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Statistic Model to Analyze Student’s Performance

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# Introduction

Academic success is important because it is strongly connected to the positive outcomes we value. Students who are academically successful and with high levels of education are more likely to get employed, have stable and better job, have more employment opportunities than those who with less education. Especially, academically successful adolescents have higher self-esteem, have lower level of depression and anxiety, and are less likely to abuse alcohol and engage in substance abuse.

In our final project for Data 603 - Statistical Modelling with Data, we have tried to develop a model to analyze the impact of various demographic and social factors on the performance of students. Academic performance, though it is not the only factor but is one of the crucial factors in shaping a student's future. To get into a good collage/university, student must score grades in school, a good college can lead a better future and economic stability. So, to secure good grades, getting into a great school is enough? Is there something more than a great school that can help a student to perform better? Do the social and demographic factors plays any role in student's performance? In our project we are trying to answer these questions.

Our project aims to study the internal and external factors that influence student performance using the given dataset based on the questions above. Also, we will identify and evaluate the factors that have a significant impact on student’s final grade. Finally, we will predict the student’s final grade based on the significant factors found by modeling process.

# Methodology

### Data Source

We found our datasets for our regression analysis from UC Irvine Machine Learning Repository which is a website is providing a collection of databases, domain theories, and data generators for the analysis of machine learning algorithms. Data attributes include student grades, demographic, social and school related feature. The two datasets we downloaded are provided regarding the performance in two distinct subjects: Mathematics and Portuguese language. Since we didn’t have to analyze our data by the subject, we combined those two datasets into one dataset and used it as a simple.

### Variable Explanations and Data Assumptions

The dataset we are working with is collected during 2005-2006 at 2 Portuguese schools for Mathematics and Portuguese subject. In Portugal, the secondary education consists of 3 years of schooling, preceding 9 years of basic education and followed by higher education. Most of the students join the public and free education system and there are several courses that share core subjects as the Portuguese Language and Mathematics. A 20-point grading scales is used, where 0 is the lowest grade and 20 is the highest score. During the school year, students are evaluated in three periods and the last evaluation G3 corresponds to the final grade. There are closed questions related to several demographic (e.g. mother’s education, family income), social/emotional (e.g. alcohol consumption) and school related variables (e.g. number of past class failure) that were expected to affect student performance.

In our dataset, most attributes are ordinal variables (e.g. In mother’s education, numeric: 0 - none, 1 - primary education (4th grade), 2 - 5th to 9th grade, 3 - secondary education or 4 - higher education). We considered these variables as qualitative data.

There are 649 rows instances and 30 features in the dataset. The following table is a complete list of variables used in our modeling process.

