

Chapter 8

The Relational Algebra and Relational Calculus.

* Relational Algebra

- The basic set of operations for the relational model is known as the relational algebra. These operations enable a user to specify basic retrieval requests.
 - The result is a new relation formed from one or more relations.
 - A sequence of relational algebra operations forms a relational algebra expressions, whose result will also be a relation that represents the result of a database query.
- query processing in RDBMS

* Relational Calculus

- Firm foundation of mathematical logic.
- Used in high-level declarative language for writing queries.
- No order of operations in RC expressions
- SQL is based on RC but also has some features of RA.

* Unary Relational Operations

→ SELECT (σ) Operation

- Used for selecting a subset of the tuples from a relation that satisfy a selection condition
- Denoted by $\sigma \langle \text{selection condition} \rangle (R)$
- σ (sigma) denotes select operator.
- Selection condition is a boolean expression

specified on the attributes of relation R.

Example:

Those whose salary is greater than \$30,000

$\sigma_{\text{salary} > 30,000}(\text{EMPLOYEE})$

- The SELECT operation $\sigma_{\langle \text{condition} \rangle}(R)$ produces a relation S that has same schema as R.
- SELECT operation is commutative.

$$\sigma_{\langle \text{condition}_1 \rangle}(\sigma_{\langle \text{condition}_2 \rangle}(R)) = \sigma_{\langle \text{condition}_2 \rangle}(\sigma_{\langle \text{condition}_1 \rangle}(R))$$

- A cascaded SELECT operation may be applied in any order.
- A cascaded SELECT operation may be replaced by a single selection with a conjunction of all the conditions.

→ Project (π) Operation

- Selects certain columns from the table and discards the other columns.
- Creates a vertical partitioning.
- $\pi_{\langle \text{attribute list} \rangle}(R)$
- π (called pi) is used to represent projection
- Projection operation removes any duplicate tuples, so the result of the project operation is a set of tuples and hence a valid relation.
- Example:
Employees name, salary.
 $\pi_{\text{name, salary}}(\text{EMPLOYEE})$
- Number of tuples in the result of projection is less or equal to the no. of tuples in R.

- If the list of attributes includes a key of R , then the no. of tuples is equal to the no. of tuples in R .
- Projection is not commutative

* Sequence of Operations and the RENAME Operation

→ We can write the operations as a single relational algebra expression by nesting the operations.

$\pi_{\text{Fname, salary}} (\sigma_{\text{DNO}=5} (\text{EMPLOYEE}))$

OR

We can apply one operation at a time and create intermediate result relations, giving a name to it.

$\text{DEP5_EMPS} \leftarrow \sigma_{\text{DNO}=5} (\text{EMPLOYEE})$

$\text{Result} \leftarrow \pi_{\text{Fname, salary}} (\text{DEP5_EMPS})$

→ Rename Operation (ρ)

- Operator is ρ (called Rho)
- $\rho_{S(B_1, B_2, \dots, B_n)} (R)$ is a renamed relation S based on R with column names B_1, B_2, \dots, B_n .
- Example:

$\rho_{\langle \text{fn, ln, dno} \rangle} (\pi_{\langle \text{fname, lname, dnumber} \rangle} (\text{EMPLOYEE}))$

* Relational Algebra Operations from Set Theory.

→ UNION Operation

- The result of this operation, denoted by $R \cup S$, is a relation that includes all tuples that are either in R or in S or in both R and S . Duplicate

tuples are eliminated.

- The union produces the tuples that are in R , or R_2 or both. The 2 operands must be type compatible (same domain and datatype and degree)

→ Intersection Operation.

- The result of this operation, denoted by $R \cap S$ is a relation having tuples that are common to the both operand relations. Must be type compatible

→ Difference.

- The result of this operation, denoted by $R - S$, is a relation that includes all tuples that are in R but not in S . Two operands must be type compatible.

- * Both union and intersection are commutative.

$$R \cup S = S \cup R \quad \text{and} \quad R \cap S = S \cap R$$

- * Both union and intersection are treated as n-ary operations and are associative.

$$R \cup (S \cap T) = (R \cup S) \cap T \quad \text{and} \quad (R \cap S) \cup T = R \cap (S \cup T)$$

- * The minus, is not commutative.

$$R - S \neq S - R.$$

→ Cartesian (or cross product) operation.

