

Uplink User-Assisted Relaying in Cellular Networks

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Dual Degree Phase 1 Presentation

October 27, 2015

Overview

- ▶ Introduction
- ▶ Partial Decode-and-Forward Relaying
- ▶ PDF in Cellular Networks
- ▶ Cooperation Policies
- ▶ Simulations and Results
- ▶ Future Work

Introduction

- ▶ Relaying cooperative communications will play important roles in future generations wireless networks.
- ▶ Relay-aided cooperative communication techniques represent a promising technology that improves average rate
- ▶ We use Partial Decode-and-Forward scheme for relaying
- ▶ We will explore two policies by which active User Equipments (UEs) pick their relays

Partial Decode-and-Forward Relaying

Two Phases

Total transmission period is divided into phases: 1. Broadcast phase and 2. Multicast phase as shown in the figure below.

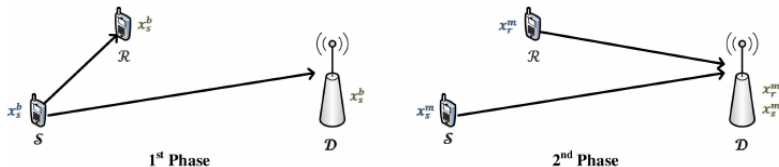


Figure: Two phases in PDF relaying.

Partial Decode-and-Forward Relaying

Transmit Signals

The signals transmitted by source and relay are as follows:

$$\text{Phase 1: } x_s^b = \sqrt{P_s^b} U_s^b,$$

$$\text{Phase 2: } x_r^m = \sqrt{P_r^m} U_s^{m_1},$$

$$x_s^m = \sqrt{P_s^{m_1}} U_s^{m_1} + \sqrt{P_s^{m_2}} V_s^{m_2}$$

- ▶ All codewords above are picked from independent Gaussian codebooks with zero mean and unit variance.
- ▶ $\alpha_1 P_s^b + \alpha_2 P_s^m = P_s$, $P_s^{m_1} + P_s^{m_2} = P_s^m$, $\alpha_2 P_r^m = P_r$ where $\alpha_2 = 1 - \alpha_1$

Partial Decode-and-Forward Relaying

Received Signals

Signals received at relay, BS during broadcast(b) and multicast(m) phases:

$$Y_r^b = h_{sr}x_s^b + Z_r^b, \quad Y_d^b = h_{sd}x_s^b + Z_d^b$$

Z_r^b and Z_d^b are *i.i.d* $\mathcal{CN}(0, \sigma^2)$ that represent noises at \mathcal{R} and \mathcal{D} .

$$Y_d^m = h_{sd}x_s^m + h_{rd}x_r^m + Z_d^m$$

The above expression is true only if \mathcal{D} has knowledge about the phase offset between \mathcal{S} and \mathcal{R} .

Partial Decode-and-Forward Relaying

Achievable Rate

With received signals as above and joint ML decoding rule at destination, the achievable rate for this relaying scheme is:

$$R_{PDF} \leq \min(C_1 + C_2, C_3)$$

where $C_1 = \alpha_1 \log \left(1 + |h_{sr}|^2 P_s^b \right),$

$$C_2 = \alpha_2 \log \left(1 + |h_{sd}|^2 P_s^{m_2} \right),$$

$$C_3 = \alpha_1 \log \left(1 + |h_{sd}|^2 P_s^b \right) \\ + \alpha_2 \log \left(1 + |h_{sd}|^2 P_s^{m_2} + \left(|h_{sd}| \sqrt{P_s^{m_1}} + |h_{rd}| \sqrt{P_r^m} \right)^2 \right)$$

PDF in Cellular Networks

Network Geometry

- ▶ Active users in different cells using same resource block are distributed according to a homogeneous and stationary Poisson point process (PPP) Φ_1 with intensity λ_1
- ▶ Idle UEs that can participate in relaying are distributed according to another PPP Φ_2 with intensity λ_2 .
- ▶ Φ_1 and Φ_2 are independent.
- ▶ BS is uniformly distributed in the Voronoi cell of its served UE

