Babble: learning better abstractions with egraphs and anti-unification

david cao et al. (POPL 2023)

Presented by JS. Kwon

```
int Max(int X, int Y) {
  if (X > Y)
    return X;
  else
    return Y;
}
int main() {
  return Max(3, 8);
}
```

User-defined Function 1

User-defined Function ¹





#include <algorithm.h>
int main() {
 return Max(3, 8);
}

User-defined Function 1







```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = Y + 1;

return tmp1 + tmp2 + 1;
}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 1;
}
```

Program 2

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = Y + 1;

return tmp1 + tmp2 + 1;
}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 1;
}
```

Program 2

Library:

```
int add_1(int X) {
  return X + 1;
}
```

Library Learning



```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = Y + 1;

return tmp1 + tmp2 + 1;
}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 1;
}
```

Program 2

Library:

```
int add_1(int X) {
  return X + 1;
}
```

Refactored Programs:

```
int foo1(int X, int Y) {
  return add_1(add_1(X) add_1(Y);
}
```

Program 1'

```
int foo2(int X, int Y) {
  return add_1(X) + add_1(Y);
}
```

Program 2'

Library Learning



• Automatically extract common functionality into libraries

Abstract common functionality to express their intent more clearly and concisely

Challenge 1: Precise candidate generation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = Y + 1;

return tmp1 + tmp2 + 2;
}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 2;
}
```

Challenge 1: Precise candidate generation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
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}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 2;
}
```

Program 2

```
Candidate Generation
```

```
int foo(int X, int Y) {
  return X + Y;
}
```

Candidate 1

```
int foo(int X) {
  return X + 1;
}
```

Candidate 2

```
int foo(int X) {
  return X + 2;
}
```

Candidate 3

Challenge 1: Precise candidate generation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = Y + 1;

return tmp1 + tmp2 + 2;
}
```

Program 1

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;

return tmp1 + Y + 2;
}
```

Program 2

```
Candidate Generation

Candidate Generation
```

int foo(int X) {
 return X + 1;
}

Candidate 2

int foo(int X, int Y) {

return X + Y;

```
int foo(int X) {
  return X + 2;
}
```

Challenge 2: Robust to superficial variation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

Program 1

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

Challenge 2: Robust to superficial variation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

Program 1

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

Program 2

Library:

```
int add_1(int X) {
  return X + 1;
}
```

Library Learning



Challenge 2: Robust to superficial variation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

Program 1

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

Program 2

Library:

```
int add_1(int X) {
  return X + 1;
}
```

Library Learning



Refactored Programs:

```
int foo1(int X, int Y) {
  return add_1(add_1(X));
}
```

Program 1'

Challenge 2: Robust to superficial variation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

Program 1

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
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}
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Library:

```
int add_1(int X) {
  return X + 1;
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Library Learning



Refactored Programs:

```
int foo1(int X, int Y) {
  return add_1(add_1(X));
}
```

Program 1'

```
int foo2(int X, int Y) {
  return 1 + add_1(X);
}
```

Program 2'

Solution: Library Learning Modulo Theories (LLMT)

- Precise Candidate Generation via Anti-Unification
 - Useful abstractions must be used at least twice
 - Abstractions should be "as concrete as possible"

Solution: Library Learning Modulo Theories (LLMT)

- Precise Candidate Generation via Anti-Unification
 - Useful abstractions must be used at least twice
 - Abstractions should be "as concrete as possible"

- Robustness via E-Graphs
 - use domain-specific equational theory, find programs that are semantically equivalent

Program Corpus

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

Step1: Equality Saturation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

$$X + Y \equiv Y + X$$

domain-specific equational theory

Step1: Equality Saturation

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

$$X + Y \equiv Y + X$$

domain-specific equational theory

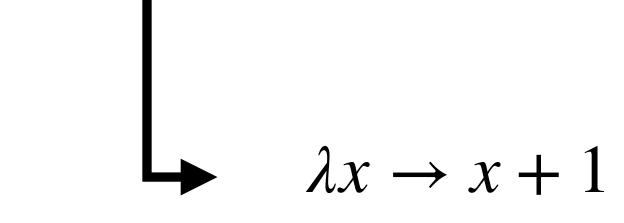
```
int foo3(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

Step2: Anti-Unification (Candidate Generation)

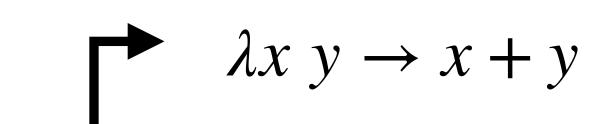
```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

```
int foo3(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```



matched to corpus at least twice



Candidates

Step3: Select Optimal Library

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

```
int foo3(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```



(Cost: 1, requires one arguments)

(Cost: 2, requires two arguments) $\lambda x \nu \rightarrow x + \nu$

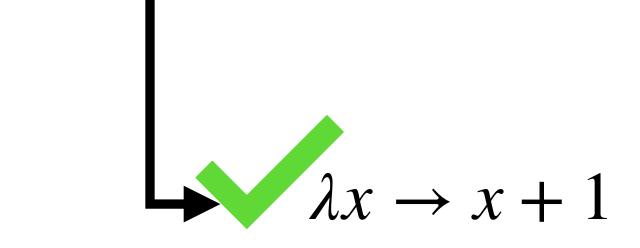
Candidates

Step3: Select Optimal Library

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = 1 + tmp1;
  return tmp2;
}
```

```
int foo3(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```



(Cost: 1, requires one arguments)

(Cost: 2, requires two arguments) $\lambda x y \rightarrow x + y$

Candidates

Library:

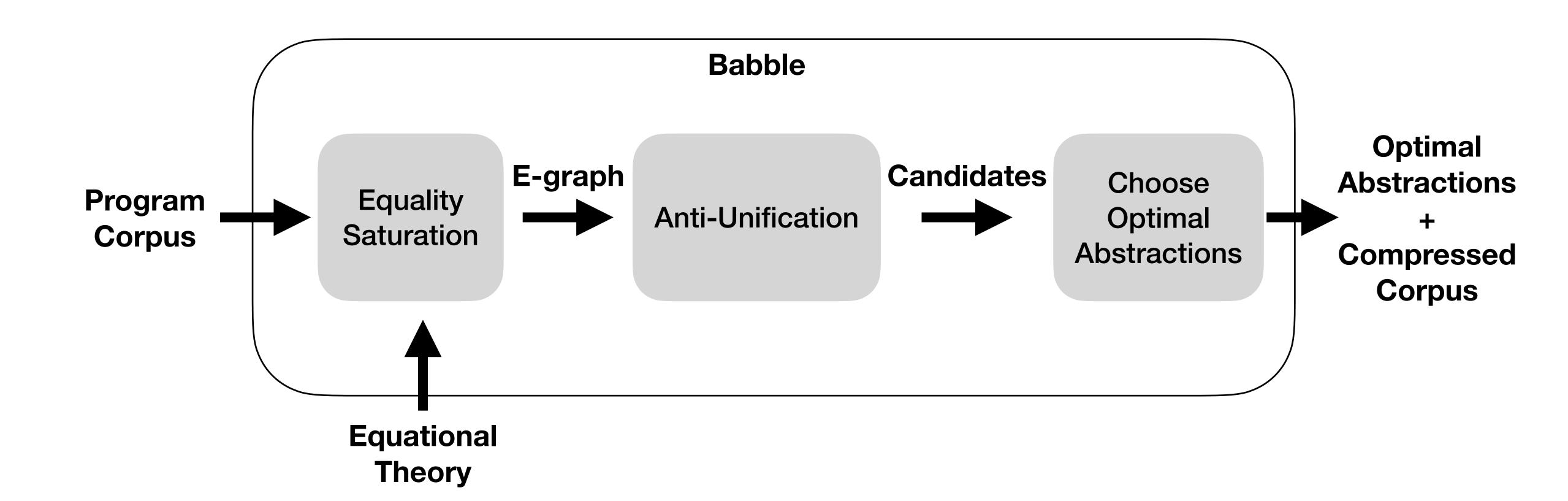
```
int add_1(int X) {
  return X + 1;
}
```

Compressed Corpus:

```
int foo1(int X, int Y) {
  return add_1(add_1(X));
}
```

```
int foo3(int X, int Y) {
  return add_1(add_1(X));
}
```

Babble: Overall Process



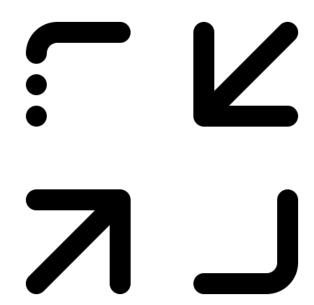
Appealing Result

Low Cost

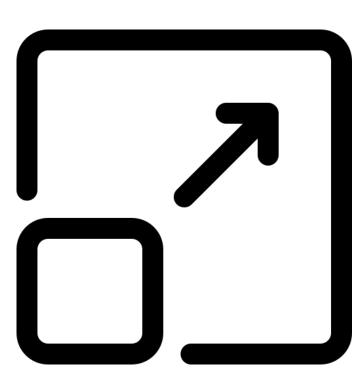


10x faster

Performance



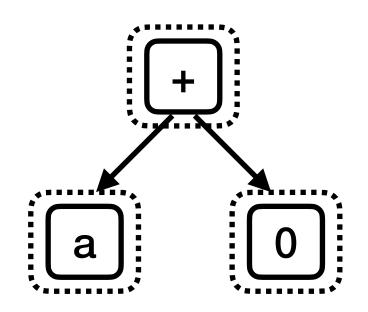
30% better Compression Ratio **Scalability**



