

# Complete Data Science and Machine Learning Using Python

By  
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# What is Calculus?

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- Small pebbles
- Used for counting in Abacus
- Continuous small Change
- One of the most widely used concept in Machine Learning Optimization

# Rate of Change

# Rate of Change

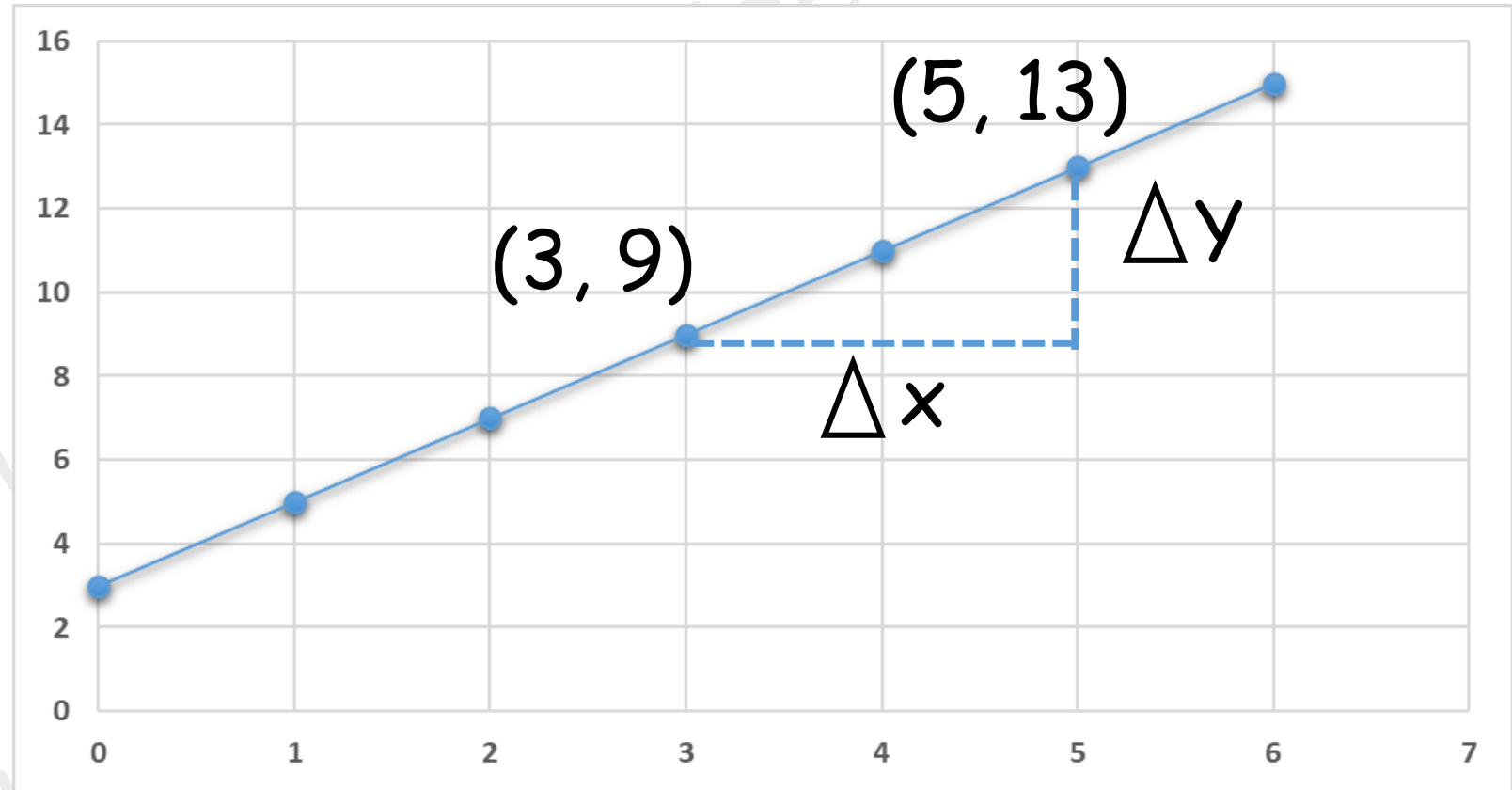
$$y = 2x + 3$$

Rate of Change

$$= \frac{\Delta y}{\Delta x}$$

$$= \frac{13 - 9}{5 - 3}$$

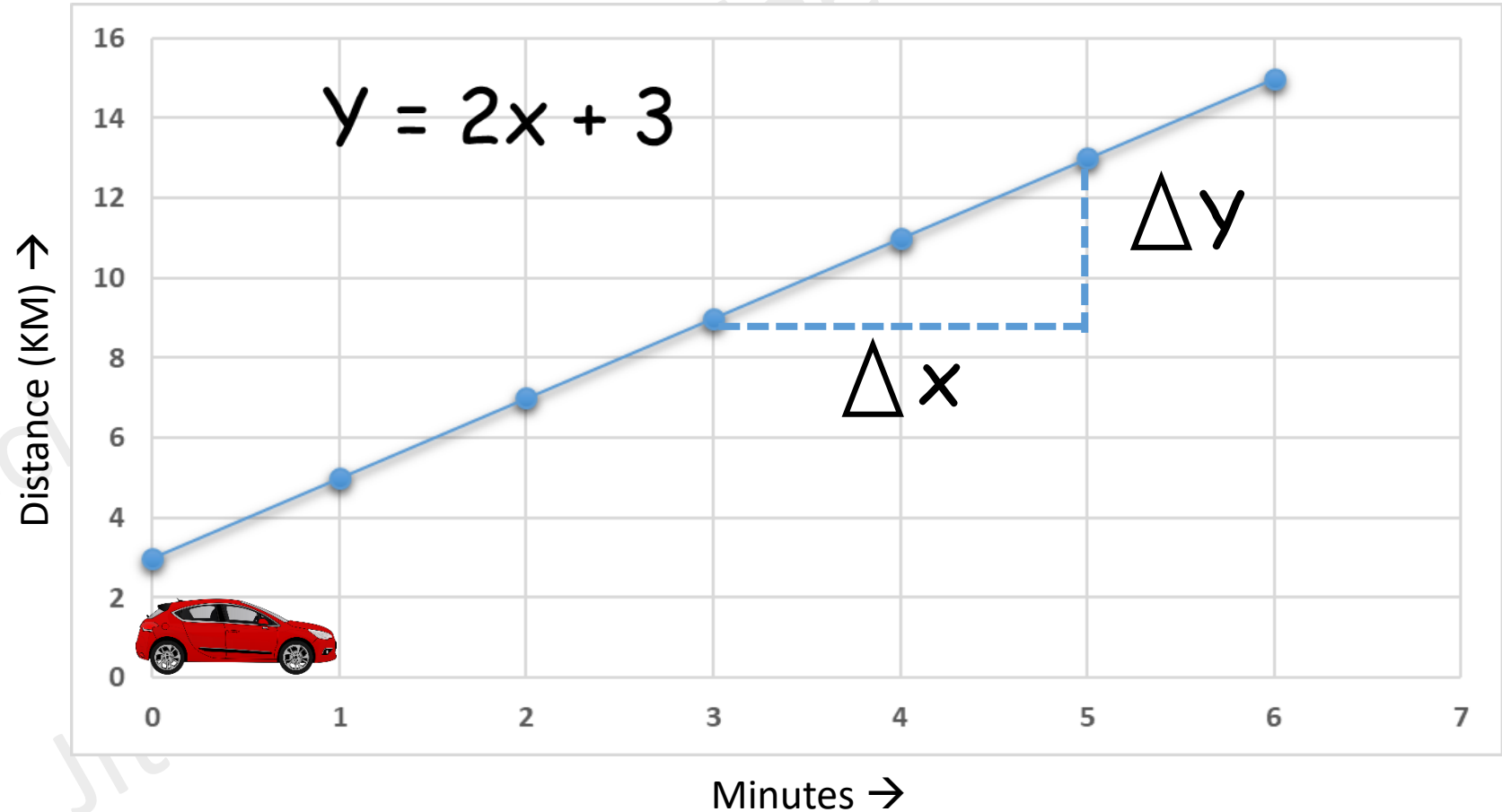
$$= 2$$



# Rate of Change

## Rate of Change

$$\frac{\Delta \text{Distance}}{\Delta \text{Time}}$$