PDF in Cellular Networks

Network Geometry

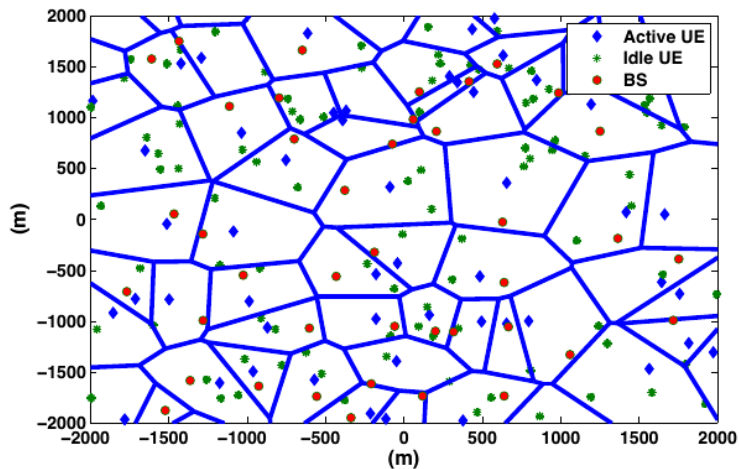


Figure: Sample Network Layout

PDF in Cellular Networks

Channel Model

Consider i^{th} active UE, we model the received signals at the relay and base station in this cell during 1st phase as

$$Y_{r,i}^b = h_{sr}^{(i)} x_{s,i}^b + I_{r,i}^b + Z_{r,i}^b,$$

$$Y_{d,i}^b = h_{sd}^{(i)} x_{s,i}^b + I_{d,i}^b + Z_{d,i}^b$$

where $I_{r,i}^b$ and $I_{d,i}^b$ represent the interference received at the i^{th} relay and destination. In second phase of the transmission, the received signal at the BS can be modelled as

$$Y_{d,i}^m = h_{sd}^{(i)} x_{s,i}^m + h_{rd}^{(i)} x_{r,i}^m + I_{d,i}^m + Z_{d,i}^m$$

PDF in Cellular Networks

Interference

$$I_{r,i}^b = \sum_{k \neq i} B_k h_{sr}^{(k,i)} x_{s,k}^b + (1 - B_k) h_{sr}^{(k,i)} x_{s,k},$$

$$I_{d,i}^b = \sum_{k \neq i} B_k h_{sd}^{(k,i)} x_{s,k}^b + (1 - B_k) h_{sd}^{(k,i)} x_{s,k},$$

$$I_{d,i}^m = \sum_{k \neq i} B_k \left(h_{sd}^{(k,i)} x_{s,k}^m + h_{rd}^{(k,i)} x_{r,k}^m \right) + (1 - B_k) h_{sd}^{(k,i)} x_{s,k}$$

where $B_k = 1$ if k^{th} user has a relay. B_k can be seen as a Bernoulli RV with success probability equal to cooperation probability of the policy by which relays are picked

PDF in Cellular Networks

Interference

- ▶ Interference at either the relay or destination is the sum of many signals undergoing independent fading from nodes distributed in the infinite 2-D plane
- ▶ Approximate the interference as a complex Gaussian distribution by using law of large numbers
- ▶ Distributions: $I_{d,i}^b \sim \mathcal{CN}(0, Q_{d,i}^b)$, $I_{d,i}^m \sim \mathcal{CN}(0, Q_{d,i}^m)$, and $I_{r,i}^b \sim \mathcal{CN}(0, Q_{r,i})$

