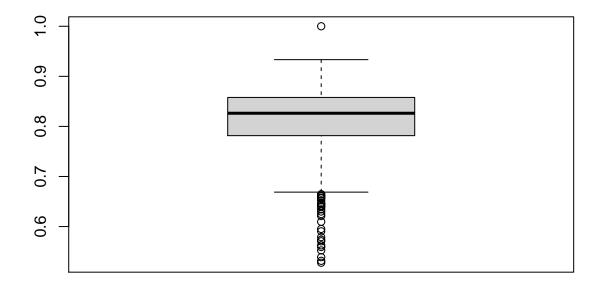
Homework 6

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Question 1

```
scorePlot = boxplot(demo$Prof_Score)
```



```
scoreOutliers = scorePlot$out
scoreBreaks = scorePlot$stats

outlierMin = min(scoreOutliers)
outlierMax = max(scoreOutliers)
```

IQR

```
minRange = c(outlierMin, first(scoreBreaks))
maxRange = c(last(scoreBreaks), outlierMax)
```

```
outlierCount = length(scoreOutliers)
minRange
## [1] 0.5277778 0.6687500
```

maxRange

[1] 0.9333333 1.0000000 outlierCount

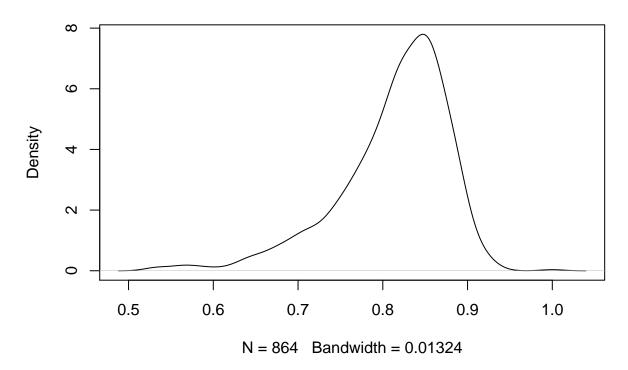
[1] 32

Outliers range from $[0.5278,\,0.6688)$ and (0.9333,1] There are a total of 32 outliers using IQR as our detection method.

Standard Deviation

```
plot(density(demo$Prof_Score))
```

density.default(x = demo\$Prof_Score)



```
scoreSd = sd(demo$Prof_Score)
scoreMean = mean(demo$Prof_Score)

upper = scoreMean + (3*scoreSd)
lower = scoreMean - (3*scoreSd)

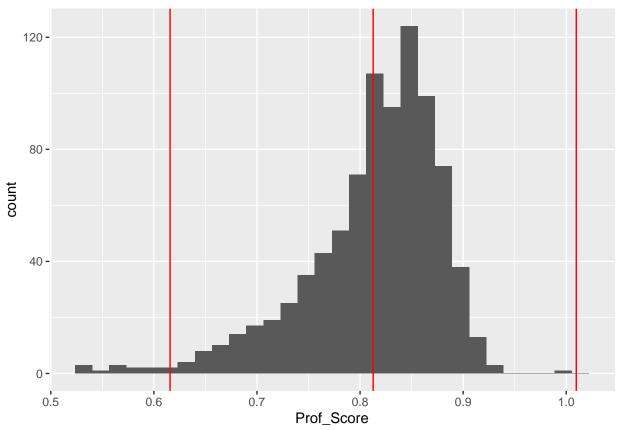
upperOut = demo$Prof_Score > upper
```

```
lowerOut = demo$Prof_Score < lower

sdUpperOutliers = demo$Prof_Score[upperOut]
sdLowerOutliers = demo$Prof_Score[lowerOut]

ggplot(demo, aes(x=Prof_Score)) +
   geom_histogram() +
   geom_vline(xintercept = lower, color='red') +
   geom_vline(xintercept = upper, color='red') +
   geom_vline(xintercept = scoreMean, color='red')</pre>
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
sdOutliers = c(sdLowerOutliers, sdUpperOutliers)
sdOutliers

## [1] 0.5315789 0.5523810 0.5388889 0.5590909 0.6095238 0.5625000 0.5277778

## [8] 0.5705882 0.5736842 0.5952381 0.5789474 0.5904762

sdOutlierRange = c(min(sdOutliers), max(sdOutliers))
sdOutlierRange

## [1] 0.5277778 0.6095238

length(sdOutliers)
```

