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MASTER THESIS

Differential cryptanalysis with SAT solvers

Author:

Lukas Prokop

Supervisor:

Maria Eichlseder
Florian Mendel

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Lukas Prokop, BSc BSc

Differential cryptanalysis with SAT solvers

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Dipl.-Ing. Dr.techn., Florian Mendel

Institute of Applied Information Processing and Communications

Second advisor: Maria Eichlseder

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AFFIDAVIT

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ABSTRACT

Hash functions are ubiquitous in the modern information age. They provide preimage, second preimage and collision resistance which are needed in a wide range of applications.

In August 2006, Wang et al. showed efficient attacks against several hash function designs including MD4, MD5, HAVAL-128 and RIPEMD. With these results differential cryptanalysis has been shown useful to break collision resistance in hash functions. Over the years advanced attacks based on those differential approaches have been developed.

To find collisions like Wang et al., a cryptanalyst needs to specify a differential characteristic. Looking at the differential behavior of the underlying operations of the hash algorithm shows how differential values propagate in the algorithm. The goal is to find a differential characteristic whose differences cancel out in the output. Once such a differential characteristic was discovered, in a second step the actual values for those differences are defined yielding an actual hash collision.

Finding a differential characteristic can be a cumbersome and tedious task. Whereas propagations can be automated using dedicated tools, finding an initial differential characteristic is a difficult task as they can be specified with arbitrary levels of granularity.

SAT research at same time faces similar problems. SAT solvers implement heuristics to find satisfying assignments for Boolean functions. They also propagate values once knowledge about the problem gets derived.

In this thesis we look at differential characteristics and encode them as SAT problem. A SAT solver tells us whether a differential characteristic can represent a hash collision or not. We implemented a framework which allows us to verify differential behavior for integer operations. We then looked at the encoded problems in details and tried to change the encoding to improve the runtime of the SAT solver. We also provide a small CNF analysis library to compare an encoded problem with others.

Keywords: hash function, differential cryptanalysis, differential characteristic, MD4, SHA-256, collision resistance, satisfiability, SAT solver

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And finally I am grateful for the support by Martina, who also supported me during good and bad days with this thesis, and my parents which provided a prosperous environment to me to be able to stand where I am today.

Thank you.

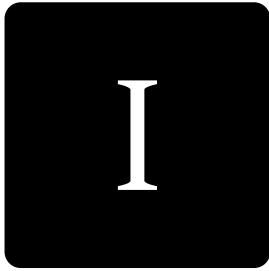
どもありがとうございました。

All source code is available at lukas-prokop.at/proj/megosat and published under terms and conditions of Free/Libre Open Source Software. This document was printed with Lua^AT_EX and Linux Libertine Font.

Contents

1	Introduction	1
1.1	Cryptanalysis preliminaries	2
1.2	Cryptanalysis of Hash Functions	3
1.3	Differential cryptanalysis	4
1.4	Satisfiability	4
1.5	Satisfiability of hash algorithm states	6
1.6	Thesis Outline	7
2	Differential cryptanalysis	9
2.1	MD4	9
2.2	SHA-256	12
2.3	Differential notation	14
2.4	Addition example	14
2.5	Differential path	14
3	Satisfiability	17
3.1	The DIMACS de-facto standard	17
3.2	SAT features and CNF analysis	19
3.3	SAT features in comparison	20
3.4	Basic SAT solving techniques	20
3.5	SAT solvers in use	20
3.6	Encodings	20

3.6.1	STP approach	20
4	Results	23
4.1	Benchmark results	23
4.2	Related work	23
4.3	Conclusion	23
5	Summary and Future Work	25
5.1	Summary of results	25
5.2	Future work	25
	Appendices	27
A	Illustration	29
B	Testcases	31
C	Hardware setup	37



Chapter 1

Introduction

Hash functions are used as cryptographic primitives in many applications and protocols. They take an arbitrary input message and provide a hash value. Input message and hash value are considered as byte strings in a particular encoding. The hash value is of fixed length and satisfies several properties which make it useful in a variety of applications.

In this thesis we will consider the hash algorithms MD4 and SHA-256 and represent differential characteristics of hash collisions as SAT problem. If and only if satisfiability is given, the particular differential state is achievable using two different inputs leading to the same output. As far as SAT solvers return an actual model satisfying that state, we get an actual hash collision which can be verified and visualized. If the internal state of the hash algorithm is too large, the attack can be computationally simplified by modelling only a subset of steps of the hash algorithm or changing the modelled differential path.

Based on experience with these kind of problems with previous non-SAT-based tools we aim to apply best practices to a satisfiability setting. We will discuss which SAT techniques lead to best performance characteristics for our MD4 and SHA-256 testcases.

1.1 Cryptanalysis preliminaries

Definition 1.1 (*Hash function*)

A hash function is a mapping $h : X \rightarrow Y$ with $X = \{0, 1\}^*$ and $Y = \{0, 1\}^n$ for some fixed $n \in \mathbb{N}_{\geq 1}$.

- Let $x \in X$, then $h(x)$ is called *hash value of x* .
- Let $h(x) = y \in Y$, then x is called *preimage of y* .

One example showing the use of hash functions as primitives are JSON Web Tokens (JWT) specified in RFC 7519 [11]. Section 8 defines implementation requirements and refers to RFC 7518 [7], which specifies cryptographic algorithms to be implemented. “HMAC SHA-256” (besides “none”) is the only signature and MAC algorithm required to be implemented. SHA-256 as hash algorithm is used as cryptographic primitive in this configuration.

A hash function has to satisfy the following security requirements:

Definition 1.2 (*Preimage resistance*)

Given $y \in Y$, a hash function h is *preimage resistant* iff it is computationally infeasible to find $x \in X$ such that $h(x) = y$.

Definition 1.3 (*Second-preimage resistance*)

Given $x \in X$, a hash function h is *second-preimage resistant* iff it is computationally infeasible to find $x_2 \in X$ with $x \neq x_2$ such that $h(x) = h(x_2)$. x_2 is called *second preimage*.

Definition 1.4 (*Collision resistance*)

A hash function h is *collision resistant* iff it is computationally infeasible to find any two $x \in X$ and $x_2 \in X$ with $x \neq x_2$ such that $h(x) = h(x_2)$.

As far as hash functions accept input strings of arbitrary length, but return a fixed size output string, existence of collisions is unavoidable [19]. However, good hash functions make it very difficult to find collisions or preimages.

