

Lab 3: FM Simulation and USRP

Exercise 1: FM Modulator

Generalised function for FM is:

$$g(t) = A_c \cos(2\pi f_c t + \theta_m(t)), \text{ where } \theta_m(t) = 2\pi\Delta_f \int m(\tau) d\tau,$$

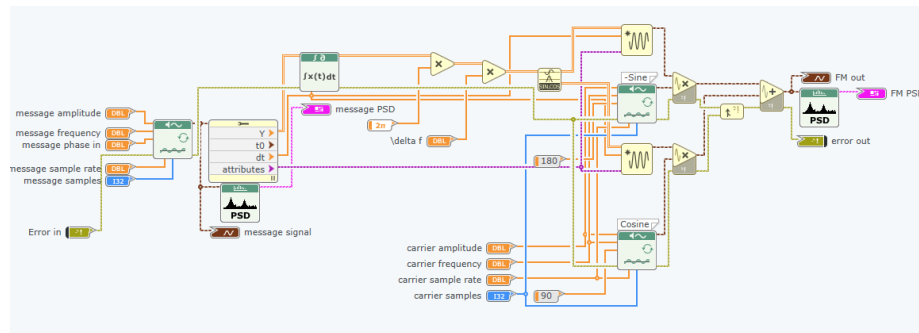
Instantaneous frequency is:

$$\omega = 2\pi f_c t + \theta_m(t)$$

Equivalent form we will be using:

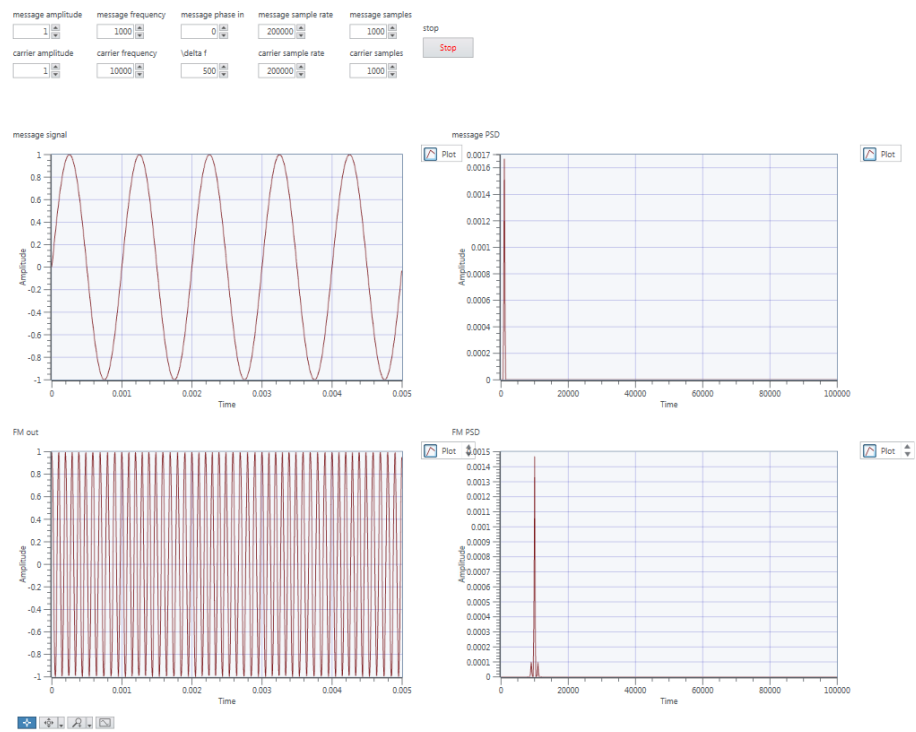
$$s(t) = A_c \cos(2\pi f_c t) \cos(\theta_m(t)) - A_c \sin(2\pi f_c t) \sin(\theta_m(t))$$