[1] 12

Using the Standard Deviation to catch outliers resulted in only 12 outliers being found between [0.528, 0.61]

The upper range of the outliers ended up being larger a score greater than 100%, which would have been impossible to achieve in this case, meaning there were no outliers found in the upper range, this is likely due to the heavily skewed distribution of scores.

Inferential Statistics

```
scores = demo$Prof_Score
gTest = grubbs.test(scores)
gOut = c()
while (gTest$p.value < 0.05)
{
    altValue = gTest$alternative
    altValue = as.numeric(strsplit(altValue," ")[[1]][3])
    gOut = append(gOut, altValue)
    scores = scores[!scores %in% altValue]
    gTest = grubbs.test(scores)
}
gRange = c(min(gOut), max(gOut))
gRange</pre>
```

```
## [1] 0.5277778 0.5789474
length(gOut)
```

```
## [1] 9
```

Using Grubbs test for each value in the list, we end up with 9 outliers between [0.5278, 0.5789]. Grubbs test also missed the outlier at 1.0 due to taking out the smallest values first.

I think that if outliers are to be removed then the IQR method is the one to use. It's the only method that accurately compensated for the outliers at the high end of the distribution, and was the least affected by the extremely skewed dataset. That said, the outliers themselves were never so far out of the range of possibility that they needed to be removed. It's not unreasonable for some students to receive a 50% or for some to receive a 100%, so if I was able to, I would probably choose not to remove any outliers at all.

Question 2

NAs appear only in Image_Quality and Smile. with a total of 3396 total records with NA values where 277 of those records have an NA in both Image_Quality and Smile.

```
missingValuesByColumn = colSums(is.na(df))

df$Image_QualityNA = as.factor(ifelse(is.na(df$Image_Quality),1,0))

df$SmileNA = as.factor(ifelse(is.na(df$Smile),1,0))

rForestImage = randomForest(Image_QualityNA ~ ., data = df[-c(5,10,13)])

rForestImage

##

## Call:

## randomForest(formula = Image_QualityNA ~ ., data = df[-c(5, 10, 13)])

##

Type of random forest: classification

##

Number of trees: 500

## No. of variables tried at each split: 3
```

```
##
           OOB estimate of error rate: 8.97%
##
## Confusion matrix:
##
        0 1 class.error
## 0 7937 52 0.00650895
## 1 736 62 0.92230576
rForestSmile = randomForest(SmileNA ~ ., data = df[-c(5,10,12)])
##
## Call:
   randomForest(formula = SmileNA ~ ., data = df[-c(5, 10, 12)])
##
##
                  Type of random forest: classification
                        Number of trees: 500
## No. of variables tried at each split: 3
##
           OOB estimate of error rate: 33.14%
##
## Confusion matrix:
##
        0 1 class.error
## 0 5836 76 0.01285521
## 1 2836 39 0.98643478
```

Based on the Random Forest test, the Image Quality is neither MCAR nor MAR, as the prediction had a fairly low error rate of 8.93% when estimating NAs for Image Quality, and that the NAs are MNAR.

Based on the Random Forest test, the Smile is also likely not MCAR or MAR. The error rate of the prediction is at 33.24% is still accurate enough to assume that the NAs are MNAR instead.

```
df = df[-c(12,13)]
dfListDelete = df[complete.cases(df),]
imputeModel = mice(df, maxit=0)
imputePredictions = imputeModel$predictorMatrix
dfMultipleImpute = mice(df, maxit=5, predictorMatrix = imputePredictions, method = imputeModel$method,
dfImputeComplete = complete(dfMultipleImpute,1)
summary(glm(Area~., data = dfListDelete))
## Call:
  glm(formula = Area ~ ., data = dfListDelete)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
##
  -153151
             -25364
                       -9754
                                 8395
                                       1443587
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          43769
                                      12857
                                              3.404 0.000668 ***
## Gendermale
                           7090
                                       2448
                                              2.896 0.003790 **
## Genderunknown
                                      10593
                                             5.435 5.74e-08 ***
                          57567
## Adult
                          -4571
                                       4463 -1.024 0.305859
## Face_Angle
                                       2373
                                              0.476 0.633767
                           1131
## Image_Color
                           3471
                                       2142
                                              1.621 0.105144
## Image_Qualitygood
                                       2186 11.018 < 2e-16 ***
                          24091
## Image_Type
                           6051
                                       3415
                                             1.772 0.076460 .
```

