IS593: Language-based Security

10. Selective X-sensitivity

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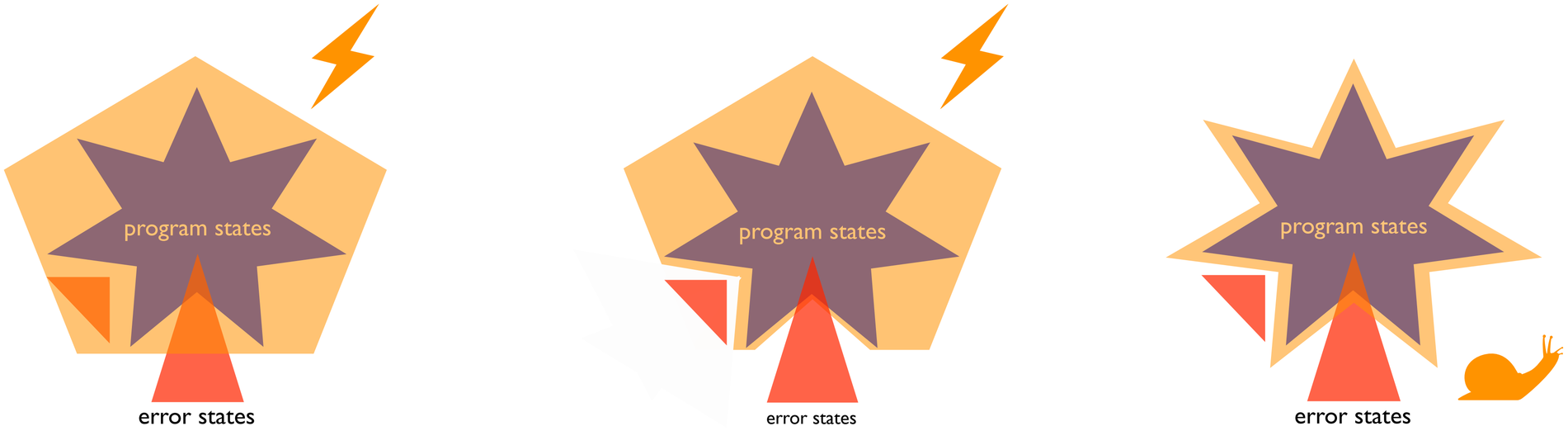
KAIST

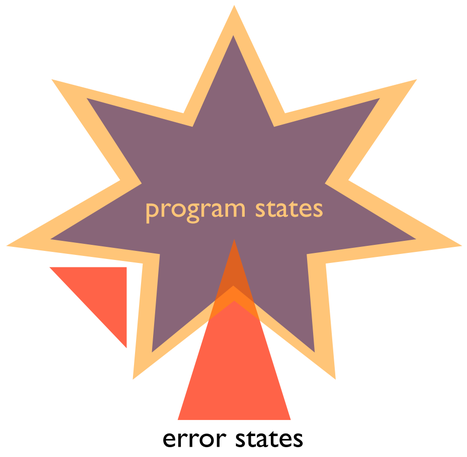
Cost-Accuracy Balance

- How to **strike a balance** between cost and accuracy?
- How to find a **minimal abstraction** to produce the **best result**?



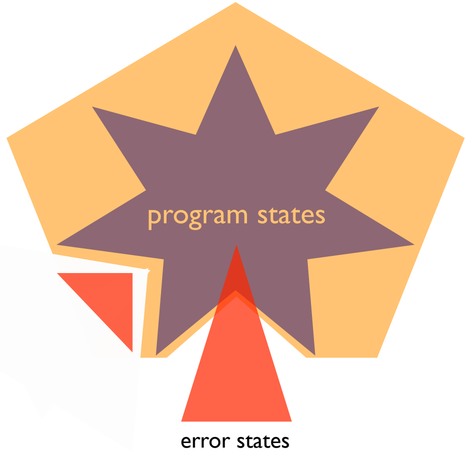
Selective X-Sensitivity

- Selectively apply a precision-improving technique X-sensitivity
  - only when/where it matters
  - X : context, flow, variable relationship, etc



Uniform (3-CFA)
False alarm 24%↓/ Overhead 1300%↑

vs
(context-sensitivity)



Selective
False alarms 24%↓/ Overhead 28%↑

*Oh et al. Selective Context-Sensitivity Guided by Impact Pre-analysis, PLDI'14

Example: Context-Sensitivity

- Suppose an analysis with the interval domain

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
5:   g();
6:   g();
   }
```

Example: Context-Sensitivity

- Context-insensitive analysis

