# Analysis of stock market recommendations using computer vision

Submitted in fulfilment of the requirements of the degree of

#### Masters of Technology

by

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## **CERTIFICATE**

This is to certify that the project entitled "Analysis of stock market recommendations using computer vision" is a genuine work of Pronoy Mandal (Registration no. 20 - 27 - 09) submitted to the Defence Institute of Advanced Technology (Pune) in fulfilment of the requirement for the award of Masters of Technology in Data Science.

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## Dissertation Approval for M.Tech.

This project report entitled Analysis of stock market recommendations using computer vision by Pronoy Mandal is certified for the degree of Masters of Technology in Data Science.

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## **DECLARATION**

I declare that this written submission represents my ideas in my own words, and where other ideas or words have been included, I have adequately cited and referenced the original sources. I also declare that I have adhered to all principles of academic honesty and integrity and that I have not misrepresented, fabricated, or falsified any idea, data, fact or source in my submission. I understand that any violation of the above will be cause for disciplinary action by the institute and can also evoke penal action from the sources which have thus not been properly cited or from whom proper permission has not been taken when needed.

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### Abstract

There are a large number of business NEWS channels broadcasting a variety of topics throughout morning and evening primetime. These range from simple stock market recommendations (strategies to BUY/SELL/HOLD) to detailed fundamental and technical analyses of various companies to in-depth quarterly performance reviews of various parties in the market. With the availability of such a volume of information from public sources; it becomes difficult to assimilate all the information in a single place and analyse it for meaningful information.

This project encompasses the ability to analyse NEWS which gives stock market recommendations (a subset of business NEWS) and presents the results in a tabular format to the user for analysis. The tabular format includes basic information from the broadcast such as the telecast date of the show, the analyst presenting the same, the stock which is being discussed, the NSE listing symbol of the concerned stock, the recommendation etc. (totalling 8 parameters). The exact reason why the Securities and Exchange Board of India (SEBI) is attempting to analyse NEWS videos is something that can't be specified within the scope of this report due to its confidentiality. However, it can be said that this project's output forms the base as well as the input of many anomaly (in the context of violations in the securities market) detection models at a later stage.

This project goes a step ahead to ease and automate the job of SEBI officers from the surveillance department by deploying the same onto an MLOPs platform and creating an equivalent free-running workflow in a virtual environment.

The aforementioned reason forms the principal motivation for doing this project i.e. it helps automate a large part of a task that is prone to human errors and mistakes such as collecting data manually by watching the NEWS shows and at the same time reduces the time required to carry out such tasks. Apart from that, since an MLOPs workflow is included in the project, this project helps establish various principles which need to be followed for any ML project in general so that it can be deployed into production.

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## Chapter 1

## Introduction

#### 1.1 Dissertation name and title

My dissertation is titled **Analysis of stock market recommendations using computer vision**.

#### 1.2 Problem statement

There is a large no. of daily broadcasts which take place throughout primetime (morning and evening) as well as outside of it. This project aims to digitize as well as summarise the recommendations cumulatively and present them to the end-user at the same time this project and its associated machine learning system are input to more sophisticated models for anomaly detection (in the context of violations in the securities market) at a later stage.

#### 1.3 Proposed solution

The proposed solution is a deep learning model aimed at solving two fundamental machine learning problems at hand:

- (a) Object detection Detect and classify important regions of interest in the frames of various NEWS broadcasts (or NEWS shows) i.e. regions having (but not restricted to) the name of the analyst/presenter, the recommendation being given, the company, commodity or the market segment being discussed and its corresponding listing symbol (if any), the various metrics of the recommendation such as stop loss, target price etc.
- (b) Optical Character Recognition (OCR) Bilingual (English and Hindi) text obtained from the above regions of interest is passed onto sophisticated OCR models which have a text detection model and an actual language model(s) (corresponding to

Chapter 1 Section 1.4

the concerned languages) working under the hood to obtain or extract the required information.