PDF in Cellular Networks

Equivalent Standard Channel Model

$$\tilde{Y}_{r,i}^b = \tilde{h}_{sr}^{(i)} x_{s,i}^b + \tilde{Z}_{r,i}^b,$$

$$\tilde{Y}_{d,i}^b = \tilde{h}_{sd}^{(i)} x_{s,i}^b + \tilde{Z}_{d,i}^b,$$

$$\tilde{Y}_{d,i}^m = \tilde{h}_{sd}^{(i)} x_{s,i}^m + \tilde{h}_{rd}^{(i)} x_{r,i}^m + \tilde{Z}_{d,i}^m,$$

where the new channel fading terms are defined as

$$\tilde{h}_{sr}^{(i)} = \frac{h_{sr}^{(i)}}{\sqrt{Q_{r,i} + \sigma^2}}, \quad \tilde{h}_{sd}^{(b,i)} = \frac{h_{sd}^{(i)}}{\sqrt{Q_{d,i}^b + \sigma^2}}$$

$$\tilde{h}_{sd}^{(m,i)} = \frac{h_{sd}^{(i)}}{\sqrt{Q_{d,i}^m + \sigma^2}}, \quad \tilde{h}_{rd}^{(i)} = \frac{h_{rd}^{(i)}}{\sqrt{Q_{d,i}^m + \sigma^2}}$$

and the noise terms are now all $\mathcal{CN}(0, 1)$

Cooperation Policies

Ideal Policy E_1

$$\begin{aligned} E_1 &= \left\{ |\tilde{h}_{(sr)}^{(k)}|^2 \geq |\tilde{h}_{(sd)}^{(k)}|^2 \right\} \\ &\simeq \left\{ \frac{g_{sr} r_2^{-\alpha}}{Q_{r,k}} \geq \frac{g_{sd} r_1^{-\alpha}}{Q_{d,k}^b} \right\} \end{aligned}$$

where r_1 and r_2 denote the direct distance between \mathcal{S} and \mathcal{D} and cooperation distance between \mathcal{S} and its closest idle UE, respectively and α is pathloss exponent. Active UE nodes should know instantaneous SINRs of the relay link($\mathcal{S} - \mathcal{R}$) and the direct link($\mathcal{S} - \mathcal{D}$)

Cooperation Policies

Pure Geometric Policy E_2

$$E_2 = \{r_2 \leq r_1, D \leq r_1\}$$

where D is the distance between \mathcal{R} and \mathcal{D} .

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- ▶ Does not require full knowledge of interference at decision making node.

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- ▶ More practical than E_1
- ▶ Does not require full knowledge of interference at decision making node.
- ▶ Only requires the decision making nodes to know the distances from the active user to the nearest idle user and to the base station.

Cooperation Policies

Hybrid Policy E_3

This policy is proposed for slow fading channels where small scale fading parameters estimation and their feedback to the decision making node is feasible.

$$E_3 = \{g_{sd}r_1^{-\alpha} \leq g_{sr}r_2^{-\alpha}, D \leq r_1\}$$

Note that this cooperation policy is still independent of the interference as in the pure geometric cooperation policy E_2 .

Cooperation Probabilities

Distributions of r_1, r_2

The distribution of the distance r_1 between the i^{th} UE and its associated BS can be shown to be Rayleigh distributed

$$f_{r_1}(r_1) = 2\pi\lambda_1 r_1 e^{-\lambda_1 \pi r_1^2},$$

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Similarly the distribution of the source-to-relay distance r_2 between the i^{th} UE and its associated relaying UE can be also shown to be Rayleigh distributed

$$f_{r_2}(r_2) = 2\pi\lambda_2 r_2 e^{-\lambda_2 \pi r_2^2}$$

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$$f_{r_2}(r_2) = 2\pi\lambda_2 r_2 e^{-\lambda_2 \pi r_2^2}$$

Can be proved from the null probability of a two dimensional PPP

Cooperation Probabilities

ρ_2, ρ_3

For policy E_2

$$\begin{aligned}\rho_2 = & \int_{-\pi/2}^{-\pi/3} \frac{2\lambda_2 \cos^2 \psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2 \psi_0)} d\psi_0 \\ & + \int_{\pi/3}^{\pi/2} \frac{2\lambda_2 \cos^2 \psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2 \psi_0)} d\psi_0 + \frac{\lambda_2}{3(\lambda_1 + \lambda_2)}\end{aligned}$$