-23080

9813 -2.352 0.018706 *

Contextauthor

```
## Contextcover
                         68235
                                     5370 12.706 < 2e-16 ***
## Contextfeature
                        -16050
                                     2663 -6.026 1.79e-09 ***
                                     2169 -11.867 < 2e-16 ***
## Multiface
                        -25740
## Raceasian
                         -4762
                                    12134 -0.392 0.694735
## Raceblack
                        -10334
                                    11869 -0.871 0.383943
                                    16079 -0.712 0.476464
## Racepacificislander
                        -11449
## Raceunknown
                                           0.531 0.595534
                          7345
                                    13836
## Racewhite
                          -8860
                                    11234 -0.789 0.430366
## Smile
                          -4582
                                     2204 -2.079 0.037630 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for gaussian family taken to be 5856141474)
##
##
       Null deviance: 3.5574e+13 on 5390 degrees of freedom
## Residual deviance: 3.1465e+13 on 5373 degrees of freedom
## AIC: 136567
##
## Number of Fisher Scoring iterations: 2
summary(glm(Area~., data = dfImputeComplete))
##
## Call:
## glm(formula = Area ~ ., data = dfImputeComplete)
## Deviance Residuals:
##
      Min
                10
                     Median
                                  30
                                          Max
                     -10582
## -157044
           -26456
                                7388
                                     1466060
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                                    10387
                                            2.583 0.009823 **
## (Intercept)
                         26825
## Gendermale
                          7480
                                     1923
                                            3.890 0.000101 ***
                                           7.937 2.32e-15 ***
## Genderunknown
                         69397
                                     8743
## Adult
                                     3382
                                           0.394 0.693342
                          1334
## Face_Angle
                          1278
                                     1856
                                            0.689 0.491115
## Image_Color
                          5689
                                     1690
                                            3.366 0.000766 ***
                                     1720 14.167 < 2e-16 ***
## Image_Qualitygood
                         24365
## Image_Type
                          9198
                                     2589
                                           3.553 0.000383 ***
## Contextauthor
                        -24864
                                     5931 -4.192 2.79e-05 ***
## Contextcover
                         54461
                                     4412 12.343 < 2e-16 ***
## Contextfeature
                        -19259
                                     1972 -9.769 < 2e-16 ***
## Multiface
                        -24205
                                     1709 -14.165 < 2e-16 ***
## Raceasian
                          5002
                                     9890
                                           0.506 0.612993
                                     9664 -0.341 0.732875
                         -3298
## Raceblack
## Racepacificislander
                        -10332
                                    12796 -0.807 0.419425
## Raceunknown
                                    11118
                                           0.739 0.460035
                          8214
## Racewhite
                           189
                                     9186
                                            0.021 0.983585
## Smile
                          -3258
                                     1738 -1.875 0.060847 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 5917085092)
##
```

```
## Null deviance: 5.7620e+13 on 8786 degrees of freedom
## Residual deviance: 5.1887e+13 on 8769 degrees of freedom
## AIC: 222674
##
## Number of Fisher Scoring iterations: 2
```

Looking at the two models, the first with Listwise Deletion and the second with Imputed Data, the first model appears to better fit the data based on its lower AIC value. This model also has much lower deviance across the board compared to the imputed model, which is reflected in its lowered AIC. In this case, it seems to be the correct choice to use listwise deletion to remove all records with missing values instead of attempting to impute them.