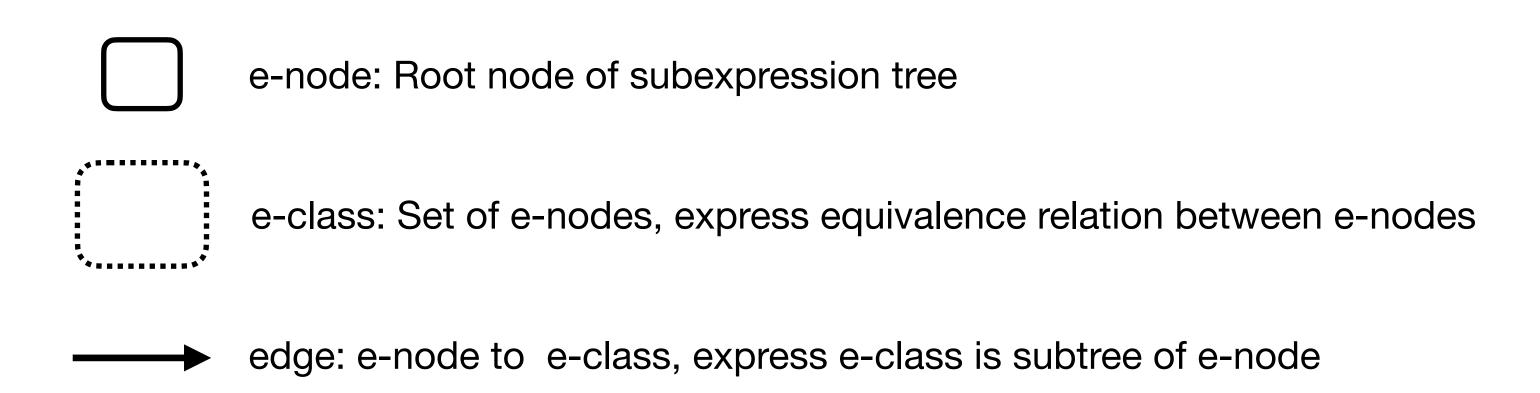
Can support 42,936 AST size input

Technical Details: How E-graphs works?

E-graphs

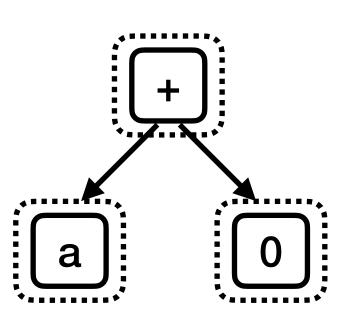


a + 0 expressed in e-graph

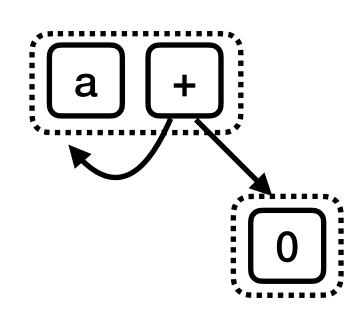


Technical Details: How E-graphs works?

E-graphs



$$X + 0 \equiv X$$



a + 0 expressed in e-graph

$$= a + 0 + 0$$

= $a + 0$
a

- e-node: Root node of subexpression tree
- e-class: Set of e-nodes, express equivalence relation between e-nodes
- edge: e-node to e-class, express e-class is subtree of e-node



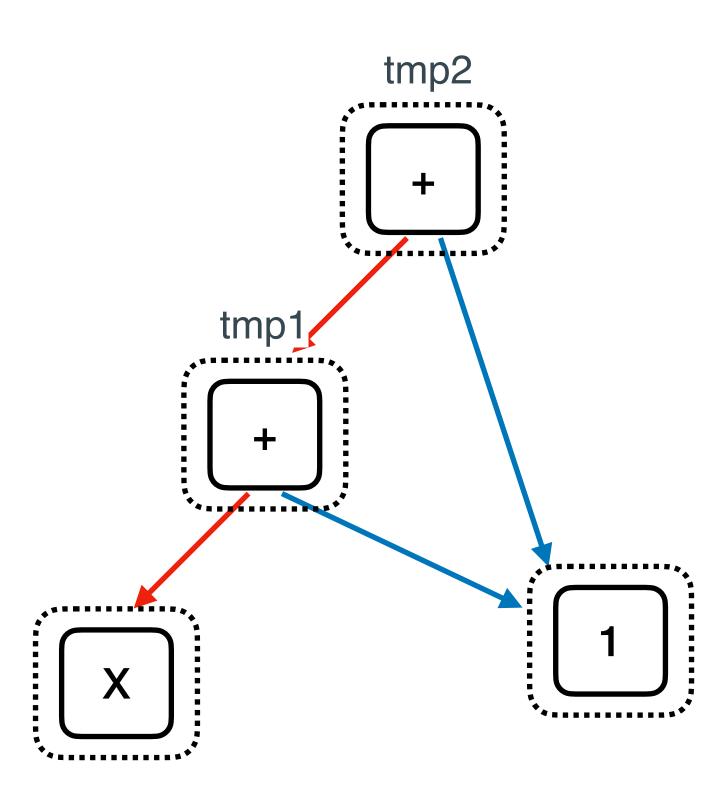
Operand 1

Operand 2

E-graph in Babble

Build E-Graph

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```



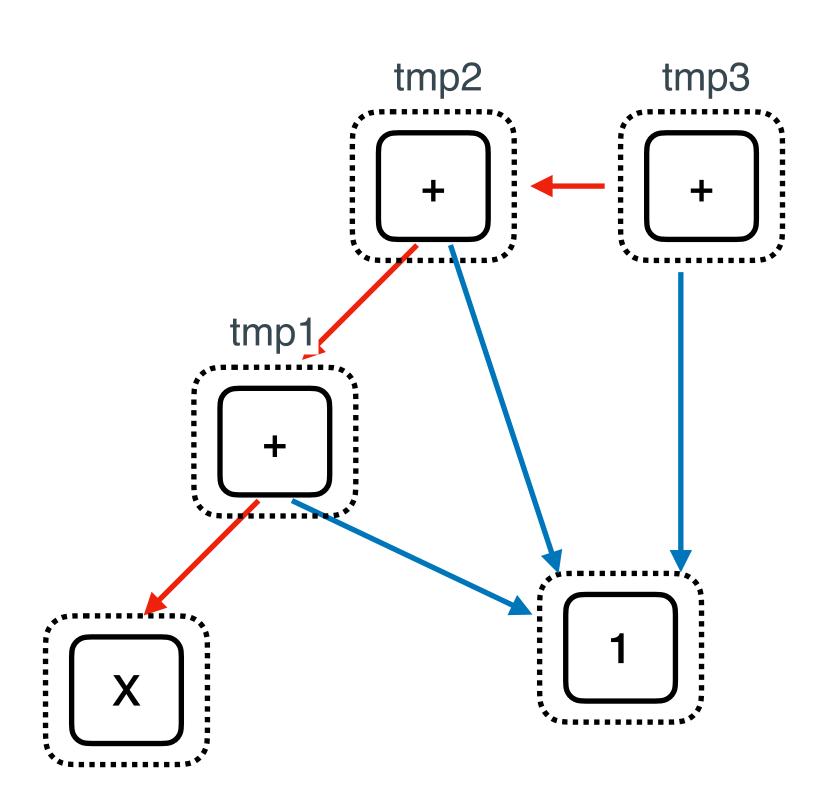
Operand 1Operand 2

E-graph in Babble

Build E-Graph

```
int foo1(int X, int Y) {
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  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  int tmp3 = tmp2 + 1;
  return tmp3;
}
```