|  |  |  |  |
| --- | --- | --- | --- |
| **Variable Name** | **Description** | **Scale** | **Type** |
| school | student's school | binary: 'GP' - Gabriel Pereira or 'MS' - Mousinho da Silveira | Qualitative |
| sex | student's sex | binary: 'F' - female or 'M' - male | Qualitative |
| age | student's age | numeric: from 15 to 22 |  |
| address | student's home address type | binary: 'U' - urban or 'R' - rural | Qualitative |
| famsize | family size | binary: 'LE3' - less or equal to 3 or 'GT3' - greater than 3 | Qualitative |
| Pstatus | parent's cohabitation status | binary: 'T' - living together or 'A' - apart | Qualitative |
| Medu | mother's education | numeric: 0 - none, 1 - primary education (4th grade), 2 - 5th to 9th grade, 3 - secondary education or 4 - higher education | Qualitative |
| Fedu | father's education | numeric: 0 - none, 1 - primary education (4th grade), 2 - 5th to 9th grade, 3 - secondary education or 4 - higher education | Qualitative |
| Mjob | mother's job | nominal: 'teacher', 'health' care related, civil 'services' (e.g. administrative or police), 'at\_home' or 'other' | Qualitative |
| Fjob | father's job | nominal: 'teacher', 'health' care related, civil 'services' (e.g. administrative or police), 'at\_home' or 'other' | Qualitative |
| reason | reason to choose this school | nominal: close to 'home', school 'reputation', 'course' preference or 'other' | Qualitative |
| guardian | student's guardian | nominal: 'mother', 'father' or 'other' | Qualitative |
| traveltime | home to school travel time | numeric: 1 - <15 min., 2 - 15 to 30 min., 3 - 30 min. to 1 hour, or 4 - >1 hour | Qualitative |
| studytime | weekly study time | (Numeric: 1 - <2 hours, 2 - 2 to 5 hours, 3 - 5 to 10 hours, or 4 - >10 hours | Qualitative |
| failures | number of past class failures | numeric: n if 1<=n<3, else 4 | Qualitative |
| schoolsup | extra educational support | binary: yes or no | Qualitative |
| famsup | family educational support | binary: yes or no | Qualitative |
| paid | extra paid classes within the course subject (Math or Portuguese) | binary: yes or no | Qualitative |
| activities | extra-curricular activities | binary: yes or no | Qualitative |
| nursery | attended nursery school | binary: yes or no | Qualitative |
| higher | wants to take higher education | binary: yes or no | Qualitative |
| internet | Internet access at home | binary: yes or no | Qualitative |
| romantic | with a romantic relationship | binary: yes or no | Qualitative |
| famrel | quality of family relationships | numeric: from 1 - very bad to 5 - excellent | Qualitative |
| freetime | free time after school | numeric: from 1 - very low to 5 - very high | Qualitative |
| goout | going out with friends | numeric: from 1 - very low to 5 - very high | Qualitative |
| Dalc | workday alcohol consumption | numeric: from 1 - very low to 5 - very high | Qualitative |
| Walc | weekend alcohol consumption | numeric: from 1 - very low to 5 - very high | Qualitative |
| health | current health status | numeric: from 1 - very bad to 5 - very good | Qualitative |
| absences | number of school absences | numeric: from 0 to 93 | Quantitative |
| G1 | first period grade | numeric: from 0 to 20 | Quantitative |
| G2 | second period grade | numeric: from 0 to 20 | Quantitative |
| G3 | final grade | numeric: from 0 to 20, output target | Quantitative |

**Table 1**

There are three different scores for student performance in the dataset (see Table). We used the final grade G3 as the dependent variable, so we dropped G1 and G2, and then used the remaining variables as independent variables for our analysis. We assumed that a student’s gender, age, address, availability of internet, and family size would not affect a student’s final grade. However, we are expecting that there would be positive affect on parent’s education level, parent’s job, study hours, school support, family education support, and extra paid class. Also, we assumed that there is a negative impact on travel time, number of past class failures, romantic, free time after school, going out with friends, alcohol consumption.

### Approach and Workflow

For the project we are going to use the techniques we learn in Data-603 Statistical Modeling with Data. We will build a multi-linear regression model with final grade (G3) as the dependent variable, then we use variable selection techniques to select significant variables and perform hypothesis testing to confirm the significance of the selected variables. Once we have our best additive model, we will check for interaction terms and higher order terms. Once we have our final regression model, we will verify all the assumptions of multi-linear regression model.

Below are the workflow steps we are going to perform:

1. Build full additive model.
2. Use forward selection procedure to find significant variables.
3. Perform F-test to check the model usability.
4. Check for interaction between variables and higher order terms.
5. Check usability of final model
6. Provide final model for G3.
7. Verify assumptions for multi-linear regression model

We plan to approach this analysis using the methods we have learned in Data 603 – Statistical Modeling with Data. We will run a linear regression model to find the best model using all variables and test the variables for multicollinearity. Since we have many variables, we assume that we have high multicollinearity among variables.

Once we are satisfied with our main effects, we will use the individual t-test to check for significant higher-order terms and interactions. We intend to test this model with another F-test

to evaluate if the higher order terms and interactions are significant. Any significant higher-order

or interaction terms will be added to our main effects to produce our final model. Our model will

then test for the following 6 assumptions as shown below:

1. Multi-collinearity test
2. Main Effects Individual T-test
3. Hypothesis Statement for Individual T-tests
4. Hypothesis Statement for Individual T-tests (Interaction Terms)
5. Interaction Term T-tests:
6. Hypothesis Statement for ANOVA Test:
7. Multiple Regression Assumptions