$$= 2\text{KM/minute}$$

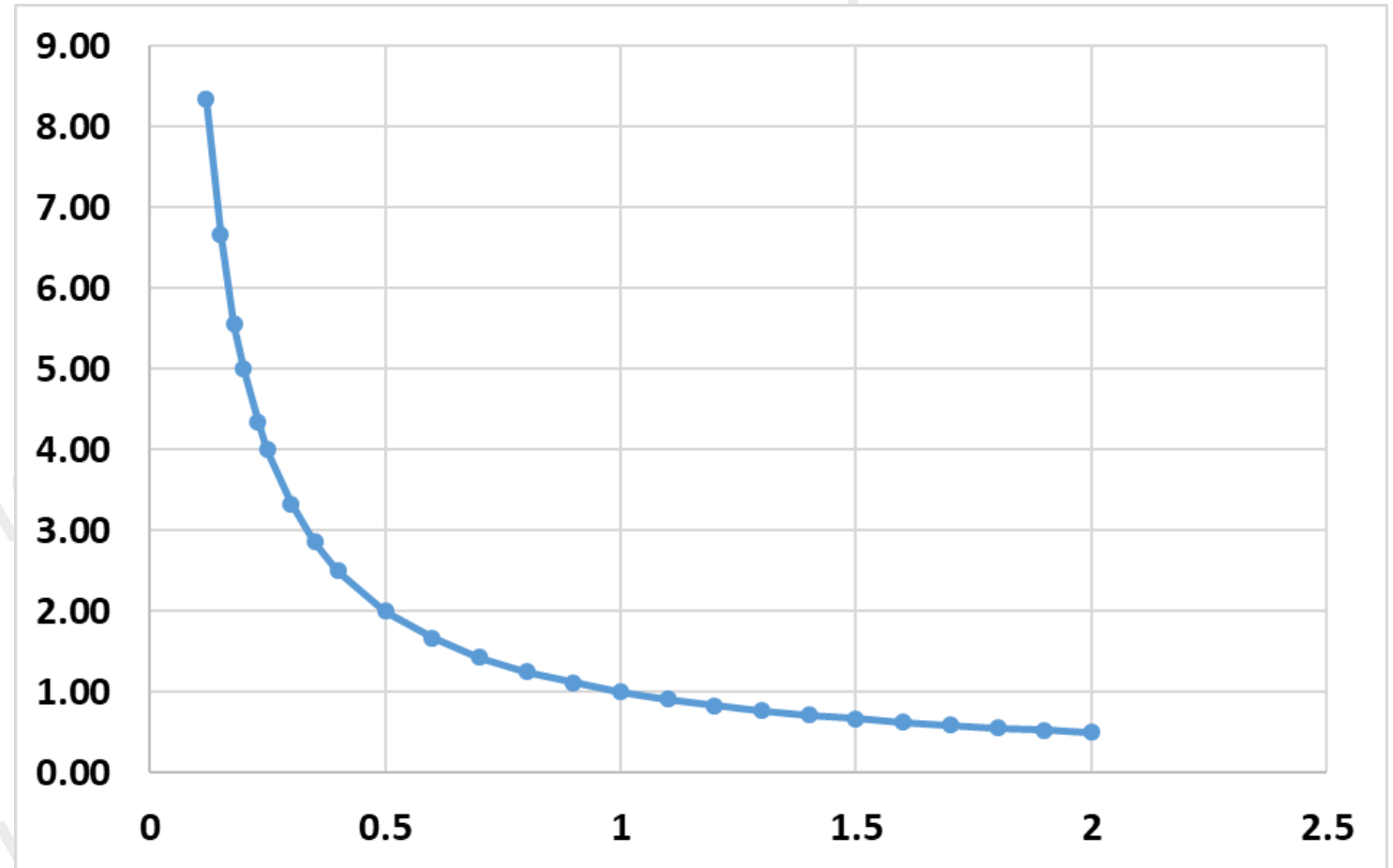


# Limits

# Limits

$$y = 1/x$$

$$x \neq 0$$

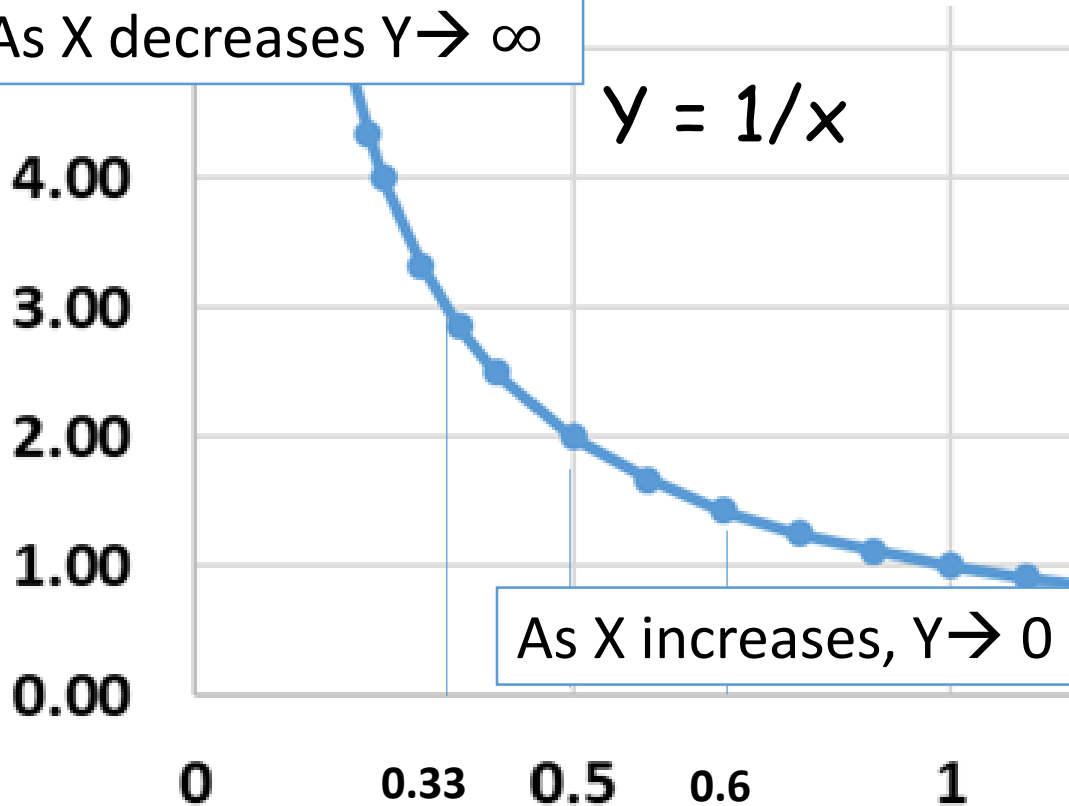


# Limits

As X decreases  $Y \rightarrow \infty$

$$Y = 1/x$$

As X increases,  $Y \rightarrow 0$



X	Y
1	1
10	0.1
100	0.01
1000	0.001
10,000	0.0001
1,000,000	0.000001

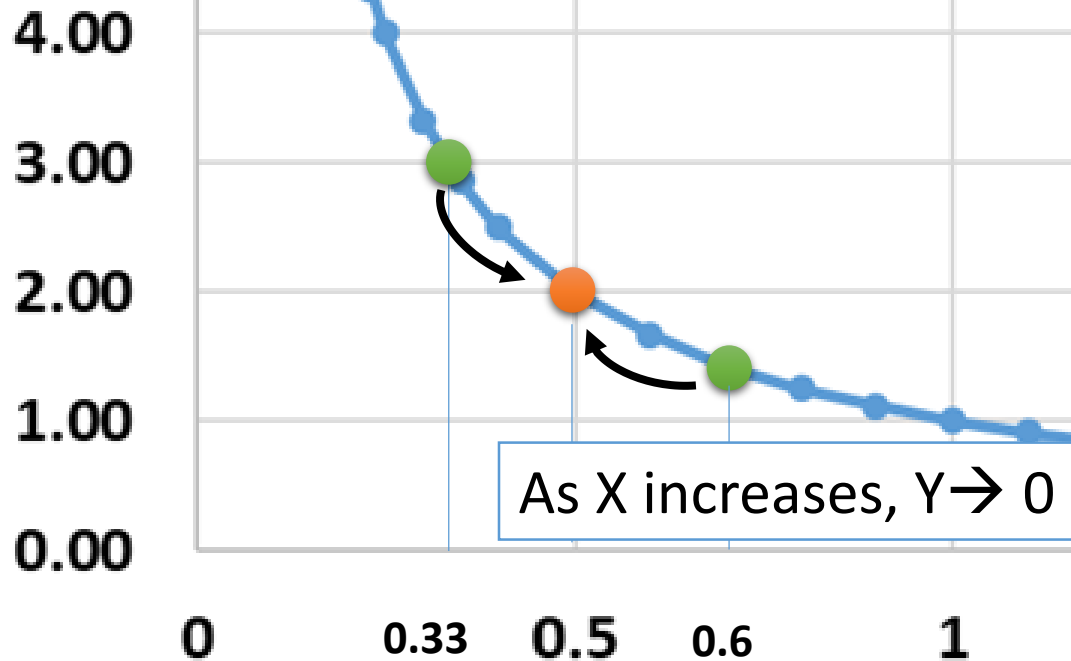
X	Y
1	1
0.5	2
0.01	100
0.001	1000
0.0001	10,000
0.000001	1,000,000



# Limits

As X decreases  $Y \rightarrow \infty$

$$Y = 1/x$$



As X increases,  $Y \rightarrow 0$

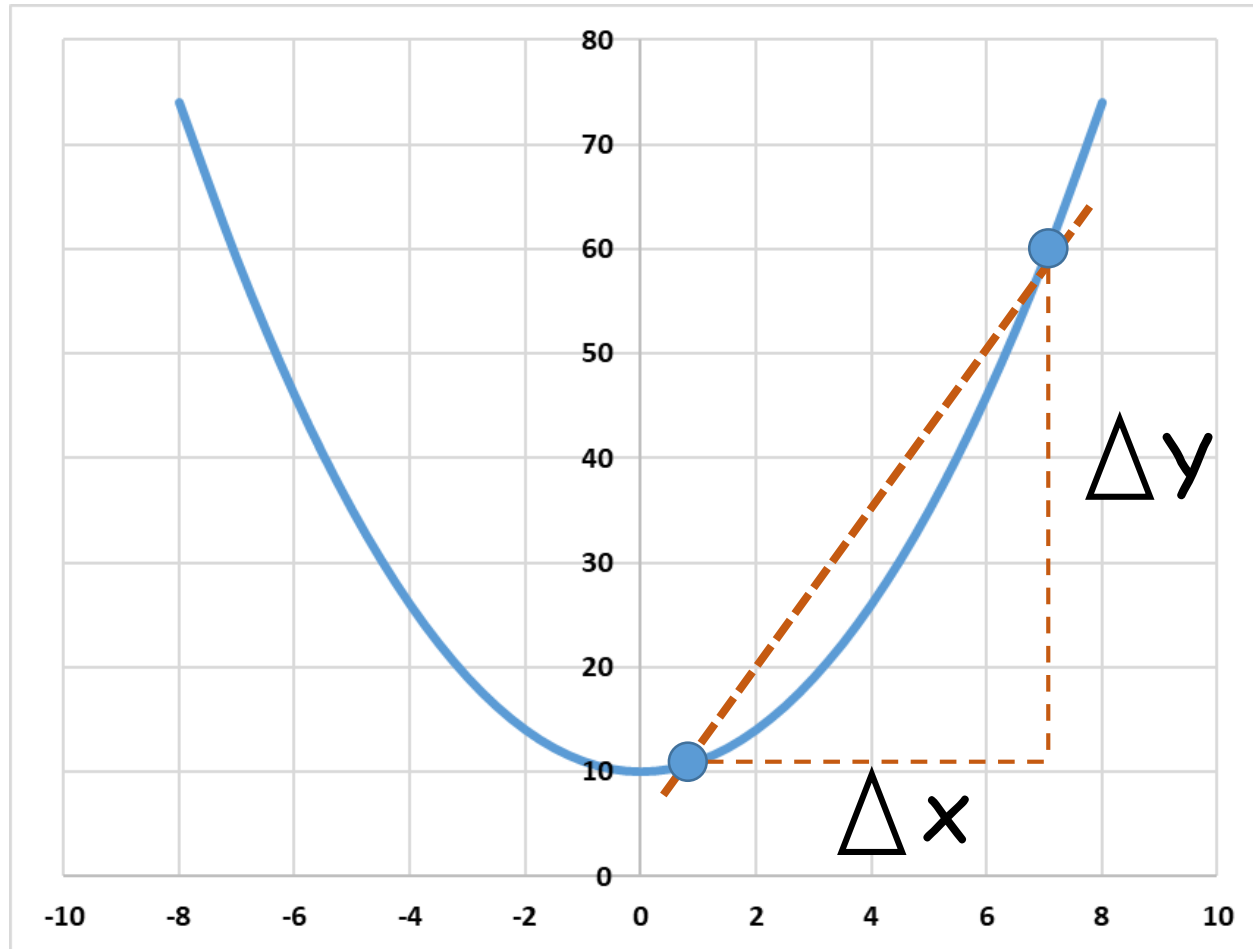
$$\lim_{x \rightarrow 0.5} \frac{1}{x} = 2$$

