A Genetic Algorithm based Heuristic Method for Test Set Generation in Reversible Circuits

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Abstract-Low power circuit design has been one of the major growing concerns in integrated circuit technology. Reversible circuit (RC) design is a promising future domain in computing which provides the benefit of less computational power. With the increase in the number of gates and input variables, the circuits become complex and the need for fault testing becomes crucial in ensuring high reliability of their operation. Various fault detection methods based on exhaustive test vector search approaches have been proposed in the literature. With increase in circuit complexity, a faster test generation method for providing optimal coverage becomes desirable. In this paper, a Genetic Algorithm (GA) based heuristic test set generation method for fault detection in reversible circuits is proposed which avoids the need for an exhaustive search. Two approaches, one involving random search and the other, involving directed search have been proposed and validated on benchmark circuits considering missing-gate fault (complete and partial), bridging fault and stuck-at fault with optimum coverage and reduced computational efforts.

Index Terms—Reversible logic, Genetic Algorithm, ATPG, Fault Coverage, Computation Time

I. INTRODUCTION

With the rising demands for quantum computing methods for their promising low power dissipation properties and higher data representation and retention capabilities, the field has witnessed rapid advancements. Landauer's principle [1] states that logical reversibility is associated with physical reversibility which serves the purpose of minimal heat generation per machine cycle. The device is said to be logically irreversible if its output is not uniquely defined by the inputs. A logic circuit is reversible if it computes bijective (one-to-one and onto) logic functions. No information loss occurs during the entire operation, thus lowering power consumption to a large extent. Bennet [2] showed that, if computations are carried out irreversibly, $kT \ln 2$ (where k is the Boltzmann constant- $1.3806 \times 10^{-23} m^2 kg^{-2} K^{-1}$ and T is the absolute temperature at which computation takes place)

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power dissipation would occur for each bit of information erasure or throwaway. Hence, lossless computation must be reversible. Reversible circuits used with newer technologies such as quantum computing [3], optical computing [4], Quantum Cellular Automata (QCA) [5], trapped-ion technology [6], adiabatic CMOS [7] offer reduction in power dissipation. Different types of reversible gates including but not limited to Toffoli [8], Fredkin [9] and Peres [10] have been logically designed and many reversible logic circuits are being built with the same. As the versatility of reversible circuits increase with its capability to handle a large number of gates and its bits storage capacity, the vulnerability of the circuits to potential faults increases and thus the requirement for a testing system to detect faults in such circuits becomes very crucial to ensure the correctness of the implemented logic circuit.

Authors in [11], [12] and [13] have proposed various testing algorithms for reversible gates using SAT and Exact methods, respectively. As described in these papers, one common approach is to test the circuit using the entire set or at least a majority of the 2^n test vectors (n being the number of lines in the RC) which makes the algorithm exponentially complex for $n \ge 15$. Since the test generation process is an NP-hard problem and exponentially complex, an exhaustive search approach quickly becomes impractical as the search space grows colossal in size. GA thus provides a heuristic approach for arriving at the optimum solution by attempting to find better solutions in each iteration until a threshold criterion is met. GA based algorithms have been extensively studied and found to be very useful in solving NP-hard problems [14], where the problems cannot be characterized by a polynomial expression. An improvisation over GA by taking into account the quality of individuals (test vectors) selected in each generationan adaptive algorithm [15] can be developed to obtain an optimum solution in a reasonable amount of time.

In this paper, an alternate solution is proposed to the existing testing methods which is efficient in terms of time, space and effort required to obtain a test set, and which can detect a large number of faults for small (n < 8), medium (8 < n < 30) and large (n > 30) circuits,

with ranges as found in [16]. Quantum circuits implemented on QCA tend to have defects such as cell displacement fault and cell misalignment faults which can be tested with stuck-at fault models [17]. Authors in [18] have discussed the applicability of various Register Transfer Level fault models such as single and multiple stuck-at faults that deal with Quantum gate interconnection which can be readily adapted to Quantum Circuits. According to [19] and [7], classical fault models—stuck-at faults, delay faults, missing-gate faults, wrong gate faults and bridging faults—need to be considered for RCs implemented as information reversible circuits and, missing-gate faults and wrong gate faults for RCs implemented as energy reversible circuits.

The proposed work focuses on the set of all missinggate faults which can occur in both information and energy reversible circuits, stuck-at faults and bridging gate faults which find their relevance in information reversible circuits only. Using GA for fault detection eliminates the requirement of testing with all the 2^n vectors thereby reducing the overall computation time. The proposed GA based testing with a Random search approach and a Directed search approach have been validated on small, medium and large benchmark circuits from the libraries-Negative control Toffoli (NCT), Multiple control Toffoli (MCT), Multiple control Fredkin (MCF) and Peres (P) as referred in [20] and [21]. The algorithm has been coded using C language and applied to circuits in .tfc and .real formats on a computer with an Intel i5 processor operating on 4 GB RAM at 1.7 GHz clock speed.

The major contributions of this work are:

- 1 A heuristic GA based strategy using Random search method for obtaining optimum fault coverage for RCs designed using Toffoli, Fredkin and Peres gates for faults- single stuck-at, bridging and set of all missing-gate faults (partial and complete missing-gate faults).
- 2 Directed search approach, an improvisation over Random search approach is proposed which reduces the computation time significantly for k-CNOT circuits.
- 3 A single test set to detect a combination of faults for the set of all missing-gate faults.

The rest of the paper is organized as follows:

Section II briefs about existing reversible circuit testing algorithms. In Section III, various fault models and their detection methodologies relevant for reversible circuits are discussed and a brief on GA is given. Section IV presents the proposed algorithm with an illustrative example. Section V discusses the results obtained and compares it with recent work in this domain. Section VI concludes the work and scope for future work follows.

II. LITERATURE REVIEW ON REVERSIBLE CIRCUITS TESTING

Various fault detection methodologies are described in the literature for the testing of RCs. There are two major classifications of testing, namely, online and offline testing. Online testing is a process that can be carried out during normal operation whereas, offline testing is performed on the circuit in the test mode. Various online testing methods applied for RCs using dual-rail coding, NAND blocks, design for testability (DFT) methods are discussed in [22], [23], [24], [25] and [26].

An offline testing methodology using Integer Linear Programming (ILP) is proposed in [27]. Various fault models affecting RCs have been considered and tested for in the literature. A detection methodology for missing control fault model is proposed in [28], which includes several subsets of this model-single missinggate fault (SMGF) also termed as complete missinggate fault (CMGF), multiple missing-gate fault (MMGF), repeated gate fault (RGF) and partial missing-gate fault (PMGF)-emphasizing that, modelling of reversible circuit faults using only single stuck-at fault would not suffice. Authors in [19] state that only missing-gate faults are possible fault models to be considered in quantum reversible circuits. Detection of multiple missing-gate faults and repeated missing-gate faults have been carried out in [29], [30], [31] and [32], and a test set for combined fault models has been derived. Work in [33] indicates that cross point models are better suited for reversible circuits than stuck-at fault models. Bridging faults are more frequent as compared to stuck-at and missing-gate faults and are complicated to detect. A universal test set for bridging faults has been proposed in [34]. Further, an exact approach for bridging fault detection with a minimal test set is applied to reversible circuits in [35]. A Boolean satisfiability based fault detection for missing-gate faults is dealt with in [11]. Work in [36] proposes a method for the fault detection of Additional control and Repeated gate faults. Recent work in [37] proposes that symmetric functions with only PMGF can be detected with a maximum of 3 vectors (for any n).

Genetic Algorithm has been explored in literature for reversible and irreversible circuit synthesis and optimisation. A design based on GA for space exploration framework for parameterized System-On-Chip (SOC) platforms is proposed in [38]. Fault detection in irreversible circuits using GA has been proposed in [39] for the testing of Single Event Upsets in SRAM-FPGA, in [40] for testing large synchronous circuits and [41] employs GA to obtain an Automatic Test Vector Cultivation for combinational and sequential VLSI circuits. However, GA for fault detection and test set generation in reversible circuits has not yet been explored. With faults

in quantum circuits following a probabilistic distribution, stochastic methods for detection and diagnosis would be very effective [42]. GA being a heuristic approach can therefore be expected to give favorable results for testing RCs which find their applicability in quantum computing.

III. PRELIMINARIES

A. Reversible Logic, Fault Models and detection methodology

RCs, unlike irreversible circuits have the property of input retrieval through output as every input combination has a unique output combination. Standard reversible gates used to build RCs are shown in Fig. 1, with their logical expressions in Table I. Quantum Cost (QC), Gate Count (GC), Ancilla Inputs (AI), Garbage Outputs (GO) and Delay (\triangle) govern the performance of these circuits. Toffoli and Feynman gates come under the class of k-CNOT gates with k values 3 and 2 respectively. The k-CNOT gate is a k-input, k-output reversible gate which transforms $[V_1, V_2, ... V_{k-1}, V_k]$ to $[V_1, V_2, ..., V_{k-1}, (V_1 \cdot$ $V_2 \cdot ... \cdot V_{k-1}) \oplus V_k$]. The functionality of a Peres gate is the same as that of a cascade of Toffoli and Feynman gates. Fredkin gate functions as a controlled swap with input A being the control. A class of Fredkin gates with multiple controls are classified under MCF.