The considered hash functions apply padding to their input to normalize their input size to a multiple of its block size. The round function follows afterwards. In the following, we always consider input of block size instead of the original input message as bytestring. Padding is negligible, because once we have two colliding blocks, the collision will be reflected in the output in these single-pipe Merkle-Darmgård designs. This results in a length extension attack, making input padding negligible for cryptanalysis.

Message 1			
4d7a9c83	d6cb927a	29d5a578	57a7a5ee
de748a3c	dcc366b3	b683a020	3b2a5d9f
c69d71b3	f9e99198	d79f805e	a63bb2e8
45dc8e31	97e31fe5	2794bf08	b9e8c3e9
Message 2			
4d7a9c83	56cb927a	b9d5a578	57a7a5ee
de748a3c	dcc366b3	b683a020	3b2a5d9f
c69d71b3	f9e99198	d79f805e	a63bb2e8
45dd8e31	97e31fe5	2794bf08	b9e8c3e9
Hash value of Message 1 and Message 2			
5f5c1a0d	71b36046	1b5435da	9bod807a

TABLE 1.1: One of two MD4 hash collisions provided in [22]. Values are given in hexadecimal, message words are enumerated from left to right, top to bottom. Differences are highlighted in bold for illustration purposes. For comparison the first bits of Message 1 are 11000001... and the last bits are ...10011101. A message represents one block of 512 bits.

1.2 Cryptanalysis of Hash Functions

In August 2004, Wang et al. published results at Crypto'04 [22] which revealed that MD4, MD5, HAVAL-128 and RIPEMD can be broken practically using differential cryptanalysis. Their work is based on preliminary work by Hans Dobbertin [4]. On an IBM P690 machine, an MD5 collision can be computed in about one hour using this approach. Collisions for HAVAL-128, MD4 and RIPEMD were found as well. Patrick Stach's `md4coll.c` program [20] implements Wang's approach and can find MD4 collisions in few seconds on my Thinkpad x220 setup specified in [Appendix C](#).

Let n denote the digest size, i.e. the size of the hash value $h(x)$ in bits. Due to the birthday paradox, a collision attack has a generic complexity of $2^{n/2}$ whereas preimage and second preimage attacks have generic complexities of 2^n . In other words it is computationally easier to find any two colliding hash values than the preimage or second preimage for a given hash value.

Following results by Wang et al., differential cryptanalysis was shown as powerful tool for cryptanalysis of hash algorithms. This thesis applies those ideas to satisfiability approaches.

1.3 Differential cryptanalysis

Definition 1.5 (*Hash collision*)

Given a hash function h , a hash collision is a pair (x, x_2) with $x \neq x_2$ such that $h(x) = h(x_2)$.

Differential cryptanalysis is based on the idea to consider two execution states of hash algorithms for slightly different input messages. We trace those difference to learn about the propagation of message differences.

Hash algorithms consume input values as blocks of bits. As far as the length of the input must not conform to the block size, padding is applied. Now consider such a block of input values and another copy of it. We use those two blocks as inputs for two hash algorithm implementations, but provide slight modifications in few bits. MD4 has 48 round function applications in 3 rounds. Differential cryptanalysis considers the difference in the evaluation state between the two instances (compare with Figure 1.1).

Visualizing those differences helps the cryptanalyst to find modifications yielding a small number of differences in the evaluation state. The cryptanalyst consecutively modifies the input values to eventually receive a collision in the output value. If the number of differences in the evaluation state is small, this trail is expected to result in a hash collision with higher probability.

1.4 Satisfiability

Definition 1.6

A *Boolean function* is a mapping $h : X \rightarrow Y$ with $X = \{0, 1\}^n$ for $n \in \mathbb{N}$ and $Y = \{0, 1\}$.

The following definition gives three basic Boolean functions:

Definition 1.7

Let AND, OR and NOT be three Boolean functions.

- AND maps $X = \{0, 1\}^2$ to 1 if all values of X are 1.
- OR maps $X = \{0, 1\}^2$ to 1 if any value of X is 1.
- NOT maps $X = \{0, 1\}^1$ to 1 if the single value of X is 0.

All functions return 0 in the other case.

Definition 1.8

A *truth table* unambiguously defines a Boolean function by enlisting the evaluated truth value for all possible sets of inputs.

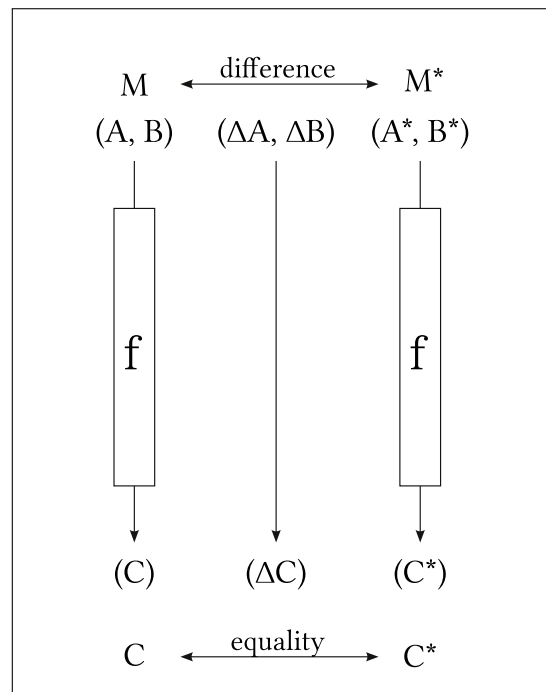


Figure 1.1: Typical attack setting for a collision attack: Hash function f is applied to two inputs M and M^* which differ by some predefined bits. M describes the difference between these values. A hash collision is given if and only if output values C and C^* show the same value. In differential cryptanalysis we observe the differences between two instances applying function f to inputs M and M^* .

v_1	v_2	$f(v_1, v_2)$	v_1	v_2	$f(v_1, v_2)$	v	$f(v)$
1	1	1	1	1	1	1	0
1	0	0	1	0	1	0	1
0	1	0	0	1	1	(c) NOT	
0	0	0	0	0	0		

(A) AND

(B) OR

TABLE 1.2: Truth tables for AND, OR and NOT

Table 1.2 shows truth tables for AND, OR and NOT.

Boolean functions have an important property which is characterized in the following definition:

Definition 1.9

A Boolean function f is *satisfiable* iff there exists at least one input $x \in X$ such that $f(x) = 1$. Every input $x \in X$ satisfying this property is called *model*. Every element of X is called *assignment*.