Cooperation Probabilities

ρ_2, ρ_3

$$\begin{aligned}\rho_3 = & \int_0^2 f_\beta(z) \int_{-\pi/2}^{-\cos^{-1}(z/2)} \frac{2\lambda_2 \cos^2 \psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2 \psi_0)} d\psi_0 dz \\ & + \int_0^2 f_\beta(z) \int_{\cos^{-1}(z/2)}^{\pi/2} \frac{2\lambda_2 \cos^2 \psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2 \psi_0)} d\psi_0 dz \\ & + \int_0^2 f_\beta(z) \frac{\lambda_2 z^2 \cos^{-1}(z/2)}{\pi(\lambda_1 + \lambda_2 z^2)} dz \\ & + \int_2^\infty f_\beta(z) \int_{-\pi/2}^{\pi/2} \frac{2\lambda_2 \cos^2 \psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2 \psi_0)} d\psi_0 dz\end{aligned}$$

where $\beta = \left(\frac{g_{sr}}{g_{sd}} \right)^{1/\alpha}$ and $f_\beta(z)$ is pdf of β which can be shown to be

$$f_\beta(z) = \frac{\alpha z^{\alpha-1}}{(1+z^\alpha)^2}$$

Cooperation Probabilities

Proof

$$\begin{aligned}\rho_2 &= \mathbb{P}\{E_2\} \\ &= \mathbb{P}\{r_2 \leq r_1, r_1^2 + r_2^2 - 2r_1r_2\cos\psi_0 \leq r_1^2\} \\ &= \mathbb{P}\{r_2 \leq r_1, r_2 \leq 2r_1\cos\psi_0\}\end{aligned}$$

when $|\psi_0| < \pi/3$, $r_1 < 2r_1\cos\psi_0$

\Rightarrow if $r_2 < r_1$, r_2 satisfies both inequalities.

Accordingly, we define \mathcal{E}_1 and \mathcal{E}_2 as follows

$$\begin{aligned}\mathcal{E}_1 &= (2\pi)^2 \lambda_1 \lambda_2 \int_0^\infty \int_0^{2r_1\cos\psi_0} r_1 r_2 e^{-\pi(\lambda_1 r_1^2 + \lambda_2 r_2^2)} dr_2 dr_1 \\ &= \frac{2\lambda_2 \cos^2\psi_0}{\pi(\lambda_1 + 4\lambda_2 \cos^2\psi_0)}\end{aligned}$$

Cooperation Probabilities

Proof

$$\begin{aligned}\mathcal{E}_2 &= (2\pi)^2 \lambda_1 \lambda_2 \int_0^\infty \int_0^{r_1} r_1 r_2 e^{-\pi(\lambda_1 r_1^2 + \lambda_2 r_2^2)} dr_2 dr_1 \\ &= \frac{\lambda_2}{2\pi(\lambda_1 + \lambda_2)}\end{aligned}$$

$$\begin{aligned}\text{Now, } \rho_2 &= \int_{-\pi/3}^{\pi/3} \mathcal{E}_2 d\psi_0 + 2 \int_{\pi/3}^{\pi/2} \mathcal{E}_1 d\psi_0 \\ &= \frac{\lambda_2}{3(\lambda_1 + \lambda_2)} + 2 \int_{\pi/3}^{\pi/2} \mathcal{E}_1 d\psi_0\end{aligned}$$

Cooperation Probabilities

Proof

$$\begin{aligned}\rho_3 &= \mathbb{P}\{E_3\} \\ &= \mathbb{P}\left\{r_2 \leq \left(\frac{g_{sr}}{g_{sd}}\right)^{1/\alpha} r_1, r_1^2 + r_2^2 - 2r_1r_2\cos\psi_0 \leq r_1^2\right\} \\ &= \mathbb{P}\{r_2 \leq \beta r_1, r_2 \leq 2r_1\cos\psi_0\} \\ &= \mathbb{P}\{r_2 \leq 2r_1\cos\psi_0\} \quad \text{for } \beta > 2 \\ &= \mathbb{P}\{r_2 \leq \beta r_1\} \quad \text{for } \beta < 2 \text{ and } |\psi_0| < \cos^{-1}(\beta/2) \\ &= \mathbb{P}\{r_2 \leq 2r_1\cos\psi_0\} \quad \text{for } \beta < 2 \text{ and } \cos^{-1}(\beta/2) < |\psi_0| < \pi/2\end{aligned}$$

