University of Technology, Graz

Master Thesis

Differential cryptanalysis with SAT solvers

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Differential cryptanalysis with SAT solvers

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ABSTRACT

Hash functions are ubiquitous in the modern information age. They provide preimage, second preimage and collision resistance in a wide range of applications. They are used as cryptographic primitives in protocols and applications.

In August 2006, Wang et al. showed efficient attacks against several hash function designs including MD4, MD5, HAVAL-128 and RIPEMD. With these results differential cryptanalysis has been proven useful to break collision resistance in hash functions. Over the years advanced attacks based on those differential approaches have been developed.

In this thesis we encode differential attack settings as SAT problems. SAT solvers are utilized to solve the problem revealing actual message collisions for a defined message difference.

Keywords: hash function, differential cryptanalysis, MD4, collision resistance, satisfiability, SAT solver

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All source code is available at lukas-prokop.at/proj/megosat and published under terms and conditions of Free/Libre Open Source Software. This document was printed with Lual*IFX and Linux Libertine Font.

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Chapter 1

Introduction

Hash functions are used as cryptographic primitives in many applications and protocols. They take an arbitrary input message and provide a hash value. Input message and hash value are considered as byte strings in a particular encoding. The hash value is of fixed length and satisfies several properties which make it useful in a variety of applications.

In this thesis we will consider the hash algorithms MD4 and SHA-256 and represent differential characteristics of hash collisions as SAT problem. If and only if satisfiability is given, the particular differential state is achievable using two different inputs leading to the same output. As far as SAT solvers return an actual model satisfying that state, we get a complete hash collision which can be verified and visualized. If the internal state of the hash algorithm is too large, the attack can be easily computationally simplified by modelling only a subset of steps of the hash algorithm or changing the modelled differential path.

Gaining experience with these kind of problems with previous non-SAT-based tools we try to apply best practices to a satisfiability setting. We will discuss which SAT techniques lead to best performance characteristics for our MD $_4$ and SHA- $_256$ testcases.

1.1 Preliminaries

Definition 1.1 (Hash function)

A *hash function* is a mapping $h: X \to Y$ with $X = \{0, 1\}^*$ and $Y = \{0, 1\}^n$ for some fixed $n \in \mathbb{N}_{>1}$.

- Let $x \in X$, then h(x) is called hash value of x.
- Let $h(x) = y \in Y$, then x is called *preimage of y*.

One example showing the use of hash functions as primitives is PKCS #5 specified in RFC 2898 [5]. Section 5.2 specifies PBKDF1 and PBKDF2 using an arbitrary pseudorandom function to derive password-based keys. Hash algorithms can be used as those pseudorandom functions. Given a minimum iteration count of 1000, as defined in section 4.2, yields the additional requirement that fast computation of hash values for given $x \in X$ is desirable.

A hash function has to satisfy the following security requirements:

Definition 1.2 (Preimage resistance)

Given $y \in Y$, a hash function h is *preimage resistant* iff it is computationally infeasible to find $x \in X$ such that h(x) = y.

Definition 1.3 (Second-preimage resistance)

Given $x \in X$, a hash function h is second-preimage resistant iff it is computationally infeasible to find $x_2 \in X$ with $x \neq x_2$ such that $h(x) = h(x_2)$. x_2 is called second preimage.

Definition 1.4 (Collision resistance)

A hash function h is *collision resistant* iff it is computationally infeasible to find any two $x \in X$ and $x_2 \in X$ with $x \neq x_2$ such that $h(x) = h(x_2)$.

As far as hash functions accept input strings of arbitrary length, but return a fixed size output string, existence of collisions is unavoidable [13]. However, good hash functions make it very difficult to determine collisions or preimages.

Most hash functions apply padding to their input to normalize the input size to a multiple of its block size before running a round function. In the following we always consider input of block size meaning the round function is run only for one block and padding is always considered part of this input message. Padding is negligible, because given two colliding blocks, we can add another incomplete block. Padding will occur only in the second block and with the same values in the second blocks it yield the same padded value. This results in a length extension attack, making input padding negligible for cryptanalysis.