# Result

### Variable Selection Procedures: (Model building)

1. Build full additive model.

First, we want to test a relationship between the response and the set of independent variables. To address the overall question, we will test:

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We can perform this test through ANOVA.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| **Source of variation** | **DF** | **Sum of Square** | **Mean Square** | **F-statistic** | **P-value** |
| Regression | 66 | 4332.5 | 65.6439 | 5.7027 | 2.2e-16 |
| Residual | 977 | 11246 | 11.5107 |  |  |
| Total | 1043 | 15579 |  |  |  |

**Table 2:** ANOVA table Null Model vs Full Model

For overall modeling test, you can see the output of ANOVA table in Appendix I-2 that shows that *Fcals*=5.703 with *df*=66 and (p-value < 2.2e-16 < α=0.05), indicating that we should clearly reject the null hypothesis. In other word, it suggests that at least one of the student performance variables must be related to the final grade.

1. Since we have many variables, we will use forward selection procedure to select significant variables from our full additive model. In forward selection process we use R to perform individual t-test to test below hypothesis:

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From the result of forward selection procedure in Appendix I-3, we could still see some non-significant variables, so we removed these ones and then generate the best additive model in Appendix I-4.

Below table contains significant variables with coefficients, t-value and p-value

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | **Significant variables** | **Coefficient** | **t-value** | **p-value** |
| 1 | failures | -1.82887 | -10.595 | < 2e-16 \*\*\* |
| 2 | higheryes | 1.54720 | 3.732 | 0.000200 \*\*\* |
| 3 | studytime2 | 0.26960 | 1.030 | 0.303179 |
| 4 | studytime3 | 1.18603 | 3.346 | 0.000849 \*\*\* |
| 5 | studytime4 | 0.62526 | 1.272 | 0.203738 |
| 6 | schoolsupyes | -1.16127 | -3.392 | 0.000721 \*\*\* |
| 7 | Dalc2 | -0.73721 | -2.577 | 0.010107 \* |
| 8 | Dalc3 | -0.14301 | -0.315 | 0.753108 |
| 9 | Dalc4 | -1.65491 | -2.367 | 0.018107 \* |
| 10 | Dalc5 | 0.11089 | 0.155 | 0.877041 |
| 11 | health2 | -0.66440 | -1.540 | 0.123946 |
| 12 | health3 | -1.21726 | -0.38251 | 0.001505 \*\* |
| 13 | health4 | -0.74820 | -1.870 | 0.061751 . |
| 14 | health5 | -0.99991 | -2.882 | 0.004038 \*\* |
| 15 | romanticyes | -0.59306 | -2.574 | 0.010190 \* |
| 16 | famsizeLE3 | 0.48561 | 2.040 | 0.041625 \* |
| 17 | goout2 | 1.15597 | 2.460 | 0.014070 \* |
| 18 | Goout3 | 0.67978 | 1.482 | 0.138527 |
| 19 | Goout4 | 0.38442 | 0.800 | 0.423919 |
| 20 | Goout5 | 0.08698 | 0.173 | 0.862617 |

**Table 3:** lm(G3 ~ (failures+higher+studytime+schoolsup+Dalc+health+romantic+famsize+goout), data = studentDataset)

Using the above table, our final additive model is shown below:

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This result tells you that there is a positive impact of higheryes (students desire to go for higher study.), study time, family size, going out with friends have a positive, but there is a negative impact on the number of past course failure, school support, alcohol consumption, current health status, and a romantic relationship.

1. We can compare the residual squared error (RSE) and Adjusted R2 of Full Model and our Fina Additive Model.

|  |  |  |
| --- | --- | --- |
| Model | RSE | Adjusted R2 |
| Full Model | 3.393 | 0.2293 |
| Final Additive Model | 3.449 | 0.2036 |

The Adjusted R2 has decreased which mean that the final model has lost some prediction power. But it is better to have less Adjusted R2 value than over-fitting the model.

1. After deciding our final additive model, we can check for interaction term between variables. From the summary of our full interaction model (Appendix I-5), we can see that all the interaction terms are significant.
2. Since we have finalized our interaction model, we can check for higher order term for our quantitative variables. For this we can pairs plot to see if there is any visual clue to indicate the higher order term.

