

Problem B: Enumerating Brackets

(AN UNMATCHED LEFT PARENTHESIS
CREATES AN UNRESOLVED TENSION
THAT WILL STAY WITH YOU ALL DAY.

A *balanced bracket sequence* is a string consisting only of the characters "(" (opening brackets) and ")" (closing brackets) such that each opening bracket has a "matching" closing bracket, and vice versa. For example, "(())()" is a balanced bracket sequence, whereas "(())(())" and "()(())" are not.

Given two bracket sequences A and B of the same length, we say that A is *lexicographically smaller than* B (and write $A < B$) if:

1. A and B differ in at least one position, and
2. A has a "(", and B has a ")" in the left-most position in which A and B differ

For example " $(())()$ " $<$ " $()(())$ " because they first differ in the second position from the left, and the first string has an "(" in that position, whereas the second string has a ")". For a given length N , the " $<$ " operator defines an *ordering* on all balanced bracket sequences of length N . For example, the ordering of the sequences of length 6 is:

1. ((()))
2. (())
3. (())
4. () ()
5. () ()

Given a length N and a positive integer M , your task is to find the M^{th} balanced bracket sequence in the ordering.

Input Specification

You will be given an *even* integer N ($2 \leq N \leq 2000$), and a positive integer M . It is guaranteed that M will be no more than 10^{18} and no more than the number of balanced bracket sequences of length N (whichever is smaller).

Output Specification

Output the M^{th} balanced bracket sequence of length N , when ordered lexicographically.

Sample Input

6 4

Output for Sample Input

() (())

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