

## Problem C: Nice Prefixes

Consider strings formed from characters from an alphabet of size  $K$ . For example, if  $K = 4$ , our alphabet might be  $\{a,b,c,d\}$ , and an example string is *bbcac*.

For a string  $S$ , define  $\text{count}(S, k)$  to be the number of occurrences of the symbol  $k$  in  $S$ . For example,  $\text{count}(\text{bbcac}, b) = 2$  and  $\text{count}(\text{bbcac}, a) = 1$ .

A prefix of a string  $S$  is any string obtained from  $S$  by deleting some (possibly none) of the trailing characters of  $S$ . For example, the prefixes of *acb* are the empty string, *a*, *ac*, and *acb*.

A string  $S$  has "nice prefixes" if for every prefix  $P$  of  $S$  and for every two characters  $k_1$  and  $k_2$  in the alphabet,  $|\text{count}(P, k_1) - \text{count}(P, k_2)| \leq 2$ . For example, *bbcac* has nice prefixes, but *abbbc* does not because  $\text{count}(\text{abbb}, b) = 3$  and  $\text{count}(\text{abbb}, c) = 0$ .

Count the number of strings of length  $L$  on an alphabet of size  $K$  that have nice prefixes. This number can be large, so print its remainder when divided by 1000000007.

### Input Specification

The input is a single line containing the two integers  $L$  and  $K$ , separated by spaces, with  $1 \leq L \leq 10^{18}$  and  $1 \leq K \leq 50$ .

### Sample Input

4 2

### Output Specification

Output a single line containing the number of strings of length  $L$  on an alphabet of size  $K$  that have nice prefixes, modulo 1000000007.

### Output for Sample Input

12

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