The final output consists of a CSV (or) an excel file as required which summarises the above-obtained information.

#### 1.4 Scope and report contents

Chapter 2 goes into a detailed discussion of the literature which has been studied while preparing this report. It includes several details such as (but not restricted to) how **YoLo** models or in general object detection models are evaluated and which performance metrics and common datasets are referred to for their speed and accuracy. It has additional details regarding how advanced deep learning models like **YoLov4** can be optimised for special use cases wherein necessary. The work presented in this dissertation may be completed sequentially or parallelly and is described as follows. Additionally, the chapters to which they pertain to are also mentioned.

(a) Machine learning and computer vision: There are a total of 8 NEWS shows which are currently being targeted under this project. Machine learning used within this project is further divided into two parts: the one dealing with the recognition of various numerical parameters from the video frames of a broadcast (wherein active work is going on to increase efficiency as well as the accuracy of models) are random forest classifiers which have been trained on a large number of video frames which were earlier trained on **YoLov3** output (but needed additional training due to lesser accuracy) and templates followed by a much more robust and reliable framework i.e. YoLov4 which has been trained only for one NEWS show (i.e. *PehlaSauda* from CNBC Awaaz).

The second part of ML goes into OCR models wherein **no active work is being pursued** rather readymade models and OCR engines that are doing the job within tolerable error limits are being used. Both Tesseract – OCR and EasyOCR provided models have been used for this purpose and their performance metrics analysed. It should be noted that **no part of the report** goes into the details of the inner workings of the OCR models which are deep learning models in themselves.

As opposed to standard ML projects wherein a considerable amount of time is used for training a particular model; this project uses more time and space to carry out a variety of image processing operations on the captured video frames. This includes histogram equalization, simple grey level transformations, and complex erosion and dilation processes. After carrying out sufficient thresholding operations, these are fed into the ML models described above.

The details for the above i.e. the process of collecting the data, preparing the data for training and testing and using appropriate deep learning models for the same are discussed in chapter 3 in detail.

(b) Deployment into production: Rarely do data science projects in academia ever reach production and into a streamlined architecture. There are several reasons which

prevent it from happening so. Such details, as well as reasons, have been given in brief in chapter 4's opening sections.

Fortunately, for this project, the deployment of the data models falls within its current scope. All the ML models which would be trained and tested would be loaded onto the proprietary **Ezmeral MLOPs** platform by **HPE**. The servers for the same reside alongside the required hardware resources on SEBI's internal servers. Doing this (without going into the details) would make the entire process streamlined i.e. the process of uploading videos, and training models on new data as soon as it is available and at the same time would decrease the manual work involved while doing so. As soon as the deployment has been completed, whether for all the NEWS shows or even a few of them, the internal server would be able to serve requests from within the organization domain (*POST* methods with *JSON* body) and at the same time would be able to abstract all the complex code and scripts running in the background.

Apart from the MLOPs deployment, it is more desirable for SEBI to have a continuously running workflow that shall consist of processing a bulk or a batch of videos at once. A workflow about this has been deployed on a standalone virtual machine as a part of this project. Which projects require an MLOPs workflow and which don't, as a result, have also been discussed in chapter 4.

Chapter 5 would then go on to discuss the various results which have been obtained at the end in terms of speed and accuracy of the YoLo models involved which metrics are suitable for evaluating projects spanning multiple ML models. Chapter 6 of the report would then finally present important conclusions drawn from the entire project.

## Chapter 2

## Literature review

### 2.1 YoLo – A brief discussion on v3 and v4 for realtime object detection

YoLo standing for You Only Look Once is(are) a set of advanced deep learning models for real-time object detection. The focal point for YoLo is that it manages to perform bounding box regression and classification at the same time. The architecture or methodology which separates YoLo and other object detection frameworks is that other sophisticated frameworks (RCNN and even Fast RCNN) attempt to repurpose existing classifiers and localisers to perform object detection. They apply a single model to multiple locations within an image with variations in scale and other properties of the image multiple times. High scoring regions are labelled and classified accordingly.