Cooperation Probabilities

Proof

$$\begin{aligned}\therefore \rho_3 &= 2 \int_0^2 f_\beta(z) \int_{\cos^{-1}(z/2)}^{\pi/2} \mathcal{E}_1 d\psi_0 dz + \int_0^2 f_\beta(z) \int_{-\cos^{-1}(z/2)}^{\cos^{-1}(z/2)} \mathcal{E}_3 d\psi_0 dz \\ &\quad + \int_2^\infty f_\beta(z) \int_{-\pi/2}^{\pi/2} \mathcal{E}_1 d\psi_0 dz\end{aligned}$$

\mathcal{E}_1 is defined in part i. of the proof and $\mathcal{E}_3 = \frac{\lambda_2 z^2}{2\pi(\lambda_1 + \lambda_2 z^2)}$ which is nothing but \mathcal{E}_2 with $\lambda_2 = \lambda_2 z^2$

Cooperation Probabilities

Proof

$f_{\beta}(z)$, the pdf of β , can be obtained as follows

$$\begin{aligned} F_{\beta}(z) &= \mathbb{P}\left\{\left(\frac{x_1}{x_2}\right)^{1/\alpha} \leq z\right\} = \mathbb{P}\{x_1 \leq z^{\alpha} x_2\} \\ &= \int_0^{\infty} \int_0^{z^{\alpha} x_2} e^{-(x_1+x_2)} dx_1 dx_2 \quad \text{since } g_{sr}, g_{sd} \sim \text{Exp}(1) \\ &= 1 - \frac{1}{1+z^{\alpha}}, \quad z \in [0, \infty) \end{aligned}$$

The pdf $f_{\beta}(z)$ is then obtained by differentiating $F_{\beta}(z)$:

$$f_{\beta}(z) = \frac{dF_{\beta}(z)}{dz} = \frac{\alpha z^{\alpha-1}}{(1+z^{\alpha})^2} \quad z \in [0, \infty)$$

Simulations

Generate UEs

Consider a square region of area A .

- ▶ $N_1 \sim \text{poisson}(\lambda_1 A)$
- ▶ $N_2 \sim \text{poisson}(\lambda_2 A)$
- ▶ Distribute N_1 UEs uniformly in the region and mark them as active UEs
- ▶ Distribute N_2 UEs uniformly in the region and mark them as idle UEs

Simulations

Generating Base Stations

- ▶ Ideally, BSs corresponding to a UE should be picked uniformly from the Voronoi region of UE.

Simulations

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- ▶ One way to do that is to triangulate the polygonal Voronoi region, choose a triangle weighted by area, choose a point in that triangle.

Simulations

Generating Base Stations

- ▶ Ideally, BSs corresponding to a UE should be picked uniformly from the Voronoi region of UE.
- ▶ One way to do that is to triangulate the polygonal Voronoi region, choose a triangle weighted by area, choose a point in that triangle.
- ▶ Difficult to implement

Simulations

Generating Base Stations

BSs are generated in the following manner:

- ▶ Pick a number N_3 greater than N_1
- ▶ Distribute N_3 BSs uniformly in the whole square region

Simulations

Generating Base Stations

BSs are generated in the following manner:

- ▶ Pick a number N_3 greater than N_1
- ▶ Distribute N_3 BSs uniformly in the whole square region
- ▶ Go to each active UE and check if there are any BSs in its Voronoi region

Simulations

Generating Base Stations

- ▶ If there are more than one BS in the region, pick any one of them randomly.
- ▶ Since BSs are uniform over the whole region, they are also uniform in each Voronoi region
- ▶ But some UEs might not have a BS unlike in the actual method
- ▶ Finally, discard all active UEs without a BS