```
   int h(n) { return n; }

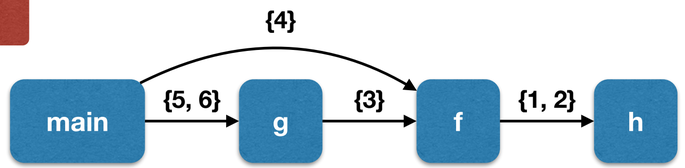
   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
5:   g();
6:   g();
   }
```

[-oo, +oo]

cannot prove



Example: Context-Sensitivity

- Uniformly context-sensitive analysis (3-CFA)

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
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   }
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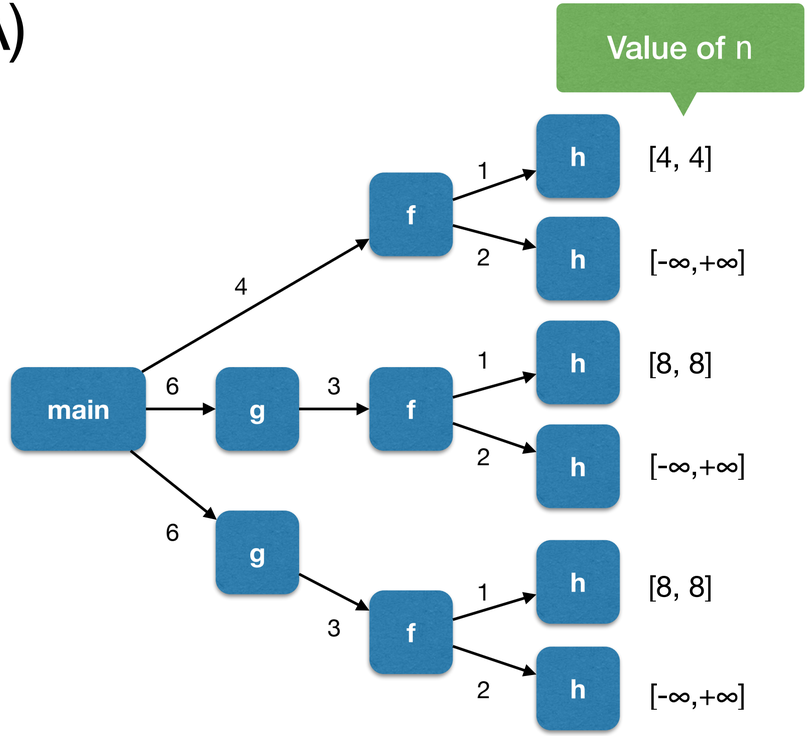


Example: Context-Sensitivity

- Uniformly context-sensitive analysis (3-CFA)

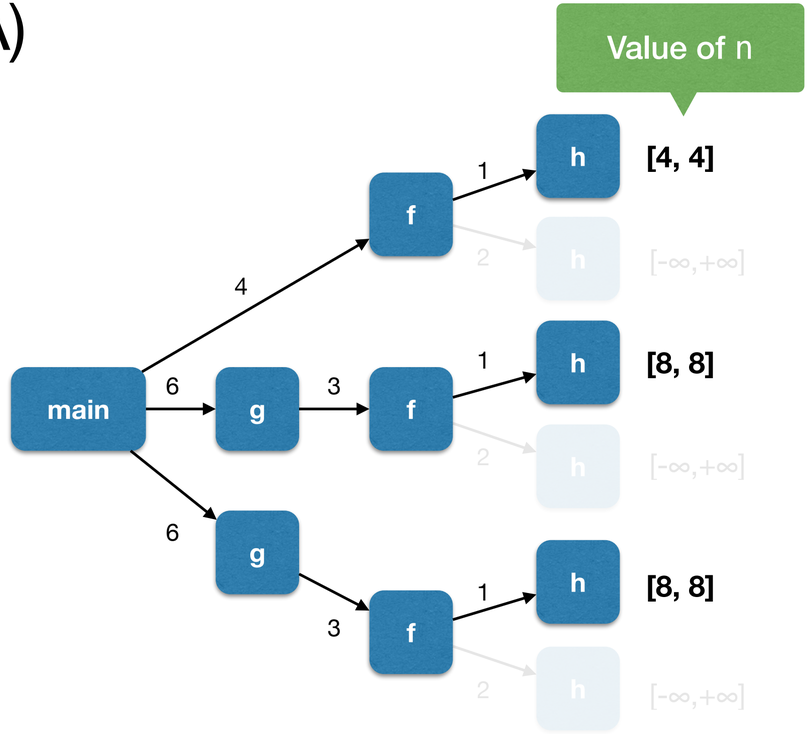
```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
5:   g();
6:   g();
   }
```

Proved!



Example: Context-Sensitivity

- Problem of uniformly sensitive analysis

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
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2:   q = h(input());
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   void main(){
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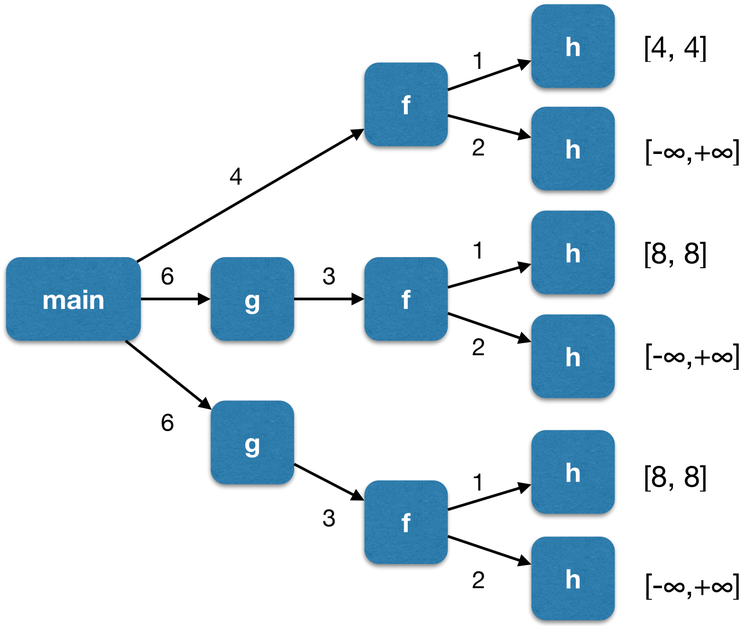

Example: Context-Sensitivity

- Problem of uniformly sensitive analysis 1: **useless** sensitivity

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
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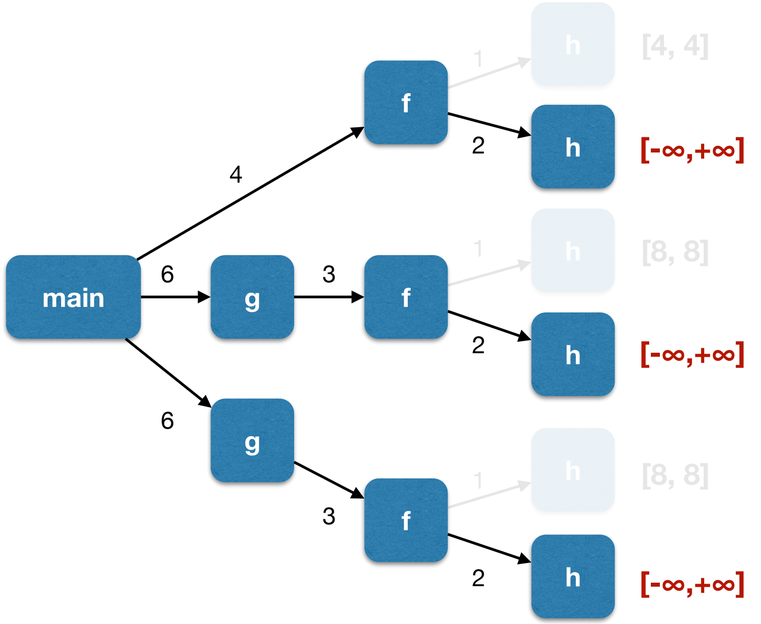
```