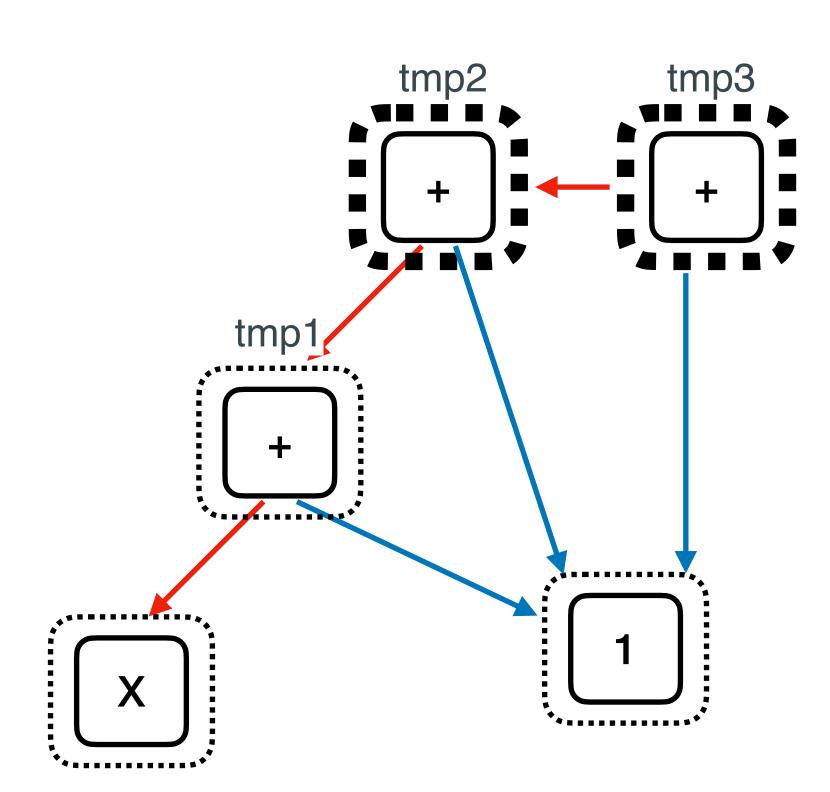


E-graph in Babble

- Generate Candidates
 - Pick two e-classes

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  int tmp3 = tmp2 + 1;
  return tmp3;
}
```



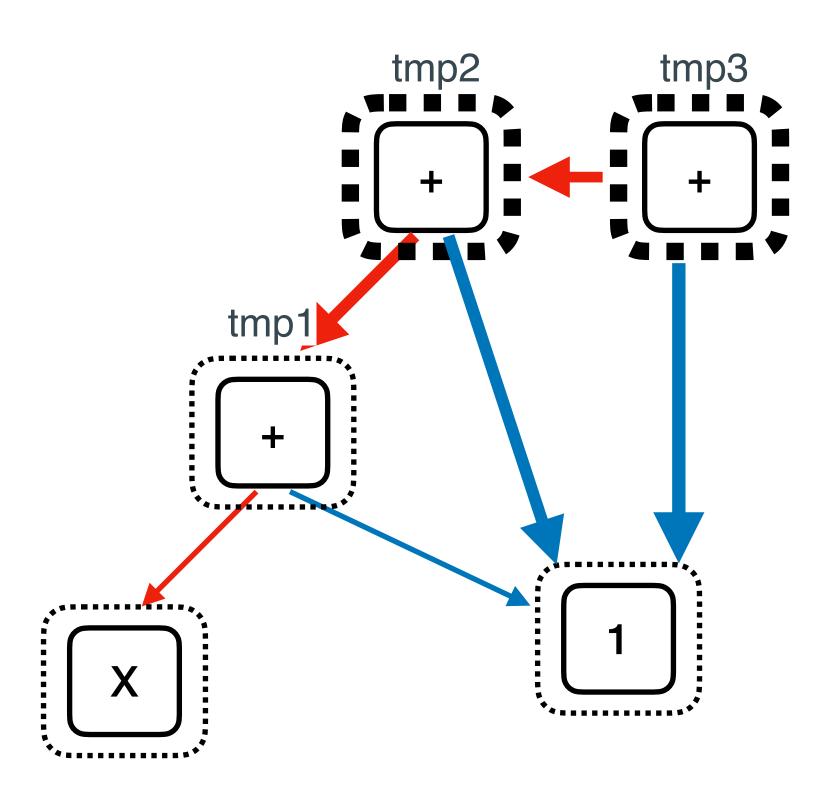
Operand 1Operand 2

E-graph in Babble

- Generate Candidates
 - Pick two e-classes
 - matching

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
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  return tmp3;
}
```



?? + 1 is common

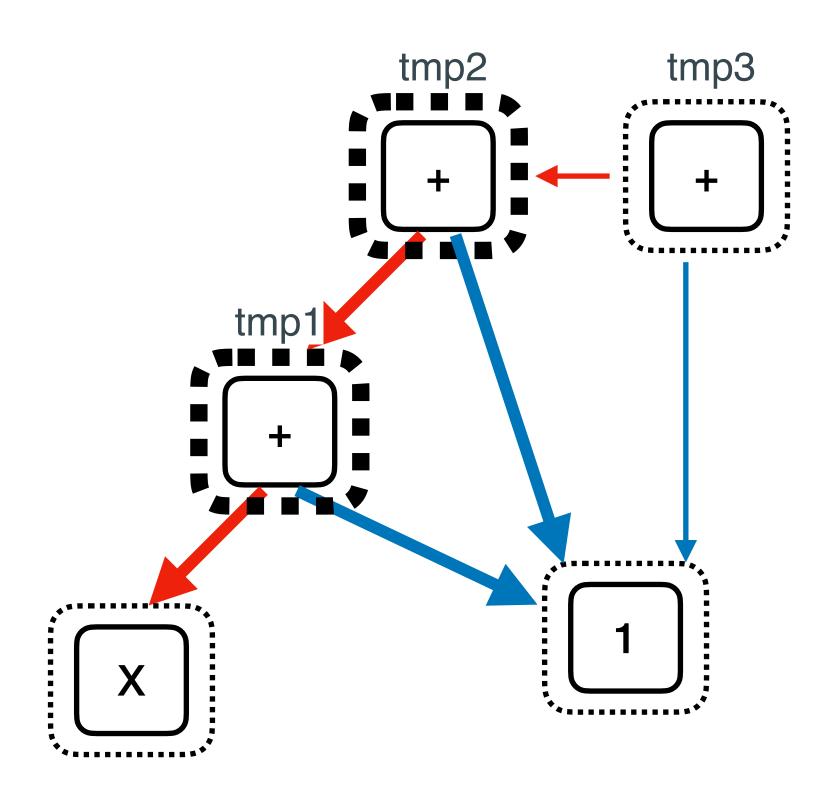


E-graph in Babble

- Generate Candidates
 - Pick two e-classes
 - matching
 - repeat

```
int foo1(int X, int Y) {
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```

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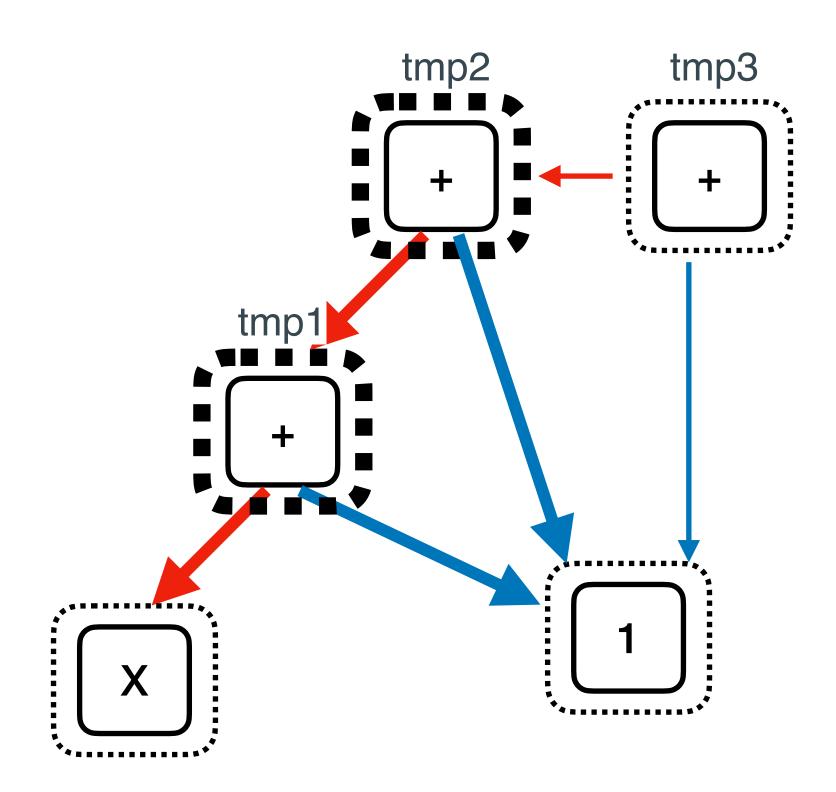


E-graph in Babble

- Generate Candidates
 - Pick two e-classes
 - matching
 - repeat

```
int foo1(int X, int Y) {
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```



