Tree HW

Pruthvi Bharadwaj

March 12, 2022

8.1

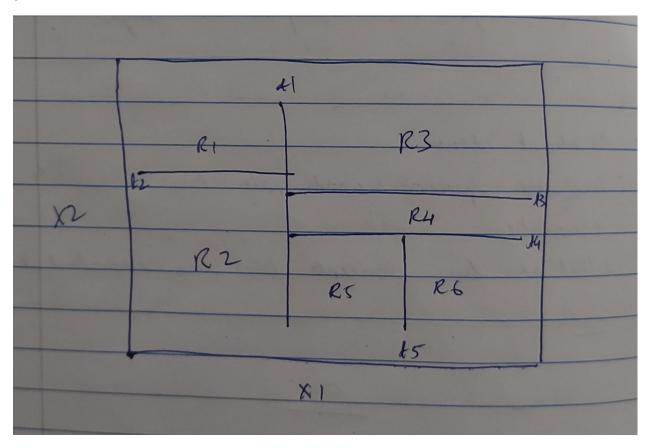


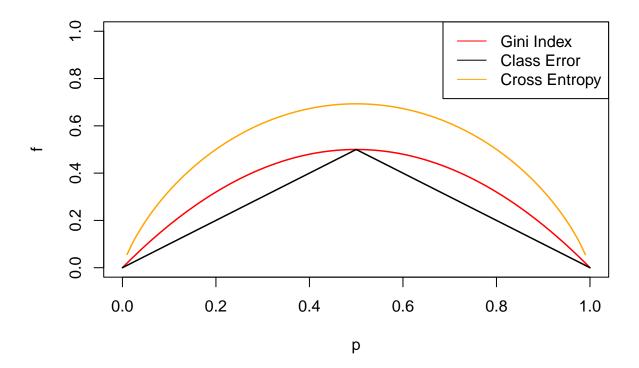
Figure 1: my answer

8.3

```
p <- seq(0,1,0.01)

#For two classes
gini <- 2*p*(1-p)
error <- 1 - pmax(p, 1-p)
entropy <- -(p*log(p) + (1-p)*log(1-p))

plot(NA, xlim = c(0,1), ylim = c(0,1), xlab = "p", ylab = "f")</pre>
```



8.5 P(Class is Red | X) is greater than 0.5 in 6 of the 10 times. Therefore, according to majority vote, final classification is Red.

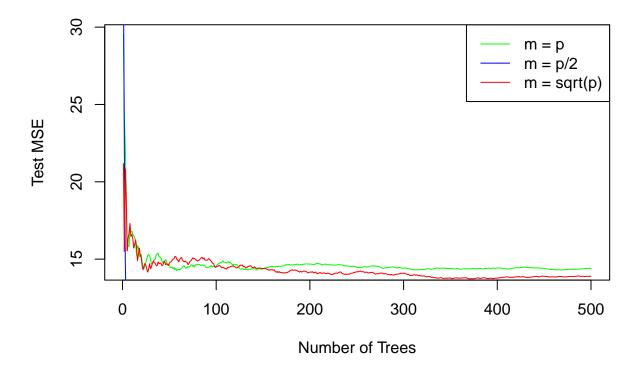
The average probability for the 10 estimates is 0.45, i.e., $P(Class is Red \mid X) < 0.5$, implying that the final classification is Green.

8.7

```
data("Boston")
set.seed(9)
train <- sample(1:nrow(Boston), nrow(Boston)/2)

Boston_train <- Boston[train, -14]
Boston_test <- Boston[-train, -14]
y_train <- Boston[train, 14]
y_test <- Boston[-train, 14]</pre>
rf1 <- randomForest(Boston_train, y = y_train, xtest = Boston_test, ytest = y_test, mtry = ncol(Boston)</pre>
```

```
rf2 <- randomForest(Boston_train, y = y_train, xtest = Boston_test, ytest = y_test, mtry = (ncol(Boston rf3 <- randomForest(Boston_train, y = y_train, xtest = Boston_test, ytest = y_test, mtry = sqrt(ncol(Bo plot(1:500, rf1$test$mse, type = "l", col = "green", xlab = "Number of Trees", ylab = "Test MSE")
lines(1:500, rf2$test$mse, type = "l", col = "blue")
lines(1:500, rf3$test$mse, type = "l", col = "red")
legend(x = "topright", c("m = p", "m = p/2", "m = sqrt(p)"), col = c("green", "blue", "red"), lty = 1)</pre>
```