The generic complexity of SAT determination is given by 2^n for n Boolean variables. The corresponding tool to determine satisfiability is defined as follows:

Definition 1.10

A *SAT solver* is a tool to determine satisfiability of a Boolean function. If satisfiability is given, it returns some model.

SAT research is heavily concerned with finding good heuristics to find some model for a given SAT problem as fast as possible. Biyearly *SAT competitions* take place to challenge SAT solvers in a set of benchmarks. The committee evaluates the most successful SAT solvers solving the most problems within a given time frame.

1.5 Satisfiability of hash algorithm states

We discussed Boolean functions and satisfiability. At the same time we looked at basic properties of hash algorithms. But the question remains how we can link those areas together? This section is dedicated to this question.

Definition 1.11

An *algorithm* is a step-wise set of instructions to solve a problem. An *I/O algorithm* transforms given input values to output values.

Hash algorithms are one example of I/O algorithms.

$$\begin{array}{rcl}
\begin{array}{rcl}
\text{1st arg:} & a_1 & a_0 \\
\text{2nd arg:} & + & b_1 & b_0 \\
\hline
\text{carry:} & & c_0 \\
\text{sum:} & = & s_1 & s_0
\end{array} & \rightsquigarrow & \begin{array}{l}
s_0 = \text{XOR}(a_0, b_0) \\
c_0 = a_0 \wedge b_0 \\
s_1 = \text{XOR}(a_0, b_0, c_0)
\end{array}
\end{array}$$

Figure 1.2: Modelling 2bit addition (left) as Boolean function (right)

I/O algorithms can be implemented as a sequence of instructions for computers. At the same time I/O algorithms can be represented as combination of Boolean functions. This claim is backed in more detail in Section 3.1 with Theorem 3.1. It follows immediately that we can represent I/O algorithms such as hash algorithms entirely as Boolean function.

Theorem 1.1

Every algorithm can be represented as Boolean function.

We consider 2bit addition as small example. Let a_i be the first argument where i denotes the binary position. If $i = 0$, the *least significant bit* (LSB) is considered. If $i = 1$, the *most significant bit* (MSB) is considered.

Let b_i be the second argument and s_i be the output value. Furthermore c_i is the carry bit, where c_1 is left out, because it is not used in 2bit addition. This model of 2bit addition as Boolean function can be seen in Figure 1.2.

1.6 Thesis Outline

This thesis is organized as follows:

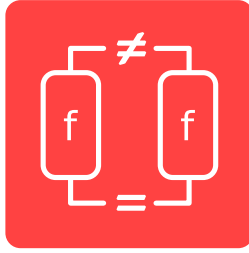
In Chapter 1 we discussed the basic properties and fundamentals of the tools in discussion including hash functions and SAT solvers.

In Chapter 2 we introduce the MD4 and SHA-256 hash functions and discuss possible approaches in differential cryptanalysis.

In Chapter 3 we discuss SAT solving and potential approaches to speed up SAT solvers for cryptographic problems.

In Chapter 4 we show results of our work and discuss its implications.

In Chapter 5 we suggest future work based on our results.



“JUST BECAUSE IT’S AUTOMATIC
DOESN’T MEAN IT WORKS.”
—Daniel J. Bernstein

Chapter 2

Differential cryptanalysis

2.1 MD4

MD4 is a cryptographic hash function originally described in RFC 1186 [16], updated in RFC 1320 [17] and declared obsolete by RFC 6150 [21]. It was invented by Ronald Rivest in 1990 with properties given in Table 2.1. Since 1995 [4] successful attacks have been found to break collisions, preimage and second-preimage resistance in MD4; including but not limited to [18] and [13]. A Python 3 implementation derived from a previous Python version is available at github [15].

block size	512 bits	namely variable block in RFC 1320 [17]
digest size	128 bits	as per Section 3.5 in RFC 1320 [17]
internal state size	128 bits	namely variables A, B, C and D
word size	32 bits	as per Section 2 in RFC 1320 [17]

TABLE 2.1: MD4 hash algorithm properties

MD4 uses three auxiliary Boolean functions:

$$\text{IF}(X, Y, Z) = (X \wedge Y) \vee (\neg X \wedge Z) \quad (2.1)$$

$$\text{MAJ}(X, Y, Z) = (X \wedge Y) \vee (X \wedge Z) \vee (Y \wedge Z) \quad (2.2)$$

$$\begin{aligned} \text{XOR}(X, Y, Z) = & (X \wedge \neg Y \wedge \neg Z) \vee (\neg X \wedge Y \wedge \neg Z) \\ & \vee (\neg X \wedge \neg Y \wedge Z) \vee (X \wedge Y \wedge Z) \end{aligned} \quad (2.3)$$

Definition 2.1

The Boolean IF function behaves the following way: If the first argument is true, the second argument is returned. If the first argument is false, the third argument is returned.

The Boolean MAJ function returns true if the number of Boolean values true in arguments is at least 2. The Boolean XOR function returns true if the number of Boolean values true in arguments is odd.

In the following a quick overview over MD4's design is given.

Padding and length extension First of all, padding is applied. A single bit 1 is appended to the input. As long as the input does not reach a length congruent 448 modulo 512, bit 0 is appended. Followingly, length appending takes place. Represent the length of the input (without the previous modifications) in binary and take its first 64 less significant bits. Append those 64 bits to the input.

Initialization The message is split into 512-bit blocks (i.e. 16 32-bit words). Four state variables A , B , C and D are initialized with these hexadecimal values:

[A] 01234567 [B] 89abcdef [C] fedcba98 [D] 76543210

Round function with state variable updates We also need an auxiliary matrix $(i_{k,l})$ which stores indices. Let $i_{k,l}$ be the value in the k -th row and l -th column of matrix $(i_{k,l})$. Analogously $j_{k,l}$ is defined for matrix $(j_{k,l})$.

$$(i_{k,l}) = \begin{pmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & 11 & 12 & 13 & 14 & 15 \\ 0 & 4 & 8 & 12 & 1 & 5 & 9 & 13 & 2 & 6 & 10 & 14 & 3 & 7 & 11 & 15 \\ 0 & 8 & 4 & 12 & 2 & 10 & 6 & 14 & 1 & 9 & 5 & 13 & 3 & 11 & 7 & 15 \end{pmatrix}$$

$$(j_{k,l}) = \begin{pmatrix} 3 & 7 & 9 & 11 \\ 3 & 5 & 9 & 13 \\ 3 & 9 & 11 & 15 \end{pmatrix}$$

Then the round function is applied to this block in three rounds with 16 iterations each. Let $1 \leq k \leq 3$ be the round counter and $1 \leq l \leq 16$ be the iteration counter. For every round, for every iteration apply the following function:

The values of state variable B , C and D are taken as arguments for function F where F is IF in the first 16 iterations, MAJ in the following 16 iterations and finally XOR in the last 16 iterations. This return value is added to the value of state variable A , the current message block M and $X_{i_{k,l}}$. This sum modulo 2^{32} is then left-rotated (see Definition 2.2) by $j_{k,l} \bmod 4$ bits and stored in value B . State variables B , C and D update variables C , D and A respectively.

