-core	algotocnf_23-t9.cnf	satelite	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	none	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	6686701995
minisat-core	algotocnf_23-t9_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_23-t9_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_24-t9.cnf	none	no		
minisat-core	algotocnf_24-t9.cnf	cmsat	no		
minisat-core	algotocnf_24-t9.cnf	minisat	no		
minisat-core	algotocnf_24-t9.cnf	satelite	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	none	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014	3308202991
minisat-core	algotocnf_24-t9_diff-desc.cnf	minisat	no		
minisat-core	algotocnf_24-t9_diff-desc.cnf	satelite	no		
minisat-core	algotocnf_27-t10-diff.cnf	none	no	134722 / 8320	134722
minisat-core	algotocnf_27-t10-diff.cnf	cmsat	no	o / o	o
minisat-core	algotocnf_27-t10-diff.cnf	lingeling	no	o / o	o
minisat-core	algotocnf_27-t10-diff.cnf	minisat	no	o / o	0
minisat-core	algotocnf_27-t10-diff.cnf	satelite	no	o / o	o
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 8320	134722
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o	o
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	o / o	0
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o	o
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SAT solver	CNF file	simplified	phase	vars/clauses ]
minisat-core	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
minisat-core	algotocnf_27-t10-simplified.cnf	none	no	
minisat-core	algotocnf_27-t10-simplified.cnf	cmsat	no	
minisat-core	algotocnf_27-t10-simplified.cnf	minisat	no	
minisat-core	algotocnf_27-t10-simplified.cnf	satelite	no	
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	cmsat	no	
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	minisat	no	
minisat-core	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	
minisat-core	algotocnf_27-t10.cnf	none	no	
minisat-core	algotocnf_27-t10.cnf	cmsat	no	
minisat-core	algotocnf_27-t10.cnf	minisat	no	
minisat-core	algotocnf_27-t10.cnf	satelite	no	
minisat-core	algotocnf_27-t10_diff-desc.cnf	none	no	
minisat-core	algotocnf_27-t10_diff-desc.cnf	cmsat	no	
minisat-core	algotocnf_27-t10_diff-desc.cnf	minisat	no	
minisat-core	algotocnf_27-t10_diff-desc.cnf	satelite	no	
minisat-core	algotocnf_2_diff-desc.cnf	none	no	48704 / 329788
minisat-core	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870
minisat-core	algotocnf_2_diff-desc.cnf	lingeling	no	40767 / 106546
minisat-core	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436
minisat-core	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577
minisat-core	algotocnf_3.cnf	none	no	48704 / 222436
minisat-core	algotocnf_3.cnf	cmsat	no	23893 / 111403
minisat-core	algotocnf_3.cnf	lingeling	no	44000 / 100941
minisat-core	algotocnf_3.cnf	minisat	no	20895 / 119580
minisat-core	algotocnf_3.cnf	satelite	no	28647 / 156910
minisat-core	algotocnf_3_diff-desc.cnf	none	no	48704 / 328004
plingeling-ats101	algotocnf_1.cnf	cmsat	no	24503 / 111931
plingeling-ats101	algotocnf_1.cnf	minisat	no	20895 / 118236
plingeling-ats101	algotocnf_1.cnf	satelite	no	27495 / 153262
plingeling-ats101	algotocnf_18-t9.cnf	none	no	107839 / 590953
plingeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789 / 342139
plingeling-ats101	algotocnf_18-t9.cnf	lingeling	no	107839 / 344544
plingeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845 / 391134

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SAT solver	CNF file	simplified	phase	vars/clauses	propagation
plingeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670 / 457972	396313800
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114 / 303489	949615550
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839 / 404666	745621300
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055 / 511431	52703620
plingeling-ats101	algotocnf_18-t9_diff-desc.cnf	satelite	no	85386 / 692408	375280530
plingeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704 / 373920	4289131630
plingeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402 / 73142	3548147180
plingeling-ats101	algotocnf_1_diff-desc.cnf	lingeling	no	48704 / 101182	3180845780
plingeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107 / 158393	1965238720
plingeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950 / 226602	2491219360
plingeling-ats101	algotocnf_2.cnf	none	no	48704 / 254210	11278846250
plingeling-ats101	algotocnf_2.cnf	cmsat	no	24323 / 111661	8145031310
plingeling-ats101	algotocnf_2.cnf	minisat	no	20895 / 118688	3124819420
plingeling-ats101	algotocnf_2.cnf	satelite	no	27775 / 154276	6888905530
plingeling-ats101	algotocnf_21-t9.cnf	none	no	116800 / 636838	13018864036