YoLo frameworks take a drastically different approach: they divide the region into a large number of regions (or boxes) and simultaneously apply a single convolutional neural network to the entire image. The bounding boxes and associated probabilities are received at the output. These regions are then weighted according to these probabilities. The reason why this method supersedes other popular methods is that other neural network-based deep learning architectures (such as R-CNN) may end up using multiple network evaluations (in the order of thousands) on a single image that takes up a considerable amount of processing time. Additionally, YoLo models look at the entirety of the image during the detection phase because of which their predictions are based on the global context of the image. Although the differences don't end here, these fundamental differences are enough to give YoLo a second to third order speed advantage over Fast R-CNN and R-CNN models.

The neural network for YoLo along with its entire compilation system is known as Darknet. A typical darknet run on an image, set of images, video or a real-time stream of image content (such as through a webcam) leads to the following three things as output:

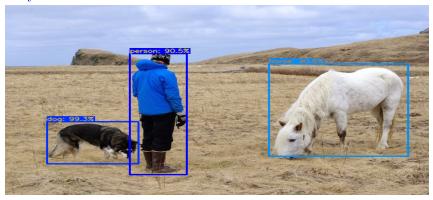
- The detected classes of objects (e.g. horse, car etc.)
- The prediction confidence (e.g. 0.91, 0.86 etc.) and
- The time it took to carry out the prediction or detection (e.g. 6s, 12s etc.)

• Sophisticated high-level libraries will also produce the bounding boxes corresponding to each

Following is the output when a high-level library like yolov4 is used to process an image as shown below.



(a) A sample image taken from the original Darknet github repository



(b) Bounding boxes and detected objects in the image

(c) The bounding box coordinates obtained

Figure 2.1: A sample Darknet run on an image

#### 2.1.1 YoLov3

Joseph Redmond is credited with designing the original neural network architecture called Darknet. This was made using all low-level languages so that it could be made as flexible

Chapter 2 Section 2.1

as it can be. This architecture went on to produce a series of computer vision wonders in the field of object detection named as YoLo: the original one, v2, v3 and then v4. Even YoLov5 has been developed (the first one to be developed by an organisation as opposed to an individual) at the time of writing this report. However, we won't be discussing it here since it hasn't been used in the concerned project.

YoLov3 is the first version using an objectivity score for the prediction of bounding boxes. It also proceeds to add further connections to the backbone of the entire architecture. Additionally, detections are also carried out at three levels of granularity which greatly increased the inferencing accuracy on smaller objects as well as objects/ smaller objects placed close to each other. There are some important parts or sections in YoLov3 which proves its robustness to a variety of real-life object detection scenarios. They relate to better bounding box prediction, class prediction, their feature extractor as well better prediction across multiple scales provided in the input. We would be discussing each of them in brief in the following paragraphs.

#### Bounding box prediction

Any bounding box in a prediction is represented by a set of four parameters namely  $t_x$  and  $t_y$ : coordinates of the centre of the bounding box and its width and height represented by  $t_w$  and  $t_h$  respectively. In the event of the top left corner of the bounding box being displaced by  $(c_x, c_y)$  respectively, the following overall changes are calculated in the dimensions (assume  $p_w$  and  $p_h$  are the width and height of the bounding box prior).

$$b_x = \sigma(t_x) + c_x$$

$$b_y = \sigma(t_y) + c_y$$

$$b_w = p_w e^{t_w}$$

$$b_h = p_h e^{t_h}$$

Unlike previous systems (or previous YoLo versions), the training phase assigns an objectness score to each bounding box. This score equals one if the current bounding box overlaps a ground truth object to an extent greater than any other previously obtained bounding box. If any previously obtained bounding box doesn't overlap the ground truth to a greater extent or overlaps only by a certain threshold (say 0.5 as stated in this paper) then the objectness score is simply zero. Following is a representation of all the important dimensions which are involved in this process.