This round function design is visualized in Figure 2.1.

2.2 SHA-256

SHA-256 is a hash function from the SHA-2 family designed by the National Security Agency (NSA) and published in 2001 [6]. It uses a Merkle-Damgård construction with a Davies-Meyer compression function. The best known preimage attack was found in 2011 and breaks preimage resistance for 52 rounds [8]. The best known collision attack breaks collision resistance for 31 rounds of SHA-256 [12] and pseudo-collision resistance for 46 rounds [9].

block size	512 bits	as per Section 1 of the standard [6]
digest size	256 bits	mentioned as Message Digest size [6]
internal state size	256 bits	as per Section 1 of the standard [6]
word size	32 bits	as per Section 1 of the standard [6]

TABLE 2.2: SHA-256 hash algorithm properties

Definition 2.2 (*Shifts, rotations and a notational remark*)

Consider a 32-bit word X with 32 binary values b_i with $0 \leq i \leq 31$. b_0 refers to the least significant bit. Shifting (\ll and \gg) and rotation (\lll and \ggg) creates a new 32-bit word Y with 32 binary values a_i . We define the following notations:

$$Y := X \ll n \iff a_i := b_{i-n} \text{ if } 0 \leq i - n < 32 \text{ and } 0 \text{ otherwise}$$

$$Y := X \gg n \iff a_i := b_{i+n} \text{ if } 0 \leq i + n < 32 \text{ and } 0 \text{ otherwise}$$

$$Y := X \lll n \iff a_i := b_{i-n \bmod 32}$$

$$Y := X \ggg n \iff a_i := b_{i+n \bmod 32}$$

Furthermore $X \oplus Y$ denotes XOR with arguments X and Y .

Besides MD4's two auxiliary functions MAJ and IF, another four auxiliary functions are defined. Be aware that \oplus denotes the XOR functions whereas $+$ denotes addition modulo 2^{32} .

$$\Sigma_0(X) := (X \ggg 2) \oplus (X \ggg 13) \oplus (X \ggg 22)$$

$$\Sigma_1(X) := (X \ggg 6) \oplus (X \ggg 11) \oplus (X \ggg 25)$$

$$\sigma_0(X) := (X \ggg 7) \oplus (X \ggg 18) \oplus (X \gg 3)$$

$$\sigma_1(X) := (X \ggg 17) \oplus (X \ggg 19) \oplus (X \gg 10)$$

Padding and length extension The padding and length extension scheme of MD4 is used also in SHA-256. Append bit 1 and followed by a sequence of bit 0 until the message reaches a length of 448 modulo 512 bits. Afterwards the first 64 bits of the binary representation of the original input are appended.

Initialization In a similar manner to MD4, initialization of internal state variables (called “working variables” in [6, Section 6.2.2]) takes place before running

the round function. The eight state variables are initialized with the following hexadecimal values:

$$\begin{aligned} A_{-1} &= 6a09e667 & A_{-2} &= bb67ae85 & A_{-3} &= 3c6ef372 & A_{-4} &= a54ff53a \\ E_{-1} &= 510e527f & E_{-2} &= 9b05688c & E_{-3} &= 1f83d9ab & E_{-4} &= 5be0cd19 \end{aligned}$$

Furthermore SHA-256 uses 64 constant values in its round function. We initialize step constants K_i for $0 \leq i < 64$ with the following hexadecimal values (which must be read left to right and top to bottom):

428a2f98	71374491	b5c0fbcf	e9b5dba5	3956c25b	59f111f1
923f82a4	ab1c5ed5	d807aa98	12835b01	243185be	550c7dc3
72be5d74	80deb1fe	9bdc06a7	c19bf174	e49b69c1	efbe4786
0fc19dc6	240ca1cc	2de92c6f	4a7484aa	5cb0a9dc	76f988da
983e5152	a831c66d	b00327c8	bf597fc7	c6e00bf3	d5a79147
06ca6351	14292967	27b70a85	2e1b2138	4d2c6dfc	53380d13
650a7354	766a0abb	81c2c92e	92722c85	a2bfe8a1	a81a664b
c24b8b70	c76c51a3	d192e819	d6990624	f40e3585	106aa070
19a4c116	1e376c08	2748774c	34b0bcb5	391c0cb3	4ed8aa4a
5b9cca4f	682e6ff3	748f82ee	78a5636f	84c87814	8cc70208
90bffffa	a4506ceb	bef9a3f7	c67178f2		

Precomputation of W Let W_i for $0 \leq i < 16$ be the sixteen 32-bit words of the padded input message. Then compute W_i for $16 \leq i < 64$ the following way:

$$W_i := \sigma_1(W_{i-2}) + W_{i-7} + \sigma_0(W_{i-15}) + W_{i-16}$$

Round function For every block of 512 bits, the round function is applied. The eight state variables are updated iteratively for i from 0 to 63.

$$\begin{aligned} E_i &:= A_{i-4} + E_{i-4} + \Sigma_1(E_{i-1}) + \text{IF}(E_{i-1}, E_{i-2}, E_{i-3}) + K_i + W_i \\ A_i &:= E_i - A_{i-4} + \Sigma_0(A_{i-1}) + \text{MAJ}(A_{i-1}, A_{i-2}, A_{i-3}) \end{aligned}$$

W_i and K_i refer to the previously initialized values.