A diagram of a graph

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1. Though there is no clear visual indication that we should add higher order term for our variable, but we can still try by adding the higher order term and check the significance. Referring to the summary of our second order model (Appendix I-6) we can see that the second order term for *failure* is significant. Comparing the RSE and Adjusted R2 for the interaction model and higher order model.

|  |  |  |
| --- | --- | --- |
| **Model** | **RSE** | **Adjusted R2** |
| Interaction Model | 3.398 | 0.22271 |
| Higher Order Model | 3.373 | 0.2384 |

We can clearly see that the Adjusted R2 is increased which is a good thing. Hence we can select our higher order model as the final model.

1. We conducted a final ANOVA test to ensure that interaction model with higher order term is significant in the presence of interaction variables. Thus, we compared the interaction model with the interaction model with higher order term. Table 3 below shows the result of the partial F-test.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| **Source of variation** | **DF** | **Sum of Square** | **Mean Square** | **F-statistic** | **P-value** |
| Regression | 1 | 178.24 | 178.24 | 15.668 | 8.087e-05 |
| Residual | 989 | 11250 | 11.3751 |  |  |
| Total | 990 | 11429 |  |  |  |

**Table 4**: ANOVA table (interaction model vs interaction model with higher order terms)

As you see Table 4, p-value that is 8.087e-05<0.05 indicating that we should reject the null hypothesis. So, we chose the interaction model with higher order terms in the presence of interaction variables.

After then, we compared the best additive model with the interaction model with higher order term. Table 3 below shows the result of the partial F-test.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| **Source of variation** | **DF** | **Sum of Square** | **Mean Square** | **F-statistic** | **P-value** |
| Regression | 34 | 918.55 | 27.0162 | 2.375 | 2.008e-05 |
| Residual | 989 | 11250 | 11.3751 |  |  |
| Total | 1023 | 12169 |  |  |  |

**Table 5**: ANOVA table (best additive model vs interaction model with higher order terms)

As you see Table 3, p-value that is <2.008e-05<0.05 indicating that we should reject the null hypothesis. So, we also chose the interaction model with higher order terms in the presence of interaction variables.

1. Provide final model for G3.

From the interaction model with higher order terms, we can see coefficient, t-value, and p-value for each significant variable in below table.