#### Class prediction

SoftMax is one of the most common types of methods used for multi-label classification, however, the method has been leading to decrementing results for the class prediction accuracy in YoLov3 as well as has been unnecessary. Therefore, simple multiple logistic classifiers are being used for the purpose and binary cross-entropy has been used as a loss function. This different approach helped in the case of much larger and more sophisticated datasets such as the Open Images Dataset wherein labels may overlap frequently. SoftMax algorithm assumes that a single bounding box corresponds to exactly one label which is often not the case.

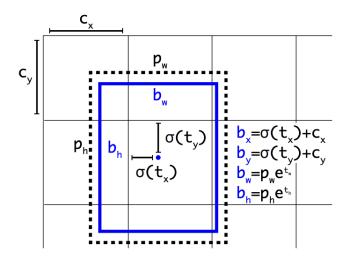


Figure 2.2: An illustration showing all the important bounding box dimesnions being used in YoLov3

#### Feature extraction

Feature extraction in YoLov3 has been a hybridisation of the one in YoLov2, Darknet – 19 (19 convolutional layers) and another residual network. But the most important part of this network is shortcut connections which increase the size of the network significantly, however, continue to supersede ResNet variants in terms of efficiency. Since this leads to a total of **53** convolutional layers it's named Darknet-53.

#### 2.1.2 YoLov4 – improvements over YoLov3

The fundamental difference between YoLov4 and all its previous variants is that the detector stage has been bifurcated into two distinct sections consisting of a single stage – detector and sparse prediction stage. Following is an illustration of the same.

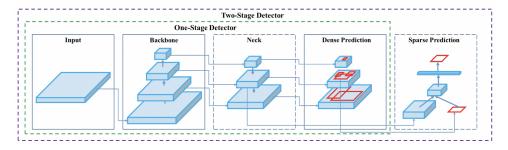


Figure 2.3: Two stage detector setup used in YoLov4

After the initial input phase, we have 3 main sections as follows.

Chapter 2 Section 2.1

#### Backbone

This is the common name for the feature extractor section of the entire neural network architecture. It should be noted that all backbones are essentially classification models. With VGG16 being the most common and the earliest deep learning classifiers, SqueezeNet, ShuffleNET and MobileNET are used along with it. These classifiers are meant for the CPU only.

#### Neck

The neck is the common name for a feature aggregator in YoLo frameworks i.e. it collects the feature maps from various sections of the backbone stage. FPN, PAN, NAS-FPN, Fully-connected FPN, BiFPN, ASFF, and SFAM are all examples of feature aggregation blocks used in YoLov4.

#### Head

This is the final stage of the entire framework: a common name for the object detector stage in YoLo frameworks. It should be noted that this stage exclusively tells the region(s) in which (an) object(s) may be located, however, doesn't tell the class or label to which the object belongs. As stated earlier, these could be a single or two-stage detector, both anchor-based and anchor-free. Some common examples are YOLO, RetinaNet, SSD, Faster – RCNN etc.

As the number of examples in each stage shows, a typical YoLov4 framework can be implemented in any combination of input, backbone, neck and head. When there are such a large number of combinations possible, the best architecture should be an optimal combination of all the sections. This optimal choice would alone make it superior to YoLov3 in terms of **performance and accuracy**. This optimal combination should be arrived at by looking at the following parameters:

- Input resolution of images and their size
- Number of convolutional layers
- Number of parameters (hyperparameters) to be optimised
- Number of output layers or filters
- YoLov4 also provides something known as *Bag of Specials* and *Bag of Freebies* which are methods or functions for increasing the respective fields and mappings between backbone levels to detector levels. This gives us another region wherein optimisation can be done.

The final architecture that was deemed optimal for YoLov4 is as follows (with backbone, neck and head in order).



Figure 2.4: The final architecture presented in the paper

A couple of other combinations were derived but the FPS of the above combination superseded everything else. A summary of the FPS values of a couple of other possibilities is given below. Now we are going to see some special sections of the architecture (but are not limited to) in detail which make it more efficient than YoLov3.