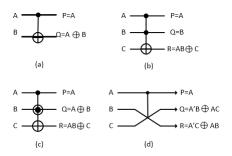


Fig. 1: (a).Feynman(F), (b).Toffoli(T), (c).Peres (P), (d). Fredkin (FR)

TABLE I: Reversible gates and Parameters

Gate		function	C
Feynman($(A, A \oplus B)$	1
Toffoli(T		$=(A,B,AB\oplus C)$	5
Peres (P	(, , - ,	$(A, A \oplus B, AB \oplus C)$	4
Fredkin (F	(/ / /	AB' + AC, AB + A'C	5

Similar to irreversible logic circuits, reversible circuits have a set of fault models described to categorize the various faults that can be observed in them [43]. The ATPG algorithm presented in Section IV is applied on RCs for the detection of faults described here by inducing them at each potential fault location. For every fault induced, the faulty output of the circuit is compared with the fault-free output R for a test vector chosen as input. If the two outputs differ, the vector is said to detect the

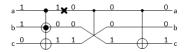


Fig. 2: Illustration of stuck-at 0 at the input of level 1

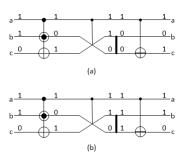


Fig. 3: (a) Illustration of 'b' AND bridged with 'c' at the input of level 2, (b) Illustration of 'b' OR bridged with 'c' at the input of level 2

fault and variable *detected* is incremented by 1 from an initial value of 0.

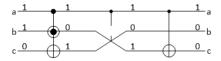


Fig. 4: Illustration of PMGF with a missing control for Fredkin

1. Stuck-at fault (SaF), Fig. 2: This fault model describes a line in the circuit at any level, stuck-at a particular signal value (0 or 1), denoted as x in Fig. 2, and does not allow any other signal value during circuit operation to change it. The majority of the faults in circuits can be mapped to this type of fault. Such a fault usually occurs during the manufacturing process. Faults of this kind are induced by forcing the input lines to 0 and 1, one at a time for all the levels of the RC with outputs computed in each case which is then compared with R, the fault-free output for the same test vector. detected is incremented in case of a mismatch. The number of stuck-at faults possible in an n input RC with N gates are,

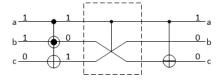


Fig. 5: Illustration of CMGF with a missing Fredkin gate

CumulatedFault = 2.n.(N+1)

2. Bridging fault (BF), Fig. 3: When the signal value on a line is influenced by the signal value on one of the other lines in the circuit, the line under consideration is said to be bridged. Depending on the way in which a line influences the signal value on the bridged line, these faults are classified into two types:

AND bridging: If line 'a' is AND bridged with line 'c', upon induction of the fault, 'a' and 'c' get the logical value 'a AND c'.

OR bridging: If line 'a' is OR bridged with line 'c', upon induction of the fault, 'a' and 'c' get the logical value 'a OR c'.

BF is introduced by picking two lines at a time from the n lines of the RC. The inputs to these lines are ANDed and the common output is forced through the lines. Every possible combination of two lines is made starting from the inputs to the first gate to the output lines after the last gate. In the case of a mismatch, detected is incremented. The entire process is repeated by ORing the input lines. Total number of such intra-level faults are,

$$CumulatedFault = \binom{n}{2}.(N+1).2$$

3. missing-gate fault: Due to manufacturing defects, it might be possible for a gate in the circuit to be skipped or one or many of the control lines to a gate in the circuit go amiss; faults of this kind are labeled missing-gate faults. Two types of missing-gate faults are considered for testing in this work:

PMGF, Fig. 4: One or more of the control lines in a gate of an RC are missing giving rise to PMGF. The CumulatedFault with one missing control is the sum total of all controls present in the gates of the RC. In order to calculate PMGF, the output R is calculated for a test vector. The same test vector is then applied to the RC with controls skipped one at a time. The resulting output is compared with R and detected is incremented in case of a mismatch.

CMGF, Fig. 5: An entire level or gate is skipped from the circuit (reducing the gate count by 1) constituting a CMGF. A circuit can have as many CMGF as the total number of gates in it. In this case, CumulatedFault is $N.\ detected$ for CMGF is calculated as in PMGF, with a gate skipped one at a time instead of the controls.

The same algorithm can also be extended to Repeated gate faults and Additional control faults. After obtaining detected the fault coverage is calculated as,

$$FaultCoverage = \frac{detected}{CumulatedFault} \times 100 \hspace{0.5cm} (1)$$

B. Genetic Algorithm

Genetic Algorithm (GA) is a popular evolutionary algorithm developed based on the observation of the

sustenance of genes from a population of living organisms. The odds of the survival of the genes depend on their fitness values. GA creates successive generations of individuals by applying simple reproduction operations. Typically, parents are chosen to mate with probability proportional to their fitness called proportional selection. This process of selection and reproduction continues until a maximum fitness is obtained. In circuit testing, the most commonly used operators include bit-string crossover, where, off-springs are formed by swapping a sub-sequence between the two parent bit strings, and bitflipping mutation in which a single bit in the string is flipped to form a new offspring string [44]. Mutation helps in faster convergence and its probability of application decreases exponentially with generations [45] and [46].

Fault detection in reversible circuits is easy as they are bijective functions with higher controllability and observability [47]. This property enables detection of maximum faults with very few undetectable faults as most of the faults can be activated through controllable inputs and observed at primary outputs. At the same time, to ensure the property of reversibility, the number of input lines should be made equal to the number of output lines and with an increase in n, the number of potential fault sites increases drastically. An efficient ATPG must converge fast with maximum fault coverage consuming less memory space. ATPG using an exhaustive search as n increases requires more effort in terms of computation time and memory to exercise the complete circuit for minimum test set generation.

Genetic algorithm, unlike other random sampling techniques, steers the search towards more prospective regions due to the combination of reproduction and mutation as directed by the fitness function. While gradient descent techniques can at best arrive at a local optimum, Genetic Algorithm can take values from various regions in the spread out curve of the function and hence can arrive at a far superior solution.

In fault detection using GA, test vectors are selected in a way so as to minimize the cost associated with it and previously selected vectors are also taken into consideration to select the filial generation. This ensures that the cost associated with the test set decreases with each generation until no further reduction is possible. This way, an optimum solution can be arrived at without sifting through the entire search space making GA the ideal solution to such problems which cannot be solved using other approaches.

IV. PROPOSED ATPG ALGORITHMS

A. GA incorporating Random search

In this section, GA along with its variant where the algorithm is directed by selecting the initial vector

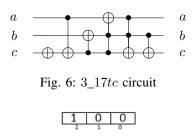


Fig. 7: Test vector as a chromosome

population for fault detection is presented. Algorithm 1 describes the basic structure of the GA for fault detection, incorporating a Random search approach to produce a test set for a given RC with n input lines and N gates. Threshold indicates the desired percentage of fault coverage with the maximum being 100%. The next subsection expands the steps with the help of an example circuit.

The path taken by the GA is determined by the initial set of vectors chosen. Random selection does not always guarantee maximum coverage for every test run. It might take many iterations to yield optimum test set if the initially selected vectors are weak, which would lead to higher computation time or might even require early termination before optimum coverage has been reached. Thus, by directing the search, faster convergence would be highly likely, especially for MCT-based RCs with a large number of input lines.

B. Illustration of proposed algorithm using random search for Complete-missing-gate fault detection

Consider the benchmark circuit 3_17tc as shown in Fig. 6 as the input for the proposed algorithm to find a test set for optimum coverage of CMGF. In this algorithm, gates are also referred to as levels and V_i in a set represents the \mathbf{i}^{th} element of the set.

Illustration 1 Illustration for GA using Random search for the circuit 3_17tc

INPUT: RC with 'n' lines and 'N' gates; *Threshold* **OUTPUT:** The test set and fault coverage%

STAGE I: Input Parameter Extraction

Step 1: Extract the parameters n and N from the RC comprising of n lines $B_0, B_1, ..., B_{n-1}$ and N levels $G_0, G_1, ..., G_{N-1}$. Set fault-type and threshold value where 100 implies maximum fault coverage. Compute max-the maximum number of input test vectors for the RC.

$$n=3$$
 $N=6$ $max=2^n=8$ $Threshold=100$ $Input_Fault_Type=complete_missing_gate$

Step 2: Initialize generation, which indicates the current iteration, as 0.

```
Algorithm 1 GA for Fault Detection in an RC
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```
1: INPUT (RC, Threshold, Input_Fault_Type)
 2: OUTPUT (fault coverage%, test set)
 3: use (RC) get (n, N)
 4: procedure SELECTION(n)\triangleright To get initial vector set
        max \leftarrow 2^n
 5:
 6:
        for i \leftarrow 1, n do
 7:
            InitPop(V_i) \leftarrow \mathbf{rand}(0, \max)
        end for
 8:
 9: end procedure
    procedure FITNESS(InitPop)
        \quad \mathbf{for} \ i \leftarrow 1, n \ \mathbf{do}
11:
12:
            use(Input \ Fault \ Type, InitPop(V_i))
            get(FaultCoverage, DetectedFaults)
13:
            FitnessFunction(V_i) \leftarrow FaultCoverage
14:
            if FitnessFunction(V_i) \geq Threshold then
15:
                Display Output, Exit
16:
            end if
17:
        end for
18:
19: end procedure
20: procedure MULTIPLY(InitPop,FitnessFunction)
        for i \leftarrow 1, n do
21:
            Parent(V_{i1}, V_{i2}) \leftarrow \textbf{Roulette}(InitPop, FitnessFunction)
22:
            ChildPopulation(V_i) \leftarrow \mathbf{CrossOver}(Parent(V_{i1}, V_{i2}))
23:
            ChildPopulation(V_i) \leftarrow \mathbf{Mutate}(Child(V_i)Population)
24:
            use Fitness(ChildPopulation(V_i))
25:
            get \ FitnessFunction(V_{i+n}), DetectedFaults
26:
        end for
27:
28: end procedure
29: FinPop \leftarrow InitPop \bigcup ChildPopulation
\textbf{30: } FinFitness \leftarrow FitnessFunction
31: ArrangeDescending(FinFitness,FinPop)
32: procedure COMBINE(FinPop,DetectedFaults)
33:
        for i \leftarrow \left[\frac{n}{2}\right], |FinPop| do
            high = 0
34:
35:
            repeat
                Combination_i(.) \leftarrow \textbf{Combinations}(i, FinPop)
36:
    37:
                fitness = Fitness(Combination(.))
                if fitness \ge Threshold then
38:
39:
                    Display Output, Exit
                end if
40:
                if high < fitness then
41:
                    high = fitness
42:
43:
            until high > fitness for |FinPop| itera-
44:
    tions
        end for
45:
        InitPop \leftarrow \mathbf{MaxFitness}(Combination(.))
47: end procedure
48: Goto line 10
```

STAGE II: Test Vector Selection

Step 3: Randomly select n-which is the upper limit on

the number of test vectors for InitPop-vectors from 0 to (max-1)-(rand(0,max)), both inclusive ensuring that none of the selected vectors repeat. InitPop is a set containing all the initially selected n vectors. FinPop has elements copied from InitPop.

