Problem B: Secret Polynomial

You may have encountered IQ tests with inane questions such as the following: find the next number in the sequence 1, 2, 3, __. Obviously the correct answer is 16, since the sequence lists the values f(1), f(2), f(3), f(4), ..., where $f(x) = 2x^3 - 12x^2 + 23x - 12$. More generally, given some information about the values of a polynomial, can you find the polynomial? We will restrict our attention to polynomials whose coefficients are all nonnegative integers.

Input Specification

The first line of input contains an integer 0 < n <= 10000, the number of polynomials to be identified. Each of the next n lines contains two integers, the values f(1) and f(f(1)), where f is the polynomial to be found. Each of these values fits within the range of a signed two's complement 32-bit integer.

Sample Input

1 3 5

Output Specification

For each polynomial to be found, output a single line listing its coefficients separated by spaces. Assuming the degree of the polynomial is d, list the d+1 coefficients in descending order of power (i.e. starting with the coefficient of \mathbf{x}^d and finishing with the coefficient of \mathbf{x}^0). If the polynomial is the zero polynomial, just output 0. If no polynomial f has the desired values of f(1) and f(f(1)), instead output a line containing the word IMPOSSIBLE. If multiple polynomials f have the desired values of f(1) and f(f(1)), instead output a line containing the word AMBIGUOUS.

Output for Sample Input

1 2

Ian Goldberg, Ondřej Lhoták



This work is licensed under a <u>Creative Commons Attribution-ShareAlike 3.0 Unported</u> License.