8.8 (a)

```
data("Carseats")
set.seed(9)
subs <- sample(1:nrow(Carseats), nrow(Carseats)*0.7)
car_train <- Carseats[subs, ]
car_test <- Carseats[-subs, ]</pre>
```

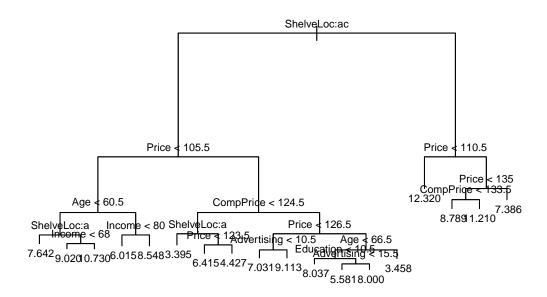
(b)

```
#Regression Tree

rtree <- tree(Sales ~ ., data = car_train)
summary(rtree)</pre>
```

##

```
## Regression tree:
## tree(formula = Sales ~ ., data = car_train)
## Variables actually used in tree construction:
## [1] "ShelveLoc" "Price"
                                  "Age"
                                                "Income"
                                                              "CompPrice"
## [6] "Advertising" "Education"
## Number of terminal nodes: 18
## Residual mean deviance: 2.621 = 686.6 / 262
## Distribution of residuals:
     Min. 1st Qu. Median
                           Mean 3rd Qu.
                                             Max.
## -5.2110 -1.0330 -0.0156 0.0000 0.9664 4.2340
plot(rtree)
text(rtree, cex = 0.65)
```



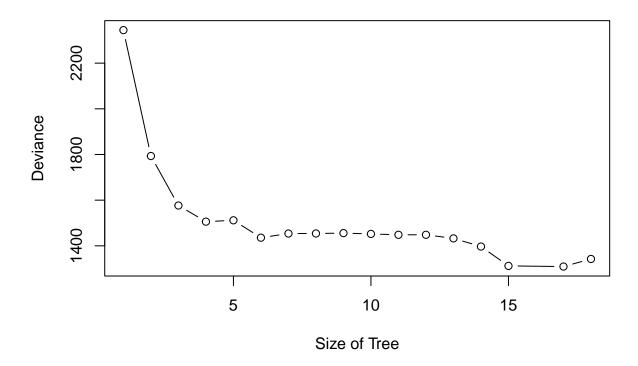
```
#MSE
pred_rtree <- predict(rtree, car_test)
mse_rtree <- mean((car_test$Sales - pred_rtree)^2)
print(paste0("The test MSE for the regression tree is: ", mse_rtree))</pre>
```

[1] "The test MSE for the regression tree is: 4.6376957387513"

(c)

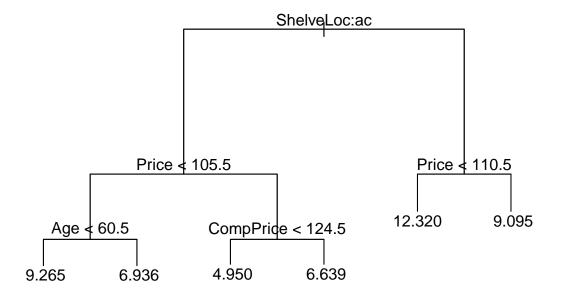
```
#Cross-Validation for tree complexity

cv_rtree <- cv.tree(rtree)
plot(cv_rtree$size, cv_rtree$dev, xlab = "Size of Tree", ylab = "Deviance", type = "b")</pre>
```



```
#Tree Pruning

prune_rtree <- prune.tree(rtree, best = 6)
plot(prune_rtree)
text(prune_rtree)</pre>
```



```
#Test MSE for pruned tree

prune_pred <- predict(prune_rtree, car_test)
prune_mse <- mean((prune_pred - car_test$Sales)^2)
print(paste0("The test MSE for the pruned tree is: ", prune_mse))</pre>
```

[1] "The test MSE for the pruned tree is: 4.62735842246563"

The pruned tree gives a slightly lower MSE than the unpruned tree.