 $InitPop = \{4, 6, 1\}$

STAGE III: Fitness Function Computation

Step 4: Represent test vector in binary form, as in Fig. 7. Compute FaultCoverage for CMGF as explained in Section. III-A. Here, test vector 4-[1 0 0], the first element in InitPop is selected. The fault-free output R and the faulty outputs after inducing the fault at each level are obtained.

$$R = 100$$

$$FaultyOutput = \{010, 010, 100, 100, 100, 100\}$$

Step 5: Obtain DetectedFault matrix.

if($FaultyOutput(V_i) != R$)

set $DetectedFault_{[vector]}(V_i)$ to indicate detection else

reset $DetectedFault_{[vector]}(V_i)$

Once FaultyOutput has been completely traversed, count the number of 1's in the set DetectedFault[vector] and store it in detected. Find FaultCoverage using Equation(1).

if($FitnessFunction(V_i) \ge Threshold$) Goto Step 18.

$$DetectedFault_{[100]} = \{1, 1, 0, 0, 0, 0\}$$

$$CumulatedFault = n, \text{ see Section. III-A}$$

$$FaultCoverage = 33.33\%$$

$$FitnessFunction(V_i) = FaultCoverage = 33.33$$

Step 6: Repeat steps 4 and 5 for all the vectors in InitPop. Copy members of FitnessFunction into FinFitness.

```
DetectedFault_{[100]} = \{1, 1, 0, 0, 0, 0\}
DetectedFault_{[110]} = \{1, 1, 0, 0, 1, 1\}
DetectedFault_{[001]} = \{1, 0, 0, 0, 0, 0, 0\}
FitnessFunction = \{33.33, 66.67, 16.67\}
FinFitness = \{33.33, 66.67, 16.67\}
```

STAGE IV: Roulette Wheel

Step 7: Select pairs of vectors from *InitPop*. The process here follows the usual flow where vectors after being conformed onto a pie chart are picked two at a time based on their fitness functions. Select *n* such pairs of parent.

 $Parent = \{(100, 110), (110, 001), (110, 100)\}$

STAGE V: Reproduction And Cross-Over

Step 8: A pair of parents is chosen and a random cross-over point is selected in the bit sequence. For 3_17tc , [1 0 0] and [1 1 0] are chosen as parents.

CrossOverPoint = rand(0, n) = 1

The child is generated taking bits before

CrossOverPoint from the first parent- '1' from [1 0 0]- and the remaining from the second parent- '1 0' from [1 1 0]- to yield [1 1 0] as the offspring. Continue until n daughters have been generated.

 $ChildPopulation = \{110, 111, 110\}$

STAGE VI: Mutation

Step 9: In order to carry out mutation, a number is randomly selected from 0 and $(100^{generation+1} - 1)$, both inclusive. If this number is less than 10, then the test vector undergoes mutation where a random bit is selected and flipped. By doing this, the probability of mutation decreases in exponents of 10 for every *generation*. The genes after mutation are:

 $ChildPopulation = \{110, 111, 100\}$

Step 10: Repeated vectors are discarded and fitness function for the non-repeated ones is computed. The new members are added into the set FinPop with their fitness values in FinFitness along with faults detected by them in DetectedFault. The fitness values of the progeny are checked to see if Threshold has been met.

$$FinPop = \{100, 110, 001, 111\}$$

$$FinFitness = \{33.33, 66.67, 16.67, 50\}$$

$$DetectedFault_{[111]} = \{1, 1, 1, 0, 0, 0\}$$

STAGE VII: Test Population Generation

Step 11: Vectors of FinPop are arranged in descending order based on their fitness values from FinFitness. Variable m is defined as shown.

$$FinPop = \{110, 111, 100, 001\}$$

$$FinFitness = \{66.67, 50, 33.33, 16.67\}$$

$$m = |FinPop| = 4$$

STAGE VIII: Minimal Test Set Generation From Test Population

Step 12: if $(\frac{n}{2} < 2)$, L = 2, else, $L = [\frac{n}{2}]$, rounded to the closest integral value. Combinations of L vectors from FinPop are made.

```
Combination_{21} = \{110, 111\}
Combination_{22} = \{110, 100\}
Combination_{23} = \{110, 001\}
Combination_{24} = \{111, 100\}
Combination_{25} = \{111, 001\}
Combination_{26} = \{100, 001\}
```

Step 13: Set upperBound as m. Reset bestCoverage which is the best coverage that the algorithm can yield for the current test run.

Step 14: Initialize x and i as 0. Reset high which gives the best fitness value for the current combination. Update DetectedFault and detected for each of the $Combination_{Li}$ and compute Fitness.

if($Fitness \geq Threshold$)

 $FinalTestSet = Combination_{Li}$, goto Step 18. if(Fitness > high)

```
7
```

```
high=Fitness
else, Increment x
if(bestCoverage < high)
bestCoverage = high, FinalTestSet = Combination_{Li}
if( x = upperBound )
Goto Step 15
Increment i and repeat Step 14 until all combinations of
vectors are made or if x hits upperBound. For 3 17tc
with combinations of 2 vectors,
Fitness = \{83.33, 66.67, 66.67, 50\}
high = 83.33
                  x = 4
Step 15: if (L = n), Goto Step 16, else, Increment L
and repeat Step 14.
          Combination_{31} = \{110, 111, 100\}
          Combination_{32} = \{110, 111, 001\}
          Combination_{33} = \{110, 100, 001\}
          Combination_{34} = \{111, 100, 001\}
          Fitness = \{83.3, 83.33, 66.67, 50\}
    high = 83.33\%
                         bestCoverage = 83.33\%
  STAGE IX: Initial Population for filial generation
Step 16: if |FinalTestSet| \le n-1
Copy all vectors from FinalTestSet into InitPop and
fill up the remaining slots upto n using random selection
method described in Step 3.
else, feed (n-1) vectors from FinalTestSet into
InitPop and select 1 vector randomly using random
selection method described in Step 3 and add it to
InitPop.
InitPop = \{110, 111, 101\}
FinPop = \{110, 111, 101\}
Vector [1 0 1] is randomly generated.
generation is incremented.
Step 17: Goto Step 4 and repeat the process for the next
generation. The values obtained are:
ChildPopulation = \{101, 101, 100\}
FinPop = \{101, 110, 111, 100\}
FinFitness = \{83.33, 66.67, 50, 33.33\}
For the combination, Combination_{21} = \{101, 110\} the
fitness is 100. Since Threshold is met, goto Step 18.
DetectedFault_{[110]||[101]} = \{1, 1, 1, 1, 1, 1\}
  STAGE X: Optimum Test Set
Step 18: Display the test set and fault coverage.
FinalTestSet = \{101, 110\}, bestCoverage = 100,
```

Since this approach is heuristic, maximum coverage for every test run cannot be expected. In case the algorithm runs indefinitely with no change in bestCoverage, the process is exited prematurely and restarted.