Table 2.1: Neural network parameters for image recognition for  $512 \times 512$  network resolution

Backbone model	Receptive field size	Parameters	Average layer size	BFLOPs	FPS
CSPResNext50	$425 \times 425$	20.6 mn	1058 K	31	62
CSPDarknet53	$725 \times 725$	27.6 mn	950 K	52	66
EfficientNet	$1311 \times 1311$	12	668 K	11	26

#### Cross Stage Partial connection (CSP)

In any large neural network-based architecture, it is common for the last and the second to last layers to lose out on a lot of contextual features seen by the initial layers. A way out of this is to introduce the concept of skip connections so that the backpropagation of gradients to the initial layers can be done easily. DenseNet was initially considered for this but it had skip connections between every other layer which proved to be inefficient. So, the researchers stuck with their initial choice of CSPResNext50 and the CSPDarknet53 as far as the architecture is concerned. Following is an illustration of the same.

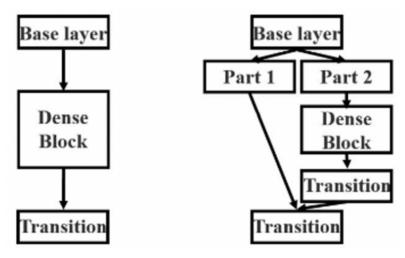


Figure 2.5: The two possible dense architectures: DenseNet and CSPDensnet

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#### Self-Adversarial Training (SAT)

Deep learning is very much susceptible to adversarial data so YoLov4 uses SAT to introduce precise amounts of perturbation in the data such that the predicted label stays the same as the original label. This helps it easily achieve good accuracies for even augmentations of simple images.

All these discussions prove the benefits and advantages of YoLov4 over YoLov3 and hence it's choice for the project. As always, all things are better quantified in a graph of MAP versus execution time as shown below.

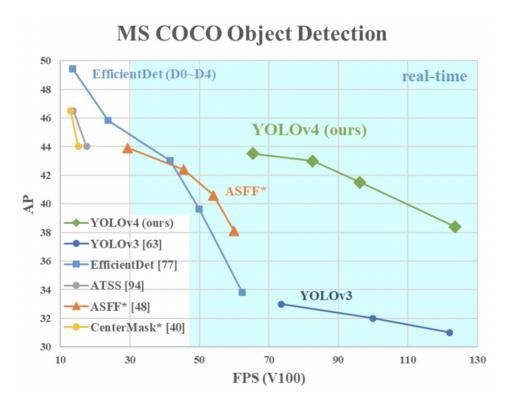


Figure 2.6: YoLov4 vs other state of the art object detectors

# 2.2 Performance metrics for evaluating object detection models [1]

The entirety of this report deals with a large number of performance metrics used to evaluate a variety of ML/DL models. Some are popular and have been used to evaluate such models for a long time while some metrics are empirical in nature because their output is a combination of a variety of models dealing with different classes of inputs and outputs which are working together. However, we would be specifically discussing metrics used for the evaluation of the performance of object detection models in this section.

#### 2.2.1 Intersection over Union (IoU)

This metric equals the amount of overlap between the ground truth denoted by  $g_t$  and the predicted value by a particular model i.e. prediction denoted by  $p_d$ . It is to be noted that since this value is a ratio, it is a fraction consisting of numerator and denominator areas in appropriate units. Mathematically, it is given by

$$IoU = \frac{area(g_t \cap p_d)}{area(g_t \cup p_d)}$$
 (2.1)

As it is very obvious for any arbitrary situation  $0 \le \text{IoU} \le 1$  wherein 0 corresponds to a null overlap and 1 corresponds to a full overlap. However, in almost all ML/DL models we don't go for such strict definitions rather we define what we call the IoU at  $\alpha$  (or abbreviated as IoU@ $\alpha$ ). This means any value of IoU  $\ge \alpha$  is considered a true positive whereas any value otherwise is considered a true negative.

