

# Reading Note: Chapter 2 & 3

Xitong Yang

Dec.23 2015

## 1 Introduction

Chapter 2 & 3 mainly give an introduction about what algorithms are and how to analyze the efficiency of an algorithm. It is important to understand the concept of the "asymptotic notation".

## 2 Key Note

- Use **loop invariant** to prove the correctness of a program. Three steps:  
(1) Initialization: true prior to the first iteration of the loop; (2) Maintenance: if true before an iteration of the loop, remains true before the next iteration; (3) Termination: when the loop terminates, the invariant helps show that the algorithm is correct.
- Asymptotic Notation
  - $f(n) = \Theta(g(n))$ :  $g(n)$  is an asymptotically tight bound for  $f(n)$ , is like  $a = b$ . Formally,  $\Theta(g(n)) = \{f(n) : \text{there exists positive constants } c_1, c_2 \text{ and } n_0 \text{ such that } 0 \leq c_1 g(n) \leq f(n) \leq c_2 g(n) \text{ for all } n \geq n_0\}$
  - $f(n) = O(g(n))$ : asymptotic upper bound, is like  $a \geq b$ .  $O()$  bound on worst-case running time also applies to its running time on *every input (even input is already sorted)*.
  - $f(n) = \Omega(g(n))$ , asymptotic lower bound, is like  $a \leq b$ .
  - $f(n) = o(g(n))$ , asymptotic loose upper bound, is like  $a > b$ .
  - $f(n) = w(g(n))$ , asymptotic loose lower bound, is like  $a < b$ .
  - Not all functions are asymptotically comparable.
- Some maths

### 3 Algorithms

- Insertion sort\* ( $\Theta(n^2)$ )
- Merge sort\* ( $\Theta(n \log n)$ )

\* Sample codes implemented in *Codes* folder