?? + 1 is common

$$\lambda x \rightarrow x + 1$$



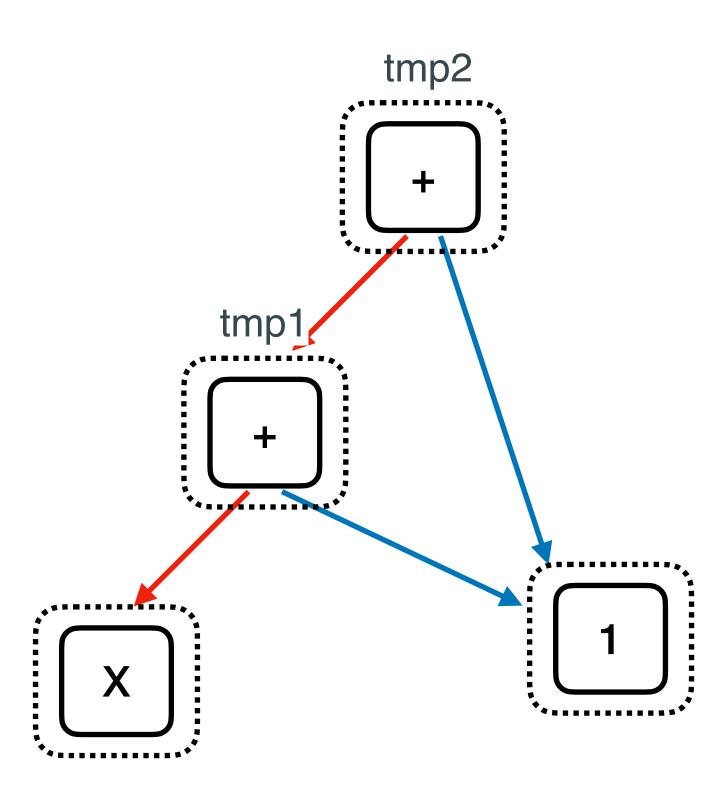
Operand 1

Operand 2

E-graph in Babble

Build E-Graph

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
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}
```





Operand 1

Operand 2

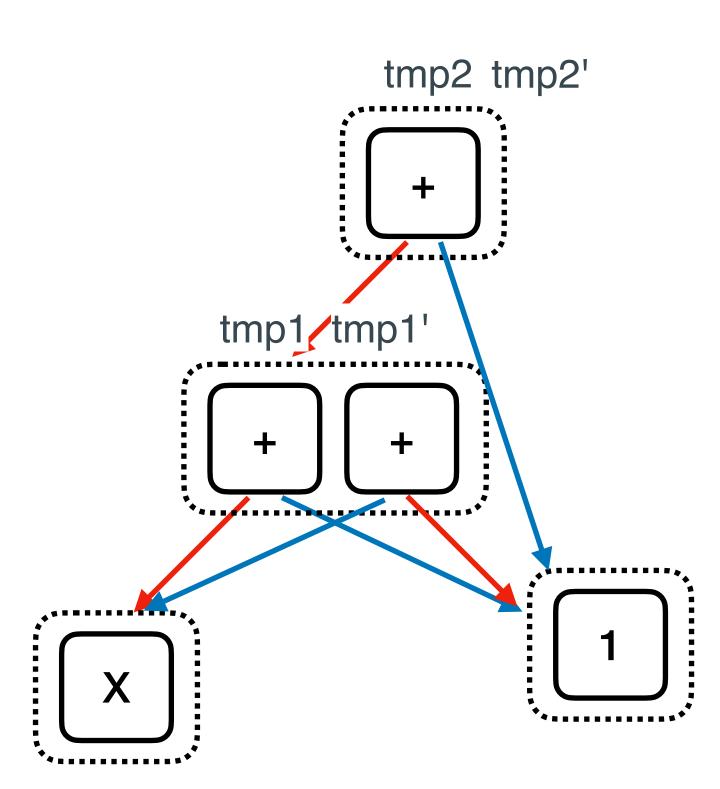
E-graph in Babble

Build E-Graph

```
X+Y\equiv Y+X domain-specific equational theory
```

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1' = 1 + X;
  int tmp2' = tmp1' + 1;
  return tmp2';
}
```





Operand 1

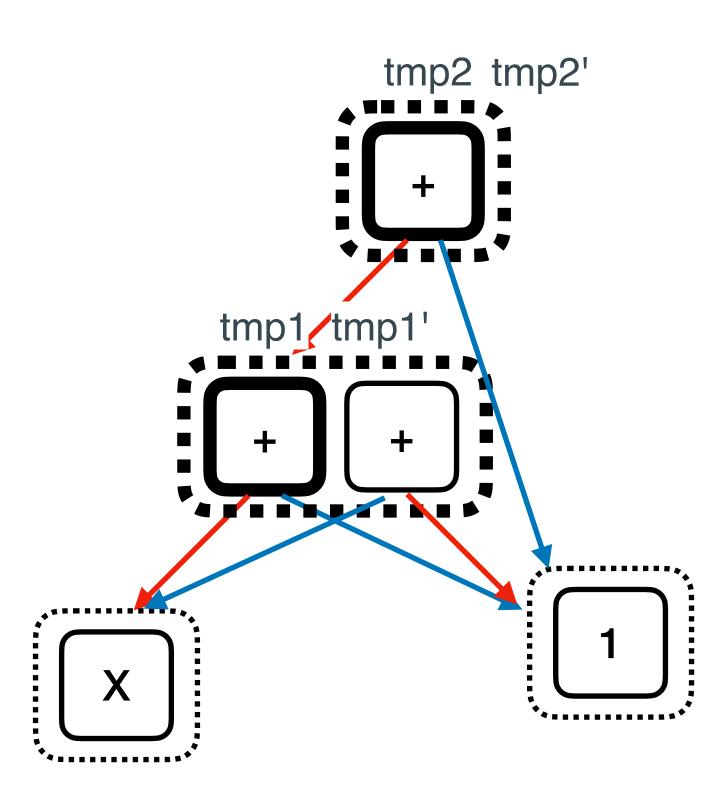
Operand 2

E-graph in Babble

- Generate Candidate
 - Pick two e-classes

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

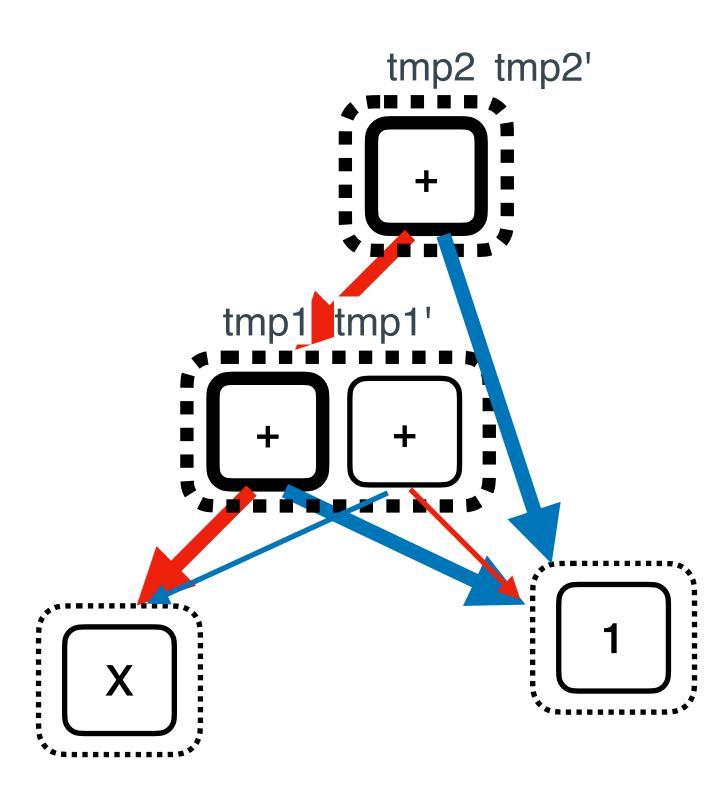
```
int foo2(int X, int Y) {
  int tmp1' = 1 + X;
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  return tmp2';
}
```



- Generate Candidate
 - Pick two e-classes
 - matching

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
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  return tmp2';
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Operand 1

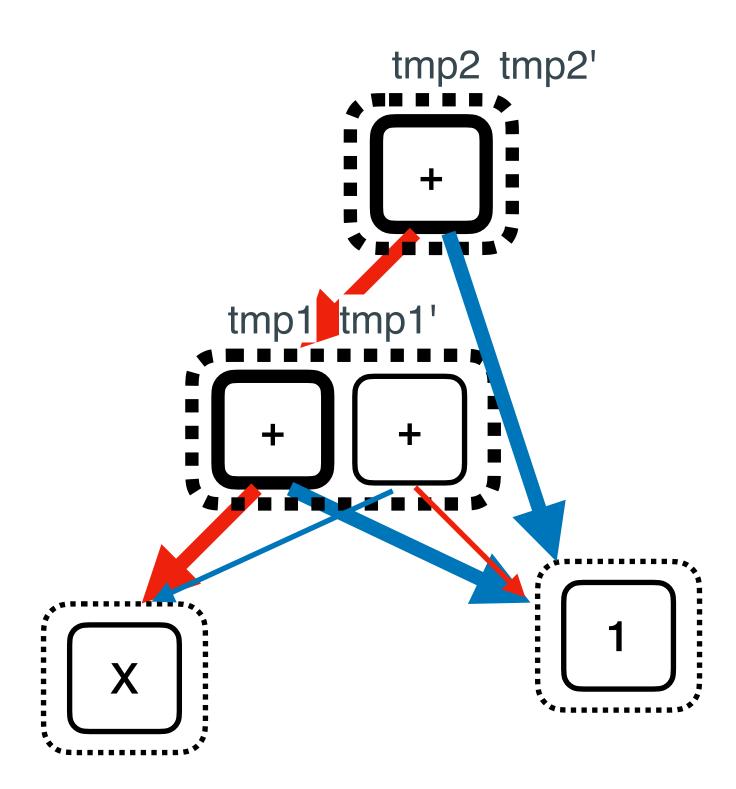


E-graph in Babble

- Generate Candidate
 - Pick two e-classes
 - matching

```
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?? + 1 is common

$$\lambda x \rightarrow x + 1$$



Operand 1

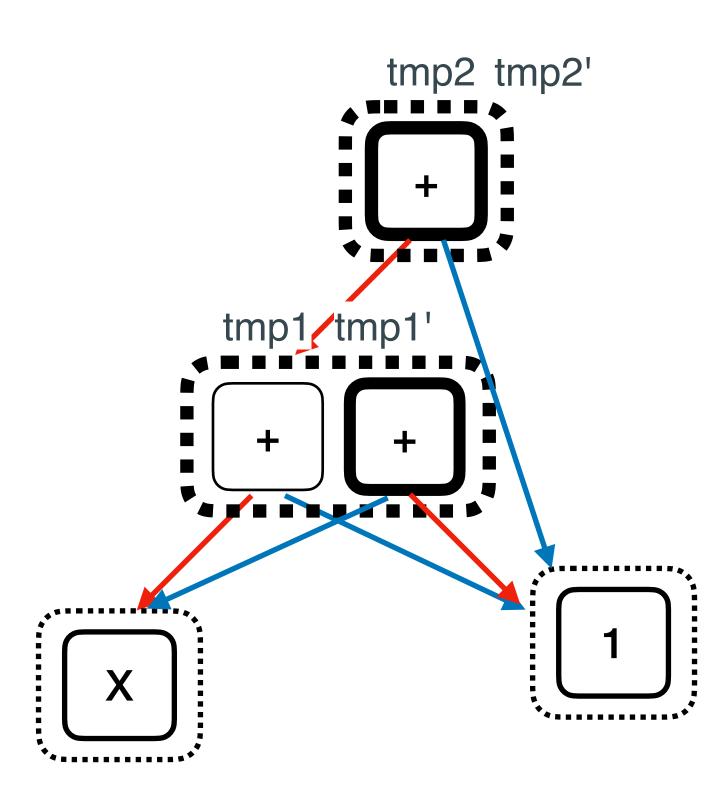
Operand 2

E-graph in Babble

- Generate Candidate
 - Pick two e-classes
 - matching
 - repeat