$$\lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

$$\lim_{x \rightarrow 0} \frac{1}{x} = \infty$$

# Differential Calculus

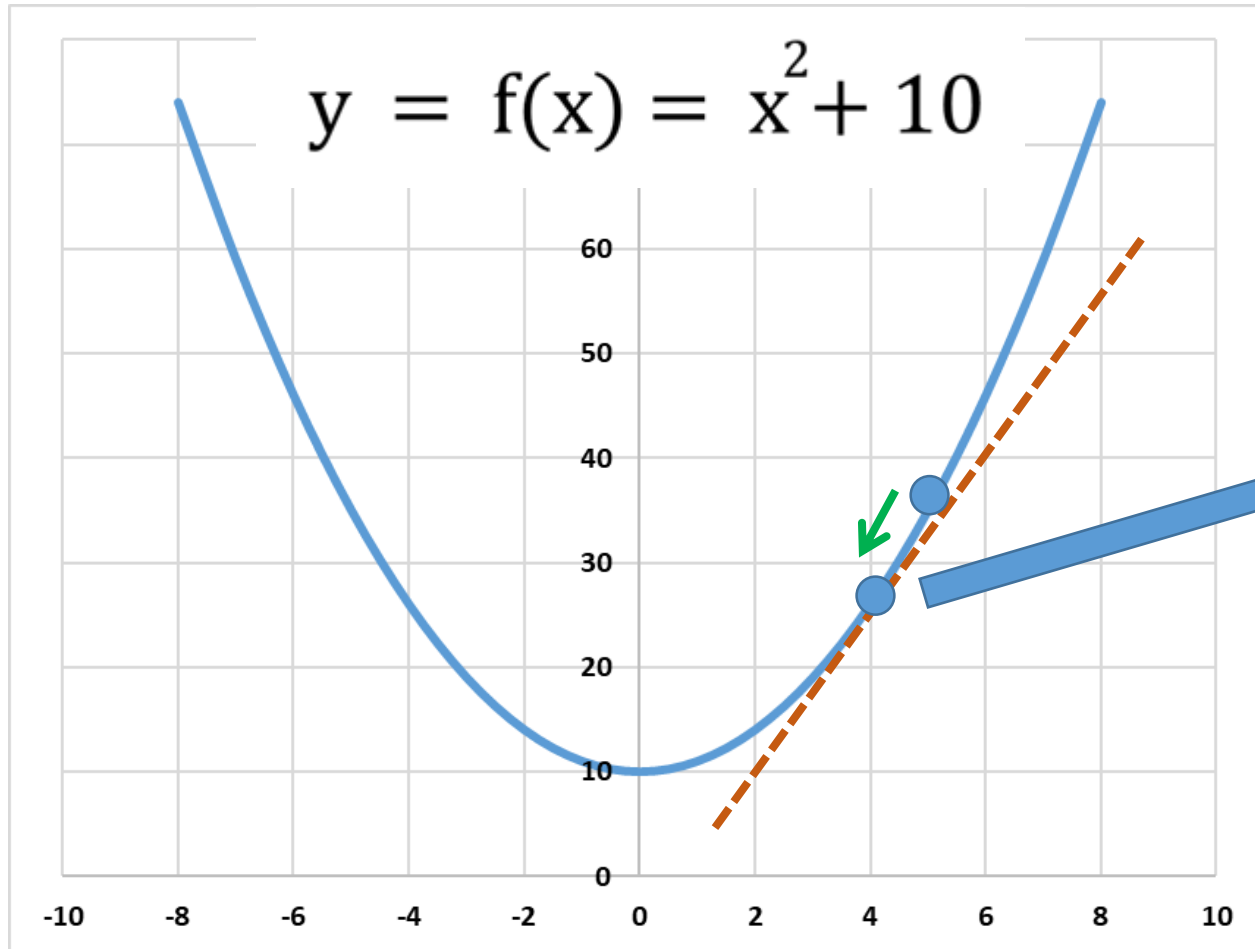
# Slope between two points



Average Slope

$$= \frac{\Delta y}{\Delta x}$$

# Derivative



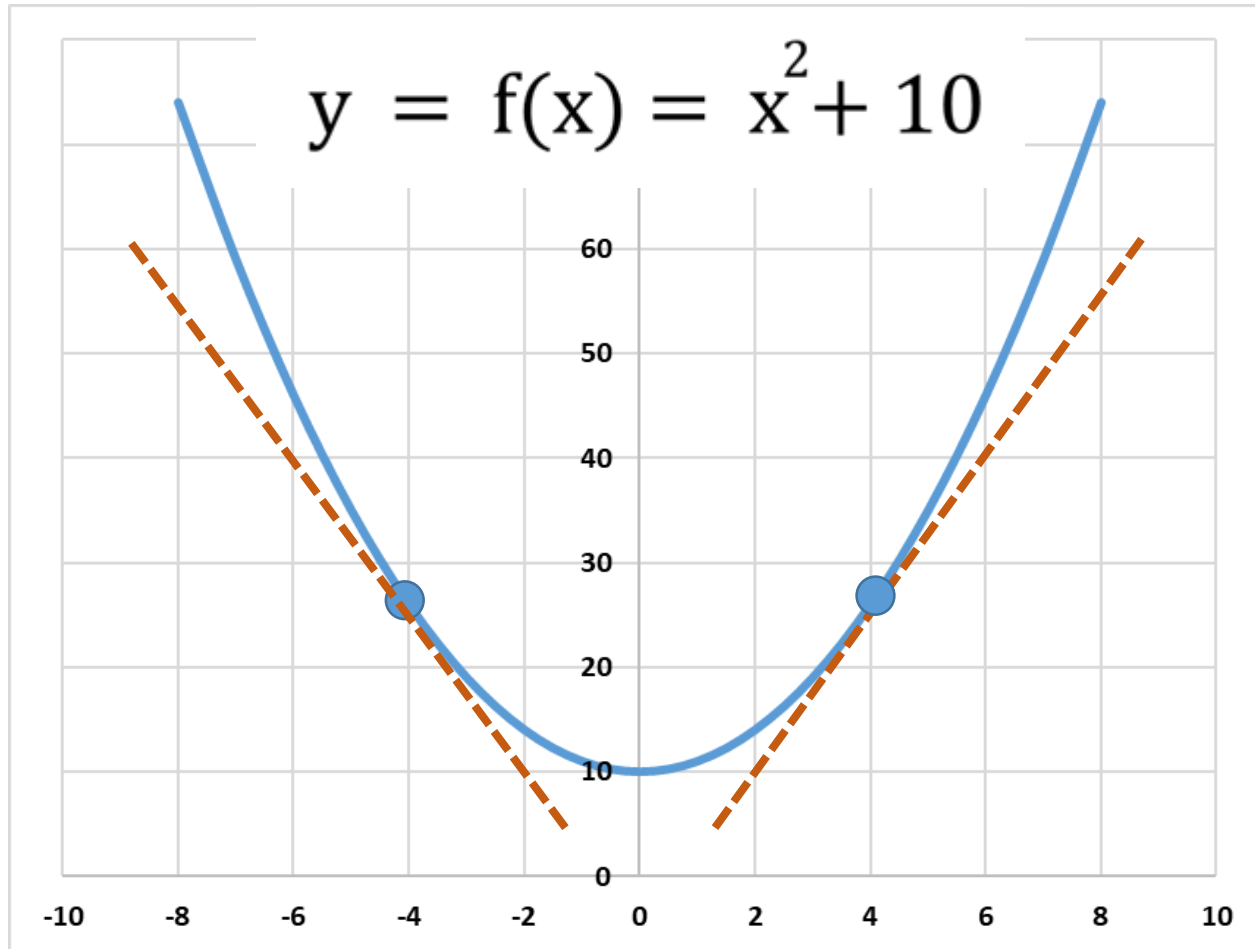
$$\text{Slope} = 2x + \Delta x$$

$$\frac{dy}{dx} = \lim_{\Delta x \rightarrow 0} (2x + \Delta x)$$

0

$$\frac{dy}{dx} = 2x$$

# Derivative



$$\frac{dy}{dx} = 2x$$

①  $x = 4$ ; slope = 8

②  $x = -4$ ; slope = -8

# Differentiability and Rules

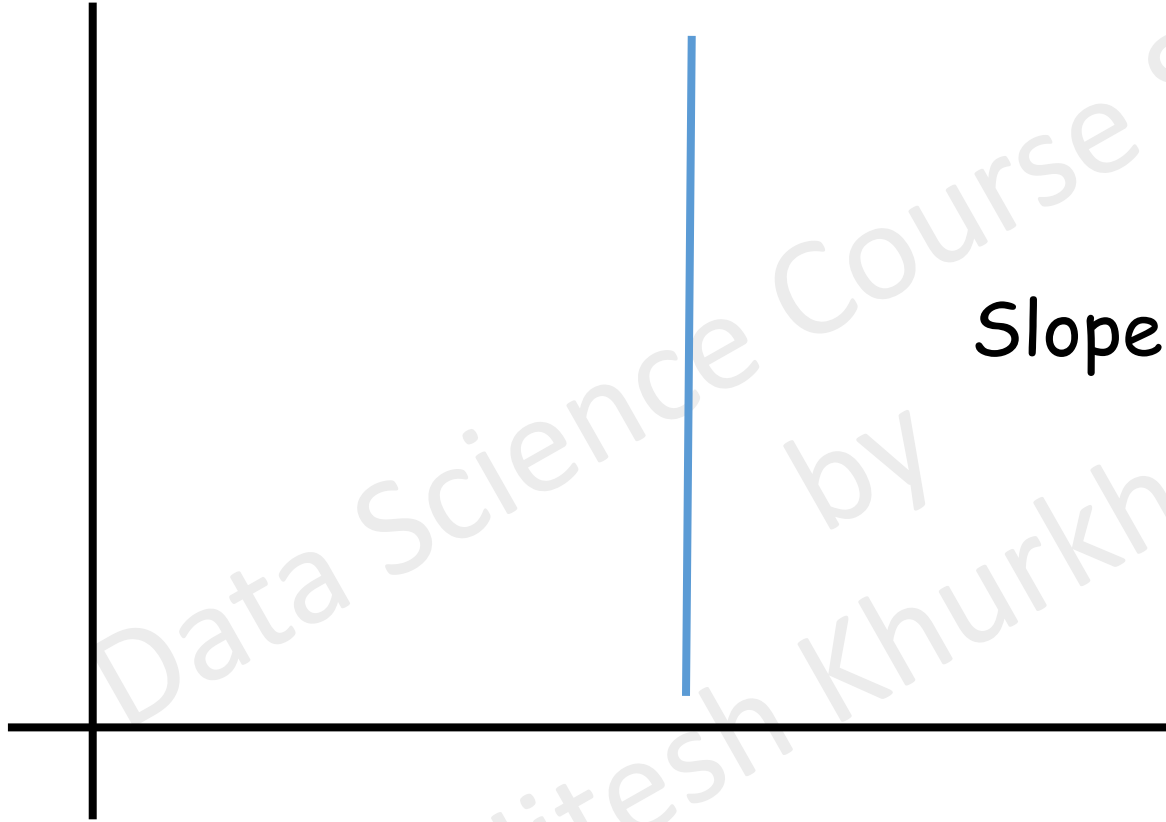
# Derivative rules

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- Derivative of a vertical line
- Derivative of a horizontal line
- Differentiability for various functions
- Power rule of derivative