Before we go ahead and define the next important metric we need to know a couple of different terms as stated below:

• **Precision** – The degree to which a model can identify only the relevant objects. It is simply the ratio of true positives and all the detections made by the model. It is given by

$$P = \frac{True\ positives}{All\ detections\ made\ by\ the\ model}$$
 (2.2)

• Recall – The degree to which the model can detect all true positives amongst all ground truths. Mathematically, it is the ratio of the number of true positives and all ground truths and is given by

$$R = \frac{True\ positives}{All\ ground\ truths}$$

(2.3)

A good model has a high precision as well as high recall.

- Precision—recall curve It is simply the plot of the variation of precision and recall against the variation of confidence values. A good model will give high precision values even when confidence is varied significantly.
- Average precision When the area under the precision-recall curve is calculated at the  $IoU@\alpha$  threshold then we get this value. Formally, it is defined using the following integral.

$$AP@\alpha = \int_{0}^{1} p(r) \, dr \tag{2.4}$$

Now we are at a stage where we can understand the next important metric

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#### 2.2.2 Mean Average Precision (mAP)

For each class, the average precision as defined above is calculated. This roughly translates to No. of average precision values  $\approx$  No. of classes. When the average of these average precision is taken we get what we know as the mean average precision. For n classes we can simply calculate it as follows:

$$mAP@\alpha = \frac{1}{n} \sum_{i=1}^{n} AP_i \tag{2.5}$$

### 2.3 Guidelines for a good YoLo project

The following rules for a good project using YoLo are mere thumb-rules and are not some strict guidelines to be followed and should be evaluated on a case to case basis for every project. Additionally, it should be noted that such rules may not be applicable for implementation in every object detection project. The following rules are bifurcated into those undertaken during the training and those in the testing (detection) phase.

#### 2.3.1 For training

- (a) The values of random should be set to 1 in your .cfg file which allows training for multiple image or video resolutions simultaneously.
- (b) Every distinct object that is liable for detection must have an appropriate label in the dataset.
- (c) Precision may be increased by keeping the height and width of images or video frames as a multiple of 32.
- (d) The training dataset should be such that every object to be detected corresponds to an exactly similar object in the training dataset. Similarity should be in terms of size, no. of classes to be detected (c), overall spatial orientation, overall illumination, augmentation (if any) etc.
  - If the size of the training dataset is N and the no. of classes is stated as above then training must run for at least Nc iterations.
- (e) Training datasets should have as many **positive** examples as there are **negative** examples (i.e. images which don't have any object to be detected). Such negative examples shall return no bounding boxes when the detection or testing run is executed. These ensure an equal sensitivity of the model to both types of images as well as eliminate a lot of post-processing operations.
- (f) Sometimes it is desirable to run your detections with the <code>-show\_imgs</code> option at the end so that it can be manually verified whether the predicted bounding boxes are correct or not. Seeing the detections and detecting some anomaly could be a direct implication of training runs going wrong or some inherent problem in the dataset.

#### 2.3.2 For testing or detection

- (a) Increase network resolution in the same way as mentioned in 1. c.
- (b) It should be noted that retraining is not required in the event of loss in your dataset or any other unintended corruption. Only the *darknet* command should be available which can be used to perform detections using the pre-trained .weights file which was trained on the  $416 \times 416$  resolution images.
- (c) To further enhance the accuracy, dataset training must proceed onto higher multiples of 32 such as  $608 \times 608$  or  $832 \times 832$ . In the event of a memory overflow (Out of memory), subdivisions in your .cfg file must be increased from 16 to 32 to 64 and so on.

# Chapter 3

# Methodology and development

# Chapter 4 Deployment in production

# Chapter 5 Results and discussions

# Chapter 6

# Conclusions

# Bibliography

[1] Kiprono Elijah Koech. Object Detection Metrics With Worked Example. English. Aug. 2020. URL: https://towardsdatascience.com/on-object-detection-metrics-with-worked-example-216f173ed31e.

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