Simulations

Transmission Powers

The average powers used by source and relay are as follows:

- ▶ Source and relays use equal power $\Rightarrow P_{s,i} = P_{r,i}$
- ▶ $\alpha_1 P_{s,i}^b + \alpha_2 P_{s,i}^m = P_{s,i}$
- ▶ Source uses equal power during broadcast and multicast phases $\Rightarrow P_{s,i}^b = P_{s,i}^m$
- ▶ $P_{s,i}^{m_1} = \beta_1 P_{s,i}^m$ and $P_{s,i}^{m_2} = (1 - \beta_1) P_{s,i}^m$
- ▶ β_1 is allocated optimally to maximize the transmission rate of the active user.

Results

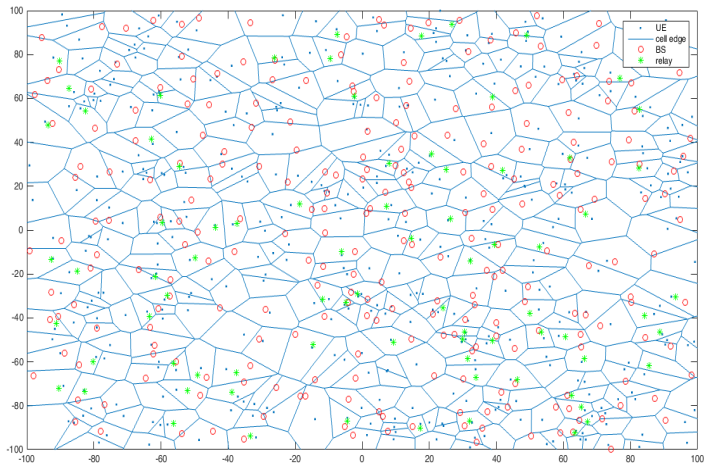


Figure: Sample Network Layout

Results

In the reference paper, there was a mistake in the derivation of expression for cooperation probability(ρ_3) of policy E_3 .

\mathcal{E}_2 was used in place of \mathcal{E}_3

$$\mathcal{E}_3 = \frac{\lambda_2 z^2}{2\pi(\lambda_1 + \lambda_2 z^2)}$$

$$\mathcal{E}_2 = \frac{\lambda_2}{2\pi(\lambda_1 + \lambda_2)}$$

Results

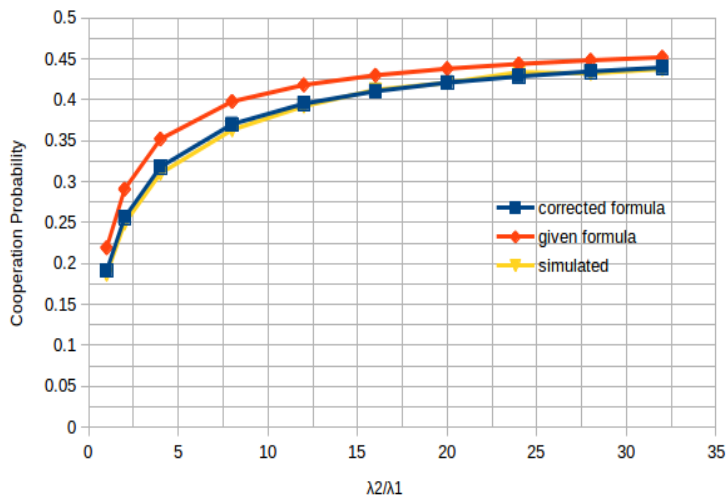


Figure: Cooperation probability of E_3 .