Computation of intermediate hash values Intermediate hash values for the Davies-Meyer construction are initialized with the following values:

$$\begin{aligned} H_0^{(0)} &:= A_{-1} & H_1^{(0)} &:= A_{-2} & H_2^{(0)} &:= A_{-3} & H_3^{(0)} &:= A_{-4} \\ H_4^{(i)} &:= E_{-1} & H_5^{(i)} &:= E_{-2} & H_6^{(i)} &:= E_{-3} & H_7^{(i)} &:= E_{-4} \end{aligned}$$

Every block creates its own E_i and A_i values for $60 \leq i < 64$. These are used to compute the next intermediate values:

$$\begin{aligned} H_0^{(j)} &:= A_{63} + H_0^{(i-1)} & H_4^{(j)} &:= E_{63} + H_4^{(i-1)} \\ H_1^{(j)} &:= A_{62} + H_1^{(i-1)} & H_5^{(j)} &:= E_{62} + H_5^{(i-1)} \\ H_2^{(j)} &:= A_{61} + H_2^{(i-1)} & H_6^{(j)} &:= E_{61} + H_6^{(i-1)} \\ H_3^{(j)} &:= A_{60} + H_3^{(i-1)} & H_7^{(j)} &:= E_{60} + H_7^{(i-1)} \end{aligned}$$

Finalization The final hash digest of size 256 bits is provided as

$$H_0^{(N)} \parallel H_1^{(N)} \parallel H_2^{(N)} \parallel H_3^{(N)} \parallel H_4^{(N)} \parallel H_5^{(N)} \parallel H_6^{(N)} \parallel H_7^{(N)}$$

where N denotes the index of the last block and operator \parallel denotes concatenation. Hence $H_0^{(N)}$ are the four least significant bytes of the digest.

2.3 Differential notation

Differential notation helps us to visualize differential characteristics by defining so-called *bit conditions*. It was introduced by Christian Rechberger and Christophe de Cannière in 2006 [2, Section 3.2] and is shown in Table 2.4.

Consider two hash algorithm implementations. Let x_i be some bit from the first implementation and let x_i^* be the corresponding bit from the second implementation. Differences are computed using a XOR and commonly denoted as $\Delta x = x_i \oplus x_i^*$. Bit conditions allow us to encode possible relations between bits x_i and x_i^* .

For example, let us take a look at the original Wang et al. hash collision in MD4 provided in Table 1.1. We extract all values with differences and represent them using differential notation. This gives us Table 2.3.

The following properties hold for bit conditions:

- If $x_i = x_i^*$ holds and some value is known, $\{0, 1\}$ contains its bit condition.
- If $x_i \neq x_i^*$ holds and some value is known, $\{u, n\}$ contains its bit condition.
- If $x_i = x_i^*$ holds and the values are unknown, its bit condition is $-$.
- If $x_i \neq x_i^*$ holds and the values are unknown, its bit condition is x .

Applying this notation to hash collisions means that arbitrary bit conditions (except for $\#$) can be specified for the input values. In one of the intermediate iterations, we enforce a difference using one of the bit conditions $\{u, n, x\}$. This excludes trivial solutions with no differences from the set of possible solutions. And the final values need to lack differences thus are represented using $-$.

2.4 Addition example

TODO illustrate how differences propagate by an addition example illustrated in differential notation

TODO reference to Magnus Daum's thesis

bit	binary	hexadecimal representation / differential notation
x_0	d6cb927a	11010110110010111001001001111010
x_1	29d5a578	001010011110101011010010101111000
x_2	45dc8e31	010001011110111001000111000110001
x_0^*	56cb927a	01010110110010111001001001111010
x_1^*	b9d5a578	101110011110101011010010101111000
x_2^*	45dd8e31	010001011110111011000111000110001
Δx		u1010110110010111001001001111010 n01n10011110101011010010101111000 0100010111101110n1000111000110001

TABLE 2.3: The three words different between Message 1 and Message 2 of the original MD4 hash collision. The last three lines show how differences can be written down using bit conditions. As far as 4 symbols are not from the set $\{0, 1\}$ it holds that the messages differ by 4 bits.

2.5 Differential path

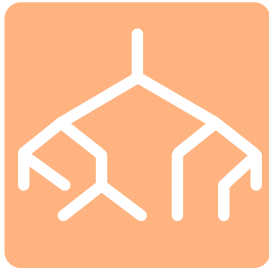
TODO refer to some testcase which shows a differential path with many unresolved differences. Then show the corresponding testcase where ? became - and x.

(x_i, x_i^*)	(0, 0)	(1, 0)	(0, 1)	(1, 1)	(x_i, x_i^*)	(0, 0)	(1, 0)	(0, 1)	(1, 1)
?	✓	✓	✓	✓	3	✓	✓		
-	✓			✓	5	✓		✓	
x		✓	✓		7	✓	✓	✓	
0	✓				A		✓		✓
u		✓			B	✓	✓		✓
n			✓		C			✓	✓
1				✓	D	✓		✓	✓
#					E		✓	✓	✓

TABLE 2.4: Differential notation as introduced in [2]. The left-most column specifies a symbol called “bit condition” and right-side columns indicate which bit configurations are possible for two given bits x_i and x_i^* .

Δx	conjunctive normal form	Δx	conjunctive normal form
#	$(x) \wedge (\neg x)$	1	$(x) \wedge (x^*)$
0	$(\neg x) \wedge (\neg x^*)$	-	$\neg(x \oplus x^*)$
u	$(x) \wedge (\neg x^*)$	A	(x)
3	$(\neg x^*)$	B	$(x \vee \neg x^*)$
n	$(\neg x) \wedge (x^*)$	C	(x^*)
5	$(\neg x)$	D	$(\neg x \vee x^*)$
x	$(x \oplus x^*)$	E	$(x \vee x^*)$
7	$(\neg x \vee \neg x^*)$?	

TABLE 2.5: All bit conditions represented as CNF using two boolean variables x and x^* to represent two bits.



“WHAT IDIOT CALLED THEM
LOGIC ERRORS RATHER THAN
BOOL SHIT?”
—Unknown

Chapter 3

Satisfiability

3.1 The DIMACS de-facto standard

Definition 3.1

A *conjunction* is a sequence of Boolean functions combined using a logical OR. A *disjunction* is a sequence of Boolean functions combined using a logical AND. A *literal* is a Boolean variable (*positive*) or its negation (*negative*).

A SAT problem is given in *Conjunctive Normal Form* (CNF) if the problem is defined as conjunction of disjunctions of literals.

A simple example for a SAT problem in CNF is the exclusive OR (XOR). It takes two Boolean values a and b as arguments and returns true if and only if the two arguments differ.

$$(a \vee b) \wedge (\neg a \vee \neg b) \tag{3.1}$$

Display 3.1 shows one conjunction (denoted \wedge) of two disjunctions (denoted \vee) of literals (denoted a and b where prefix \neg represents negation). This structure constitutes a CNF.

Analogously we define a *Disjunctive Normal Form* (DNF) as disjunction of conjunctions of literals. The negation of a CNF is in DNF, because literals are negated and conjunctions become disjunctions, vice versa.