# Derivative Rules

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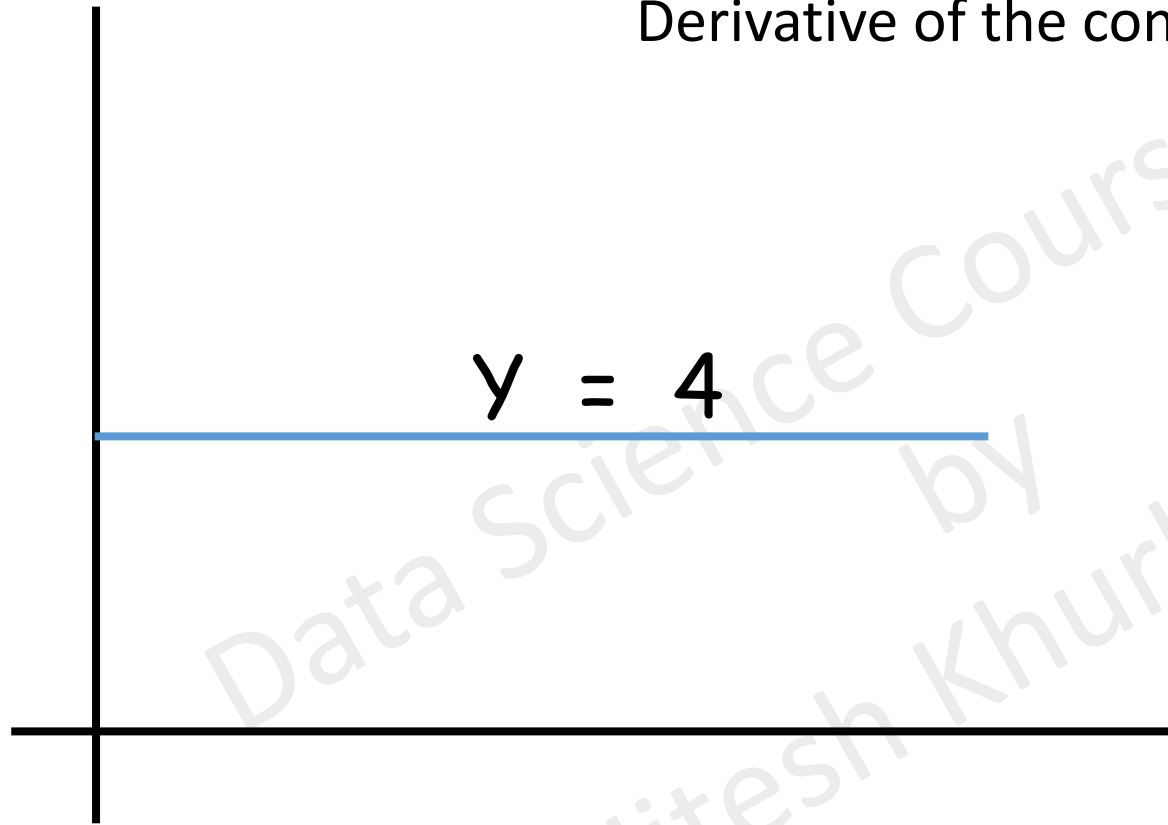
$$\Delta x = 0$$

$$\text{Slope} = \frac{\Delta y}{\Delta x} = \infty \text{ or Undefined}$$



# Derivative Rules – Constant

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Derivative of the constant is ZERO.

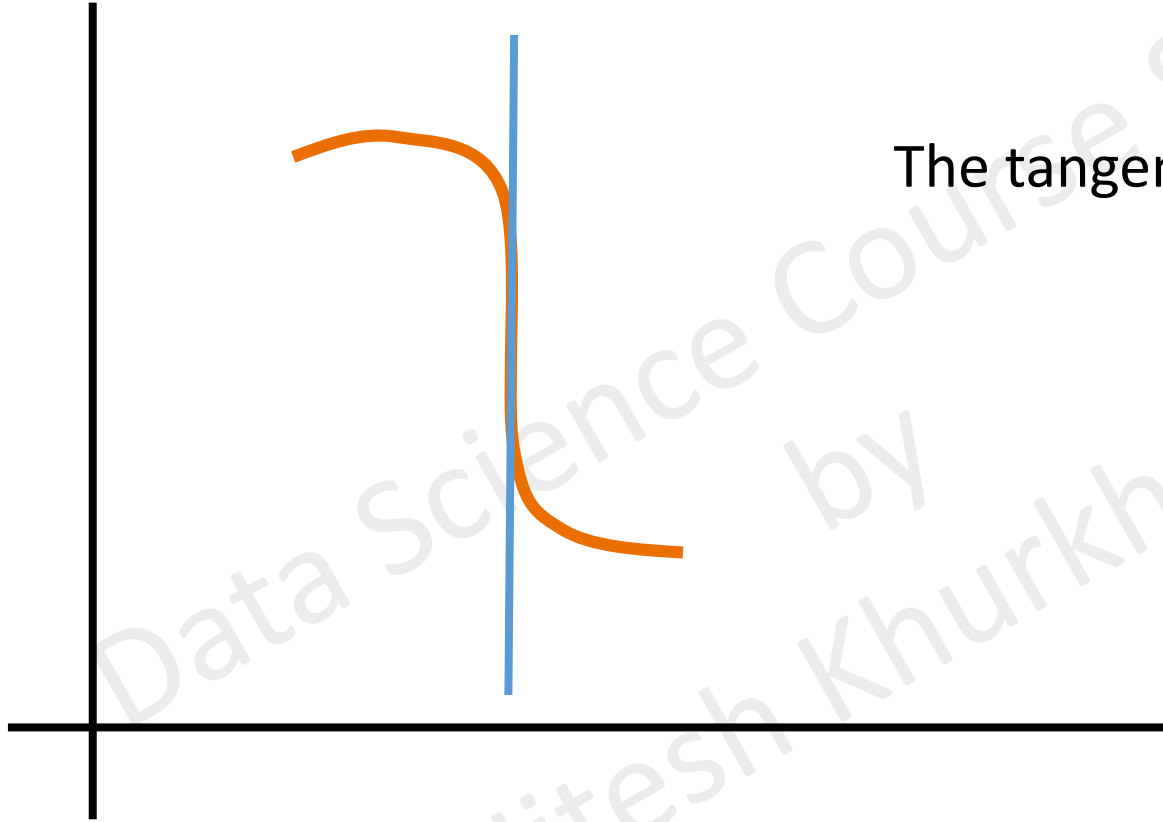
$$\Delta y = 0$$

$$\frac{dy}{dx} = 0$$

$$\frac{d(4)}{dx} = 0$$

# Differentiability

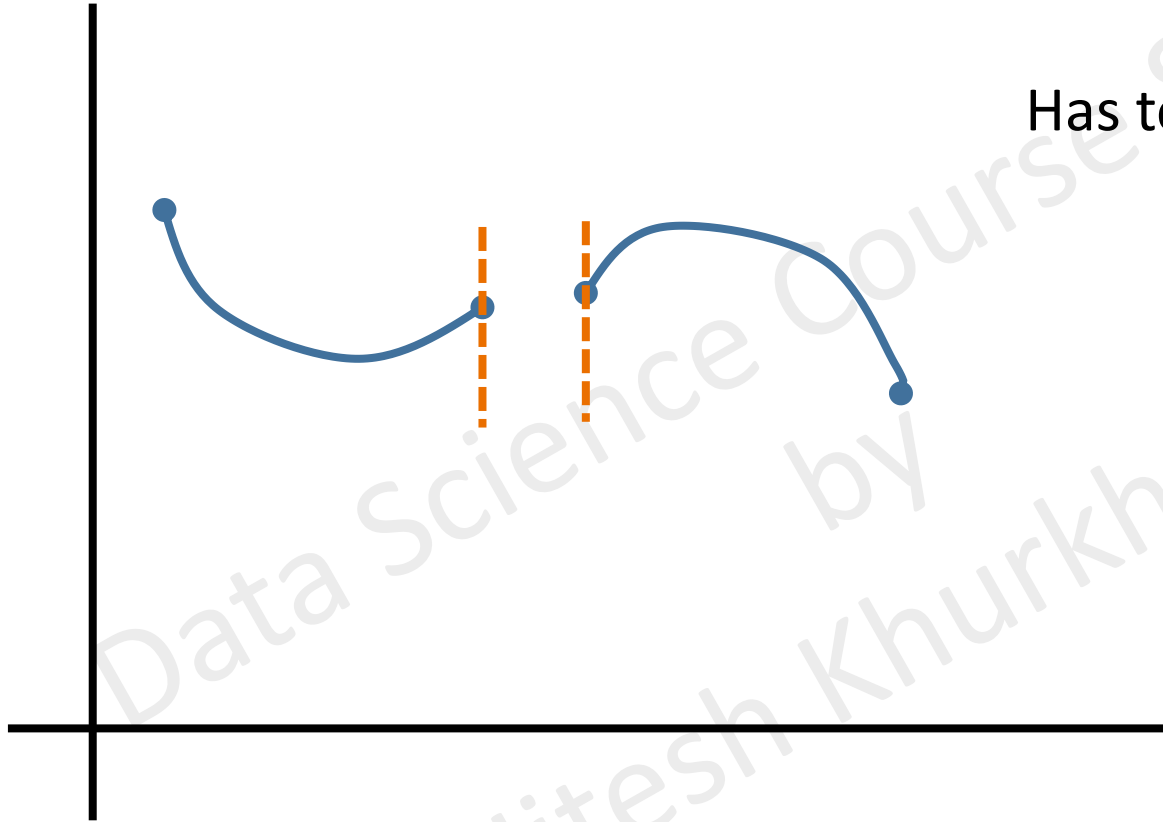
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The tangent line can not be vertical.

# Differentiability

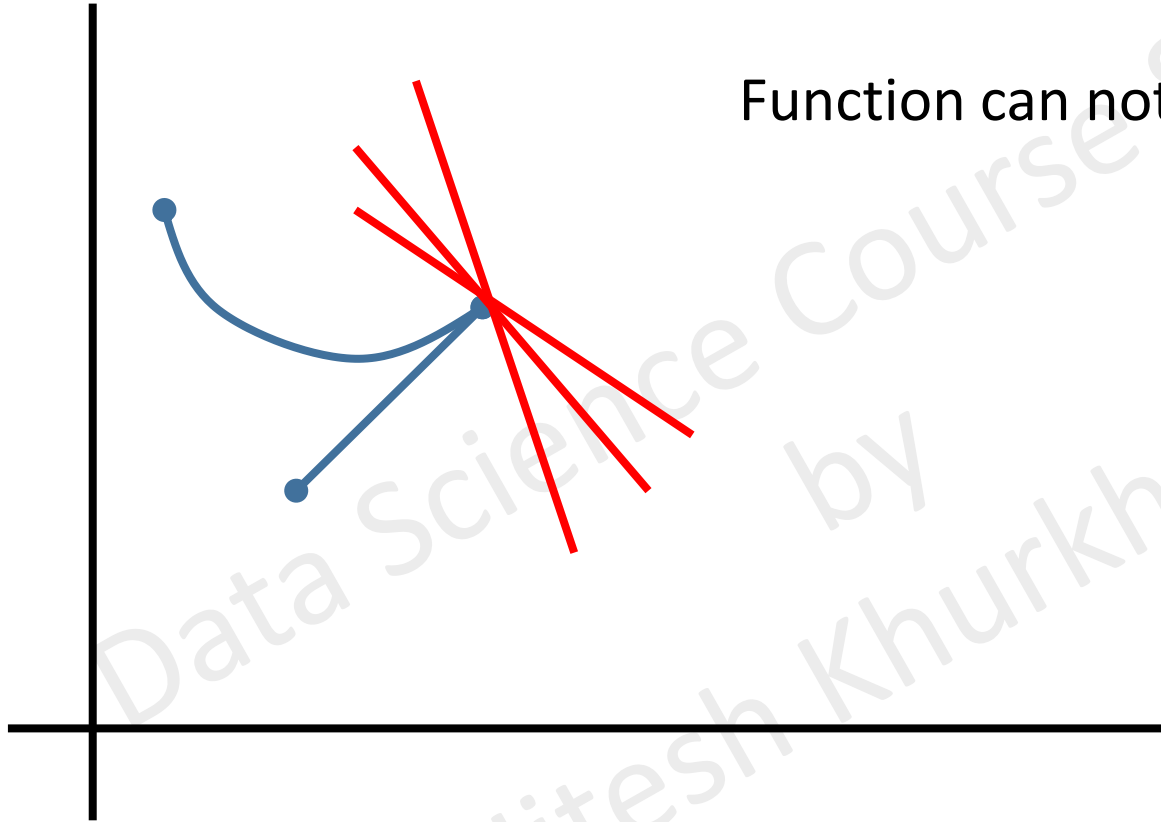
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Has to be a continuous function.