C. GA incorporating Directed search

In GA with Directed search, the initial population is selected based on the configuration of the first gate in the RC. Values for InitPop are selected such that the output

of the target is 1, which is ensured by forcing opposite

```
Algorithm 2 Directed Search for k-CNOT Circuits
 1: INPUT (RC)
 2: OUTPUT (InitPop)
 3: \mathbf{use}(RC)\mathbf{get}(controls - \{B_{c0}, B_{c1}...B_{ck}\}, target
     \{B_t\} of first gate with B_0...B_{n-1} as input lines;n)
 4: procedure Selection(n, B_t, B_{c0}, B_{c1}, ..., B_{ck})
 5:
         m\leftarrow 1
         if |controls| = \emptyset then
 6:
              Goto line 30
 7:
 8:
         end if
 9:
         v \leftarrow |target| + |controls|
         B_t \leftarrow 0
10:
         B_{c0}, B_{c1}, ..., B_{ck} \leftarrow 11...1 \quad \triangleright \text{ set all control bits}
11:
12:
         for i \leftarrow 0, n-1 do
13:
              if B_i \notin target and B_i \notin controls then
                   B_i \leftarrow \mathbf{rand}(0,2) \triangleright \mathbf{random} allocation of
14:
     0/1 for remaining input lines
              end if
15:
         end for
16:
17:
         InitPop(V_m) \leftarrow \mathbf{Decimal}(B_{n-1}B_{n-2}...B_0)
         increment m
18:
19:
         B_t \leftarrow 1
         var \leftarrow 00...0 > var, a (k+1) bit binary variable
20:
     is reset
         for j \leftarrow 1, 2^{v-1} - 1 do
21:
22:
              if m \le n-2 then
                   B_{c0}B_{c1}...B_{ck} \leftarrow var
23:
                   increment var
24:
                   repeat lines 12-18
25:
              else
26:
27:
                   Exit for
              end if
28:
         end for
29.
         for m \leftarrow m, n-2 do
30:
               InitPop(V_m) \leftarrow \mathbf{rand}(0, \max)
31:
32:
         end for
         InitPop(V_m) \leftarrow \mathbf{Decimal}(111...11)
33:
         increment m
34:
         InitPop(V_m) \leftarrow \mathbf{Decimal}(000...00)
35:
36: end procedure
```

values to the AND of control inputs and the target. Directed search makes use of the fact that by assigning opposite values to the control and target of the first gate, maximum faults can be detected. In case of Toffoli, for instance, whose function is given as $(A, B, C) = (A, B, A \cdot B \oplus C)$, line C value toggles if $A \cdot B \neq C$. When $A \cdot B = 1$, and C is 0, faults: Sa0-A, Sa0-B, Sa1-C, CMGF, PMGF-A, PMGF-B, BF-A·C, BF- B·C, BF-A+C and BF-B+C a total of 10 faults can be detected. Whereas, with test vector $[0\ 1\ 0]$, 7 faults and with $[1\ 1\ 1]$, 6 faults can be detected. By selecting a test vector which can detect

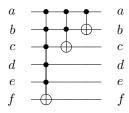


Fig. 8: A 3 level RC with multiple control k-CNOT gates

a majority of faults, probability of fault propagation increases, and with it, faster convergence of the algorithm is possible. Test set generation for GA incorporating Directed search, is explained in Algorithm 2 for k-CNOT circuits. The example circuit as shown in Fig. 8 is used to explain the method. It consists of 3 gates with the first gate comprising of 5 controls and a target f.

D. Illustration of proposed algorithm using GA with Directed search for Complete missing-gate fault detection

The fault coverage and the test set for the example circuit in Fig. 6 is obtained by substituting Directed search for Random search in Illustration 2.

Illustration 2 Illustration for GA using Directed Search for the RC 3_17tc

INPUT: RC with 'n' lines and 'N' gates; *Threshold* **OUTPUT:** The test set and fault coverage

STAGE I: Input Parameter Extraction

Extracting and initializing the appropriate values. n = 3 N = 6 Threshold = 100

 $Input_Fault_Type = complete_missing_gate$

STAGE II: Test Vector Selection

Using the method explained in Algorithm 2, the initial population is selected.

$$InitPop = \{5, 7, 0\}$$
 $FinPop = \{5, 7, 0\}$

STAGE III: Fitness Function Computation

Fitness function for the selected vectors and the DetectedFaults are determined.

$$\begin{aligned} DetectedFault_{[101]} &= \{1, 1, 1, 1, 0, 1\} \\ DetectedFault_{[111]} &= \{1, 1, 1, 0, 0, 0\} \\ DetectedFault_{[000]} &= \{1, 0, 1, 1, 1, 1\} \\ FitnessFunction &= \{83.33, 50, 83.33\} \end{aligned}$$

STAGE IV: Roulette Wheel

Parent population is arrived at using roulette wheel.

$$Parent = \{(000, 111), (000, 101), (101, 111)\}$$

STAGE V: Reproduction And Cross-Over

The parent chromosomes undergo reproduction to produce off-springs.

 $ChildPopulation = \{000, 000, 101\}$

STAGE VI: Mutation

Mutation is carried out and FinPop is arrived at. For 3_17tc , mutation did not occur for any of the vectors.

$$FinPop = \{101, 111, 000\}$$

$$FinFitness = \{83.33, 50, 83.33\}$$

Since fitness value did not meet Threshold, move to the next stage.

STAGE VII: Test Population Generation

Vectors of FinPop are arranged in descending order based on their corresponding fitness values in FinFitness.

$$FinPop = \{101, 000, 111\}$$

 $FinFitness = \{83.33, 83.33, 50\} \ m = |FinPop| = 3$

STAGE VIII: Minimal Test Set Production From Test Population

Combinations of vectors are made and checked for fitness function.

 $Combination_{21} = \{101, 000\}, Fitness = \{100\}$ Threshold has been met. Goto Stage X.

STAGE X: Output

 $FinalTestSet = \{101,000\}, \ bestCoverage = 100$ Exit.

TABLE II: Comparison of GA with Directed and Random search methods for detecting CMGF in the circuit $3\ 17tc^{\#}$

Parameter	Directed	Random	†Directed
Time(avg)⋆	< 0.01	< 0.01	< 0.01
V(avg)⋆	2	2	2
generation(avg)∗	1	1.467	1
P(100% Fault Coverage)	1	0.8	1

#Values are for 30 test runs *Values are for 100% fault coverage †For Mirrored RC

A comparison of the results obtained using GA with Directed search and Random search for the circuit in Fig. 6 is presented in Table II for CMGF.

Directed search approach poses a problem for circuits with constant inputs. In such cases, only certain vectors would be permissible which are selected and added into InitPop. In case the upper limit has not been met, vectors are randomly selected and added to the set as in the case of GA with Random search. The algorithm described here is extended to the other fault models as well. The only difference arises in the computation of

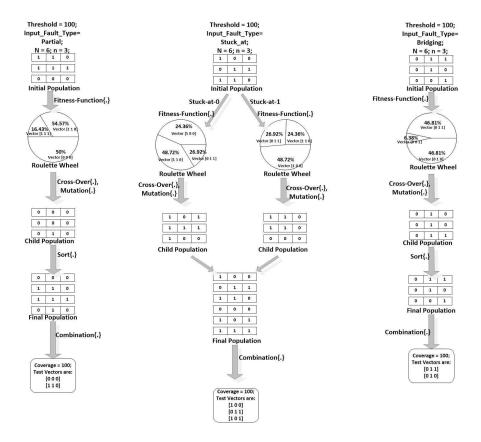


Fig. 9: GA applied to detect (a) PMGF, (b) SaF and (c) BF in 3_17tc

fault coverage% which is carried out as described in Section III-A.

In the case of SaF, through analysis, it was found that fault coverage was always 50% when both Sa0 and Sa1 faults are considered. Since fitness function remains constant, the selection of members in ParentPop cannot be directly adopted. This problem is addressed by considering the fault coverage for Sa0 and Sa1 separately. Stages III through VI of the algorithm is performed separately for Sa0 and Sa1. CumulatedFault would be half the original value and the faults introduced would be either a 0 or a 1. The ChildPopulation obtained at the end of the two processes are combined and added into FinPop. Because of the branching, |FinPop| generally doubles. DetectedFault is found anew by introducing both Sa0 and Sa1 type of faults for all the members of the set FinPop. The rest of the process follows as in PMGF and CMGF. The process for PMGF, SaF and BF is depicted in Fig. 9.

The methodology developed in this section can be applied to the mirrored RC with data traversing from the last gate to the first gate. While doing so, the garbage outputs must take on appropriate constant values to preserve the reversible properties of the former. In

Table II results of mirrored 3_17tc have been added to illustrate the applicability of the algorithm when an input is fed to the last gate. Directed search is performed by feeding opposite values to the inputs b and c for the inverted circuit. One of the possible sets of InitPop would be $\{000, 111, 010\}$.

Directed search has been devised to cater to the requirements of k-CNOT circuits, as, most benchmark circuits commence with a k-CNOT gate. The functionality of Fredkin gate requires its control to be activated for swapping contents of signal values on its target lines. In order to obtain maximum coverage, controls must be activated and targets must take on opposite values. RCs with Toffoli and Fredkin with Toffoli as the first gate can be Directed using the same approach. It can be observed from Section V that, there has been a significant improvement for k-CNOT and Peres based circuits using Directed approach and a slight improvement for Fredkin based circuits.

E. Test set generation for the set of all missing-gate Faults

The algorithm developed here is extended to obtain a single test set for the set of all missing-gate faults. Both

CMGF and PMGF are induced individually on the RC as discussed in Section III-A in Stage III of the Algorithm 1 by following the remaining steps without any change. In this case, the DetectedFault matrix takes on a larger dimension with the combined faults and results in a single test set for missing-gate faults.

V. RESULTS AND DISCUSSIONS

In this section, results obtained using the two approaches of GA are presented along with comparisons with methods proposed in the recent literature. Circuit information for every benchmark circuit is provided with n indicating the number of lines, N the number of gates and superscripts on every benchmark name to indicate the type of gate library, that the circuit has been implemented from. The circuits are sorted based on n. Computation time stated are processor specific. Tables V - VI carry out a comparison of the values obtained using GA with other proposed methods. All the existing works compared here consider 100% fault coverage. GA being a heuristic approach, cannot guarantee global minima in all cases like exact method. As is to be expected, the test set cardinality using GA has increased in a few cases over exact which can be observed in Tables V and VI. GA still remains a viable option as exact cannot be used without expending a great deal of effort for medium and large circuits. Table VIII gives the values for GA with Directed and Random search approach for each of the faults as discussed in Section IV. It can be observed that the values obtained using Directed approach have surpassed values obtained using the Random approach in terms of time taken, coverage and number of test vectors, in most cases. As the complexity of the circuit decreases, the values obtained using the two methods nearly coincide which can be attributed to the smaller | InitPop|. In the case of symmetric and cyclic circuits, as bit width increases, the disparity in the results obtained using the two methods is very large with Directed search being more favorable. This can be observed in cycle17 3 circuit for PMGF. These results lead to the conclusion that GA being a powerful tool can be amplified in terms of effectiveness by directing the search in the initial stage. Table VII shows the values obtained when the algorithm is extended to produce a single test set for missing-gate fault detection.