	Message 1			
4d7a9c83	d6cb927a	29d5a578	57a7a5ee	
de748a3c	dcc366b3	b683a020	3b2a5d9f	
c69d71b3	f9e99198	d79f805e	a63bb2e8	
45dc8e31	97e31fe5	2794bfo8	b9e8c3e9	
	Messa	age 2		
4d7a9c83	56cb927a	b9d5a578	57a7a5ee	
de748a3c	dcc366b3	b683a020	3b2a5d9f	
c69d71b3	f9e99198	d79f805e	a63bb2e8	
45dd8e31	97e31fe5	2794bfo8	b9e8c3e9	
Hash value of Message 1 and Message 2				
5f5c1aod	71b36046	1b5435da	9bod8o7a	

Table 1.1: One of two MD4 hash collisions provided in [16]. Values are given in hexadecimal, message words are enumerated from left to right, top to bottom. Differences are highlighted in bold for illustration purposes. For comparison the first bits of Message 1 are 11000001... and the last bits are ...10011101. A message represents one block of 512 bits.

1.2 Cryptanalysis of Hash Functions

In August 2004, Wang et al. published results at Crypto'04 [16] which revealed that MD4, MD5, HAVAL-128 and RIPEMD can be broken practically using differential cryptanalysis. Their work is based on preliminary work by Hans Dobbertin [4]. On an IBM P690 machine, an MD5 collision can be computed in about one hour using this approach. Collisions for HAVAL-128, MD4 and RIPEMD were found as well. Patrick Stach's md4coll.c program [14] implements Wang's approach and can find MD4 collisions in few seconds on my Thinkpad x220 setup specified in Appendix C.

Let n denote the digest size, hence the size of the hash value h(x) as number of bits. Due to the birthday paradox, a collision attack has a generic complexity of $2^{n/2}$ whereas pre-image and second pre-image attacks have generic complexities of 2^n .

Following results by Wang et al., differential cryptanalysis was shown as powerful tool for cryptanalysis of hash algorithms. This thesis applies those ideas to satisfiability approaches.

1.3 Differential cryptanalysis

Definition 1.5 (Hash collisoin)

Given a hash function h, a hash collision is a pair (x, x_2) with $x \neq x_2$ such that

v_1	v_2	$f(v_1, v_2)$	v_1	v_2	$f(v_1, v_2)$	v	f(v)
1	1	1	1	1	1	1	0
1	0	0	1	0	1	0	1
0	1	0	0	1	1	(0	e) NOT
0	0	0	0	0	0	,	,
	(a)	AND		(b) OR		

Figure 1.1: Truth tables for AND, OR and NOT

$$h(x) = h(x_2).$$

Differential cryptanalysis is based on the idea to consider two execution states of hash algorithms for slightly different input messages. We trace those difference to learn about the propagation of message differences.

Considering some hash function f, we look for two input messages x and x_2 such that the output values h(x) and $h(x_2)$ correspond yielding a hash collision.

1.4 Satisfiability

Definition 1.6

A boolean function is a mapping $h: X \to Y$ with $X = \{0, 1\}^n$ for $n \in \mathbb{N}_{\geq 1}$ and $Y = \{0, 1\}$.

The following definition gives three basic boolean functions:

Definition 1.7

AND is a boolean function mapping $X = \{0, 1\}^2$ to 1 if all values of X are 1. *OR* is a boolean function mapping $X = \{0, 1\}^2$ to 1 if any value of X is 1. *NOT* is a boolean function mapping $X = \{0, 1\}^1$ to 1 if the single value of X is 0. All functions return 0 in the other case.

Definition 1.8

A *truth table* unambiguously defines a boolean function by enlisting the evaluated truth value for all possible sets of inputs.

Table 1.1 shows truth tables for AND, OR and NOT.

In the following we discuss how boolean functions are related to computation in general and hash algorithms specifically.

Definition 1.9

An *algorithm* is a step-wise set of instructions to solve a problem.

One specific set of algorithms transform a given input to some output according to some rules. Such algorithms are said to satisfy the *I/O property*. Hash algorithms satisfy the *I/O* property.

Theorem 1.1

Every algorithm can be represented as boolean function.

This is trivial to see considering that computers are built from logic gates. However, in practice physical properties are used to employ storage of values, which does not exist in the model of boolean algebra. This can be mapped to our boolean model by constants for stored values and assuming an infinite memory.

Definition 1.10

A boolean function is *satisfiable* iff there exists at least one input $x \in X$ such that h(x) = 1. Every input $x \in X$ satisfying this property is called *model*. Every element of X is called *assignment*.