Example: Context-Sensitivity

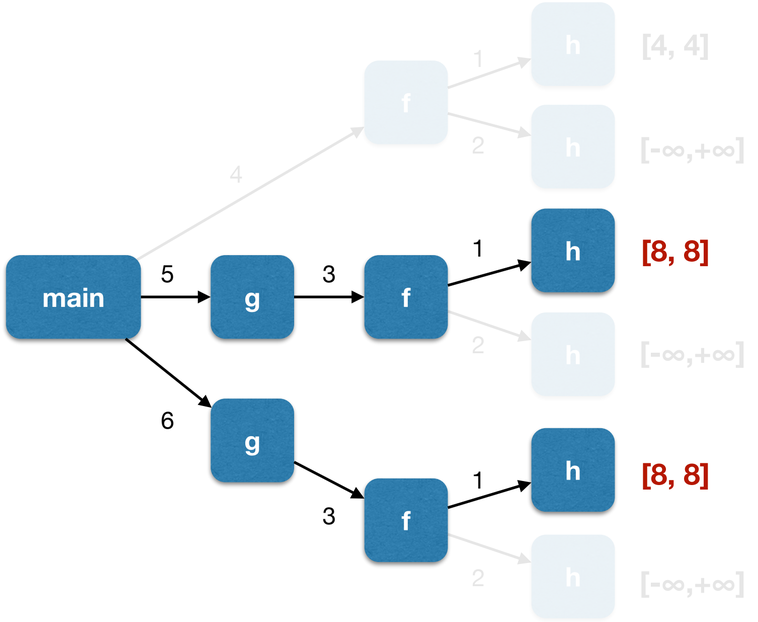
- Problem of uniformly sensitive analysis 2: **too much** sensitivity