A. Comparison of results for BF

Table V compares results obtained for BF with those proposed in [35] and [49]. There is an average reduction of 37.14% test vectors with GA compared to [49]. For the same test set, time taken by GA is less than in exact approach although the test set cardinality has increased by an average of 27%.

TABLE III: Comparison of CMGF detection parameters

Ref	Benchmark	N	n	Ret	f. Paper	I	Directe	d	Random			
	Circuit			#V	time(s)	#FC %	#V	time(s)	#FC %	#V	time(s)	
[13]	$ham7tc^{T}$	23	7	4	6.93	100	4	0.046	100	5	0.375	
	$mod5adders^{T}$	21	6	3	1.056	100	3	0.015	100	3	0.265	
	$mod5d1^{T}$	8	5	1	0.0479	100	1	< 0.01	100	1	< 0.01	
	$hwb4tc^{T}$	17	4	2	0.058	100	2	< 0.01	100	3	0.109	
	$rd32^{T}$	4	4	2	0.0202	100	2	< 0.01	100	3	< 0.01	
	$3_{17}tc^{T}$	6	3	2	0.017	100	2	< 0.01	100	2	0.015	
[11]	$hwb5_13^{T}$	88	28	8	0.05	100	5	0.772	100	6	0.797	
	$rd84_142^{T}$	28	15	9	0.06	100	6	0.046	100	4	0.359	
	$sym9_148^{T}$	210	10	32	0.59	100	1	0.29	100	1	0.297	
	$4gt12-v0_86^{T}$	14	5	3	< 0.01	100	3	0.082	100	2	< 0.01	
	$one-two-three-v0_97^{\mathrm{T}}$	11	5	3	< 0.01	100	3	0.015	100	3	< 0.01	
[12]	hwb5_13	88	28	7	0.24	100	5	0.578	100	5	0.563	
	$rd84_142^{T}$	28	15	8	0.14	100	5	0.046	100	9	0.125	
	$sym9_148^{T}$	210	10	14	1.79	100	1	0.525	100	5	24.456	
	$4gt12-v0_86^T$	14	5	5	0.02	100	2	< 0.01	100	2	0.015	
	$one-two-three-v0_97^{\mathrm{T}}$	11	5	3	0.02	100	3	¡0.01	100	3	0.015	

 $\#V = No. \ Of \ Test \ Vectors \ for \ detection \ \#FC \ \% = Fault \ Coverage \ Percentage \ x^T = Toffoli \ based \ circuit$

TABLE IV: Comparison of PMGF detection parameters

Ref	Benchmark	N	n	Ref	. Paper	I	Directe	d	Random			
	Circuit			#V	time(s)	#FC %	#V	time(s)	#FC %	#V	time(s)	
[13]	$ham7tc^{T}$	23	7	4	6.83	100	4	0.062	100	4	0.328	
	$mod5adders^{T}$	21	6	3	1.076	100	3	0.015	100	3	0.078	
	$mod5d1^{T}$	8	5	1	0.0486	100	1	< 0.01	100	2	0.062	
	$hwb4tc^{T}$	17	4	2	0.054	100	2	0.015	100	2	0.062	
	$rd32^{\mathrm{T}}$	4	4	2	0.0196	100	2	0.015	100	2	0.062	
	3_17tc^{T}	6	3	2	0.016	100	2	< 0.01	100	2	0.015	
[11]	$hwb5_13^{T}$	88	28	9	0.07	100	5	0.578	100	5	0.563	
	$rd84_142^{T}$	28	15	120	0.03	100	5	0.046	100	9	0.125	
	$sym9_148^{T}$	210	10	120	3.71	100	1	0.525	100	5	24.456	
	$4gt12-v0_{-}86^{T}$	14	5	10	< 0.01	100	2	< 0.01	100	2	0.015	
	$one-two-three-v0_97^{\mathrm{T}}$	11	5	3	0.02	100	3	¡0.01	100	3	0.015	

 $\#V = No. Of Test Vectors for detection <math>\#FC \% = Fault Coverage Percentage x^T = Toffoli based circuit$

TABLE V: Comparison of BF Detection Parameters

Ref	Benchmark	N	n	R	ef. Paper	er Directed		Random			
	Circuit			#V	time(s)	#FC %	#V	time(s)	#FC %	#V	time(s)
[49]	$rd32^{T}$	28	15	6	*	100	4	< 0.01	100	3	0.015
	$ham7tc^{T}$	23	7	4	*	100	6	0.343	100	6	0.187
	$graycode6^{T}$	5	6	9	*	100	3	0.031	100	5	0.093
	$xor5d1^{T}$	4	5	8	*	100	3	0.015	100	4	0.062
	4_49-12-32 ^T	12	4	5	*	100	4	0.015	100	4	< 0.01
	$ham3tc^{T}$	5	3	3	*	100	3	< 0.01	100	3	0.015
[35]	$gf2^{4}mult_{19}_{83}^{T}$	19	12	4	76.3734	98.56	8	1.093	98.64	6	0.656
	nth_prime6_inc_55_667 ^T	55	6	4	116.3606	100	6	3.219	100	6	1.673
	$2of5d1^{T}$	18	6	4	25.4031	100	5	0.343	100	5	0.031
	$5mod5_fc^{T}$	10	6	3	4.768	100	4	0.109	100	5	0.015

 $\#V = No. Of Test Vectors for detection \#FC \% = Fault Coverage Percentage <math>x^T = Toffoli based circuit \star time not mentioned in reference [49]$

TABLE VI: Comparison of SaF Detection Parameters with [13]

Benchmark	N	n	Rei	f. Paper	I	Directe	1	Random				
Circuit			#V	time(s)	#FC %	#V	time(s)	#FC %	#V	time(s)		
$ham7tc^{T}$	23	7	3	7.126	100	5	0.078	100	5	0.187		
$mod5adders^{T}$	21	6	3	1.12	100	3	0.046	100	4	0.265		
$mod5d1^{T}$	8	5	3	0.1866	98.89	4	0.031	98.89	4	0.171		
$hwb4tc^{T}$	17	4	3	0.0839	100	3	< 0.01	100	3	0.046		
$rd32^{T}$	4	4	3	0.0408	97.5	3	< 0.01	97.5	4	0.125		
3_17tc^{T}	6	3	3	0.018	100	3	< 0.01	100	3	0.031		

 $\#V = No. \ Of \ Test \ Vectors \ for \ detection \ \#FC \ \% = Fault \ Coverage \ Percentage \ x^T = Toffoli \ based \ circuit$

TABLE VII: Test set and coverage for combination of missing-gate faults- CMGF and PMGF

Benchmark	N	n	Faults		Directed	l		Random			
Circuit				#V	TIME(s)	#FC %	#V	time(s)	#FC %		
$gf2^{10mult_{109_{509}T}}$	109	30	318	2	4.142	100	20	276.76	71.70		
cycle17_3 ^T	48	20	457	3	2.531	100	10	32.111	1.31		
$cnt3-5_180^{T}$	20	16	60	1	0.657	100	2	0.719	100		
0410184_169 ^T	46	14	95	4	0.109	100	9	0.218	100		
$sym6_316^{T}$	29	14	72	11	0.062	100	10	0.078	100		
$nth_prime7_inc_1427_3172^{T}$	1427	7	3197	7	706.275	98	7	735.567	96.90		

 $\#V = No. \ Of \ Test \ Vectors \ for \ detection \ \#FC \ \% = Fault \ Coverage \ Percentage \ x^T = Toffoli \ based \ circuit$

B. Comparison of results for missing-gate faults

Tables III and IV compare the values obtained for missing-gate type faults with exact method as described in [13], SAT method in [11] and PBO in [12]. The number of test vectors required for complete fault coverage in the case of GA is found to be the same in most of the cases as that using the exact approach with lesser computation time. Test set requirement for full coverage is much less compared to SAT and PBO based approaches with an average decrease of 72.73% and 56.76% test vectors, respectively. PMGF results compared with [11] show a decrease of 93.89% test vectors on average. Directed search produced better results than Random search in a majority of circuits.

C. Comparison of results for SaF

Table VI compares values obtained for SaF type faults using GA and exact approach stated in [13]. GA takes much lesser time for computation in all cases with nearly the same number of test vectors.

D. Comparison of GA incorporating Directed and Random approach

Figs. 10 through 13 show the variation of fault coverage percentage with generation. Directed approach selects individuals which generally have higher fitness function than most vectors in the gene pool while in Random search approach, the probability of selection of the same vector would be $\frac{1}{2^n}$ which is a very small value as bit size increases. In the case of ham15-109-214, though the initial selection was poorer in GA with the Directed approach than in the Random approach, it produced maximum coverage in 2 generation while random approach required 4 due to constancy in fault coverage% for 3 such generations. Circuits $gf2^{10}mult_{109}509$, sym_{148} and $cycle_{10}2$ converge within one generation for Directed approach. The Random approach in $qf2^{\wedge}10mult\ 109\ 509$ yields a fault coverage% less than 65% even with 25 generation while Directed approach produces the result in a single generation demonstrating the superiority of Directed approach over Random when applied to k-CNOT circuits with high input variables.