In the following we will establish some theory to reach the following property:

Definition 1.11

A boolean function is *satisfiable* iff a certain state in two hash algorithm instances is achievable.

The generic complexity of SAT determination is given by 2^n for n boolean variables. The corresponding tool to determine satisfiability is defined in the following.

Definition 1.12

A *SAT solver* is a tool to determine satisfiability of a boolean function. If satisfiability is given, it returns some model.

1.5 Thesis Outline

This thesis is organized as follows:

- **In Chapter 1** we discussed the basic properties and fundamentals of the tools in discussion including hash functions and SAT solvers.
- **In Chapter 2** we introduce the MD₄ and SHA-256 hash functions and discuss possible approaches in differential cryptanalysis.
- **In Chapter 3** we discuss SAT solving and potential approaches to speed up SAT solvers for cryptographic problems.

In Chapter 4 we show results of our work and discuss its implications.

In Chapter 5 we suggest future work based on our results.



"Just because it's automatic doesn't mean it works." —Daniel J. Bernstein

Chapter 2

Differential cryptanalysis

2.1 MD4

MD4 is a cryptographic hash function originally described in RFC 1186 [10], updated in RFC 1320 [11] and declared obsolete by RFC 6150 [15]. It was invented by Ronald Rivest in 1990 with properties given in Table 2.1. Since 1995 [4] successful attacks have been found to break collisions, preimage and second-preimage resistance in MD4; including but not limited to [12] and [7]. A Python 3 implementation derived from a previous Python version is available at github [9].

```
block size 512 bits namely variable block in RFC 1320 [11] digest size 128 bits as per section 3.5 in RFC 1320 [11] internal state size 128 bits namely variables A, B, C and D word size 32 bits as per section 2 in RFC 1320 [11]
```

Table 2.1: MD4 hash algorithm properties

In the following a quick overview over MD4's design is given.

First of all, padding is applied. A single bit 1 is appended to the input. As long as the input does not reach a length congruent 448 modulo 512, bit 0 is appended. Followingly, length appending takes place. Represent the length of the input (without the modifications of the previous step) in binary and take its first 64 bits.

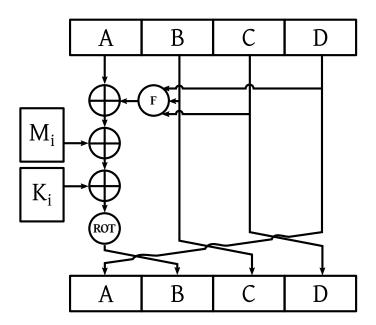


Figure 2.1: MD4 round function

Append those 64 bits to the input.

The message is split into 512-bit blocks (i.e. 16 32-bit words). Four state variables A, B, C and D are initialized with hexadecimal values:

To process one block, three auxiliary boolean functions are defined:

$$\operatorname{IF}(X, Y, Z) = (X \wedge Y) \vee (\neg X \wedge Z) \tag{2.1}$$

$$MAJ(X, Y, Z) = (X \land Y) \lor (X \land Z) \lor (Y \land Z) \tag{2.2}$$

$$XOR(X, Y, Z) = X \oplus Y \oplus Z$$
 (2.3)

Definition 2.1

The boolean IF function behaves the following way: If the first argument is true, the second argument is returned. If the first argument is false, the third argument is returned.

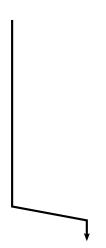
The boolean MAJ function returns true if the number of boolean values true in arguments is at least 2. The boolean XOR function returns true if the number of boolean values true in arguments is odd.

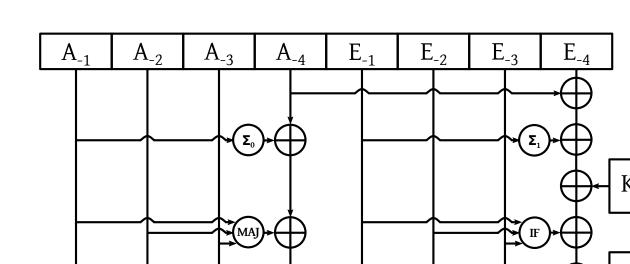
2.2. SHA-256 9

- 2.2 SHA-256
- 2.3 Differential notation

[2]

- 2.4 Addition example
- 2.5 Differential path







"What idiot called them logic errors rather than bool shit?"