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
5:   g();
6:   g();
   }
```



Example: Context-Sensitivity

- Solution: **selective** context-sensitive analysis

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
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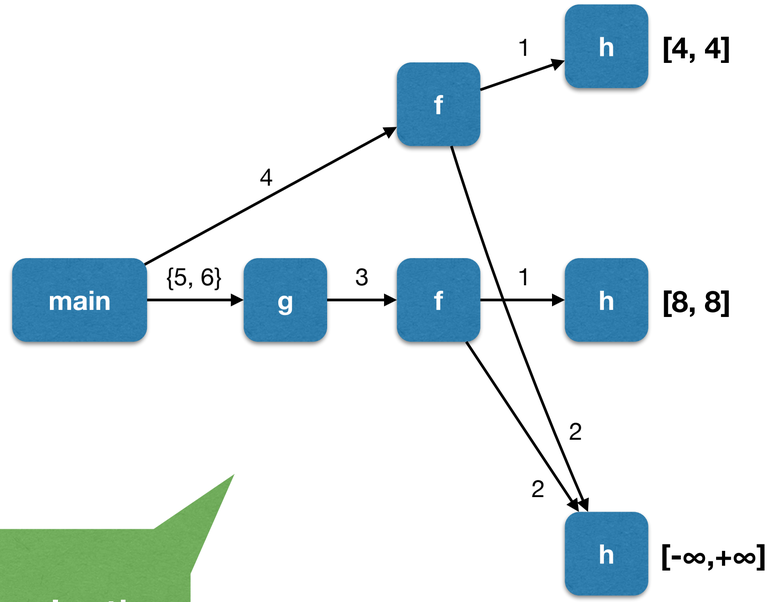
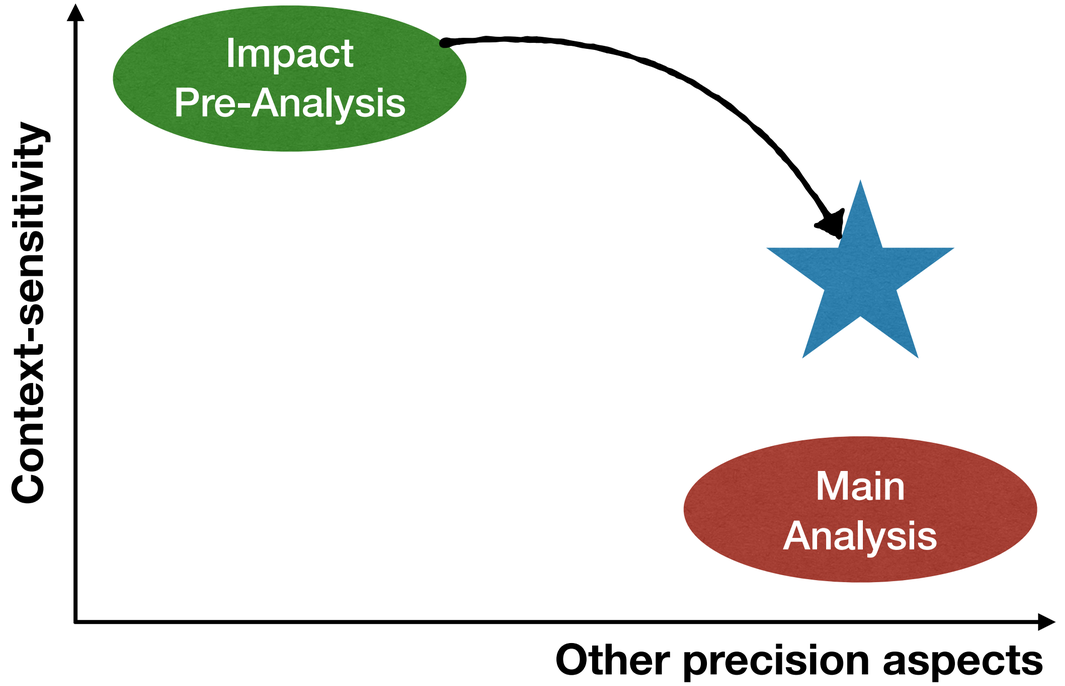


Q: How to infer this selective context-sensitivity?

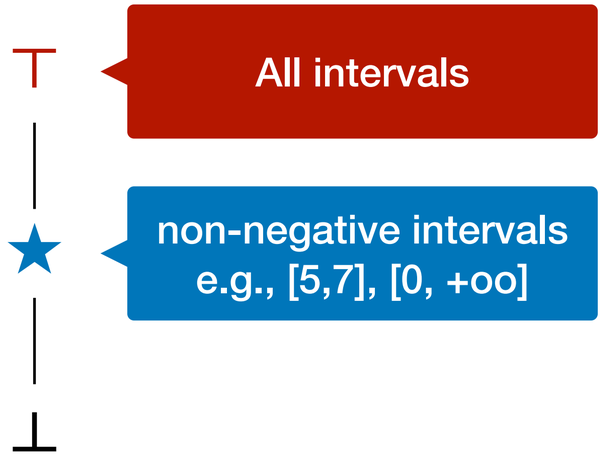
Key Idea: Impact Pre-Analysis

- Estimate the impact of X-sensitivity on main analysis
  - Fully X-sensitive, but approximated in other precision aspects



Design of Impact Pre-Analysis

- Main analysis: context-insensitive + interval domain
- Impact pre-analysis: fully context-sensitive + approximated interval domain



$$\wp(\mathbb{Z}^\sharp) \underset{\alpha}{\overset{\gamma}{\leftrightarrows}} \{\bot, \bigstar, \top\}$$

Running Impact Pre-Analysis