# Differentiability

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Function can not take sudden change in direction.

# Power Rule of Derivative

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$$y = f(x) = ax^n \quad \longrightarrow \quad \frac{dy}{dx} = a \cdot n \cdot x^{n-1}$$

# Power Rule of Derivative

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$$y = f(x) = x^2 + 10 \quad \longrightarrow \quad \frac{dy}{dx} = 2x$$

$$y = f(x) = x^3 + 10 \quad \longrightarrow \quad \frac{dy}{dx} = 3x^2$$

(Original Index \* Original Coefficient)  $\uparrow$

$\swarrow$  (Original Index - 1)

Remove constant

# Power Rule of Derivative

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$$y = f(x) = x^3 + 10$$



$$\frac{dy}{dx}$$

$$= 3x^2$$

(Original Index - 1)

Remove constant

(Original Index \* Original Coefficient)

$$y = f(x) = 2x^3 + 4x^2 - 7x + 9$$



$$\frac{dy}{dx}$$

$$= 6x^2 + 8x - 7$$

# Direction, Maxima and Minima



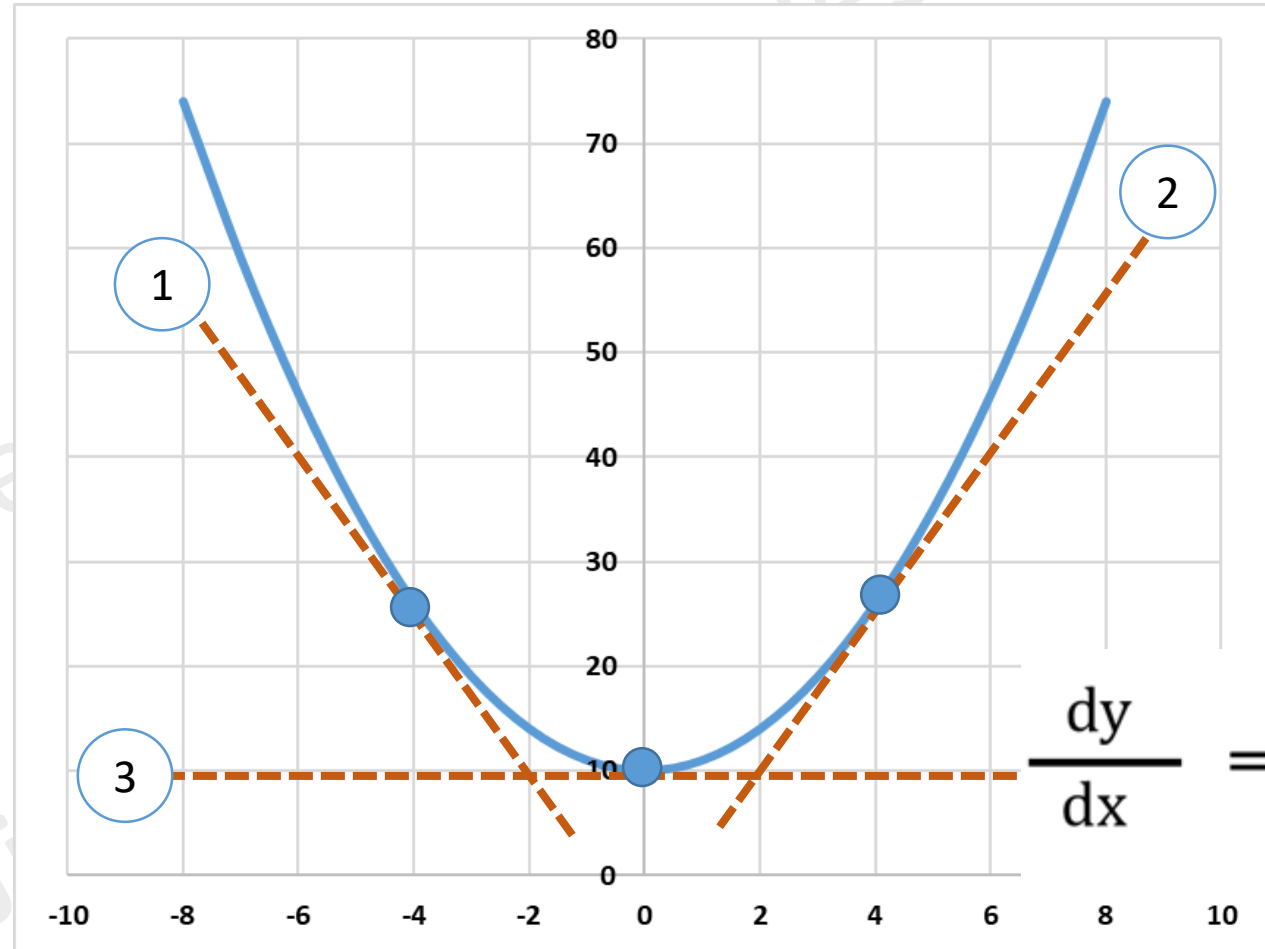
# Derivative for directions

$$y = f(x) = x^2 + 10$$

$$\frac{dy}{dx} = 2x$$

$$\textcircled{1} \quad \frac{dy}{dx} = -8$$

$$\textcircled{2} \quad \frac{dy}{dx} = +8$$



## Second Order Derivative

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$$\frac{d\left(\frac{dy}{dx}\right)}{dx} = \frac{d^2y}{dx^2}$$

## Second Order Derivative

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$$y = f(x) = x^2 + 10 \quad \longrightarrow \quad \frac{dy}{dx} = 2x \quad \longrightarrow \quad \frac{d^2y}{dx^2} = 2$$

$$y = f(x) = -x^2 + 10 \quad \longrightarrow \quad \frac{dy}{dx} = -2x \quad \longrightarrow \quad \frac{d^2y}{dx^2} = -2$$

# Rules for Maxima and Minima

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Second Derivative  $< 0$   Local Maxima

Second Derivative  $> 0$   Local Minima

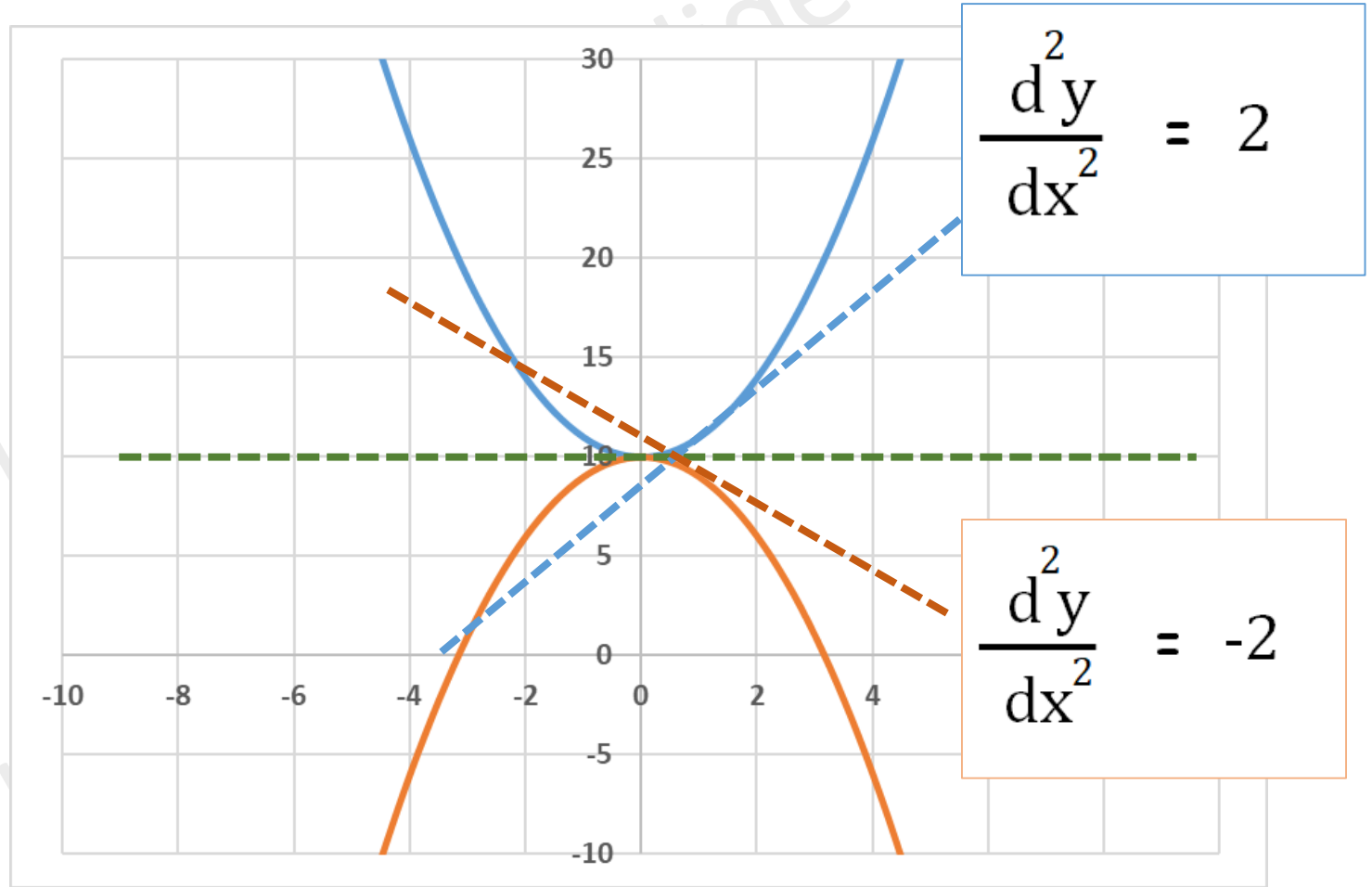
# Maxima or Minima?

$$y = f(x) = x^2 + 10$$

Minima at  $y = 10$

$$y = f(x) = -x^2 + 10$$

Maxima at  $y = 10$



# Derivative for Maxima and Minima

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$$y = 6x^4 - 2x^3 - 12x^2 + x + 1$$