Theorem 3.1

Every Boolean function can be represented as CNF.

Theorem 3.1 is easy to prove. Consider the truth table of an arbitrary Boolean function f with k input arguments and j rows of output value false. We represent f as CNF.

Consider Boolean variables $b_{i,l}$ with $0 \leq i \leq j$ and $0 \leq l \leq k$. For every row i of the truth table with assignment (r_i) , add one disjunction to the CNF. This disjunction contains $b_{i,l}$ if $r_{i,l}$ is false. The disjunction contains $\neg b_{i,l}$ if $r_{i,l}$ is true.

As far as f is an arbitrary k -ary Boolean function, we have proven that any function can be represented as CNF.

SAT problems are usually represented in the DIMACS de-facto standard. Consider a SAT problem in CNF with $nbclauses$ clauses and enumerate all variables from 1 to $nbvars$. A DIMACS file is an ASCII text file. Lines starting with “c” are skipped (comment lines). The first remaining line has to begin with “p cnf” followed by $nbclauses$ and $nbvars$ separated by spaces (header line). All following non-comment lines are space-separated indices of Boolean variables optionally prefixed by a minus symbol. Then one line represents one clause and must be terminated with a zero symbol after a space. All lines are conjuncted to form a CNF.

Variations of the DIMACS de-facto standard also allow multiline clauses (the zero symbol constitutes the end of a clause) or arbitrary whitespace instead of spaces. The syntactical details are individually published on a per competition basis.

LISTING 3.1: Display 3.1 represented in DIMACS format

```
p cnf 2 2
a b
-a -b
0
```

Definition 3.2

A *clause* is a disjunction of literals. A *k-clause* is a clause consisting of exactly k literals. A *unit clause* is a 1-clause. A *Horn clause* is a clause with at most one positive literal. A *definite clause* is a clause with exactly one positive literal.

3.2 SAT features and CNF analysis

At the very beginning I was very intrigued with the question “What is an ‘average’ SAT problem?”. Answers to this question can help to optimize SAT solver memory layouts. But originally I was wondering whether our differential cryptanalysis SAT problems distinguish from “average” SAT problems in some very basic properties. First of all, we need to elaborate on the question itself.

Definition 3.3 (SAT feature)

A SAT *feature* is a statistical value (named *feature value*) retrievable from some given SAT problem in some well-defined encoding.

A SAT feature is called *performance-driven* if the runtime of any computation contributes to the feature value.

The most basic example of a SAT feature is the number of variables and clauses of a given SAT problem. This SAT feature is stored in the CNF header of a SAT problem encoded in the DIMACS format.

It should be computationally easy to evaluate SAT features of a given SAT problem. The general goal is to write a tool which evaluates several SAT features at the same time and retrieve them for comparison with other problems. A SAT feature is expected to be computable in linear time and memory with the number of variables and number of clauses. But a suggested limit is only given with polynomial complexity for evaluation algorithms. Sticking to this convention implies that evaluation of satisfiability must not be necessary to evaluate a SAT feature under the assumption that $\mathcal{P} \neq \mathcal{NP}$. Hence the number of valid models cannot be a SAT feature as far as satisfiability needs to be determined. But no actual hard boundary for runtime requirements is given. Previous work has shown that expensive algorithms can provide useful data in a small time frame if they are limited to a constant subproblem size.

The most similar resource I found looking at SAT features was the SATzilla project [14, 23] in 2012. The authors systematically defined 138 SAT features categorized in 12 groups. The features themselves are not defined formally, but an implementation is provided bundled with example data.

POSNEG_RATIO_CLAUSE_mean ratio of positive to negative clauses, mean

Many SAT solvers collect feature values to improve algorithm selection, restart strategies and estimate problem sizes. Recent trends to apply Machine Learning to SAT solving imply feature evaluation. SAT features and the resulting satisfiability runtime are used as training data for Machine Learning. One example using SAT features for algorithm selection is ASlib [1].

However, most of these SAT features are performance-driven. Examples for performance-driven SAT features include the number of restarts within a certain time frame or evaluation of local minima.

POSNEG-RATIO-CLAUSE-mean

In the following section we want to evaluate SAT features and compare test cases.

3.3 SAT features in comparison

Proposition 3.1

The set of public benchmarks in SAT competitions between 2008 and 2015 represent average SAT problems

Define a large set of SAT features. Present data. Categorize data.

3.4 Basic SAT solving techniques

3.5 SAT solvers in use

3.6 Encodings

3.6.1 STP approach

Given a set of clauses, return a subset of clauses satisfying given criterion	
clauses_allLitsNeg	all literals are negative
clauses_oneLitNeg	exactly one literal is negative
clauses_geqOneLitNeg	more than one literal is negative
clauses_allLitsPos	all literals are positive
clauses_oneLitPos	exactly one literal is positive
clauses_geqOneLitPos	more than one literal is positive
clauses_length1	clause contains exactly one literal (“unit clause”)
clauses_length2	clause contains exactly two literals
clauses_unique	clause did not yet occur
clauses_tautological	clause contains some literal and its negation
Given a set of literals/variables, return Boolean property	
literals_existential	literal does not occur negated
literals_unit	literal occurs in clause of length 1
literals_contradiction	literal occurs with its negation on one clause
literals_1occ	literal occurs only in one clause once
literals_2occs	literal occurs two times in clauses
literals_3occs	literal occurs three times in clauses
variables_unit	variable occurs in clause of length 1
Given a set of clauses, return real number based on this clause	
clauses_mapLength	number of literals in clause
clauses_mapRatioPosNeg	number of positive literals divided by total number of literal
clauses_mapNumPos	number of positive literals in clause
Given one clause, return Boolean property	
clauselits_someEx	any is literal existential
clauselits_allEx	all literals are existential
clauselits_someUnit	contains unit variable
clauselits_someContra	contains contradiction variable
clauselits_all1occ	all variables occur only once in all clauses
clauselits_all12occ	all variables occur only once or twice in all clauses
Given all clauses, return the following property	
concomp_variable	number of connected components where two variables are in the same component iff they occur in at least one clause together
concomp_literal	number of connected components where two literals are in the same component iff they occur in at least one clause together
xor2_count	Number of clause pairs $(a \vee b, \neg a \vee b)$ for two variables a and b