- Impact pre-analysis: fully context-sensitive + approximated interval domain

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
     assert(p > 1); // Q1: always true
2:   q = h(input());
     assert(q > 1); // Q2: not always true
   }

3: void g() { f(8); }

   void main(){
4:   f(4);
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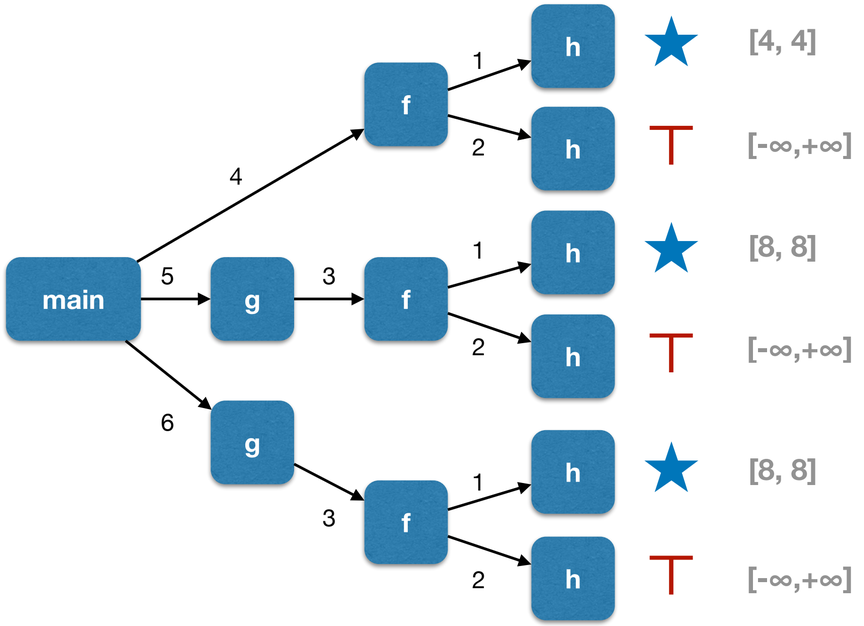

Constructing Selective Sensitivity

1. Collect queries whose expressions are assigned with ★

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
   ★ assert(p > 1); // Q1: always true
2:   q = h(input());
   ⊤ assert(q > 1); // Q2: not always true
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3: void g() { f(8); }

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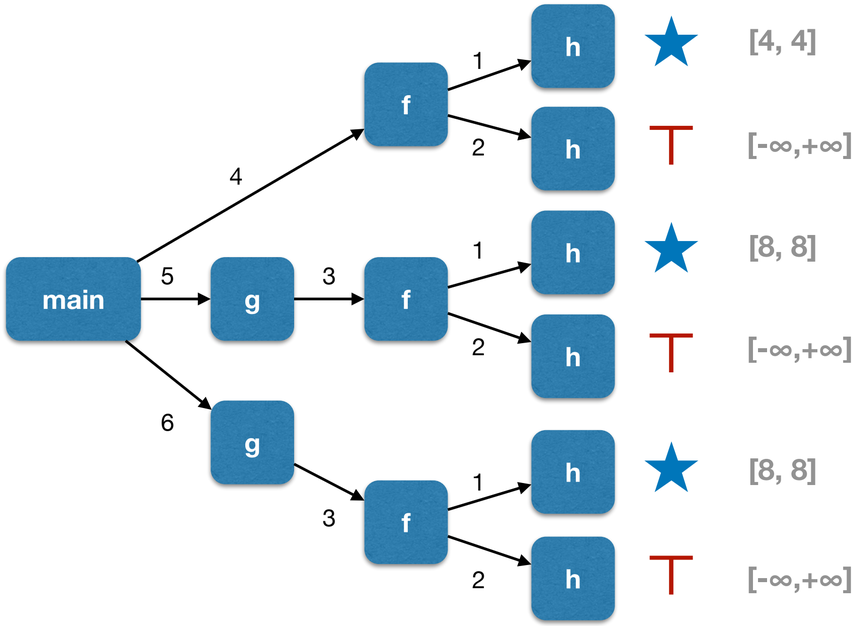

Constructing Selective Sensitivity

2. Find contexts that contribute to the selected queries