```
int foo1(int X, int Y) {
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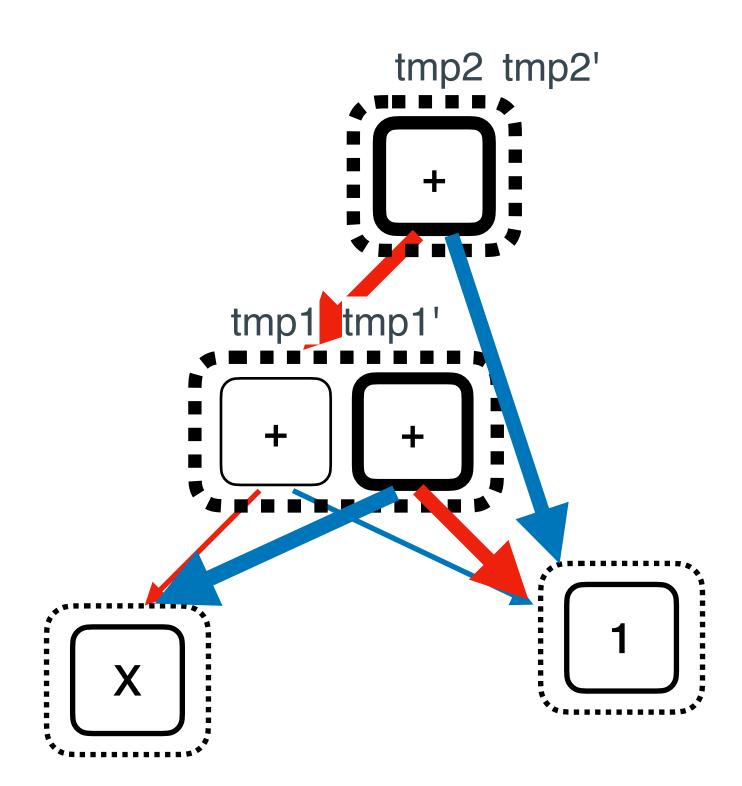




- Generate Candidate
 - Pick two e-classes
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```
int foo1(int X, int Y) {
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int foo2(int X, int Y) {
  int tmp1' = 1 + X;
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}
```



$$\lambda x y \rightarrow x + y$$

Choose Optimal Abstraction

2 Candidates

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

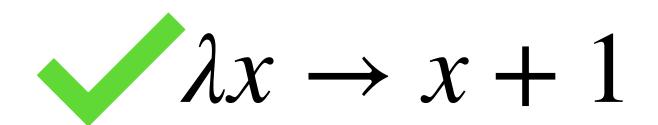
$$\lambda x \rightarrow x + 1$$

$$\lambda x y \rightarrow x + y$$

Choose Optimal Abstraction

2 Candidates

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```



$$\lambda x y \rightarrow x + y$$

(Cost: 1, requires one arguments) (Cost: 2, requires two arguments)

Compress

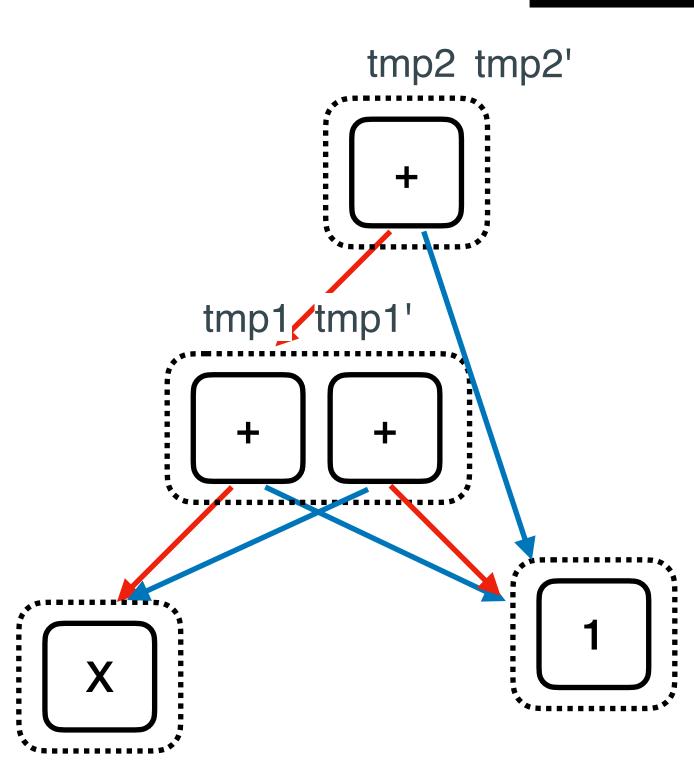
```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1' = 1 + X;
  int tmp2' = tmp1' + 1;
  return tmp2';
}
```

Library:

$$\lambda x \rightarrow x + 1$$

```
int add_1(int X) {
  return X + 1;
}
```



Compress

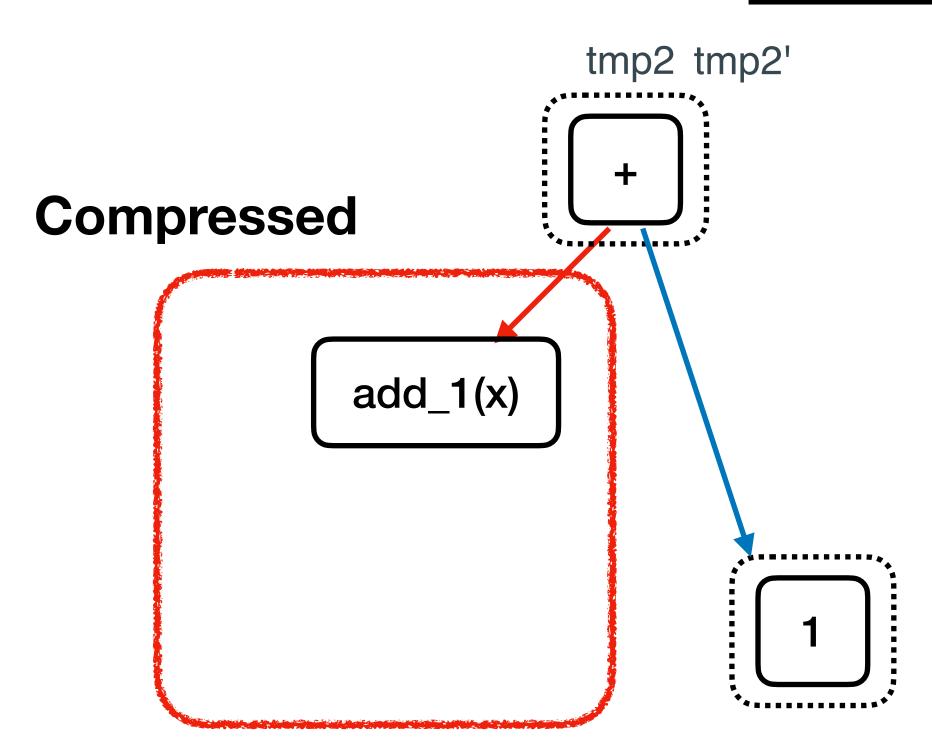
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int foo1(int X, int Y) {
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int foo2(int X, int Y) {
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```

Library:

```
\lambda x \rightarrow x + 1
```

```
int add_1(int X) {
  return X + 1;
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```



Compress

```
int foo1(int X, int Y) {
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Library:

```
int add_1(int X) {
  return X + 1;
}
```

```
Compressed
```

 $\lambda x \rightarrow x + 1$

Library:

E-graph in Babble

Compress

```
\lambda x \rightarrow x + 1
```

```
int add_1(int X) {
  return X + 1;
}
```

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp1' = 1 + X;
  int tmp2' = tmp1' + 1;
  return tmp2';
}
```

Compressed result

Compressed Corpus:

```
int foo1(int X, int Y) {
  return add_1(add_1(X));
}
```

```
int foo2(int X, int Y) {
  return add_1(add_1(X));
}
```