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | **Significant variables** | **Coefficient** | **t-value** | **p-value** |
|  | failures | -3.8453 | -7.851 | 1.07e-14 \*\*\* |
|  | I(failures^2) | 0.7576 | 3.958 | 8.09e-05 \*\*\* |
|  | higheryes | 1.4940 | 3.639 | 0.000288 \*\*\* |
|  | studytime2 | 2.5596 | 2.285 | 0.022504 \* |
|  | studytime3 | 7.4010 | 3.514 | 0.000462 \*\*\* |
|  | studytime4 | -1.7682 | -0.803 | 0.422394 |
|  | schoolsupyes | 0.4547 | 0.306 | 0.760012 |
|  | Dalc2 | -0.7863 | -2.727 | 0.006511 \*\* |
|  | Dalc3 | 0.1068 | 0.234 | 0.814862 |
|  | Dalc4 | -1.3768 | -1.975 | 0.048525 \* |
|  | Dalc5 | 0.2097 | 0.283 | 0.777071 |
|  | health2 | 0.7798 | 0.916 | 0.360150 |
|  | health3 | -0.9041 | -1.203 | 0.229152 |
|  | health4 | 0.2467 | 0.321 | 0.747981 |
|  | health5 | -0.4384 | -0.675 | 0.499822 |
|  | romanticyes | -0.59306 | -2.574 | 0.010190 \* |
|  | famsizeLE3 | 0.48561 | 2.040 | 0.041625 \* |
|  | goout2 | 1.15597 | 2.460 | 0.014070 \* |
|  | Goout3 | 0.67978 | 1.482 | 0.138527 |
|  | Goout4 | 0.38442 | 0.800 | 0.423919 |
|  | Goout5 | 0.08698 | 0.173 | 0.862617 |
|  | failures:schoolsupyes | 1.4629 | 2.773 | 0.005665 \*\* |
|  | studytime2:health2 | -2.2138 | -2.182 | 0.029361 \* |
|  | studytime3:health2 | -1.4987 | -0.922 | 0.356618 |
|  | studytime4:health2 | 0.2277 | 0.111 | 0.911696 |
|  | studytime2:health3 | -0.5703 | -0.627 | 0.530916 |
|  | studytime3:health3 | -1.9426 | -1.360 | 0.174180 |
|  | studytime4:health3 | -1.1523 | -0.743 | 0.457822 |
|  | studytime2:health4 | -1.4005 | -1.492 | 0.135926 |
|  | studytime3:health4 | -2.7377 | -1.897 | 0.058132 |
|  | studytime4:health4 | -2.1322 | -1.039 | 0.299055 |
|  | studytime2:health5 | -0.6203 | -0.779 | 0.436179 |
|  | studytime3:health5 | -2.3509 | -1.742 | 0.081736 |
|  | studytime4:health5 | -0.2144 | -0.137 | 0.891296 |
|  | studytime2:goout2 | -1.1239 | -1.066 | 0.286582 |
|  | studytime3:goout2 | -4.2356 | -2.345 | 0.019244 \* |
|  | studytime4:goout2 | 4.9803 | 2.287 | 0.022411 \* |
|  | studytime2:goout3 | -1.3213 | -1.287 | 0.198229 |
|  | studytime3:goout3 | -3.9000 | -2.190 | 0.028790 \* |
|  | studytime4:goout3 | 3.3769 | 1.517 | 0.129630 |
|  | studytime2:goout4 | -1.8888 | -1.793 | 0.073252 . |
|  | studytime3:goout4 | -5.1949 | -2.719 | 0.006670 \*\* |
|  | studytime4:goout4 | 1.8847 | 0.696 | 0.486475 |
|  | studytime2:goout5 | -1.7584 | -1.618 | 0.106088 |
|  | studytime3:goout5 | -3.2727 | -1.636 | 0.102214 |
|  | studytime4:goout5 | 2.3971 | 1.094 | 0.274432 |
|  | schoolsupyes:health2 | 2.3211 | 1.642 | 0.100989 |
|  | schoolsupyes:health3 | 2.3842 | 1.892 | 0.058844 . |
|  | schoolsupyes:health4 | 2.9360 | 2.304 | 0.021438 \* |
|  | schoolsupyes:health5 | 2.9259 | 2.471 | 0.013625 \* |
|  | schoolsupyes:goout2 | -5.5980 | -4.165 | 3.38e-05 \*\*\* |
|  | schoolsupyes:goout3 | -4.5044 | -3.316 | 0.000948 \*\*\* |
|  | schoolsupyes:goout4 | -3.8287 | -2.814 | 0.004993 \*\* |
|  | schoolsupyes:goout5 | -5.5483 | -3.573 | 0.000370 \*\*\* |

**Table 6**

lm(G3 ~ (failures+I(failures^2)+higher+studytime+schoolsup+Dalc+health+romantic+famsize +goout+failures:schoolsup+studytime:health+studytime:goout +schoolsup:health+schoolsup:goout), data = studentDataset)

Since we chose the interaction model with higher order terms as the best fit model for our project, the final model is

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1. Verify assumptions for multi-linear regression model

### Main Effects Individual T-tests:

Assumption Verification

1 Linearity Assumption:

2

3

4

5

6

### Hypothesis Statement for Individual T-tests

### Hypothesis Statement for Individual T-tests (Interaction Terms)

### Interaction Term T-tests:

### Hypothesis Statement for ANOVA Test:

### Multiple Regression Assumptions

1. Linearity Assumption
2. Independence Assumption
3. Normality Assumption
4. Equal Variance Assumption
5. Multicolinearity Tests
6. Influential Points and Outliers
7. Interpreting Coefficients
8. Prediction

# Conclusion

# Discussion

# Appendix I

1. Full model test

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1. ANOVA test between null model and full model

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1. Forward Selection Procedure

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1. Dropping non-significant variables from forward selection process.

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1. Interaction model.

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1. Higher Order

A group of buildings with different colored dots

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1. ANOVA test between interaction model and interaction model with higher order

A computer screen shot of text

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1. ANOVA test between the best additive model and interaction model with higher order.

A computer screen shot of a code

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