

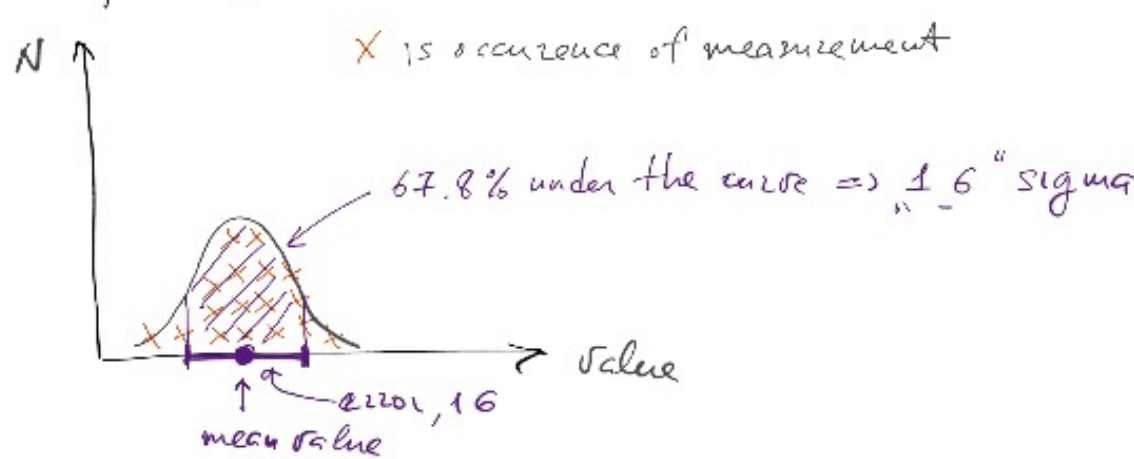
## What we will use:

- \* Python 2.7, install Anaconda on your computer from continuum analytics  
We will use mainly numpy  $\rightarrow$  collection of numerical methods, pandas  $\rightarrow$  for the data
- \* Github will be used to store all files of our course and store programs that we will write

We have 2 servers and you will be given access to them

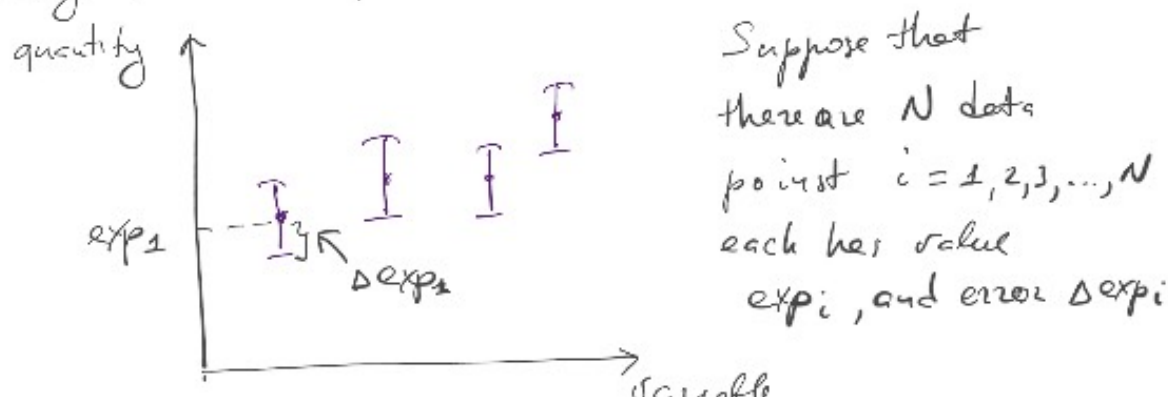
## First lecture: Experimental data and fitting

What is experimental data? Result of the measurement of a certain quantity



The bell shaped curve is normal distribution in most cases, generically this histogram is called probability density function "pdf"

Now imagine several experimental data



Suppose that there are  $N$  data points  $i = 1, 2, 3, \dots, N$  each has value  $exp_i$ , and error  $\Delta exp_i$

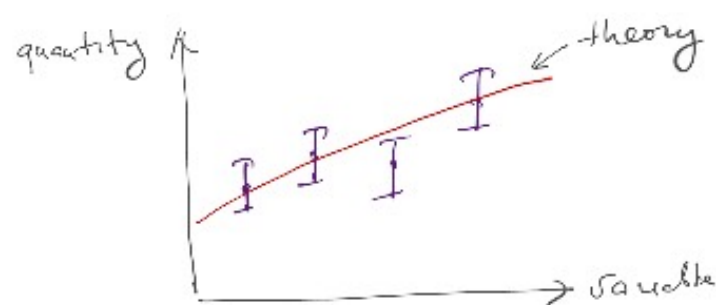
Suppose that we have a theory that should describe the data. This theory will depend on unknown parameters "a". We would like to study those parameters.