plingeling-ats101	algotocnf_21-t9.cnf	cmsat	no	63555 / 358308	17255856970
plingeling-ats101	algotocnf_21-t9.cnf	minisat	no	65572 / 414470	19127495743
plingeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562 / 486714	13270281976
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800 / 911629	18514838920
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528 / 318049	14450240650
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650 / 534965	21718771620
plingeling-ats101	algotocnf_21-t9_diff-desc.cnf	satelite	no	90236 / 720755	23804708950
plingeling-ats101	algotocnf_23-t9.cnf	none	no	122774 / 667438	23192521256
plingeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880 / 369775	25198320234
plingeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979 / 429734	26199150579
plingeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835 / 506217	22883132571
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774 / 955067	55888853190
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510 / 307118	25488237880
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080 / 550727	39712137130
plingeling-ats101	algotocnf_23-t9_diff-desc.cnf	satelite	no	93504 / 740545	53177836930
plingeling-ats101	algotocnf_24-t9.cnf	none	no	125761 / 682722	76819121092
plingeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579 / 377228	27427809301
plingeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023 / 436292	25106209612
plingeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486 / 515977	29514712835
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761 / 976770	43878084770

SAT solver	CNF file	simplified	phase	vars/clauses
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447 / 302014
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312 / 558731
plingeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154 / 750557
plingeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722 / 728349
plingeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	o / o
plingeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	134722 / o
plingeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	o / o
plingeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	o / o
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	none	no	134722 / 1041654
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	o / o
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722 / 0
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	o / o
plingeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	o / o
plingeling-ats101	algotocnf_27-t10-simplified.cnf	none	no	134722 / 728542
plingeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175 / 392680
plingeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909 / 460404
plingeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	no	84442 / 544998
plingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	none	no	134722 / 1041847
plingeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735 / 789589
plingeling-ats101	algotocnf_27-t10.cnf	none	no	134722 / 728030
plingeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044 / 411276
plingeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897 / 465248
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722 / 1041335
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956 / 311219
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850 / 619480
plingeling-ats101	algotocnf_27-t10_diff-desc.cnf	satelite	no	105733 / 857675
plingeling-ats101	algotocnf_2_diff-desc.cnf	none	no	48704 / 374146
plingeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342 / 72870
plingeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	48704 / 106546
plingeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531 / 149436
plingeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428 / 204577
plingeling-ats101	algotocnf_3.cnf	none	no	48704 / 254656
plingeling-ats101	algotocnf_3.cnf	cmsat	no	23893 / 111403
plingeling-ats101	algotocnf_3.cnf	lingeling	no	48704 / 100941
plingeling-ats101	algotocnf_3.cnf	minisat	no	20895 / 119580

SAT solver	CNF file	simplified	phase	vars/clauses	propaga
plingeling-ats101	algotocnf_3.cnf	satelite	no	28647 / 156910	637183
plingeling-ats101	algotocnf_3_diff-desc.cnf	none	no	48704 / 374592	220439
treengeling-ats101	algotocnf_1.cnf	cmsat	no	24503.0 / 111931.0	175862
treengeling-ats101	algotocnf_1.cnf	minisat	no	20895.0 / 118236.0	117398
treengeling-ats101	algotocnf_1.cnf	satelite	no	27495.0 / 153262.0	125001
treengeling-ats101	algotocnf_18-t9.cnf	none	no	107839.0 / 590953.0	8099:
treengeling-ats101	algotocnf_18-t9.cnf	cmsat	no	61789.0 / 342139.0	40223
treengeling-ats101	algotocnf_18-t9.cnf	lingeling	no	107839.0 / 344544.0	61139