Evaluation: Set-up

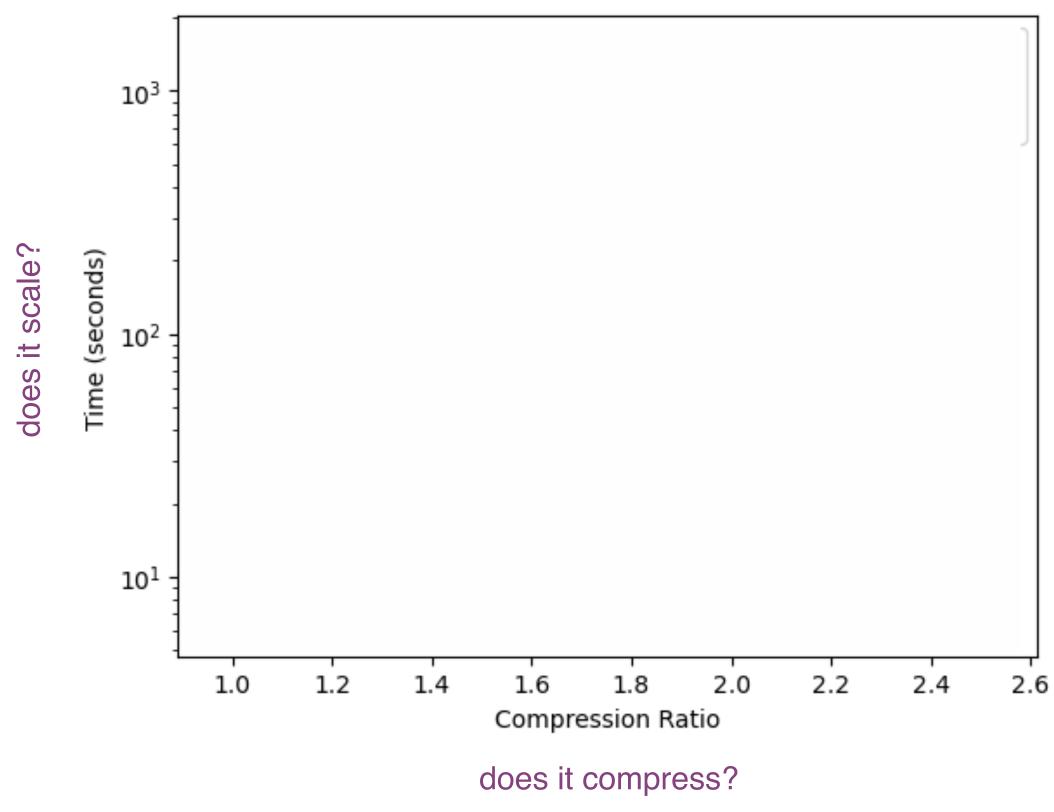
- Baseline: DreamCoder (SOTA)
- RQs
 - RQ1: Can Babble compress programs better than SOTA?
 - RQ2: Main technique is important to the performance?

- Baseline: DreamCoder (SOTA), BabbleSyn (Babble without Equality Thoery)
- Benchmarks: List domain

```
Sum List
[1 2 3] -> 6
[4 6 8 1] -> 17

Double
[1 2 3] -> [2 4 6]
[4 5 1] -> [8 10 2]

Check Evens
[0 2 3] -> [T T F]
[2 9 6] -> [T F T]
```

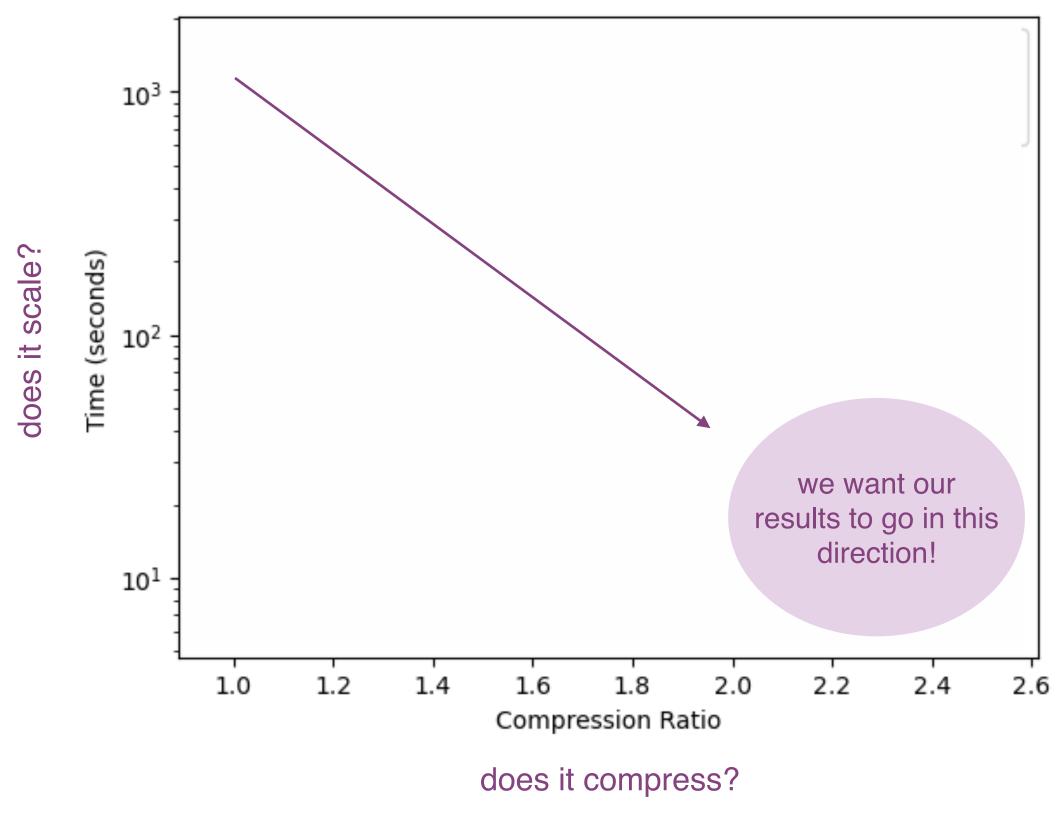


- Baseline: DreamCoder (SOTA), BabbleSyn (Babble without Equality Thoery)
- Benchmarks: List domain

```
Sum List
[1 2 3] -> 6
[4 6 8 1] -> 17

Double
[1 2 3] -> [2 4 6]
[4 5 1] -> [8 10 2]

Check Evens
[0 2 3] -> [T T F]
[2 9 6] -> [T F T]
...
```