—Unknown

Chapter 3

Satisfiability

3.1 The DIMACS de-facto standard

Definition 3.1

A *conjunction* is a sequence of boolean functions combined using a logical OR. A *disjunction* is a sequence of boolean functions combined using a logical AND. A *literal* is a boolean variable (*positive*) or its negation (*negative*).

A SAT problem is given in *Conjunctive Normal Form* (CNF) if the problem is defined as conjunction of disjunctions of literals.

A simple example for a SAT problem in CNF is the exclusive OR (XOR). It takes two boolean values a and b as arguments and returns true if and only if the two arguments differ.

$$(a \lor b) \land (\neg a \lor \neg b) \tag{3.1}$$

Display 3.1 shows one conjunction (denoted \land) of two disjunctions (denoted \lor) of literals (denoted a and b where prefix \neg represents negation). This structure constitutes a CNF.

Analogously we define a *Disjunctive Normal Form* (DNF) as disjunction of conjunctions of literals. The negation of a CNF is in DNF, because literals are negated and conjunctions become disjunctions, vice versa.

Theorem 3.1

Every boolean function can be represented as CNF.

Theorem 3.1 is easy to prove. Consider the truth table of an arbitrary boolean function f with k input arguments and j rows of output value false. We represent f as CNF.

Consider boolean variables $b_{i,l}$ with $0 \le i \le j$ and $0 \le l \le k$. For every row i of the truth table with assignment (r_i) , add one disjunction to the CNF. This disjunction contains $b_{i,l}$ if $r_{i,l}$ is false. The disjunction contains $b_{i,l}$ if $r_{i,l}$ is true.

As far as f is an arbitrary k-ary boolean function, we have proven that any function can be represented as CNF.

SAT problems are usually represented in the DIMACS de-facto standard. Consider a SAT problem in CNF with *nbclauses* clauses and enumerate all variables from 1 to *nbvars*. A DIMACS file is an ASCII text file. Lines starting with "c" are skipped (comment lines). The first remaining line has to begin with "p cnf" followed by *nbclauses* and *nbvars* separated by spaces (header line). All following non-comment lines are space-separated indices of boolean variables optionally prefixed by a minus symbol. Then one line represents one clause and must be terminated with a zero symbol after a space. All lines are conjuncted to form a CNF.

Variations of the DIMACS de-facto standard also allow multiline clauses (the zero symbol constitutes the end of a clause) or arbitrary whitespace instead of spaces. The syntactical details are individually published on a per competition basis.

ソースコード 3.1: Display 3.1 represented in DIMACS format

```
\begin{center}
  %\fbox{%
    \begin{verbatim}
p cnf 2 2
a b
-a -b \end{verbatim}
  %}
\end{center}
```

Definition 3.2

A *clause* is a disjunction of literals. A k-clause is a clause consisting of exactly k literals. A *unit clause* is a 1-clause. A *Horn clause* is a clause with at most one

positive literal. A *definite clause* is a clause with exactly one positive literal.

3.2 SAT features and CNF analysis

At the very beginning I was very intrigued with the question "What is an 'average' SAT problem?". Answers to this question can help to optimize SAT solver memory layouts. But originally I was wondering whether our differential cryptanalysis SAT problems distinguish from "average" SAT problems in some very basic properties. First of all, we need to elaborate on the question itself.

Definition 3.3 (SAT feature)

A *SAT feature* is a statistical value (named *feature value*) retrievable from some given SAT problem in some well-defined encoding.

A SAT feature is called *performance-driven* if the runtime of any computation contributes to the feature value.

The most basic example of a SAT feature is the number of variables and clauses of a given SAT problem. This SAT feature is stored in the CNF header of a SAT problem encoded in the DIMACS format.

It should be computationally easy to evaluate SAT features of a given SAT problem. The general goal is to write a tool which evaluates several SAT features at the same time and retrieve them for comparison with other problems. A SAT feature is expected to be computable in linear time and memory with the number of variables and number of clauses. But a suggested limit is only given with polynomial complexity for evaluation algorithms. Sticking to this convention implies that evaluation of satisfiability must not be necessary to evaluate a SAT feature under the assumption that $P \neq NP$. Hence the number of valid models cannot be a SAT feature as far as satisfiability needs to be determined. But no actual hard boundary for runtime requirements is given. Previous work has shown that expensive algorithms can provide useful data in a small time frame if they are limited to a constant subproblem size.