Chapter 4

Results

4.1 Benchmark results

4.2 Related work

4.3 Conclusion

Chapter 5

Summary and Future Work

5.1 Summary of results

5.2 Future work

Appendices

Appendix A

Illustration

i		$VS_{i,0}$	$VS_{i,1}$	$VS_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101010110011111110		
-1	A:	1110111110011011010101110001001		
0	A:	01101011110101001110010000010010	W:	01001101011110101001110010000011
1	A:	0111011001001111111011100 <u>u</u> 110001	W:	<u>u</u> 1010110110010111001001001111010
2	A:	101010110100000001110 <u>u</u> 01 <u>n</u> 110010	W:	<u>n</u> 01 <u>n</u> 100111010101101001010111000
3	A:	101011 <u>u</u> 1001111010101001001010001	W:	0101011110100111101001011110110
4	A:	00101100011000110101010111110010	W:	1101110011101001000101000111100
5	A:	000110100110001010 <u>u</u> 1101000000001	W:	11011001100001101100110110011
6	A:	0001101100 <u>unuu</u> 110001000001111010	W:	1011011010000111010000000100000
7	A:	00101011100000010 <u>unn</u> 011001010000	W:	00111011001010100101110110011111
8	A:	011100110010001 <u>u</u> 1111111110110000	W:	11000110100111010111000110110011
9	A:	101011 <u>n</u> 01 <u>unnu</u> 0001111100110011111	W:	11111001111010011001000110011000
10	A:	10 <u>n</u> 00100100001010100000010101110	W:	11010111000111111000000001011110
11	A:	<u>u</u> 1000110101101100100101011111111	W:	10100110001110111011001011101000
12	A:	001011 <u>u</u> 00 <u>u</u> 1010111111110001111011	W:	010001011101110 <u>n</u> 1000111000110001
13	A:	10 <u>un</u> 1 <u>n</u> 01001100010100000111100101	W:	10010111111000110001111111100101
14	A:	00001010010100011000100011010110	W:	00100111100101001011111100001000
15	A:	0001111010101 <u>u</u> 010110011011010100	W:	10111001111010001100001111101001
16	A:	<u>n</u> 00 <u>n</u> 0 <u>un</u> 0110100101001101101011111		
17	A:	00011111001110100001001000011110		
18	A:	01010111000011010000000010010100		
19	A:	<u>u</u> 1 <u>n</u> 10000000101111001101011000100		
20	A:	<u>n</u> 1 <u>un</u> 1001111111011101000000110100		
21	A:	11110011101100000101111111010100		
22	A:	01011101110011010011001100111010		
23	A:	01010000111011101100011110001111		
24	A:	00000010000100100011011100011010		
25	A:	10110000100101100001010011101010		
26	A:	00001010100010010111011101000001		
27	A:	000001101110111101011010110011		
28	A:	10110110010111010110110000100101		
29	A:	10100010000011010100100001101001		
30	A:	0010100111010111100011101100011		
31	A:	11111100100100101101011110110110		
32	A:	01001111110100100110100000101111		
33	A:	00111000001111010110111011100100		
34	A:	00100000011101011110100000010101		
35	A:	<u>n</u> 0100000001100110000010001110010		
36	A:	<u>n</u> 0000111111010111101111001011001		
37	A:	11001000000110100100001100001100		
38	A:	1011000001100111110100110101100		
39	A:	00010010000010100001101100011100		
40	A:	11000000010010000111000110000101		
41	A:	00000110100001101111010100100110		
42	A:	01001110110111011111111010000110		
43	A:	01010000011000111101000001101101		
44	A:	11111000000101101111011100001100		
45	A:	10001010110110110010110000000100		
46	A:	10000010100110010101100011011100		
47	A:	10000001111001011011010010111101		

TABLE A.1: One of the original MD₄ collision given by Wang, et al.

Appendix B

Testcases

Figures B.1, B.2, B.3 and B.4 show testcases used to test performance measures.

i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	100110001011101010110011111110		
-1	A:	1110111110011011010101110001001		
0	A:	x-----	W:	--x-----
1	A:	-----	W:	-----
2	A:	-----x-----	W:	x-----
3	A:	xxx-----	W:	-----
4	A:	-----xx	W:	x-----
5	A:	-----xxxxxxxxxxxxx-x-----	W:	-----
6	A:	x-----x-----x-x-xxxx--x	W:	-----
7	A:	-----x-x-x-----	W:	-----
8	A:	-----x-----x-x-x-----	W:	x-----
9	A:	-----x-x-x-----	W:	-----
10	A:	-----x-x--xxx-xxx-----	W:	-----
11	A:	x-----xxx-x-----	W:	-----
12	A:	--x--x-----	W:	x-----
13	A:	-----	W:	-----
14	A:	-x-----	W:	-----
15	A:	x-x-----x-----	W:	-----
16	A:	-xxx-----		
17	A:	-----		
18	A:	-----		
19	A:	x-----		
20	A:	x-----		
21	A:	-----		
22	A:	-----		
23	A:	-----		
24	A:	-----		
25	A:	-----		
26	A:	-----		
27	A:	-----		
28	A:	-----		
29	A:	-----		
30	A:	-----		
31	A:	-----		
32	A:	x-----		
33	A:	-----		
34	A:	-----		
35	A:	-----		
36	A:	-----		
37	A:	-----		
38	A:	-----		
39	A:	-----		
40	A:	-----		
41	A:	-----		
42	A:	-----		
43	A:	-----		
44	A:	-----		
45	A:	-----		
46	A:	-----		
47	A:	-----		

TABLE B.1: TODO description

i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	10011000101110101101110011111110		
-1	A:	1110111110011011010101110001001		
0	A:	????????????????????????????????	W:	--x-----
1	A:	????????????????????????????????	W:	-----
2	A:	????????????????????????????????	W:	x-----
3	A:	????????????????????????????????	W:	-----
4	A:	????????????????????????????????	W:	x-----
5	A:	????????????????????????????????	W:	-----
6	A:	????????????????????????????????	W:	-----
7	A:	????????????????????????????????	W:	-----
8	A:	????????????????????????????????	W:	x-----
9	A:	????????????????????????????????	W:	-----
10	A:	????????????????????????????????	W:	-----
11	A:	????????????????????????????????	W:	-----
12	A:	????????????????-----	W:	x-----
13	A:	????????????????-----	W:	-----
14	A:	????????????????-----	W:	-----
15	A:	????????????????-----	W:	-----
16	A:	???x-----		
17	A:	?-----		
18	A:	?-----		
19	A:	?-----		
20	A:	x-----		
21	A:	-----		
22	A:	-----		
23	A:	-----		
24	A:	-----		
25	A:	-----		
26	A:	-----		
27	A:	-----		
28	A:	-----		
29	A:	-----		
30	A:	-----		
31	A:	-----		
32	A:	x-----		
33	A:	-----		
34	A:	-----		
35	A:	-----		
36	A:	-----		
37	A:	-----		
38	A:	-----		
39	A:	-----		
40	A:	-----		
41	A:	-----		
42	A:	-----		
43	A:	-----		
44	A:	-----		
45	A:	-----		
46	A:	-----		
47	A:	-----		