```
   int h(n) { return n; }

   void f(s) {
1:   p = h(s);
   ★ assert(p > 1); // Q1: always true
2:   q = h(input());
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   void main(){
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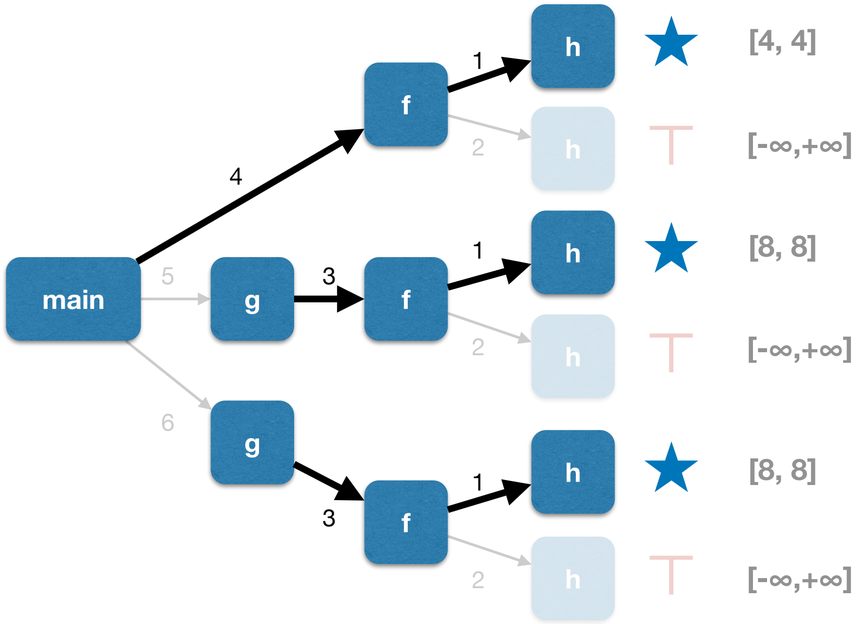