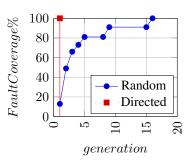


Fig. 10: Variation of fault coverage with *generation* for the circuit *cycle*10_2 using GA with Random and Directed approaches

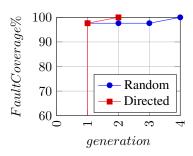


Fig. 11: Variation of fault coverage with generation for the circuit ham15-109-214 using GA with Random and Directed approaches

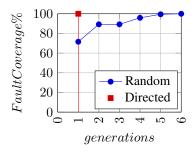


Fig. 12: Variation of fault coverage with generation for the circuit $sym9_148$ using GA with Random and Directed approaches

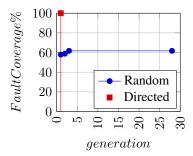


Fig. 13: Variation of fault coverage with generation for the circuit $gf2^{\wedge}10mult_109_509$ using GA with Random and Directed approaches

12

TABLE VIII: Test set and coverage for PMGF, CMGF, SaF, BF using Directed and Random search approach for benchmark circuits

						PMGF							CMGF			
					Direct	ed		Randor	n			Directe	ed		Rando	m
BenchMark Circuit	N	n	Total Faults	#FC %	#V	time(s)	#FC %	#V	time(s)	Total Faults	#FC %	#V	time(s)	#FC %	#V	time(s)
bw_{291}^{T}	307	87	307	100	4	9.593	100	5	16.406	432	100	4	3.5	100	5	6.421
$hwb7_302^{F}$	281	73	281	100	26	39.85	100	29	39.96	426	100	17	31.09	100	18	33.67
$hwb6_14^{\rm F}$	159	46	159	100	9	5.76	100	9	6.64	241	100	11	4.328	100	11	4.69
$ham15_298^{T}$	153	45	153	100	1	0.109	100	2	4.48	157	100	1	0.09	100	2	4.142
$cycle10_293^{T}$	78	39	78	100	2	0.828	100	3	1.203	98	100	1	0.09	100	2	6.143
rd84_313 ^T	104	34	104	100	16	1.31	100	21	2.734	143	100	19	1.33	100	23	2.69
$gf2^{10}mult_{109}_{509}^{T}$	109	30	209	100	2	2.546	61.72	4	74.039	109	100	2	1.828	63.3	15	24.845
$t-add-8^{\mathrm{T}}$	122	24	160	100	14	1.339	88.13	22	6.437	122	100	14	1.132	90.16	17	4.296
mux_246^{T}	35	22	131	25.95	2	0.156	4.58	2	5.54	35	97.14	22	12.156	34.29	17	2.063
cycle17_3 ^T	48	20	409	100	3	2.071	0.73	2	39.799	48	100	3	0.908	6.25	2	9.015
ryy6_256 ^T	44	17	328	37.8	8	10.859	37.8	8	15.562	44	100	2	1.671	54.55	2	6.656
cnt3-5_180 ^T	20	16	40	100	2	0.078	100	2	0.453	20	100	2	0.594	100	2	0.328
$ham15tc1^{T}$	132	15	352	95.74	15	12.178	93.18	8	45.348	132	96.97	14	4.851	98.48	9	24.455
0410184_169 ^T	46	14	49	100	4	0.078	100	3	0.062	46	100	5	0.062	100	4	0.063
		-														
sym6_316 ^T	29	14	43	100	11	0.062	100	10	0.031	29	100	10	0.062	100	11	0.031
squar5_261 ^T	43	13	95	100	7	0.265	100	6	0.219	43	100	8	0.281	100	9	0.203
cycle10_2 ^T	19	12	100	100	2	0.062	100	2	0.07	19	100	2	0.062	100	2	0.201
sym9_148 ^T	210	10	756	100	1	0.525	100	1	17.273	210	100	1	0.29	100	1	9.592
sys6-v0_144 ^{T+P}	15	10	23	100	4	0.015	100	4	0.015	15	100	3	0.015	100	3	0.078
$urf_2_{277}^{T}$	3144	8	3777	94.07	8	74.455	94.07	8	74.455	44	100	2	1.671	54.55	2	6.656
$nth_prime7_inc_1427_3172^{\mathrm{T}}$	1427	7	1770	95.58	7	16.957	95.99	7	16.304	1427	97.83	7	14.909	96.71	7	43.472
$hwb7_60^{F}$	166	7	396	100	7	9.375	100	7	8.937	30	100	7	13.329	98.80	7	49.23
$rd53_131^{T}$	28	7	24	100	5	0.015	100	6	0.046	28	100	7	0.062	100	6	< 0.01
$hwb6_57^{\mathrm{F}}$	65	6	122	100	5	0.438	100	5	1.515	65	100	6	2.249	100	6	1.218
$hwb5_54^{F}$	24	5	30	100	4	0.015	100	4	0.125	24	100	4	0.0310	100	5	0.421
$4gt12-v0_86^{T}$	14	5	20	100	3	0.015	100	3	0.015	14	100	3	0.11	100	2	< 0.01
$one-two-three-v0_97^{\mathrm{T}}$	11	5	23	100	3	< 0.01	100	3	< 0.01	11	100	3	0.015	100	3	0.015
$alu-v0_26^{T}$	6	5	8	100	2	0.015	100	2	< 0.01	6	100	2	0.015	100	2	0.015
$hwb4_51^{F}$	11	4	10	100	2	0.015	100	2	0.015	11	100	2	0.015	100	2	0.015
						SaF							BF			
					Direct	ed		Randor	n			Directe	ed		Rando	m
BenchMark Circuit	N	n	Total Faults	#FC %	#V	time(s)	#FC %	#V	time(s)	Total Faults	#FC %	#V	time(s)	#FC %	#V	time(s)
bw_291 ^T	307	87	53592	82.28	5	663.81	-	-	†TO	2304456	-	-	†TO	-	-	†TO
hwb7_302 ^F	281	73	41172	99.9	7	1971.547	-	-	†TO	1482192	-	-	†TO	-	-	†TO
hwb6_14 ^F	159	46	14720	82.29	6	79.296	82.29	6	84.95	331200	87.13	6	681.655	86.54	14	2075.418
ham15_298 ^T	153	45	13860	80.84	5	527.958	80.84	6	975.797	304920	91.26	9	5057.34	87	4	4649.65
cycle10_293 ^T	78	39	6162	83.14	19	109.056	82.88	19	140.925	117078	92.12	11	680.173	91.84	4	791.142
rd84_313 ^T	104	34	7140		_	107.050	02.00		140.723	117070	72.12	1.1	000.175			171.172
$ras4_s1s$ $gf2^{10}mult_109_509^{T}$	104	34	/140	70.42	0	252.00	70.2	0	225 410	117010	07.55	22	677 572			627.14
$gj2$ 10 mut_109_509 t-add-8 ^T		20	6600	79.43	8	252.99	79.3	8	235.418	117810	87.55	22	677.573	87.43	22	627.14
	_	30	6600	95.5	7	121.809	88.83	15	102.88	95700	97.16	15	577.157	87.43 92.68	22 15	718.27
	122	24	5904	95.5 91.82	7 12	121.809 46.877	88.83 89.33	15 12	102.88 46.877	95700 67896	97.16 97.46	15 14	577.157 259.306	87.43 92.68 95.81	22 15 13	718.27 263.918
mux_246 ^T	122 35	24 22	5904 1584	95.5 91.82 99.94	7 12 11	121.809 46.877 3.687	88.83 89.33 86.36	15 12 11	102.88 46.877 3.437	95700 67896 16632	97.16 97.46 100	15 14 14	577.157 259.306 90.024	87.43 92.68 95.81 93.94	22 15 13 11	718.27 263.918 14.534
mux_246^{T} $cycle17_3^{\mathrm{T}}$	122 35 48	24 22 20	5904 1584 1960	95.5 91.82 99.94 100	7 12 11 7	121.809 46.877 3.687 34.769	88.83 89.33 86.36 90.2	15 12 11 10	102.88 46.877 3.437 16.174	95700 67896 16632 18620	97.16 97.46 100 99.33	15 14 14 13	577.157 259.306 90.024 81.332	87.43 92.68 95.81 93.94 97.79	22 15 13 11 10	718.27 263.918 14.534 143.758
$\begin{array}{c} mux_246^{\mathrm{T}} \\ cycle17_3^{\mathrm{T}} \\ ryy6_256^{\mathrm{T}} \end{array}$	122 35 48 44	24 22 20 17	5904 1584 1960 1530	95.5 91.82 99.94 100 99.87	7 12 11 7 12	121.809 46.877 3.687 34.769 73.207	88.83 89.33 86.36 90.2 96.01	15 12 11 10 18	102.88 46.877 3.437 16.174 10.515	95700 67896 16632 18620 12240	97.16 97.46 100 99.33 99.98	15 14 14 13 9	577.157 259.306 90.024 81.332 31.316	87.43 92.68 95.81 93.94 97.79 99.77	22 15 13 11 10 8	718.27 263.918 14.534 143.758 61.864
mux_246^{T} $cycle17_3^{T}$ $ryy6_256^{T}$ $cnt3-5_180^{T}$	122 35 48 44 20	24 22 20 17 16	5904 1584 1960 1530 672	95.5 91.82 99.94 100 99.87 92.56	7 12 11 7 12 8	121.809 46.877 3.687 34.769 73.207 9.438	88.83 89.33 86.36 90.2 96.01 92.56	15 12 11 10 18 8	102.88 46.877 3.437 16.174 10.515 18.297	95700 67896 16632 18620 12240 5040	97.16 97.46 100 99.33 99.98 97.34	15 14 14 13 9 15	577.157 259.306 90.024 81.332 31.316 3.093	87.43 92.68 95.81 93.94 97.79 99.77 97.62	22 15 13 11 10 8	718.27 263.918 14.534 143.758 61.864 31.051
mux_2246^{T} $cycle17_3^{T}$ $ryy6_2256^{T}$ $cnt3-5_180^{T}$ $ham15tc1^{T}$	122 35 48 44 20 132	24 22 20 17 16 15	5904 1584 1960 1530 672 3990	95.5 91.82 99.94 100 99.87 92.56 100	7 12 11 7 12 8 10	121.809 46.877 3.687 34.769 73.207 9.438 63.631	88.83 89.33 86.36 90.2 96.01 92.56	15 12 11 10 18 8 7	102.88 46.877 3.437 16.174 10.515 18.297 30.126	95700 67896 16632 18620 12240 5040 27930	97.16 97.46 100 99.33 99.98 97.34 100	15 14 14 13 9 15	577.157 259.306 90.024 81.332 31.316 3.093 151.116	87.43 92.68 95.81 93.94 97.79 99.77 97.62	22 15 13 11 10 8 9	718.27 263.918 14.534 143.758 61.864 31.051 96.02
mux_2246^{T} $cycle17_23^{\mathrm{T}}$ $ryy6_2256^{\mathrm{T}}$ $cnt35180^{\mathrm{T}}$ $ham15tc1^{\mathrm{T}}$ 0410184169^{T}	122 35 48 44 20 132 46	24 22 20 17 16 15 14	5904 1584 1960 1530 672 3990 1316	95.5 91.82 99.94 100 99.87 92.56 100	7 12 11 7 12 8 10 6	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687	88.83 89.33 86.36 90.2 96.01 92.56 100	15 12 11 10 18 8 7 6	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578	95700 67896 16632 18620 12240 5040 27930 8554	97.16 97.46 100 99.33 99.98 97.34 100	15 14 14 13 9 15	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100	22 15 13 11 10 8 9 9	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172
mux_246^{T} $cycle17_3^{\mathrm{T}}$ $ryy6_256^{\mathrm{T}}$ $cnt3-5_180^{\mathrm{T}}$ $ham15tc1^{\mathrm{T}}$ 0410184_169^{T} $sym6_316^{\mathrm{T}}$	122 35 48 44 20 132	24 22 20 17 16 15	5904 1584 1960 1530 672 3990	95.5 91.82 99.94 100 99.87 92.56 100 100 91.31	7 12 11 7 12 8 10	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29	88.83 89.33 86.36 90.2 96.01 92.56	15 12 11 10 18 8 7	102.88 46.877 3.437 16.174 10.515 18.297 30.126	95700 67896 16632 18620 12240 5040 27930	97.16 97.46 100 99.33 99.98 97.34 100	15 14 14 13 9 15	577.157 259.306 90.024 81.332 31.316 3.093 151.116	87.43 92.68 95.81 93.94 97.79 99.77 97.62	22 15 13 11 10 8 9 9 8 13	718.27 263.918 14.534 143.758 61.864 31.051 96.02
mux_2246^{T} $cycle17_23^{\mathrm{T}}$ $ryy6_2256^{\mathrm{T}}$ $cnt35180^{\mathrm{T}}$ $ham15tc1^{\mathrm{T}}$ 0410184169^{T}	122 35 48 44 20 132 46	24 22 20 17 16 15 14	5904 1584 1960 1530 672 3990 1316	95.5 91.82 99.94 100 99.87 92.56 100	7 12 11 7 12 8 10 6	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687	88.83 89.33 86.36 90.2 96.01 92.56 100	15 12 11 10 18 8 7 6	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578	95700 67896 16632 18620 12240 5040 27930 8554	97.16 97.46 100 99.33 99.98 97.34 100	15 14 14 13 9 15 12	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100	22 15 13 11 10 8 9 9 8 13 7	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172
mux_246^{T} $cycle17_3^{\mathrm{T}}$ $ryy6_256^{\mathrm{T}}$ $cnt3-5_180^{\mathrm{T}}$ $ham15tc1^{\mathrm{T}}$ 0410184_169^{T} $sym6_316^{\mathrm{T}}$	122 35 48 44 20 132 46 29	24 22 20 17 16 15 14	5904 1584 1960 1530 672 3990 1316 840	95.5 91.82 99.94 100 99.87 92.56 100 100 91.31	7 12 11 7 12 8 10 6	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31	15 12 11 10 18 8 7 6	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922	95700 67896 16632 18620 12240 5040 27930 8554 5460	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15	15 14 14 13 9 15 12 11	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08	22 15 13 11 10 8 9 9 8 13	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609
mux_246^{T} $cycle17_3^{T}$ $ryy6_256^{T}$ $cnt3-5_180^{T}$ $ham15tc1^{T}$ 0410184_169^{T} $sym6_316^{T}$ $squar5_261^{T}$	122 35 48 44 20 132 46 29 43	24 22 20 17 16 15 14 14	5904 1584 1960 1530 672 3990 1316 840 1144	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67	7 12 11 7 12 8 10 6 7 6	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67	15 12 11 10 18 8 7 6 7	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92	15 14 14 13 9 15 12 11 12 8	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92	22 15 13 11 10 8 9 9 8 13 7	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047