treengeling-ats101	algotocnf_18-t9.cnf	minisat	no	61845.0 / 391134.0	60568
treengeling-ats101	algotocnf_18-t9.cnf	satelite	no	69670.0 / 457972.0	12679
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	cmsat	no	57114.0 / 303489.0	198613
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	lingeling	no	107839.0 / 404666.0	9802
treengeling-ats101	algotocnf_18-t9_diff-desc.cnf	minisat	no	78055.0 / 511431.0	27418:
treengeling-ats101	algotocnf_1_diff-desc.cnf	none	no	48704.0 / 373920.0	357794
treengeling-ats101	algotocnf_1_diff-desc.cnf	cmsat	no	15402.0 / 73142.0	584854
treengeling-ats101	algotocnf_1_diff-desc.cnf	minisat	no	25107.0 / 158393.0	183160
treengeling-ats101	algotocnf_1_diff-desc.cnf	satelite	no	30950.0 / 226602.0	568539
treengeling-ats101	algotocnf_2.cnf	none	no	48704.0 / 254210.0	138155
treengeling-ats101	algotocnf_2.cnf	cmsat	no	24323.0 / 111661.0	21519
treengeling-ats101	algotocnf_2.cnf	minisat	no	20895.0 / 118688.0	60162
treengeling-ats101	algotocnf_2.cnf	satelite	no	27775.0 / 154276.0	136587
treengeling-ats101	algotocnf_21-t9.cnf	satelite	no	74562.0 / 486714.0	4895202
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	none	no	116800.0 / 911629.0	733199
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	cmsat	no	59528.0 / 318049.0	42250
treengeling-ats101	algotocnf_21-t9_diff-desc.cnf	minisat	no	81650.0 / 534965.0	216384
treengeling-ats101	algotocnf_23-t9.cnf	none	no	122774.0 / 667438.0	4370733
treengeling-ats101	algotocnf_23-t9.cnf	cmsat	no	64880.0 / 369775.0	4261582
treengeling-ats101	algotocnf_23-t9.cnf	minisat	no	67979.0 / 429734.0	4360860
treengeling-ats101	algotocnf_23-t9.cnf	satelite	no	77835.0 / 506217.0	3489623
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	none	no	122774.0 / 955067.0	206455
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	cmsat	no	57510.0 / 307118.0	622033
treengeling-ats101	algotocnf_23-t9_diff-desc.cnf	minisat	no	84080.0 / 550727.0	119542
treengeling-ats101	algotocnf_24-t9.cnf	cmsat	no	65579.0 / 377228.0	3937230
treengeling-ats101	algotocnf_24-t9.cnf	minisat	no	69023.0 / 436292.0	4209019
treengeling-ats101	algotocnf_24-t9.cnf	satelite	no	79486.0 / 515977.0	5006094

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SAT solver	CNF file	simplified	phase	vars/clauses
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	none	no	125761.0 / 976770
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	cmsat	no	56447.0 / 302014.
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	minisat	no	85312.0 / 558731.
treengeling-ats101	algotocnf_24-t9_diff-desc.cnf	satelite	no	95154.0 / 750557.
treengeling-ats101	algotocnf_27-t10-diff.cnf	none	no	134722.0 / 728349
treengeling-ats101	algotocnf_27-t10-diff.cnf	cmsat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	lingeling	no	134722.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	minisat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff.cnf	satelite	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	cmsat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	lingeling	no	134722.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	minisat	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-diff_diff-desc.cnf	satelite	no	0.0 / 0.0
treengeling-ats101	algotocnf_27-t10-simplified.cnf	cmsat	no	67175.0 / 392680.
treengeling-ats101	algotocnf_27-t10-simplified.cnf	minisat	no	72909.0 / 460404.
treengeling-ats101	algotocnf_27-t10-simplified.cnf	satelite	no	84442.0 / 544998.
treengeling-ats101	algotocnf_27-t10-simplified_diff-desc.cnf	satelite	no	100735.0 / 789589
treengeling-ats101	algotocnf_27-t10.cnf	none	no	134722.0 / 728030
treengeling-ats101	algotocnf_27-t10.cnf	cmsat	no	72044.0 / 411276.
treengeling-ats101	algotocnf_27-t10.cnf	minisat	no	73897.0 / 465248.
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	none	no	134722.0 / 1041335
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	cmsat	no	57956.0 / 311219.
treengeling-ats101	algotocnf_27-t10_diff-desc.cnf	minisat	no	94850.0 / 619480.
treengeling-ats101	algotocnf_2_diff-desc.cnf	cmsat	no	15342.0 / 72870.0
treengeling-ats101	algotocnf_2_diff-desc.cnf	lingeling	no	48704.0 / 106546.
treengeling-ats101	algotocnf_2_diff-desc.cnf	minisat	no	23531.0 / 149436.
treengeling-ats101	algotocnf_2_diff-desc.cnf	satelite	no	29428.0 / 204577.
treengeling-ats101	algotocnf_3.cnf	none	no	48704.0 / 254656.
treengeling-ats101	algotocnf_3.cnf	cmsat	no	23893.0 / 111403.
treengeling-ats101	algotocnf_3.cnf	lingeling	no	48704.0 / 100941.
treengeling-ats101	algotocnf_3.cnf	minisat	no	20895.0 / 119580.
treengeling-ats101	algotocnf_3.cnf	satelite	no	28647.0 / 156910.
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