The most similar resource I found looking at SAT features was the SATzilla project [8, 17] in 2012. The authors systematically defined 138 SAT features categorized in 12 groups. The features themselves are not defined formally, but an implementation is provided bundled with example data.

POSNEG RATIO CLAUSE mean ratio of positive to negative clauses, mean

Many SAT solvers collect feature values to improve algorithm selection, restart strategies and estimate problem sizes. Recent trends to apply Machine Learning to

SAT solving imply feature evaluation. SAT features and the resulting satisfiability runtime are used as training data for Machine Learning. One example using SAT features for algorithm selection is ASlib [1].

However, most of these SAT features are performance-driven. Examples for performance-driven SAT features include the number of restarts within a certain time frame or evaluation of local minima.

POSNEG-RATIO-CLAUSE-mean

In the following section we want to evaluate SAT features and compare test cases.

3.3 SAT features in comparison

Proposition 3.1

The set of public benchmarks in SAT competitions between 2008 and 2015 represent average SAT problems

Define a large set of SAT features. Present data. Categorize data.

3.4 Basic SAT solving techniques

3.5 SAT solvers in use

3.6 Encodings

3.6.1 STP approach

3.6. ENCODINGS

Given a set of clause	es, return a subset of clauses satisfying given criterion
clauses_allLitsNeg	all literals are negative
clauses_oneLitNeg	exactly one literal is negative
clauses_geqOneLitNeg	more than one literal is negative
clauses_allLitsPos	all literals are positive
clauses_oneLitPos	exactly one literal is positive
clauses_geqOneLitPos	more than one literal is positive
clauses_length1	clause contains exactly one literal ("unit clause")
clauses_length2	clause contains exactly two literals
clauses_unique	clause did not yet occur
clauses_tautological	clause contains some literal and its negation
Given a set	of literals/variables, return boolean property
literals_existential	literal does not occur negated
literals_unit	literal occurs in clause of length 1
literals_contradiction	literal occurs with its negation on one clause
literals_1occ	literal occurs only in one clause once
literals_2occs	literal occurs two times in clauses
literals_3occs	literal occurs three times in clauses
variables_unit	variable occurs in clause of length 1
Given a set of	clauses, return real number based on this clause
clauses_mapLength	number of literals in clause
clauses_mapRatioPosNeg	number of positive literals divided by total number of literal
clauses_mapNumPos	number of positive literals in clause
Give	n one clause, return boolean property
clauselits_someEx	any is literal existential
clauselits_allEx	all literals are existential
clauselits_someUnit	contains unit variable
clauselits_someContra	contains contradiction variable
clauselits_all1occ	all variables occur only once in all clauses
clauselits_all12occ	all variables occur only once or twice in all clauses
Given a	all clauses, return the following property
concomp_variable	number of connected components where
	two variables are in the same component
	iff they occur in at least one clause together
concomp_literal	number of connected components where
	two literals are in the same component
	iff they occur in at least one clause together
xor2_count	Number of clause pairs $(a \lor b, \neg a \lor b)$
	for two variables a and b