TABLE B.2: TODO description

i		$\nabla S_{i,0}$	$\nabla S_{i,1}$	$\nabla S_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	10011000101110101101110011111110		
-1	A:	11101111110011011010101110001001		
0	A:	????????????????????????????????	W:	--x-----
1	A:	????????????????????????????????	W:	-----
2	A:	????????????????????????????????	W:	x-----
3	A:	????????????????????????????????	W:	-----
4	A:	????????????????????????????????	W:	x-----
5	A:	????????????????????????????????	W:	-----
6	A:	????????????????????????????????	W:	-----
7	A:	????????????????????????????????	W:	-----
8	A:	????????????????????????????????	W:	x-----
9	A:	????????????????????????????????	W:	-----
10	A:	????????????????????????????????	W:	-----
11	A:	????????????????????????????????	W:	-----
12	A:	????????????????????????????????	W:	x-----
13	A:	????????????????????????????????	W:	-----
14	A:	????????????????????????????????	W:	-----
15	A:	????????????????????????????????	W:	-----
16	A:	????????????????????????????????		
17	A:	????????????????????????????????		
18	A:	????????????????????????????????		
19	A:	????????????????????????????????		
20	A:	????????????????????????????????		
21	A:	-----		
22	A:	-----		
23	A:	-----		
24	A:	-----		
25	A:	-----		
26	A:	-----		
27	A:	-----		
28	A:	-----		
29	A:	-----		
30	A:	-----		
31	A:	-----		
32	A:	x-----		
33	A:	-----		
34	A:	-----		
35	A:	-----		
36	A:	-----		
37	A:	-----		
38	A:	-----		
39	A:	-----		
40	A:	-----		
41	A:	-----		
42	A:	-----		
43	A:	-----		
44	A:	-----		
45	A:	-----		
46	A:	-----		
47	A:	-----		

TABLE B.3: TODO description

i		$VS_{i,0}$	$VS_{i,1}$	$VS_{i,2}$
-4	A:	01100111010001010010001100000001		
-3	A:	00010000001100100101010001110110		
-2	A:	10011000101110101101110011111110		
-1	A:	1110111110011011010101110001001		
0	A:	????????????????????????????????	W:	????????????????????????????????
1	A:	????????????????????????????????	W:	????????????????????????????????
2	A:	????????????????????????????????	W:	????????????????????????????????
3	A:	????????????????????????????????	W:	????????????????????????????????
4	A:	????????????????????????????????	W:	????????????????????????????????
5	A:	????????????????????????????????	W:	????????????????????????????????
6	A:	????????????????????????????????	W:	????????????????????????????????
7	A:	????????????????????????????????	W:	????????????????????????????????
8	A:	????????????????????????????????	W:	????????????????????????????????
9	A:	????????????????????????????????	W:	????????????????????????????????
10	A:	????????????????????????????????	W:	????????????????????????????????
11	A:	????????????????????????????????	W:	????????????????????????????????
12	A:	????????????????????????????????	W:	????????????????????????????????
13	A:	????????????????????????????????	W:	????????????????????????????????
14	A:	????????????????????????????????	W:	????????????????????????????????
15	A:	????????????????????????????????	W:	????????????????????????????????
16	A:	????????????????????????????????		
17	A:	????????????????????????????????		
18	A:	????????????????????????????????		
19	A:	????????????????????????????????		
20	A:	????????????????????????????????		
21	A:	-----		
22	A:	-----		
23	A:	-----		
24	A:	-----		
25	A:	-----		
26	A:	-----		
27	A:	-----		
28	A:	-----		
29	A:	-----		
30	A:	-----		
31	A:	-----		
32	A:	x????????????????????????????????		
33	A:	-----		
34	A:	-----		
35	A:	-----		
36	A:	-----		
37	A:	-----		
38	A:	-----		
39	A:	-----		
40	A:	-----		
41	A:	-----		
42	A:	-----		
43	A:	-----		
44	A:	-----		
45	A:	-----		
46	A:	-----		
47	A:	-----		

TABLE B.4: TODO description

Appendix C

Hardware setup

In the following we introduce two hardware setups which were used to run our testcases. The first setup is referred to as “Thinkpad x220” throughout the document whereas the second setup is referred to as “Cluster”.

<i>Type model</i>	Thinkpad Lenovo x220 tablet, 4299-2P6
<i>Processor</i>	Intel i5-2520M, 2.50 GHz, dual-core, Hyperthreaded
<i>RAM</i>	16 GB (extension to common retail setup)
<i>Memory</i>	160 GB SSD
<i>L3 cache size</i>	3072 KB

TABLE C.1: Thinkpad x220 Tablet specification [10]

<i>Processor</i>	Intel Xeon X5690, 3.47 GHz, 6 cores, Hyperthreaded
<i>RAM</i>	192 GB
<i>L3 cache size</i>	12288 KB

TABLE C.2: Cluster node nehalem192go specification [3]

Index

- k*-clause, 18
- Algorithm, 6
- AND (Boolean function), 4
- Assignment, 6
- Bit condition, 14
- Boolean function, 4
- Clause, 18
- Collision resistance, 2
- Conjunction, 17
- Conjunctive Normal Form, 17
- Definite clause, 18
- Differential notation, 14
- Disjunction, 17
- Disjunctive Normal Form, 17
- Feature value, 19
- Hash collision, 4
- Hash function, 2
- Hash value, 2
- Horn clause, 18
- I/O Algorithm, 6
- Least significant bit, 7
- Left-rotation, 12
- Left-shift, 12
- Literal, 17
- MD4, 9
- Model, 6
- Most significant bit, 7
- Negative literal, 17
- NOT (Boolean function), 4
- OR (Boolean function), 4
- Positive literal, 17
- Preimage, 2
- Preimage resistance, 2
- Right-rotation, 12
- Right-shift, 12
- SAT feature, 19
- SAT solver, 6
- Satisfiability, 6
- Second-preimage resistance, 2
- SHA-256, 12
- Truth table, 4
- Unit clause, 18

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