Selected contexts for function h: {4·1, 3·1}

Generality

- The same principle is applicable to other types of sensitivity

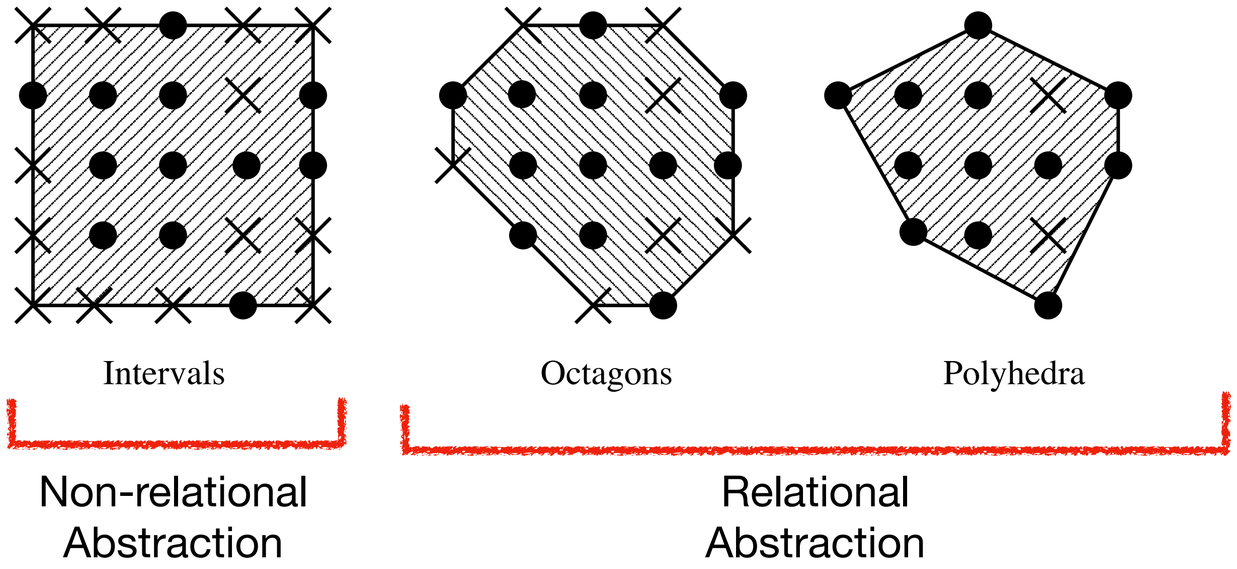
  1. Running an impact pre-analysis
     (full X-sensitivity + aggressive abstraction of other aspects)

  2. Select queries that are judged promising by the pre-analysis

  3. Construct X-sensitivity that contributes to the selected queries

Example: Relational Analysis

- Keep track of relationships between variables in a certain form
  - E.g., octagon analysis: $(\pm x) - (\pm y) \leq c$



*A. Mine, The Octagon Abstract Domain, HOSC'06

Example: Relational Analysis

- Non-relational analysis with the interval domain

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();           // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);           // Q1: always true
5:   assert(i < c);           // Q2: not always true
6: }
```

Var	Val
a	[-oo, +oo]
b	[-oo, +oo]
c	[-oo, +oo]
i	[0, +oo]

Example: Relational Analysis

- Fully relational analysis with the octagon domain: $(\pm x) - (\pm y) \leq c$

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();           // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);           // Q1: always true
5:   assert(i < c);           // Q2: not always true
6: }
```

	a	b	c	i
a	0	∞	∞	∞
b	∞	0	∞	∞
c	∞	∞	0	∞
i	∞	∞	∞	0

{a, b, c, i}

*Consider x - y ≤ c only, for simplicity

Example: Relational Analysis

- Fully relational analysis with the octagon domain: $(\pm x) - (\pm y) \leq c$

```
// b = [-oo, +oo]
1: int a = b;
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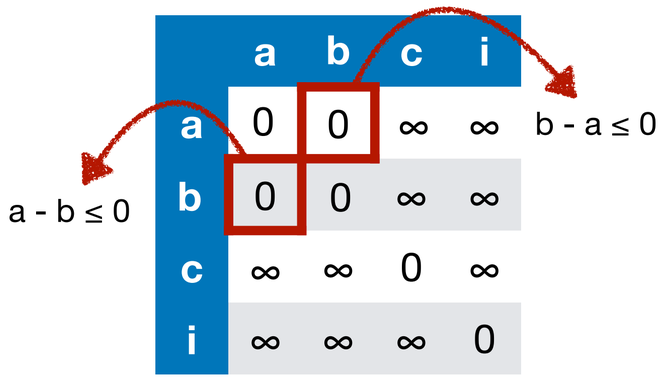

{a, b, c, i}

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Example: Relational Analysis

- Fully relational analysis with the octagon domain: $(\pm x) - (\pm y) \leq c$

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// b = [-oo, +oo]
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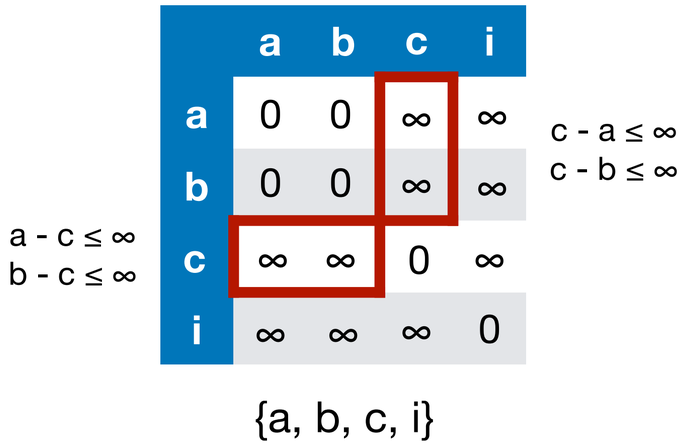

	a	b	c	i
a	0	0	∞	∞
b	0	0	∞	∞
c	∞	∞	0	∞
i	∞	∞	∞	0

{a, b, c, i}

*Consider x - y ≤ c only, for simplicity

Example: Relational Analysis

- Fully relational analysis with the octagon domain: $(\pm x) - (\pm y) \leq c$

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();            // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);            // Q1: always true
5:   assert(i < c);            // Q2: not always true
6: }
```