Chapter 4

Results

- 4.1 Benchmark results
- 4.2 Related work
- 4.3 Conclusion

Chapter 5

Summary and Future Work

- 5.1 Summary of results
- 5.2 Future work

Appendices

Appendix A

Illustration

i		∇S_{i0}	$\nabla S_{i,1}$	∇S_{i2}
-4	A:	01100111010001010010001100000001	V U 1,1	¥3 _{1,2}
-3	A:	0001000000110010010101010001110110		
-2	A:	1001100010111010110111100111111110		
-1	A:	1110111111100110110101011110001001		
0	A:	0110101111101010011110010000010010	w:	01001101011110101001110010000011
1	A:	011101100100111111111100111000110010	W:	u10101101100101111001001001111010
2	A:	1010101101000000001110u01n1110010	W:	n01n1001110101011010010111111000
3	A:	101011u1001111010101001001010001	W:	010101111010011110100101111101110
4	A:	001011000110001101010101111110010	W:	110111100111101001000101000111100
5	A:	000110100110001010u1101000000001	W:	1101110011000011011001101011011
6	A:	0001101100unuu110001000001111010	W:	10110110100000111010000000100000
7	A:	00101011100000010unn011001010000	w:	001110110010101001011110110011111
8	A:	011100110010001u111111111110110000	W:	11000110100111010111000110110011
9	A:	101011n01unnu00011111100110011111	W:	11111001111010011001000110011000
10	A:	10n001001000010101000000010101110	W:	11010111110011111110000000010111110
11	A:	u100011010110110010010101111111111	W:	101001100011101110110010111101000
12	A:	001011u00u1010111111111100011111011	W:	010001011101110n1000111000110001
13	A:	10un1n01001100010100000111100101	w:	10010111111100011000111111111100101
14	A:	00001010010100011000100011010110	W:	0010011110010100101111111100001000
15	A:	0001111010101u0101100110110110100	w:	10111001111010001100001111101001
16	A:	n00n0un01101001010011011010111111	""	
17	A:	00011111001110100001001000011110		
18	A:	01010111000011010000000001001010100		
19	A:	u1n10000000101111001101011000100		
20	A:	n1un10011111111011101000000110100		
21	A:	111100111011000001011111111010100		
22	A:	01011101110011010011001100111010		
23	A:	01010000111011101100011110001111		
24	A:	00000010000100100011011100011010		
25	A:	10110000100101100001010011101010		
26	A:	00001010100010010111011101000001		
27	A:	00000110111011110101101010110011		
28	A:	10110110010111010110110000100101		
29	A:	10100010000011010100100001101001		
30	A:	001010011101011111100011101100011		
31	A:	111111001001001011010111110110110		
32	A:	01001111110100100110100000101111		
33	A:	00111000001111010110111011100100		
34	A:	00100000011101011110100000010101		
35	A:	n0100000001100110000010001110010		
36	A:	n0000111111101011111011111001011001		
37	A:	11001000000110100100001100001100		
38	A:	101100000110011111110100110101100		
39	A:	00010010000010100001101100011100		
40	A:	11000000010010000111000110000101		
41	A:	00000110100001101111010100100110		
42	A:	010011101101110111111111010000110		
43	A:	01010000011000111101000001101101		
44	A:	11111000000101101111011100001100		
45	A:	10001010110110110010110000000100		
46	A:	10000010100110010101100011011100		
47	A:	100000011110010110110100101111101		

Table A.1: One of the original MD4 collision given by Wang, et al.

Appendix B

Testcases

Figures B.1, B.2, B.3 and B.4 show testcases used to test performance measures.

-		76	77C	776
i	Α.	$ abla S_{i,0}$ 01100111010001010010001100000001	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:			
-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101011011100111111110		
-1	A:	1110111111100110110101011110001001		
0	A:	x	W:	x
1	A:		W:	
2	A:	x	W:	x
3	A:	xxx	W:	
4	A:	xx	W:	x
5	A:	xxxxxxxxxxxxxxxxx	W:	
6	A:	xx-x-x-xxxxx	W:	
7	A:	xx	W:	
8	A:	x-x-x-x-x-x-x-x-x-x-x-x-x-x-x-x-x	W:	x
9	A:	xx	W:	
10	A:	xxxxx-xxx	W:	
11	A:	xxxx-x	W:	
12	A:	xx	W:	x
13	A:		W:	
14	A:	-x	W:	
15	A:	x-xx	W:	
16	A:	-xxx		
17	A:			
18	A:			
19	A:	x		
20	A:	x		
21	A:			
22	A:			
23	A:			
24	A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30	A:			
31	A:			
32	A:	x		
33	A:			
34	A:			
35	A:			
36	A:			
37	A:			
38	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:			