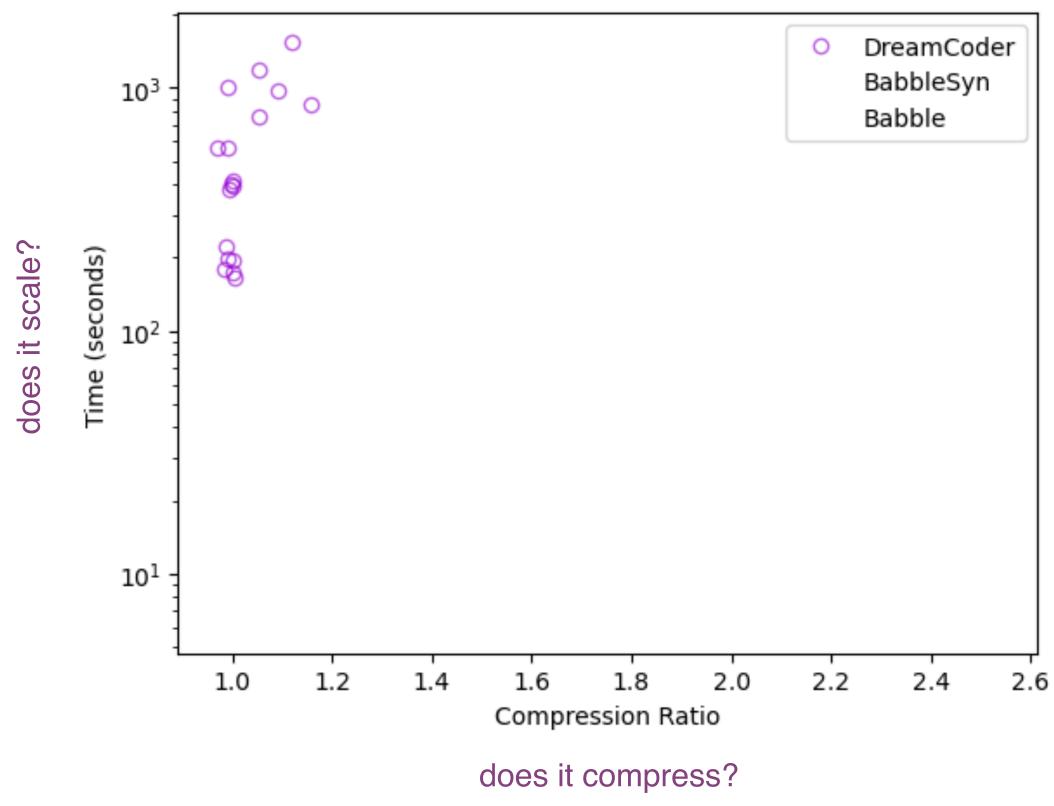


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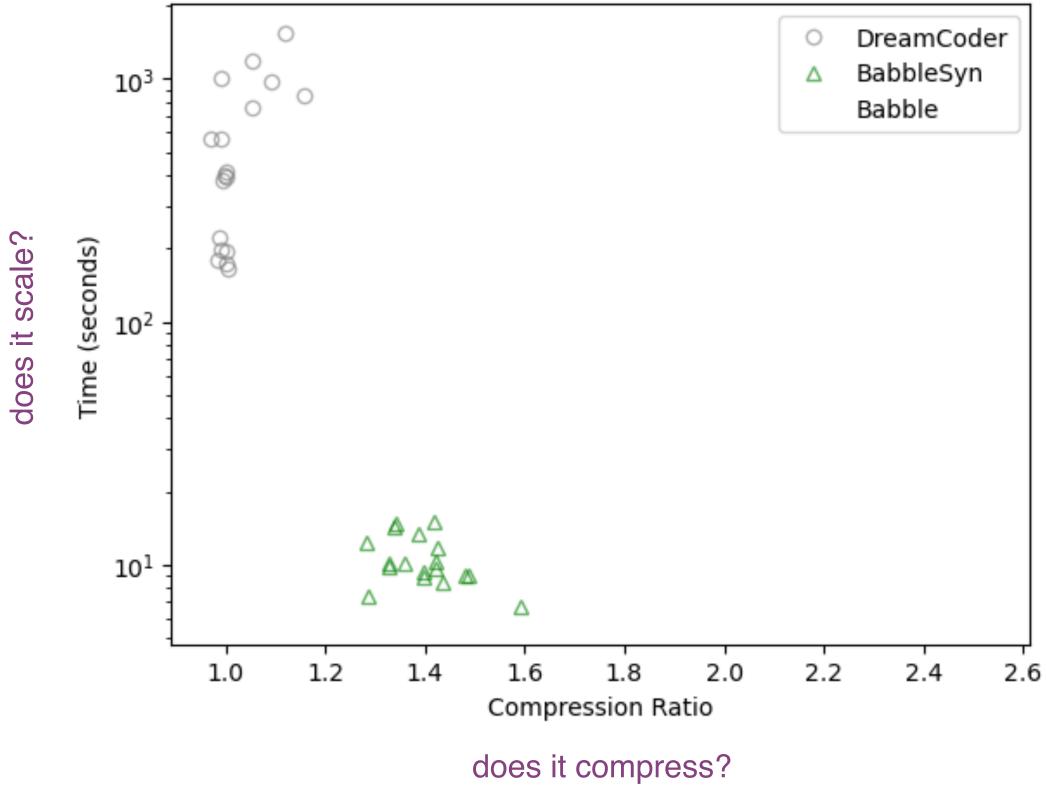


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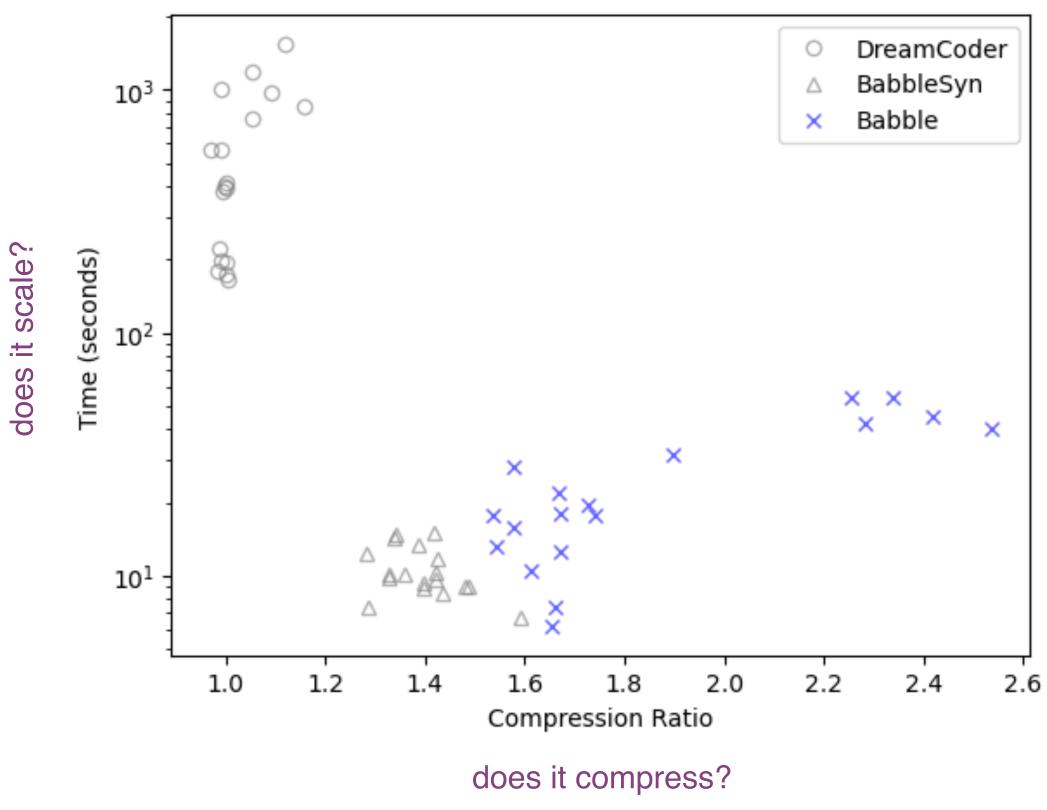


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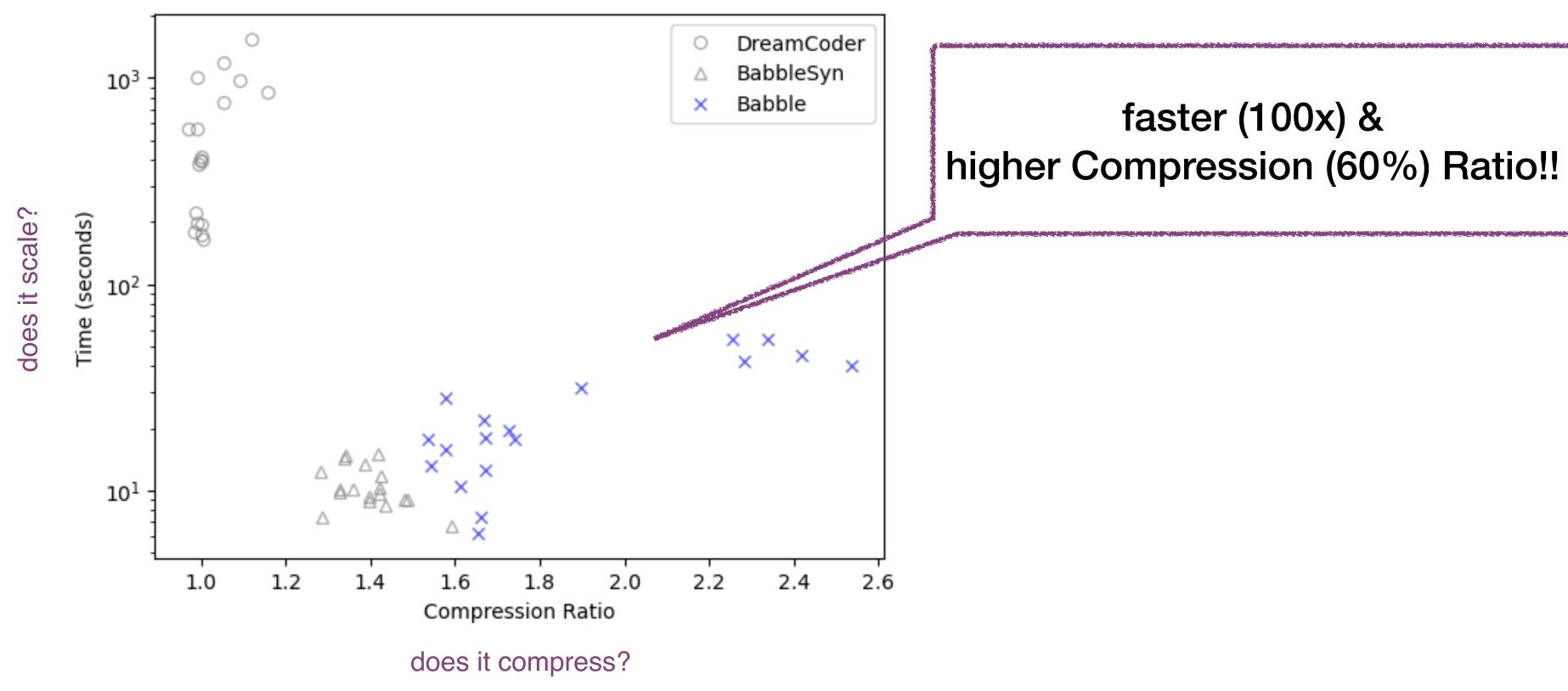