In order to do so one has to construct  $\chi^2$  function

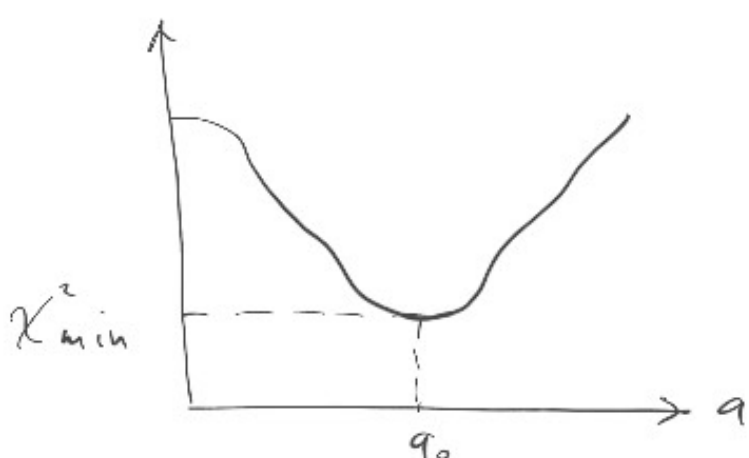
$$\chi^2(a) = \sum_{i=1}^N \left( \frac{th_i - exp_i}{\Delta exp_i} \right)^2$$

here  $th_i$  is theory prediction for experimental measurement of point  $i$

Remember that "th" is a function of parameters "a" and variable



Minimizing  $\chi^2(a)$  will yield values of parameters  $a$  where  $\chi^2$  is minimal an equal  $\chi^2_{min}$



How can we study errors of  $a_0$ ?

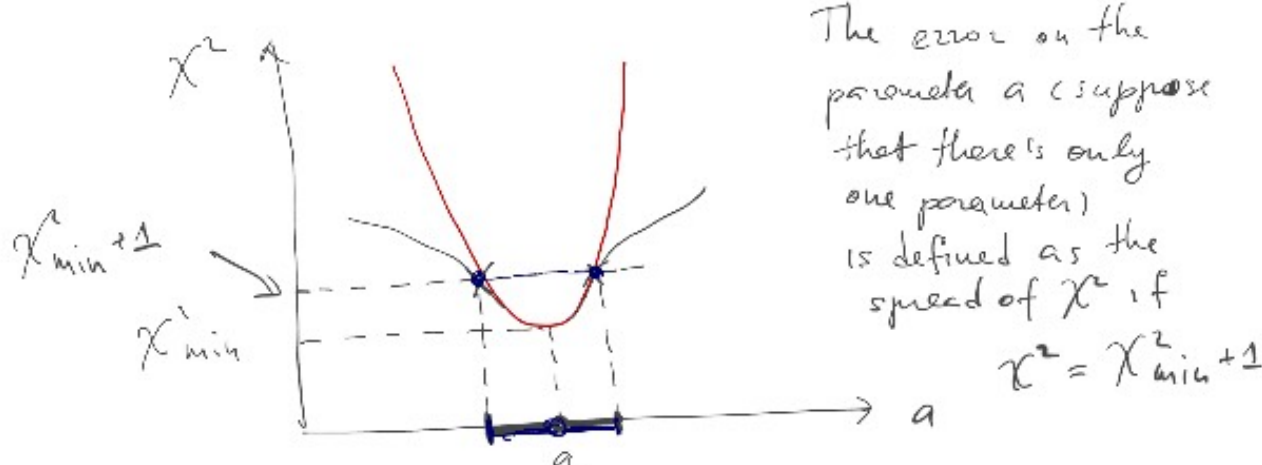
$$\chi^2(a) = \chi^2(a_0) + \underbrace{\frac{\partial \chi^2}{\partial a}(a_0)}_{=0 \text{ as we are at minimum}} (a - a_0) + \frac{1}{2} \frac{\partial^2 \chi^2}{\partial a^2}(a_0) (a - a_0)^2 + \dots$$

$$\Rightarrow \chi^2(a) \approx \chi^2(a_0) + \frac{1}{2} \frac{\partial^2 \chi^2}{\partial a^2}(a_0) (a - a_0)^2$$

quadratic approximation

Usually there will be minimizers already available in Python for us. We will need to program explicitly  $\chi^2$  function.

Let us see how quadratic approximation works:



The error on the parameter  $a$  (suppose that there is only one parameter) is defined as the spread of  $\chi^2$  if  $\chi^2 = \chi^2_{min} + 1$

As you can see from the plot, sometimes this approximation will work fine, sometimes it will fail