mux_246^{T} $cycle17_3^{\mathrm{T}}$ $ryy6_256^{\mathrm{T}}$ $cnt3-5_180^{\mathrm{T}}$ $ham15tc1^{\mathrm{T}}$ 0410184_169^{T} $sym6_316^{\mathrm{T}}$ $squar5_261^{\mathrm{T}}$ $cycle10_2^{\mathrm{T}}$	122 35 48 44 20 132 46 29 43 19	24 22 20 17 16 15 14 14 13	5904 1584 1960 1530 672 3990 1316 840 1144 480	95.5 91.82 99.94 100 99.87 92.56 100 100 91.31 94.67	7 12 11 7 12 8 10 6 7 6 3	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67	15 12 11 10 18 8 7 6 7 9	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92	15 14 14 13 9 15 12 11 12 8	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92	22 15 13 11 10 8 9 9 8 13 7	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391
mux_246^{T} $cycle17_3^{T}$ $ryy6_256^{T}$ $cnt3-5_180^{T}$ $ham15tc1^{T}$ 0410184_169^{T} $sym6_316^{T}$ $squar5_261^{T}$ $cycle10_2^{T}$ $sys6-v0_144^{T+p}$	122 35 48 44 20 132 46 29 43 19	24 22 20 17 16 15 14 14 13 12	5904 1584 1960 1530 672 3990 1316 840 1144 480 320	95.5 91.82 99.94 100 99.87 92.56 100 100 91.31 94.67 100 95.63	7 12 11 7 12 8 10 6 7 6 3 5	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63	15 12 11 10 18 8 7 6 7 9 4	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47	15 14 14 13 9 15 12 11 12 8 7	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100	22 15 13 11 10 8 9 9 8 13 7	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829
mux_246^{T} $cycle17_3^{T}$ $ryy6_256^{T}$ $cnt3-5_180^{T}$ $ham15tc1^{T}$ 0410184_169^{T} $sym6_316^{T}$ $squar5_261^{T}$ $cycle10_2^{T}$ $sys6-v0_144^{T+P}$ $sym9_148^{T}$	122 35 48 44 20 132 46 29 43 19 15 210	24 22 20 17 16 15 14 14 13 12 10	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67 100 95.63 99.98	7 12 11 7 12 8 10 6 7 6 3 5	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27	15 12 11 10 18 8 7 6 7 9 4 7	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350	97.16 97.46 100 99.33 99.98 97.34 100 96.15 95.92 100 98.47	15 14 14 13 9 15 12 11 12 8 7	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47	22 15 13 11 10 8 9 9 8 13 7 7 8	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831
mux_246^{T} $cycle17_3^{T}$ $ryy6_256^{T}$ $cnt3-5_180^{T}$ $ham15tc1^{T}$ 0410184_169^{T} $sym6_316^{T}$ $squar5_261^{T}$ $cycle10_2^{T}$ $sys6-v0_144^{T+P}$ $sym9_148^{T}$ $urf_2_277^{T}$	122 35 48 44 20 132 46 29 43 19 15 210 3144	24 22 20 17 16 15 14 14 13 12 10 10 8	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220 50320	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67 100 95.63 99.98	7 12 11 7 12 8 10 6 7 6 3 5 10	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141 101.898 184.11	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27 99.86	15 12 11 10 18 8 7 6 7 9 4 7	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485 723.68	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350 18990	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47 100	15 14 14 13 9 15 12 11 12 8 7 7	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25 43.89 2590.541	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47 100	22 15 13 11 10 8 9 9 8 13 7 7 8 9	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831 2597.485
$\begin{array}{c} mux_246^{\mathrm{T}} \\ cycle17_3^{\mathrm{T}} \\ ryy6_256^{\mathrm{T}} \\ cnt3-5_180^{\mathrm{T}} \\ ham15tc1^{\mathrm{T}} \\ 0410184_169^{\mathrm{T}} \\ sym6_316^{\mathrm{T}} \\ squar5_261^{\mathrm{T}} \\ cycle10_2^{\mathrm{T}} \\ sys6-v0_144^{\mathrm{T+P}} \\ sym9_148^{\mathrm{T}} \\ urf_2_277^{\mathrm{T}} \\ nth_prime7_inc_1427_3172^{\mathrm{T}} \\ hwb7_60^{\mathrm{F}} \end{array}$	122 35 48 44 20 132 46 29 43 19 15 210 3144 1427 166	24 22 20 17 16 15 14 14 13 12 10 10 8 7	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220 50320 19992 2338	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67 100 95.63 99.98 99.9	7 12 11 7 12 8 10 6 7 6 3 5 10 8 7 2	121.809 46.877 3.687 34.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141 101.898 184.11 391.9	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27 99.86 99.86	15 12 11 10 18 8 7 6 7 9 4 7 10 8 7 5	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485 723.68 229.698 6.875	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350 18990 176064 59976	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47 100 99.73	15 14 14 13 9 15 12 11 12 8 7 7 7 9 8 7	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25 43.89 2590.541 693.734 520.108	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47 100 99.73 99.7	22 15 13 11 10 8 9 9 8 8 13 7 7 8 9 8 8	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831 2597.485 701.58
$\begin{array}{c} mux_246^{\mathrm{T}} \\ cycle17_3^{\mathrm{T}} \\ ryy6_256^{\mathrm{T}} \\ cnt3-5_180^{\mathrm{T}} \\ ham15tc1^{\mathrm{T}} \\ 0410184_169^{\mathrm{T}} \\ sym6_316^{\mathrm{T}} \\ squar5_261^{\mathrm{T}} \\ cycle10_2^{\mathrm{T}} \\ sys6-v0_144^{\mathrm{T+P}} \\ sym9_148^{\mathrm{T}} \\ urf_2_277^{\mathrm{T}} \\ nth_prime7_inc_1427_3172^{\mathrm{T}} \\ hwb7_60^{\mathrm{F}} \\ rd53_131^{\mathrm{T}} \end{array}$	122 35 48 44 20 132 46 29 43 19 15 210 3144 1427 166 28	24 22 20 17 16 15 14 14 11 10 10 8 7 7	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220 50320 19992 2338 406	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67 100 95.63 99.98 99.9 99.78 100	7 12 11 7 12 8 10 6 7 6 3 5 10 8 7 2 3	121.809 46.877 3.687 3.4.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141 101.898 184.11 391.9 7.5 0.062 28	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27 99.86 99.86 100 98.28	15 12 11 10 18 8 7 6 7 9 4 7 10 8 7 7 10 8	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485 723.68 229.698 6.875 0.078	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350 18990 176064 59976 7014 1218	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47 100 99.73 99.7	15 14 14 13 9 15 12 11 12 8 7 7 7 9 8 7	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25 43.89 2590.541 693.734 520.108	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47 100 99.73 99.7 99.86 99.84	22 15 13 11 10 8 9 9 8 13 7 7 8 8 9 8 7 7 5	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831 2597.485 701.58 7.344 0.234
$\begin{array}{c} mux_246^{\mathrm{T}} \\ cycle17_3^{\mathrm{T}} \\ ryy6_256^{\mathrm{T}} \\ cnt3-5_180^{\mathrm{T}} \\ ham15tc1^{\mathrm{T}} \\ 0410184_169^{\mathrm{T}} \\ sym6_316^{\mathrm{T}} \\ squar5_261^{\mathrm{T}} \\ cycle10_2^{\mathrm{T}} \\ sys6-v0_144^{\mathrm{T+P}} \\ sym9_148^{\mathrm{T}} \\ urf_2_277^{\mathrm{T}} \\ nth_prime7_inc_1427_3172^{\mathrm{T}} \\ hwb7_60^{\mathrm{F}} \\ rd53_131^{\mathrm{T}} \\ hwb6_57^{\mathrm{F}} \end{array}$	122 35 48 44 20 132 46 29 43 19 15 210 3144 1427 166 28 65	24 22 20 17 16 15 14 14 13 12 10 10 8 7 7	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220 50320 19992 2338 406 792	95.5 91.82 99.94 100 99.87 92.56 100 100 91.31 94.67 100 95.63 99.98 99.9 99.78 100	7 12 11 7 12 8 10 6 7 6 3 5 10 8 7 2 3	121.809 46.877 3.687 3.4.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141 101.898 184.11 391.9 7.5 0.062 28 0.641	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27 99.86 100 98.28 100	15 12 11 10 18 8 7 6 7 9 4 7 10 8 7 5 4 5	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485 723.68 229.698 6.875 0.078	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350 18990 176064 59976 7014 1218 1980	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47 100 99.73 99.7 100 99.84 100	15 14 13 9 15 12 11 12 8 7 7 7 9 8 7 7 5 5	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25 43.89 2590.541 693.734 520.108 0.124	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47 100 99.73 99.7 99.86 99.84 100	22 15 13 11 10 8 9 9 8 13 7 7 8 9 8 7 7 5 5	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831 2597.485 701.58 7.344 0.234
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$\begin{array}{c} mux_246^{\mathrm{T}} \\ cycle17_3^{\mathrm{T}} \\ ryy6_256^{\mathrm{T}} \\ cnt3-5_180^{\mathrm{T}} \\ ham15tc1^{\mathrm{T}} \\ 0410184_169^{\mathrm{T}} \\ sym6_316^{\mathrm{T}} \\ squar5_261^{\mathrm{T}} \\ cycle10_2^{\mathrm{T}} \\ sys6-v0_144^{\mathrm{T+P}} \\ sym9_148^{\mathrm{T}} \\ urf_2_277^{\mathrm{T}} \\ nth_prime7_inc_1427_3172^{\mathrm{T}} \\ hwb7_60^{\mathrm{F}} \\ rd53_131^{\mathrm{T}} \\ hwb6_57^{\mathrm{F}} \\ hwb5_54^{\mathrm{F}} \\ 4gt12-v0_86^{\mathrm{T}} \\ \end{array}$	122 35 48 44 20 132 46 29 43 19 15 210 3144 1427 166 28 65 24 14	24 22 20 17 16 15 14 14 13 12 10 10 8 7 7 7 6 5 5	5904 1584 1960 1530 672 3990 1316 840 1144 480 320 4220 50320 19992 2338 406 792 250 150	95.5 91.82 99.94 100 99.87 92.56 100 91.31 94.67 100 95.63 99.98 99.9 99.78 100 98.28 100	7 12 11 7 12 8 10 6 7 6 3 5 10 8 7 2 2 2 4	121.809 46.877 3.687 3.4.769 73.207 9.438 63.631 1.687 0.891 29 2.82 0.875 0.141 101.898 184.11 391.9 7.5 0.062 28 0.641 0.046	88.83 89.33 86.36 90.2 96.01 92.56 100 91.31 94.67 100 95.63 99.27 99.86 100 98.28 100 100 95.33	15 12 11 10 18 8 7 6 7 9 4 7 10 8 7 5 5 4	102.88 46.877 3.437 16.174 10.515 18.297 30.126 1.578 0.922 2.658 0.546 0.515 93.485 723.68 229.698 6.875 0.078 0.593 1.375 0.015	95700 67896 16632 18620 12240 5040 27930 8554 5460 6864 2640 1350 18990 176064 59976 7014 1218 1980 500 300	97.16 97.46 100 99.33 99.98 97.34 100 100 96.15 95.92 100 98.47 100 99.73 99.7 100 99.84 100 100	15 14 14 13 9 15 12 11 12 8 7 7 7 9 8 7 7 5 5 5 4 4	577.157 259.306 90.024 81.332 31.316 3.093 151.116 4.484 1.687 8.628 3.046 0.25 43.89 2590.541 693.734 520.108 0.124 1.344 0.266 0.015	87.43 92.68 95.81 93.94 97.79 99.77 97.62 100 100 96.08 95.92 100 98.47 100 99.73 99.7 99.86 99.84 100 100 100	22 15 13 11 10 8 9 9 8 13 7 7 7 8 8 9 9 8 7 7 5 5 5 4 4	718.27 263.918 14.534 143.758 61.864 31.051 96.02 4.172 13.609 4.047 2.391 0.829 48.831 2597.485 701.58 7.344 0.234 1.032 0.016