Table B.1: TODO description

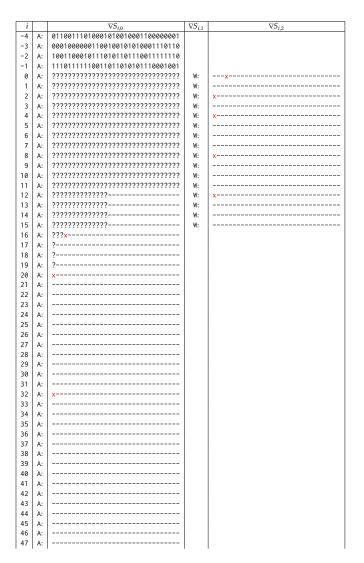


Table B.2: TODO description

		76	17C	700
i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101011011110011111110		
-1	A:	111011111100110110101011110001001		
0	A:	???????????????????????????????	W:	x
1	A:	???????????????????????????????	W:	
2	A:	???????????????????????????????	W:	x
3	A:	???????????????????????????????	W:	
4	A:	???????????????????????????????	W:	x
5	A:	??????????????????????????????	W:	
6	A:	???????????????????????????????	W:	
7	A:	???????????????????????????????	W:	
8	A:	???????????????????????????????	W:	x
9	A:	???????????????????????????????	W:	
10	A:	???????????????????????????????	W:	
11	A:	???????????????????????????????	W:	
12	A:	???????????????????????????????	W:	x
13	A:	???????????????????????????????	W:	
14	A:	???????????????????????????????	W:	
15	A:	??????????????????????????????	W:	
16	A:	??????????????????????????????		
17	A:	??????????????????????????????		
18	A:	??????????????????????????????		
19	A:	??????????????????????????????	l	
20	A:	??????????????????????????????		
21	A:			
22	A:			
23	A:			
24	A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30	A:			
31	A:			
32	A:	x		
33	A:			
34	A:			
35	A:			
36	A:			
37	A:			
38	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:			
<u> </u>	٠			l

Table B.3: TODO description

i		∇S_{i0}	$\nabla S_{i,1}$	∇S_{i2}
-4	A:	01100111010001010010001100000001	.,.	*50
-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101011011100111111110		
-1	A:	111011111100110110101011110001001		
0	A:	7777777777777777777777777777777	W:	77777777777777777777777777777777
1	A:	7777777777777777777777777777777	W:	77777777777777777777777777777777
2	A:	77777777777777777777777777777777	W:	77777777777777777777777777777777777
3	A:	7777777777777777777777777777777	W:	777777777777777777777777777777777
4	A:	7777777777777777777777777777777	W:	777777777777777777777777777777777
5	A:	7777777777777777777777777777777	W:	7777777777777777777777777777777777
6	A:	7777777777777777777777777777777	W:	7777777777777777777777777777777777
7	A:	7777777777777777777777777777777	W:	7777777777777777777777777777777777
8	A:	77777777777777777777777777777777	W:	77777777777777777777777777777777777
9	A:	7777777777777777777777777777777	W:	77777777777777777777777777777777777
10	A:	7777777777777777777777777777777	W:	7777777777777777777777777777777777777
11	A:	7777777777777777777777777777777	W:	77777777777777777777777777777777
12	A:	7777777777777777777777777777777	W:	77777777777777777777777777777777
13	A:	7777777777777777777777777777777	W:	7777777777777777777777777777777777777
14	A:	7777777777777777777777777777777	W:	777777777777777777777777777777777777
15	A:	77777777777777777777777777777777777	W:	777777777777777777777777777777777777777
16	A:	7777777777777777777777777777777	٧٠.	
17	A:	77777777777777777777777777777777777		
18	A:	77777777777777777777777777777777		
19		7777777777777777777777777777777		
20	A: A:	77777777777777777777777777777777		
21	A:			
23	A:			
24	A: A:			
25	A:			
26	A:			
27	A:			
28	A:			
29	A:			
30				
31	A: A:			
31	A: A:	x??????????????????????????????		
33				
34	A:			
35	A: A:			
36	A:			
37				
38	A:			
	A:			
39	A:			
40	A:			
41	A:			
42	A:			
43	A:			
44	A:			
45	A:			
46	A:			
47	A:			

Table B.4: TODO description

Appendix C

Hardware setup

In the following we introduce two hardware setups which were used to run our testcases. The first setup is referred to as "Thinkpad x220" throughout the document whereas the second setup is referred to as "Cluster".

Type model	Thinkpad Lenovo x220 tablet, 4299-2P6
Processor	Intel i5-2520M, 2.50 GHz, dual-core, Hyperthreaded
RAM	16 GB (extension to common retail setup)
Memory	160 GB SSD
L3 cache size	3072 KB

Table C.1: Thinkpad x220 Tablet specification [6]

Processor	Intel Xeon X5690, 3.47 GHz, 6 cores, Hyperthreaded
RAM	192 GB
L3 cache size	12288 KB

Table C.2: Cluster node nehalem192go specification [3]

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