

what does $-32 \text{ lbf}/300 \text{ lbm}$ mean? lbf/lbm has units of force/mass, so it is an acceleration. But how to convert to something useful like ft/s^2 ? Multiply by 1 in the funny form of $g_c = 1 = 32.174 \text{ lbm ft} / \text{lbf s}^2$, of course!

$$\text{acceleration} = (-32 \text{ lbf}/300 \text{ lbm}) (32.174 \text{ lbm ft} / \text{lbf s}^2) = -3.43 \text{ ft}/\text{s}^2$$

or, since $g_{\text{earth}} = 32.174 \text{ ft}/\text{s}^2$,

$$\text{acceleration} = (-3.43 \text{ ft}/\text{s}^2) / (32.174 \text{ ft}/\text{s}^2 g_{\text{earth}}) = -0.107 g_{\text{earth}}.$$

The negative sign indicates the acceleration is in the $-x$ direction, i.e. down the slope of course.

A good function test is that the acceleration has to be less than $1 g_{\text{earth}}$, which is what you would get if you dropped the block vertically in a frictionless environment. Obviously, a block sliding down a slope (not vertical) with friction and with an external force acting up the slope must have a smaller acceleration.

Example 4. Wheels and friction

A car of known weight W is equipped with rubber tires with coefficient of static friction μ_s . Unlike the earlier example, there is no cable but the wheels are locked and thus the tires exert a friction force parallel to and in the plane of the ramp surface. As with the previous example, the car is on a ramp of angle θ with respect to horizontal. The center of gravity of the vehicle is a distance “ c ” above the ramp, a distance “ a ” behind the front wheels, and a distance “ b ” in front of the rear wheels.

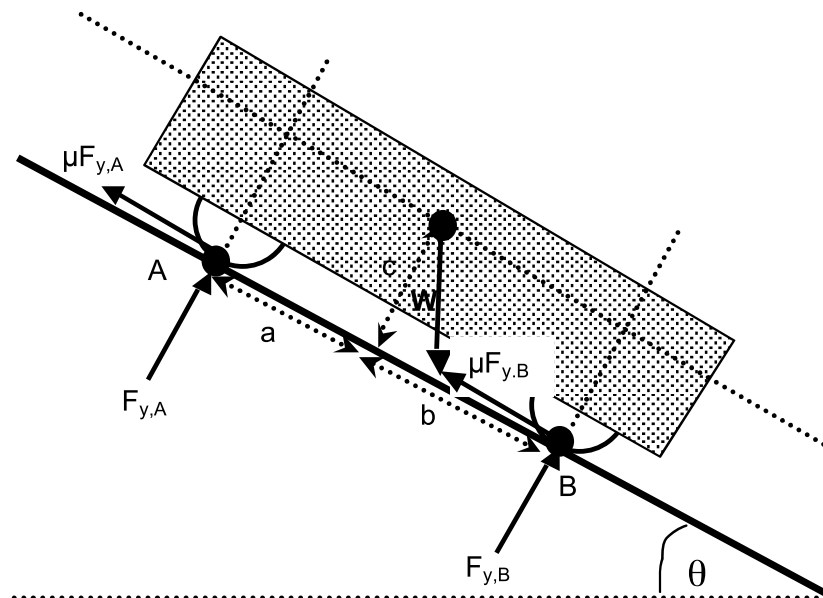


Figure 9. Free body diagram for car-on-ramp with friction example

(a) What is the minimum μ_s required to keep the car from sliding down the ramp?