	a	b	c	i
a	0	0	∞	∞
b	0	0	∞	-1
c	∞	∞	0	∞
i	∞	∞	∞	0

i - b ≤ -1

{a, b, c, i}

*Consider x - y ≤ c only, for simplicity

Example: Relational Analysis

- Fully relational analysis with the octagon domain: $(\pm x) - (\pm y) \leq c$

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();              // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);              // Q1: always true
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6: }
```

	a	b	c	i
a	0	0	∞	-1
b	0	0	∞	-1
c	∞	∞	0	∞
i	∞	∞	∞	0

{a, b, c, i}

b - a ≤ 0
∧ i - b ≤ -1
⇒ i - a ≤ -1

*Consider x - y ≤ c only, for simplicity

Example: Relational Analysis

- Problem of fully relational analysis: **useless** relationship

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();           // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);           // Q1: always true
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6: }
```

	a	b	c	i
a	0	0	∞	-1
b	0	0	∞	-1
c	∞	∞	0	∞
i	∞	∞	∞	0

{a, b, ~~c~~, i}

*Consider x - y ≤ c only, for simplicity

Example: Relational Analysis

- Solution: **selective** relational analysis

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();            // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);            // Q1: always true
5:   assert(i < c);            // Q2: not always true
6: }
```

	a	b	i
a	0	0	-1
b	0	0	-1
i	∞	∞	0

{a, b, i}

+

Var	Val
c	[-oo, +oo]

{c}

*Consider x - y ≤ c only, for simplicity

Design of Impact Pre-Analysis

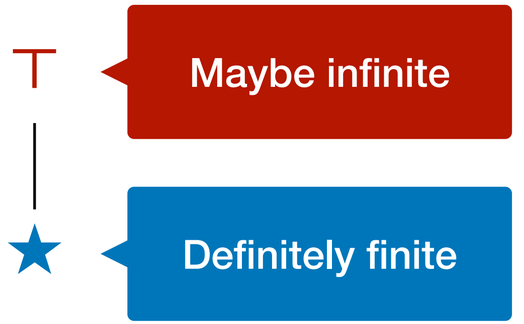
- Main analysis: non-relational analysis
- Impact pre-analysis: fully relational analysis + approximated upper bound

	a	b	c	i
a	0	0	∞	-1
b	0	0	∞	-1
c	∞	∞	0	∞
i	∞	∞	∞	0

Fully relational octagon analysis

	a	b	c	i
a	★	★	⊤	★
b	★	★	⊤	★
c	⊤	⊤	★	⊤
i	⊤	⊤	⊤	★

Fully relational impact pre-analysis



Constructing Selective Sensitivity

1. Collect queries whose expressions are assigned with ★

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();              // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a);  ★           // Q1: always true
5:   assert(i < c);  ⊤           // Q2: not always true
6: }
```

	a	b	c	i
a	★	★	⊤	★
b	★	★	⊤	★
c	⊤	⊤	★	⊤
i	⊤	⊤	⊤	★

Constructing Selective Sensitivity

2. Find variable relationships that contribute to the selected queries

```
// b = [-oo, +oo]
1: int a = b;
2: int c = input();              // User input
3: for (i = 0; i < b; i++) {
4:   assert(i < a); ★           // Q1: always true
5:   assert(i < c); ⊤           // Q2: not always true
6: }
```

	a	b	c	i
a	★	★	⊤	★
b	★	★	⊤	★
c	⊤	⊤	★	⊤
i	⊤	⊤	⊤	★

Selected variables: {a, b, i}

Summary

- Selective X-sensitivity: a framework for balancing between **cost & accuracy**
- Key idea: **“Apply X-sensitivity only when it matters”**
- Estimate the impact of X using the **impact pre-analysis**
  - Full X-sensitivity + aggressive approximation of other precision aspects
- Construct selective X-sensitivity from the guidance of the impact estimation