#V = No. Of Test Vectors for detection #FC % = Fault Coverage Percentage x^T = Toffoli based circuit x^F = Fredkin based circuit x^P = Peres based circii †TO - time out

VI. CONCLUSION

In this paper, a GA based platform is used to obtain a test set for optimum coverage using less computation time for small, medium and large circuits. This is the first attempt in reversible literature to use principles of GA for test set generation with optimum fault coverage for a wide class of faults. A GA based method for fault detection in RCs designed with k-CNOT, Peres and Fredkin gates has been proposed. An algorithm for a Directed search method exploring unique properties of reversible circuits as opposed to the random search approach inherent to GA is also presented. Significant improvement is observed with respect to the number of generations, computation time and fault coverage. It is observed that the algorithm worked very well with circuits having small, medium and large input lines in the case of missing-gate faults. Detection of SaF and BF in large RCs takes longer convergence time owing to the increased fault cardinality in the order of 106. It would be interesting to combine circuit partitioning method with GA to catalyze convergence. The fault detection methodology used here can be extended to other subsets of reversible fault models such as Additional gate and Additional control faults.

To conclude, by using GA proposed in this paper teamed with an appropriate algorithm to direct the initial stage, faster convergence can be ensured. In RCs having few input lines but a large number of gates, the time taken for convergence was found to be relatively higher. Hence, future work would involve exploring ways to decrease the number of test vectors, reduce test generation complexity by using a suitable circuit partitioning technique and to devise an algorithm for new quantum fault models. Fault diagnosis using GA has also been earmarked for future research.

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