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Sum List
[1 2 3] -> 6
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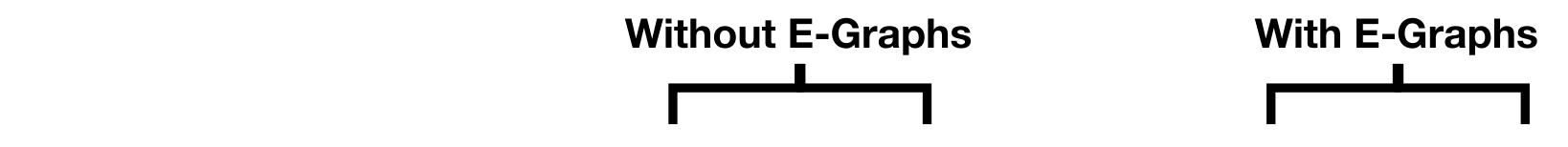
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[1 2 3] -> [2 4 6]
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Check Evens
[0 2 3] -> [T T F]
[2 9 6] -> [T F T]
...
```



Evaluation: Does E-graphs works?

• Benchmarks: 2D CAD



Benchmark	Input Size	Compression Rate	Time(s)	Compression Rate	Time(s)
Nuts & Bolts	19,009	9.23	19	10.90	40
Vehicles	35,427	5.47	79	6.44	78
Gadgets	35,713	5.25	75	7.09	82
Furniture	42,936	4.07	133	4.56	110

Evaluation: Does E-graphs works?

Benchmarks: 2D CAD

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Without E-Graphs

Higher Compression Ratio!!

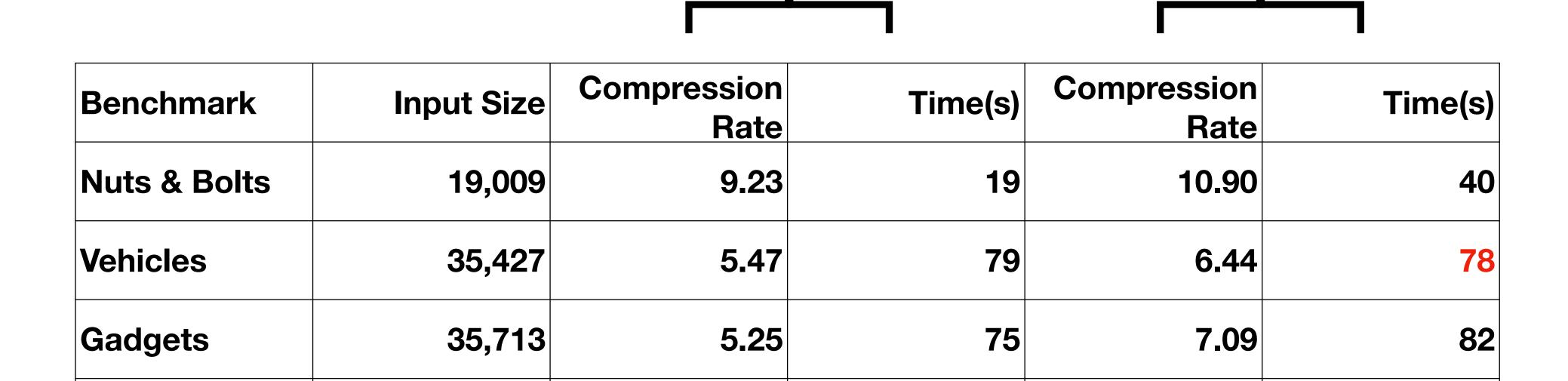
With E-Graphs

Evaluation: Does E-graphs works?

42,936

Benchmarks: 2D CAD

Furniture



Without E-Graphs

Can reduce Time!!

110

With E-Graphs

4.56

4.07

133

Conclusion

- Library Learning Modulo Theory (LLMT)
 - learning abstractions (generate library) from a corpus
- E-Graph Anti-Unification
 - Efficiently generates candidate abstractions
- Faster, Higher Compression Ratio (CR)
 - 100x Faster, 60% higher CR than SOTA

Review (My Opinion)

- Strengths
 - E-graph reduce search space and make candidates smarter.
 - Formally defined new strategy for library learning, established a solid system

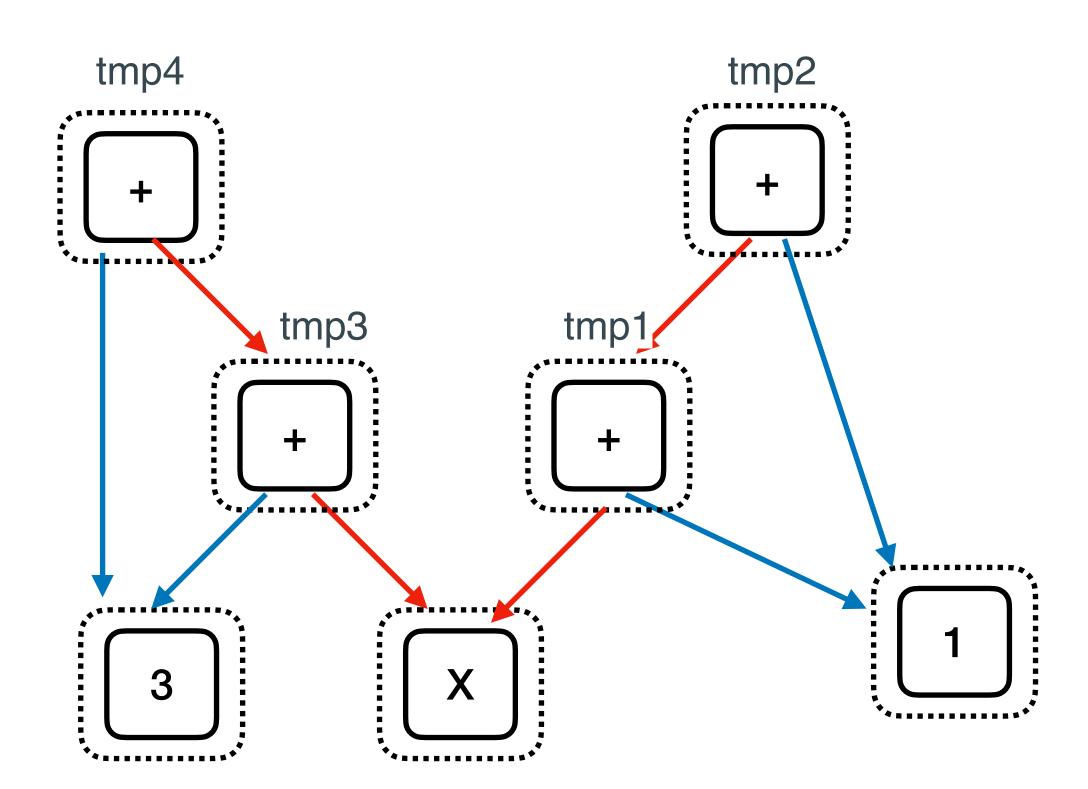
- Weaknesses
 - It is difficult to define **EQ** relations for higher languages such as C/C++
 - Too naive approach in using E-graph. (in E-class matching)

Appendix

Build E-Graph

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp3 = X + 3;
  int tmp4 = tmp1 + 3;
  return tmp2;
}
```



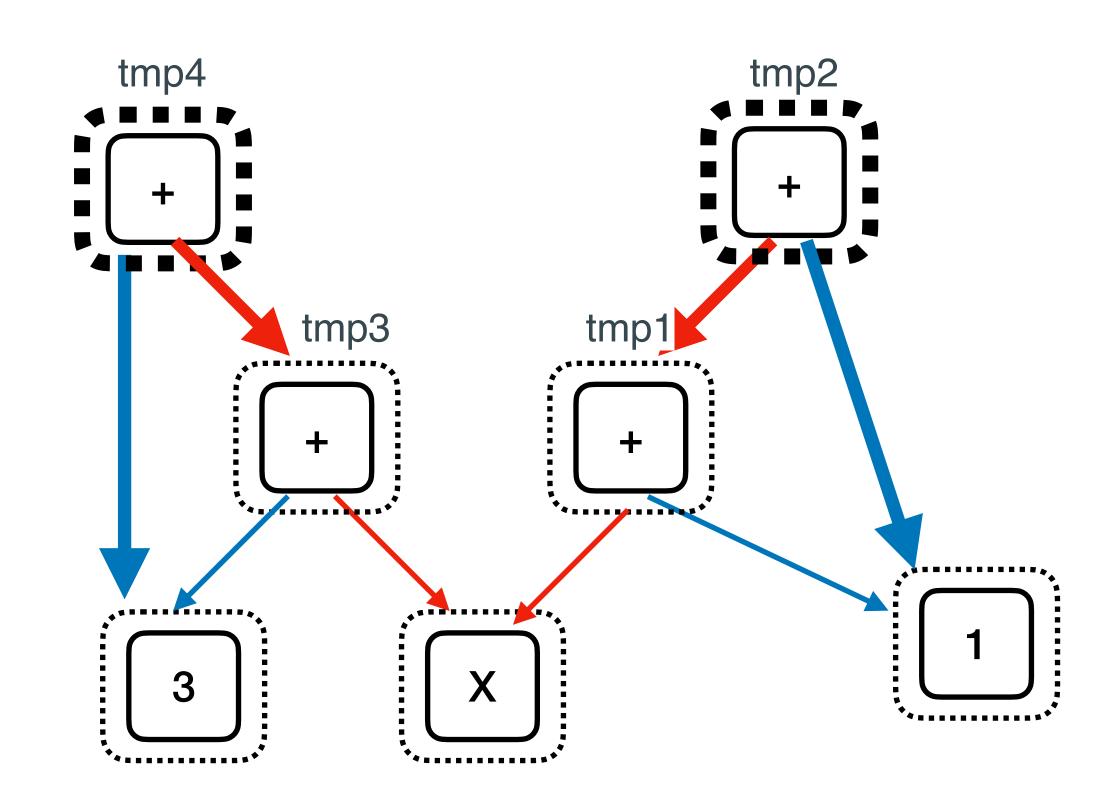
Operand 2

E-graph in Babble

Build E-Graph

```
int foo1(int X, int Y) {
  int tmp1 = X + 1;
  int tmp2 = tmp1 + 1;
  return tmp2;
}
```

```
int foo2(int X, int Y) {
  int tmp3 = X + 3;
  int tmp4 = tmp1 + 3;
  return tmp2;
}
```



?? + ?? is common $\lambda x \ y \rightarrow x + y$