Step 1 – Get the first Derivative

Step 2 – Get the Second Derivative

Step 3 – Identify points where slope is zero

Step 4 – Get the second derivative when slope is zero

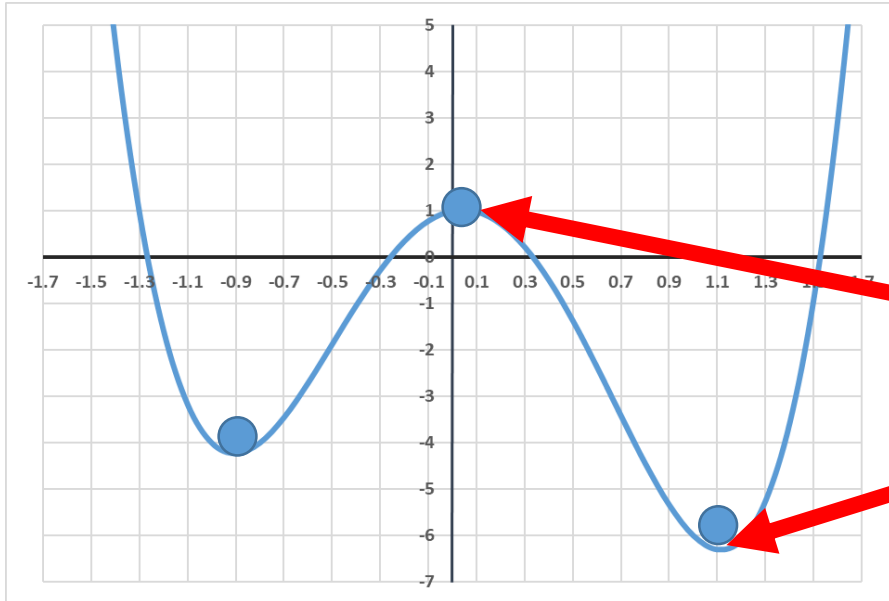
Step 5 – Apply the rules for maxima and minima

# Derivative for Maxima and Minima

$$y = 6x^4 - 2x^3 - 12x^2 + x + 1$$

$$\frac{dy}{dx} = 24x^3 - 6x^2 - 24x + 1$$

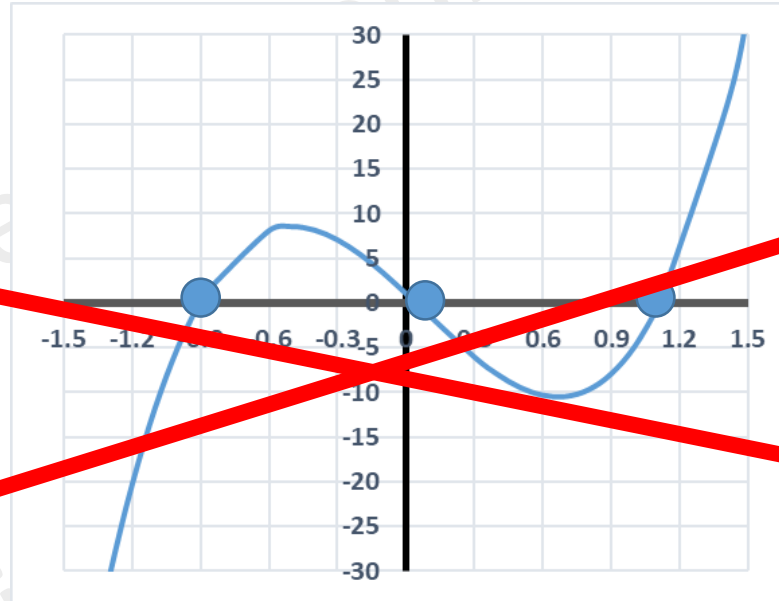
$$\frac{d^2y}{dx^2} = 72x^2 - 12x - 24$$



-0.9054

0.04131

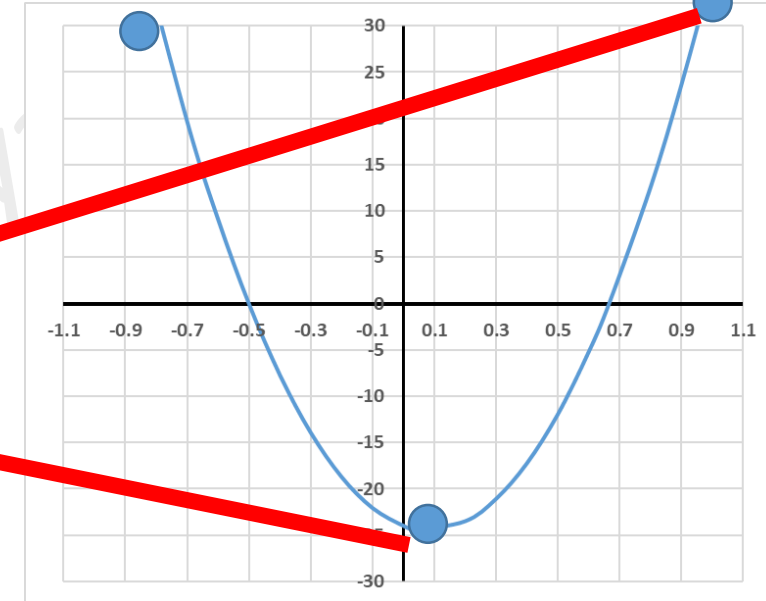
1.1141



-0.9054

0.04131

1.1141



-0.9054

0.04131

1.1141

# Partial Derivative



# Partial Derivative

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$$f(x, y) = x^2 + y^2$$

$$\begin{aligned} \text{X} \rightarrow \frac{d(f(x, y))}{dx} &= \frac{d(x^2 + y^2)}{dx} = \frac{d(x^2 + c)}{dx} = 2x \\ \text{y} \rightarrow \frac{d(f(x, y))}{dy} &= \frac{d(x^2 + y^2)}{dy} = \frac{d(c + y^2)}{dy} = 2y \end{aligned}$$

# Partial Derivative

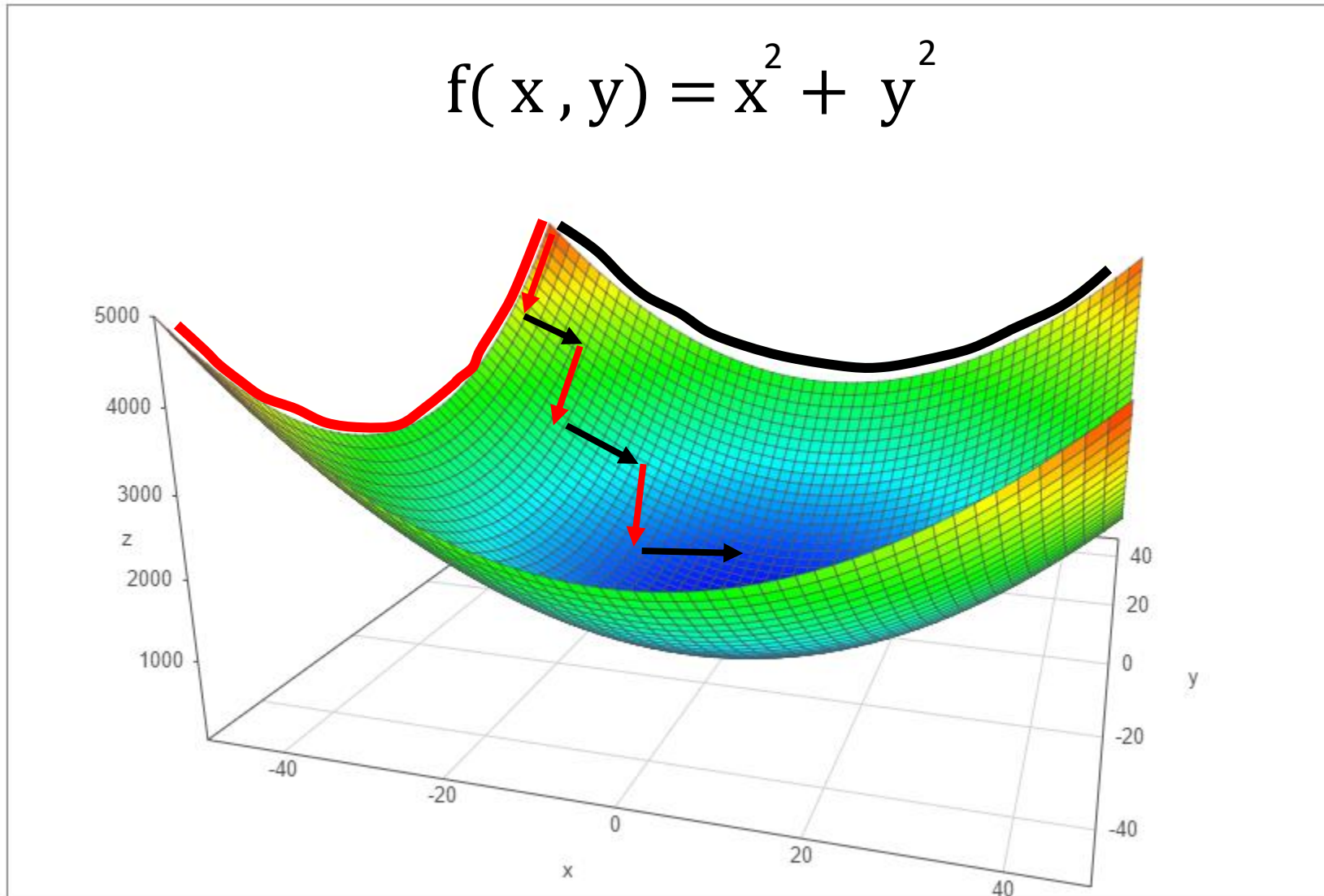
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$$f(x, y) = x^2 + y^2$$

$$\begin{matrix} x \\ \rightarrow \end{matrix} \frac{\partial(f(x, y))}{\partial x} = 2x$$