Results

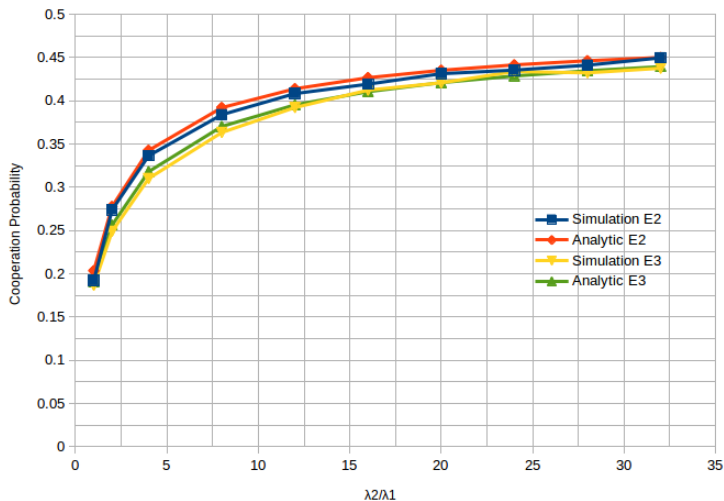


Figure: Cooperation probabilities v/s User ratio density.

Results

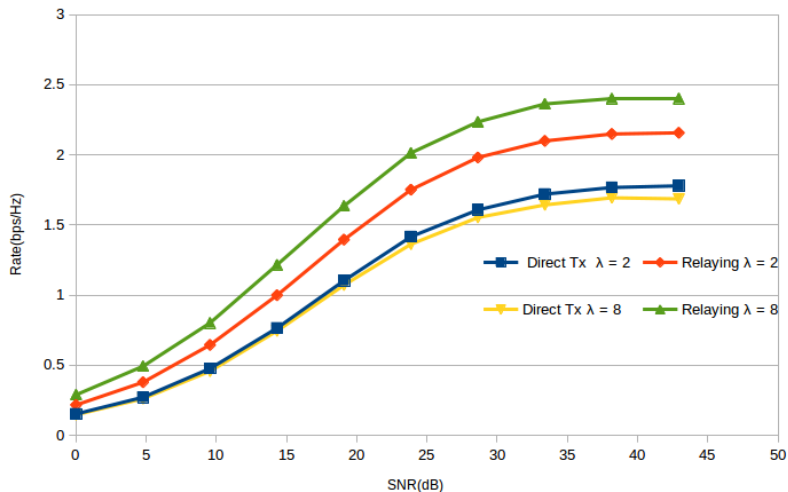


Figure: Per user average rate v /s SNR.

Future Work

New Policy

- ▶ In the policies E_2 , E_3 , only the first neighbour of the active UE is seen as a potential relay.
- ▶ Any relay which is at a distance r_2 from active UE and satisfies $r_2 < r_1$, $D < r_1$ can be treated as a potential relay

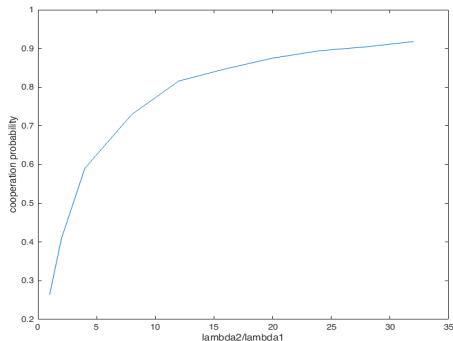


Figure: Cooperation Probability v/s User density ratio

Future Work

New Policy

- ▶ This also means higher interference
- ▶ If rate decreases for some users, then there should be a way of deciding which users should use the relaying so that rate will be high for all users.

Future Work

β_1

Power used by UE to transmit the common codeword in second phase $P_s^{m_1} = \beta_1 P_s^m$

- ▶ Currently, β_1 is obtained by optimizing the final rate

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β_1

Power used by UE to transmit the common codeword in second phase $P_s^{m_1} = \beta_1 P_s^m$

- ▶ Currently, β_1 is obtained by optimizing the final rate
- ▶ This is not practical.
- ▶ An algorithm can be developed to estimate β_1

Future Work

Power Control

- ▶ We assumed that all nodes transmit at maximum power

Future Work

Power Control

- ▶ We assumed that all nodes transmit at maximum power
- ▶ A distance based power control method can be applied

Thank You!!