(d)

```
#Bagging

car_bag <- randomForest(Sales ~ ., data = car_train, mtry = 10, importance = TRUE, ntree = 500)
pred_bag <- predict(car_bag, car_test)
bag_mse <- mean((pred_bag - car_test$Sales)^2)
print(paste0("The test MSE for bagging method is: ", bag_mse))</pre>
```

[1] "The test MSE for bagging method is: 2.06113398392704"

Bagging reduces the test MSE to 2.062

#Importance importance(car_bag)

```
##
                 %IncMSE IncNodePurity
## CompPrice
                             277.99211
              32.2046620
## Income
               8.8431792
                             112.30771
## Advertising 20.7348575
                             179.92226
## Population -1.3035020
                              80.89917
              71.0352250
## Price
                             695.62717
## ShelveLoc 68.3097260
                             651.42916
## Age
              17.3234447
                             194.22526
## Education
               1.4399098
                              56.31854
## Urban
              -0.5457821
                              10.93868
## US
               5.4387117
                              17.93217
```

Price and ShelveLoc seem to be the two most important variables

(e)

```
#Random Forest
rf_mse <- c()
for (i in 1:10) {
   car_rf <- randomForest(Sales ~ ., data = car_train, mtry = i, importance = TRUE, ntree = 500)
   pred_rf <- predict(car_rf, car_test)
   rf_mse[i] <- mean((pred_rf - car_test$Sales)^2)
}
#Best model
which.min(rf_mse)</pre>
```

[1] 9

```
#Minimum MSE
rf_mse[which.min(rf_mse)]
```

[1] 2.067719

The best model uses 9 variables at each split.

```
importance(car_rf)
```

```
##
                 %IncMSE IncNodePurity
## CompPrice
              33.1964870
                           273.636132
## Income
               6.2208676
                           119.855006
## Advertising 21.1559605
                           184.384037
## Population -1.3882319
                            80.033794
## Price
              67.5697148
                           696.008657
## ShelveLoc 67.5922455
                           642.087660
                         190.268240
## Age
              16.8487080
## Education 1.0094581
                         52.403296
## Urban
             0.7675524
                            9.238638
## US
              6.3153951
                            17.320637
```

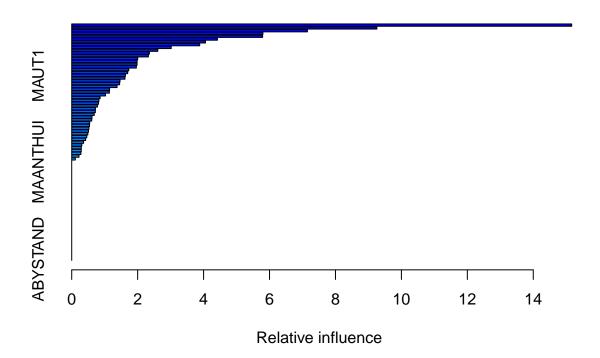
ShelveLoc seems to be the most important variable, followed by Price.

8.11 (a)

```
data("Caravan")
Caravan$Purchase <- ifelse(Caravan$Purchase == "No", 0, 1)
crv_train <- Caravan[1:1000, ]
crv_test <- Caravan[1001:5822, ]</pre>
```

(b)

```
#Boosting
set.seed(9)
boost <- gbm(Purchase ~ ., data = crv_train, shrinkage = 0.01, n.trees = 1000, distribution = "bernoull
## Warning in gbm.fit(x = x, y = y, offset = offset, distribution = distribution, :
## variable 50: PVRAAUT has no variation.
## Warning in gbm.fit(x = x, y = y, offset = offset, distribution = distribution, :
## variable 71: AVRAAUT has no variation.</pre>
kable(summary(boost), row.names = F)
```