- The cartesian product of 2 relations yields a relation with all possible combinations of the tuples of the 2 relations set operated upon.

- Anoted by a cross (\times)

- The degree of the resultant relation is the sum of the degrees of the 2 relations operated upon.
- The number of tuples (cardinality) of the new relation is the product of the numbers of tuples of the 2 relations.

$$R \times S, |R| = n_R \text{ and } |S| = n_S$$

$$\therefore |R \times S| = n_R \times n_S$$

- The 2 relations need not be type compatible.

* Binary Relational Operations.

→ JOIN (\bowtie) Operation.

- JOIN is denoted as \bowtie , used to combine related tuples from 2 relations into single longer tuples.
- It is important for relational database with more than a single relation, bcoz it allows us to process relationships among relations.
- General form of JOIN operation.

$R(A_1, A_2, \dots, A_n)$ and $S(B_1, B_2, \dots, B_m)$ is

$$R \bowtie_{\langle \text{join condition} \rangle} S$$

- Result of JOIN is a relation Q with $n+m$ attributes.

* Difference b/w Cartesian Product & JOIN.

In JOIN, only combinations of tuples satisfying the join condition appear in the result. whereas in Cartesian Product all combinations of tuples are included.

→ Theta Join.

- Each $\langle \text{condition} \rangle$ is of the form $A_i \theta B_j$
 $A_i \rightarrow$ Attribute of R .
 $B_j \rightarrow$ Attribute of S .
 $\theta \rightarrow$ One of the comparison operator $\{=, <, <=, >, >=, \neq\}$
- JOIN with such general condition is called a Theta JOIN.
- Tuples with NULL join attributes do not appear in the Result.

→ Equi-join Operation. $\bowtie a_i = b_i$

- JOIN operation with equality comparison only.
- In the result we have one or more pair of attributes that have identical values in every tuple.

→ Natural JOIN. $(*)$

- Denoted as $*$
- Natural join requires that the 2 joined attributes have the same name.

Join Selectivity

- Expected size of join result divided by the maximum size $n_R * n_S$.

→ Inner Joins

- Defined formally as a combination of cartesian product and selection

* A complete set of Relational Algebra Operations

- The set operations including σ , π , \cup , \cap , $-$ and \times is called a complete set bcoz any other relational algebra expression can be expressed by a combination of these 5 operations.

* DIVISION Operation

- Denoted by \div
- DIVISION operation is applied to 2 relations $R(Z) \div S(X)$ where the attributes of S are a subset of the attributes of R ; that is $X \subseteq Z$.
- The result of DIVISION is a relation $T(Y)$ that includes a tuple t if tuples t_R appear in R with $t_R[Y] = t$, and with $t_R[X] = t_S$ for every tuple t_S in S . This means that for combination with every tuple in S , a tuple t to appear in the result T of the DIVISION, the values in t must appear in R in combination with every tuple in S .

* Notation For Query Trees.

- A query tree is a tree data structure that corresponds to a relational algebra expression.
- It represents the input relations of query as leaf nodes of the tree.
- It represents the relational algebra operations as internal nodes.
- Also called query expression / evaluation tree.

* Additional Relational Operations.

Generalized Projection

Allows functions of attributes to be included in

the projection list

$\pi_{F_1, F_2, \dots, F_n}(R)$

* Aggregate functions and grouping

- Common functions applied to collections of numeric values.
- Includes sum, Average, Maximum, and minimum. The count function is used for counting tuples or values.
- Use of the functional operator (script F)

$\langle \text{grouping attribute} \rangle \text{ F } \langle \text{function list} \rangle (\text{Table})$

* Left Outer Join

- Denoted by \bowtie
- The LEFT OUTER JOIN operation keeps every tuple in the first, or left, relation R in $R \bowtie S$; if no matching tuple is found in S, then the attributes of S in the join result are filled or padded with NULL values.

* Right Outer Join

- Denoted by \bowtie
- It keeps every tuple in the second, or right, relation S in the result of $R \bowtie S$.

* Full Outer Join

- Denoted by \bowtie
- It keeps all tuples in both the left and right relations with no matching tuples are found, padding them with NULL values as needed.

* The Outer Union Operation

- It takes the union of tuples from 2 relations that have some common attributes, but are not union (type) compatible.