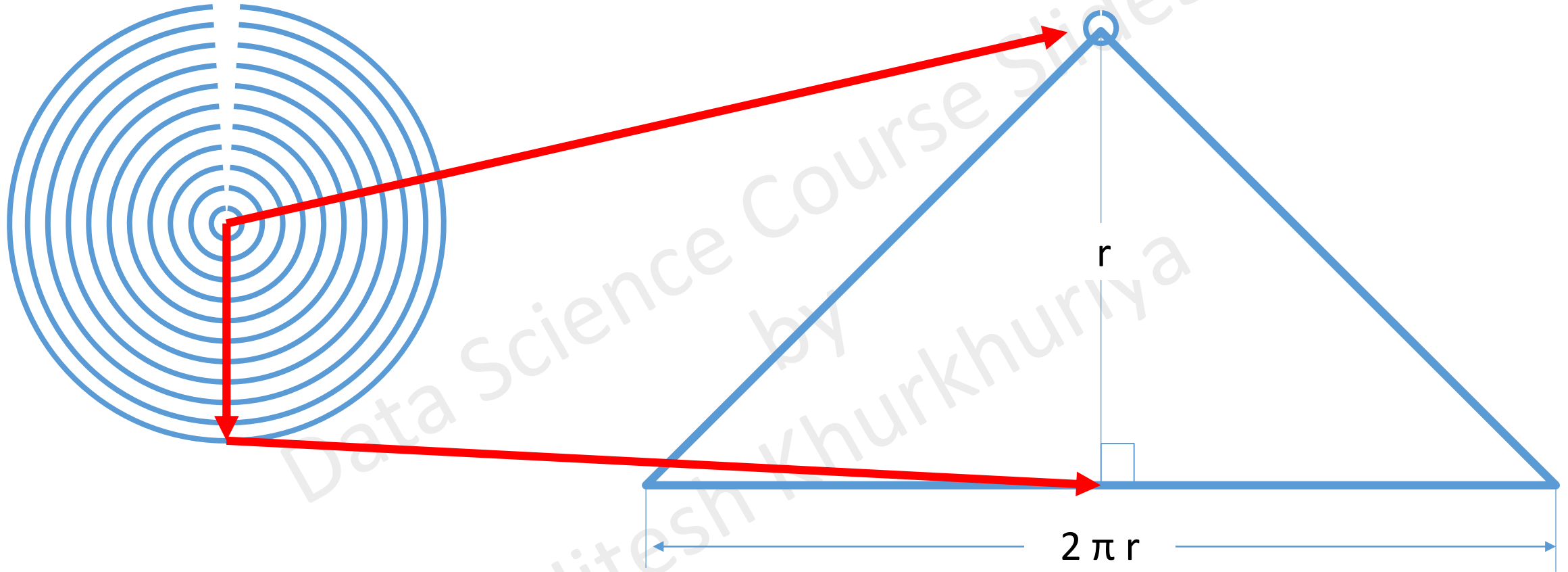
$$\begin{matrix} y \\ \rightarrow \end{matrix} \frac{\partial(f(x, y))}{\partial y} = 2y$$

# Multiple variables in a function



# Integration

# Calculating the area of a circle

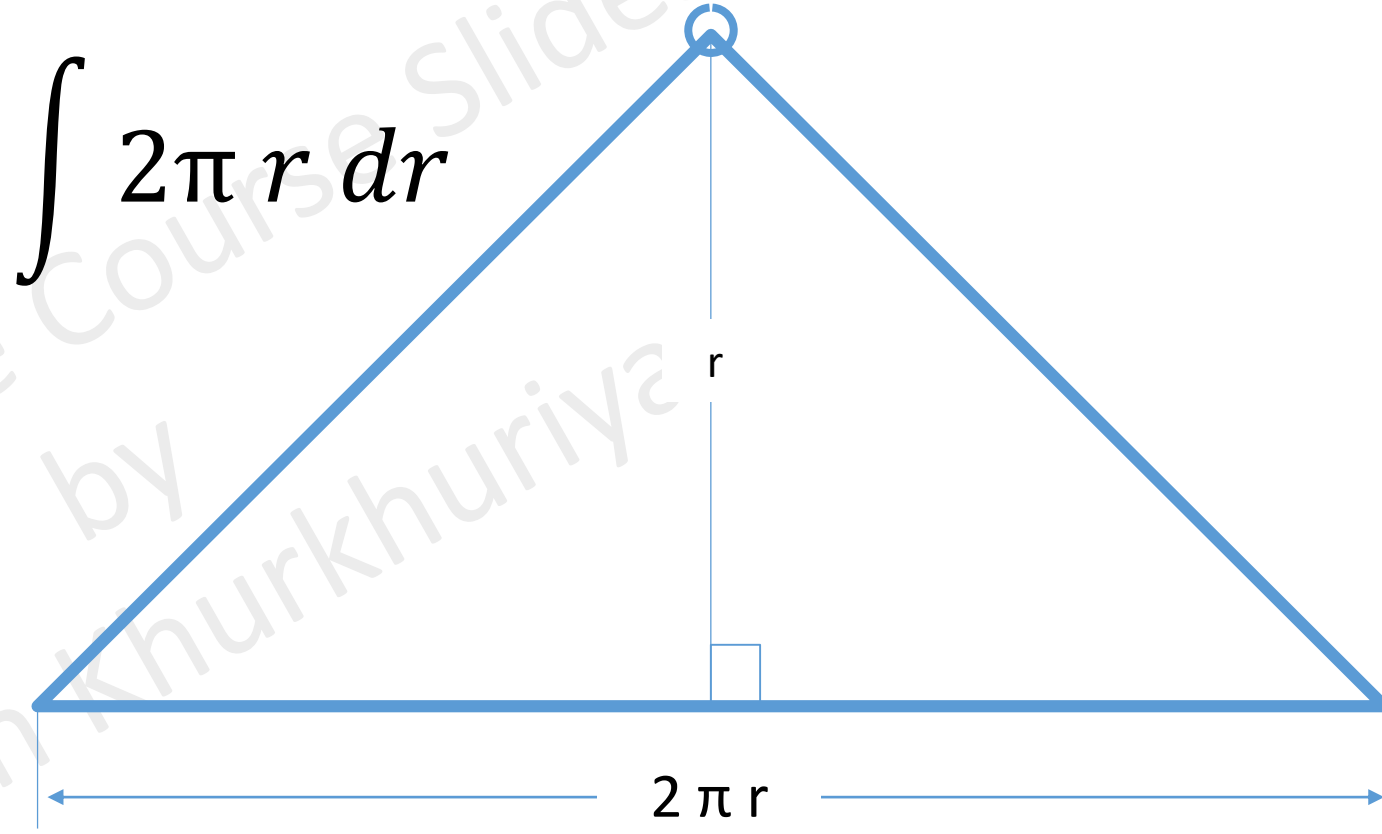


# Calculating the area of a circle

$$\text{Area} = \frac{\text{Height} * \text{Base}}{2}$$

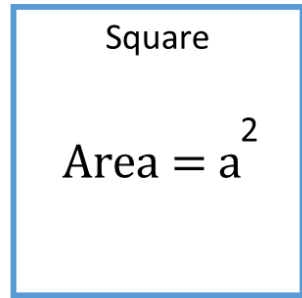
$$= \frac{2 \pi r * r}{2}$$

$$= \pi r^2$$

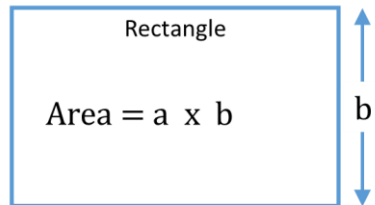


# Understanding the problem

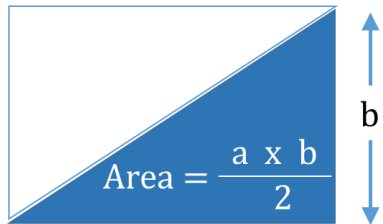
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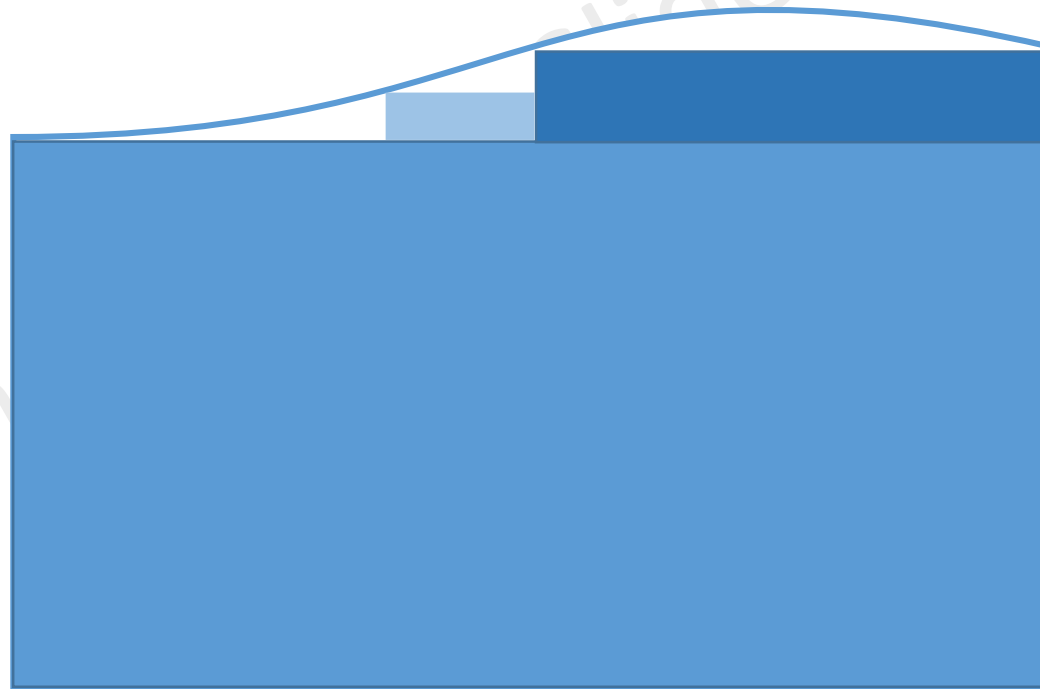
$\longleftrightarrow a$