**************************************	rel.inf
var	rel.ini
PPERSAUT	15.1650119
MKOOPKLA	9.2549208
MOPLHOOG	7.1491523
MBERMIDD	5.7988033
PBRAND	5.7897473
MGODGE	4.4197200
MINK3045	4.0569774
ABRAND	3.8816596
MOSTYPE	3.0173120
MSKA	2.6104471
MSKC	2.3567316
MAUT2	2.3263968
PWAPART	2.0023871
MINKGEM	1.9838691
MBERARBG	1.9814157
MGODPR	1.9612263
MGODOV	1.7300166
MFWEKIND	1.6986371
MAUT1	1.6287004
PBYSTAND	1.6148436
MSKB1	1.4654283
MRELGE	1.4532182
MBERHOOG	1.3751342
MHHUUR	1.1499571
MRELOV	1.1429171
APERSAUT	1.0241970
MOSHOOFD	0.8617721
MINK7512	0.8244418
MFGEKIND	0.8122327
MSKD	0.7794502
MGODRK	0.7204269
MAUT0	0.7176358
MINKM30	0.6825040
MHKOOP	0.6160159
MOPLMIDD	0.6069681
MBERARBO	0.5460070
MINK123M	0.5388234
MBERBOER	0.5211953
MGEMOMV	0.5211303
MGEMLEEF	0.4889504
MINK4575	0.4563592
MFALLEEN	0.4303392 0.4226122
PMOTSCO	0.4220122 0.3601726
MSKB2	0.3067847
MZFONDS	0.2906486
MZPART	0.2897102
MOPLLAAG	0.2787625
PLEVEN	0.2207685
MRELSA	0.1087580
MAANTHUI	0.0000000
MBERZELF	0.0000000
PWABEDR	0.0000000

var	rel.inf
PWALAND	0.0000000
PBESAUT	0.0000000
PVRAAUT	0.0000000
PAANHANG	0.0000000
PTRACTOR	0.0000000
PWERKT	0.0000000
PBROM	0.0000000
PPERSONG	0.0000000
PGEZONG	0.0000000
PWAOREG	0.0000000
PZEILPL	0.0000000
PPLEZIER	0.0000000
PFIETS	0.0000000
PINBOED	0.0000000
AWAPART	0.0000000
AWABEDR	0.0000000
AWALAND	0.0000000
ABESAUT	0.0000000
AMOTSCO	0.0000000
AVRAAUT	0.0000000
AAANHANG	0.0000000
ATRACTOR	0.0000000
AWERKT	0.0000000
ABROM	0.0000000
ALEVEN	0.0000000
APERSONG	0.0000000
AGEZONG	0.0000000
AWAOREG	0.0000000
AZEILPL	0.0000000
APLEZIER	0.0000000
AFIETS	0.0000000
AINBOED	0.0000000
ABYSTAND	0.0000000

PPERSAUT, MKOOPKLA and MOPLHOOG are the three most important variables.

(c)

```
pred_boost <- predict(boost, crv_test, n.trees = 1000, type = "response")
boost_pred <- ifelse(pred_boost > 0.2, 1, 0)
table(crv_test$Purchase, boost_pred)
```

```
## boost_pred
## 0 1
## 0 4415 118
## 1 253 36
```

The fraction of people who were predicted to make a purchase and who actually made a purchase is 36/(36 + 118), which is 0.2337 or 23.37%

```
#Logistic Regression
crv_glm <- glm(Purchase ~ ., data = crv_train, family = binomial)

## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

pred_glm <- predict(crv_glm, crv_test, type = "response")

## Warning in predict.lm(object, newdata, se.fit, scale = 1, type = if (type == :
## prediction from a rank-deficient fit may be misleading

glm_pred <- ifelse(pred_glm > 0.2, 1, 0)
table(crv_test$Purchase, glm_pred)

## glm_pred
## 0 1
## 0 4183 350
```

From Logistic Regression, the fraction of people predicted to make a purchase and who actually made a purchase is 58/(58 + 350), which is 0.1421 or 14.21%. Logistic regression performs worse than Boosting in this scenario.

1 231

##

58