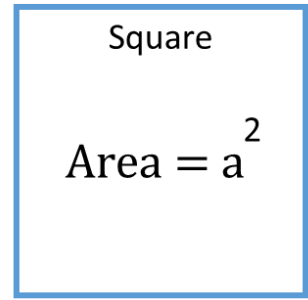
$\longleftrightarrow a$



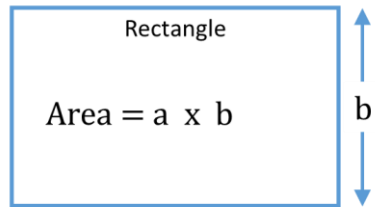
$\longleftrightarrow a$



# Understanding the problem

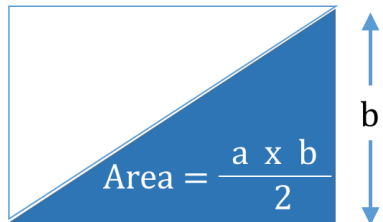


$\longleftrightarrow a$

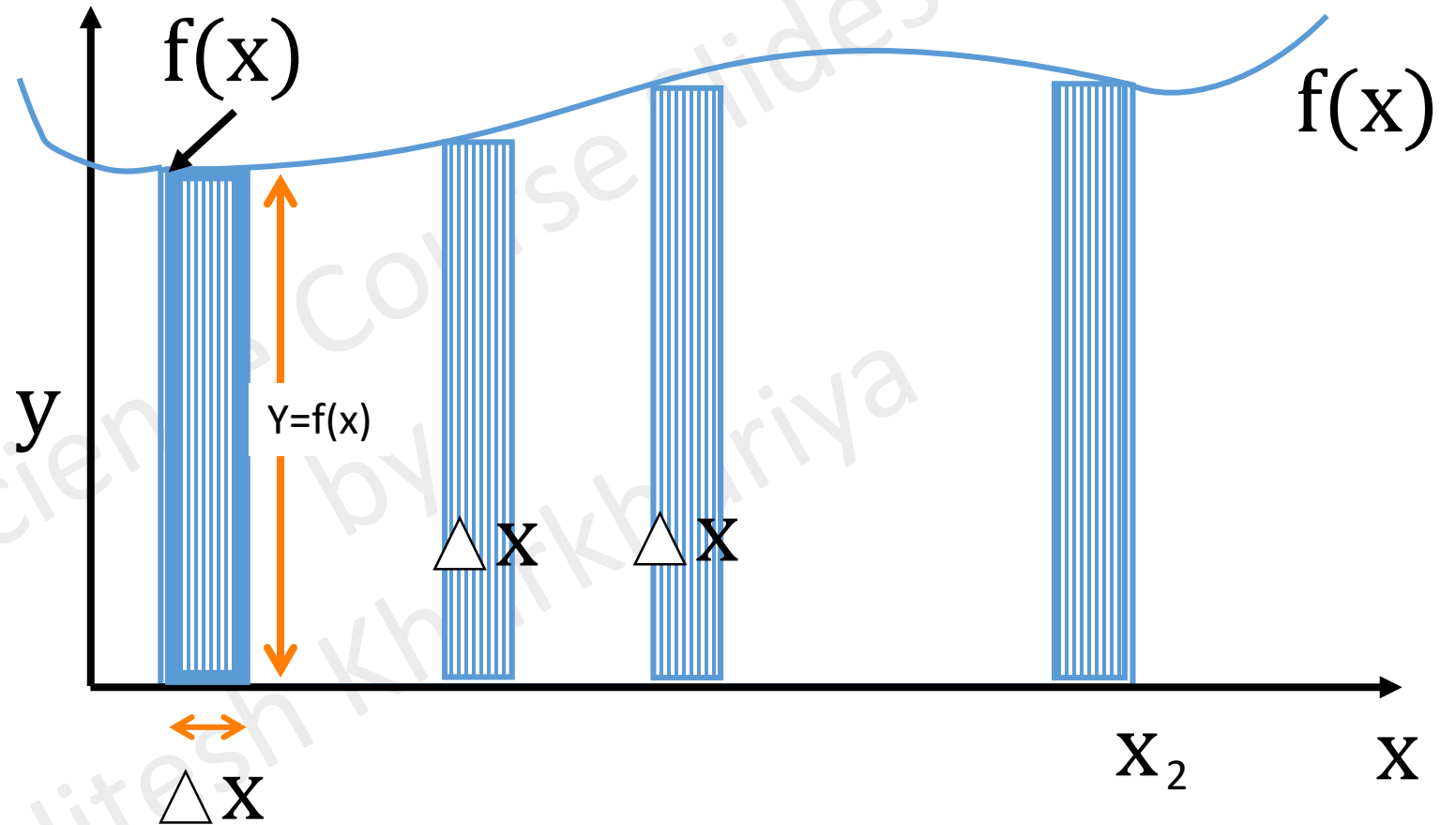


$\updownarrow b$

$\longleftrightarrow a$



$\longleftrightarrow a$



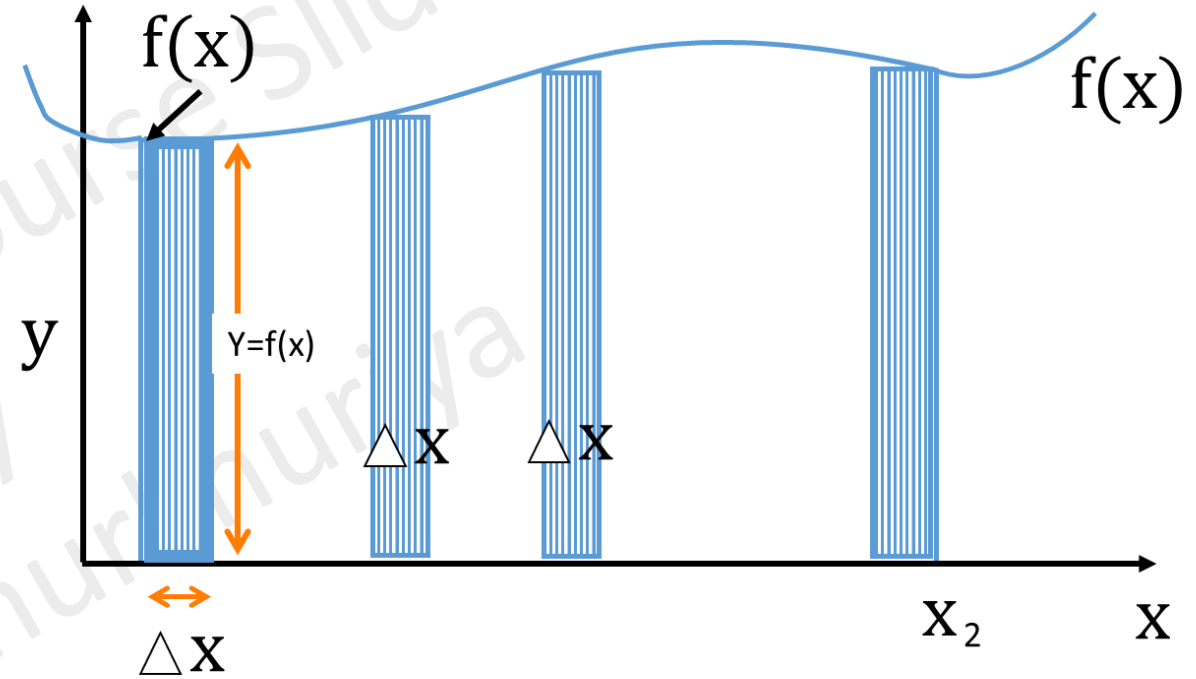


# Understanding the problem

$$\text{Area} = f(x) * \Delta x$$

$$\text{Area} = \sum_{i=1}^n f(x_i) * \Delta x_i$$

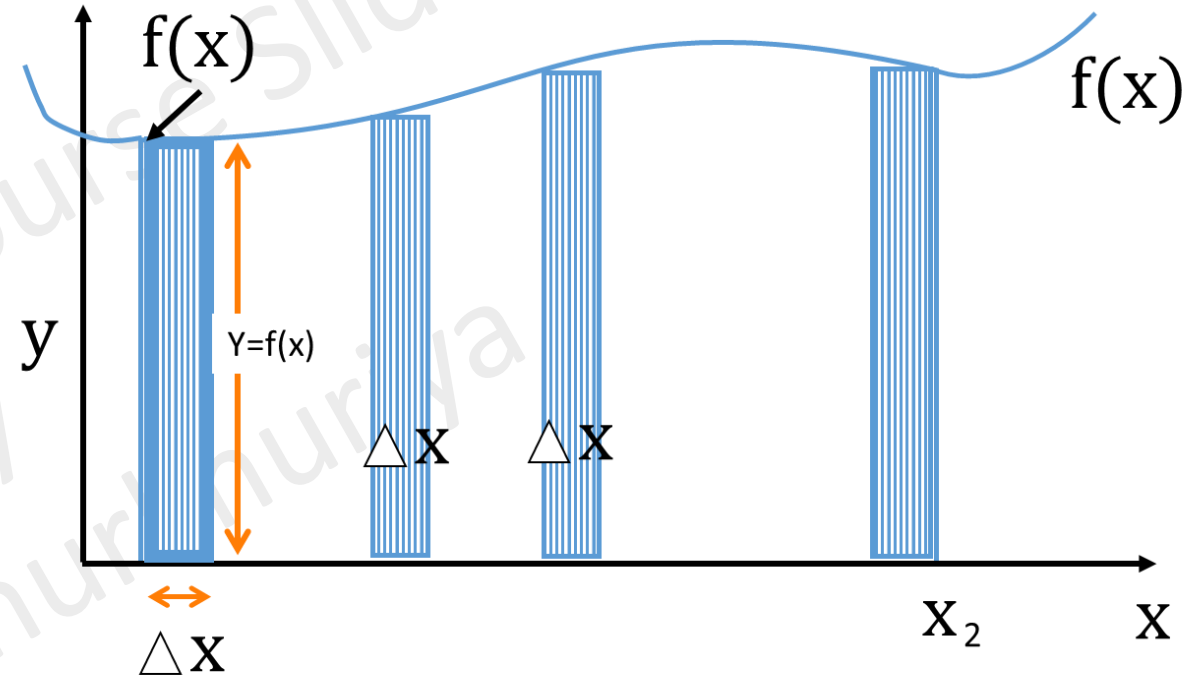
$$\text{Area} = \lim_{\Delta x \rightarrow 0} \sum_{i=1}^n f(x_i) * \Delta x_i$$



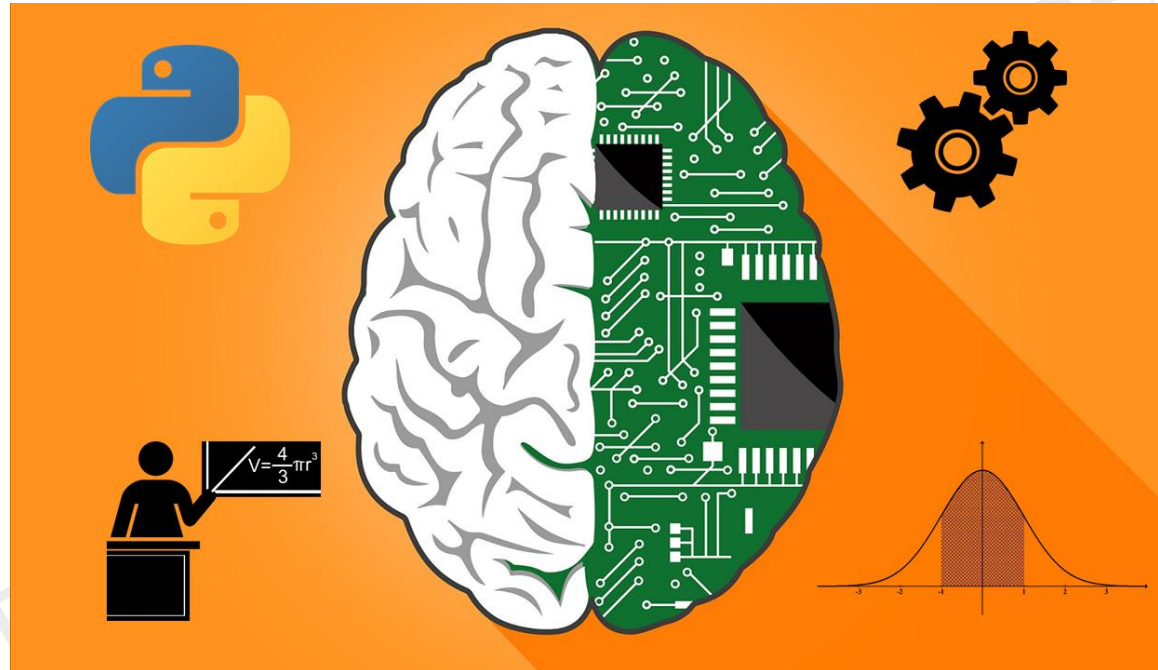
# Integration

$$\text{Area} = \lim_{\Delta x \rightarrow 0} \sum_{i=1}^n f(x_i) * \Delta x_i$$

$$\int_{x_1}^{x_2} f(x) dx$$



# Complete Data Science and Machine Learning Using Python



# Thank You!