Diagram



Varying δf

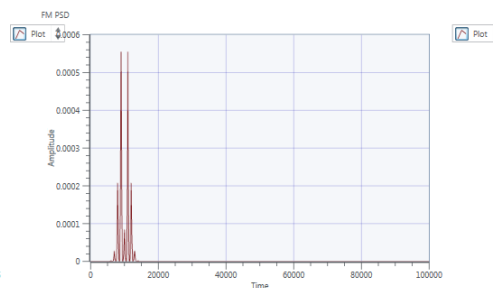
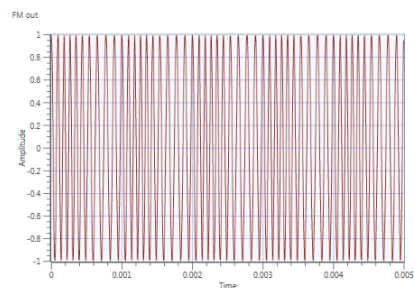
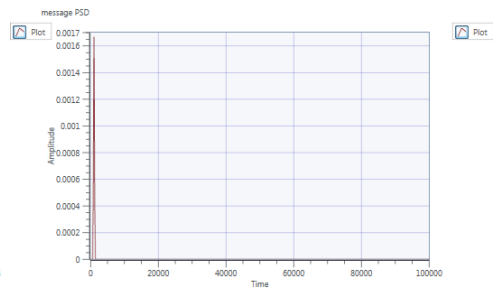
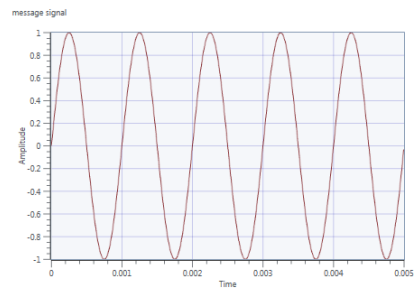
$\delta f = 500$



$\Delta f = 2000$

message amplitude	message frequency	message phase in	message sample rate	message samples
1	1000	0	200000	1000
carrier amplitude	carrier frequency	Δf	carrier sample rate	carrier samples
1	10000	2000	200000	1000

stop

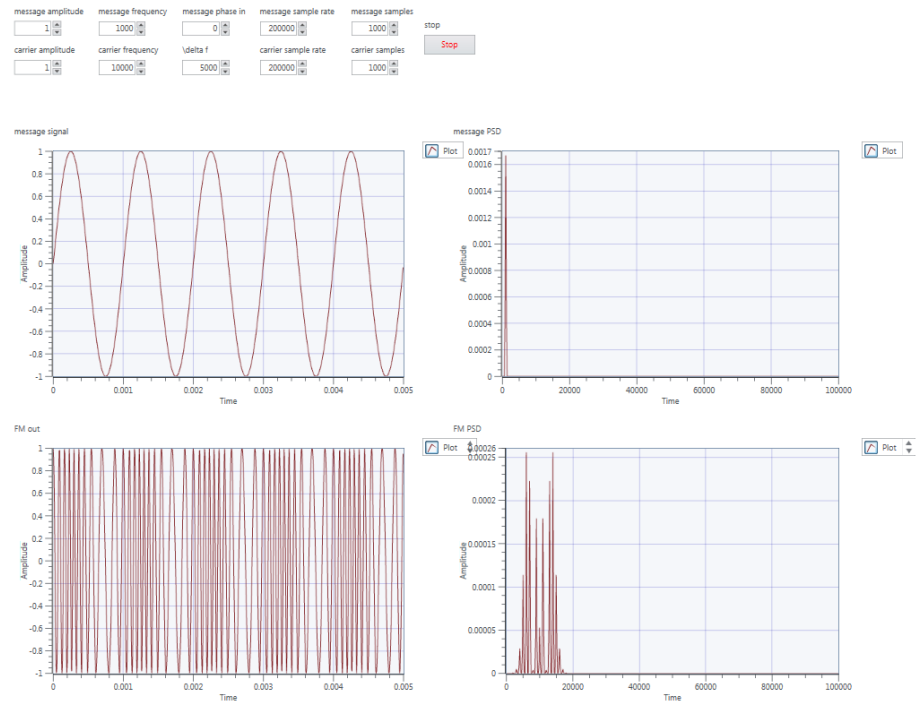


Plot

Plot

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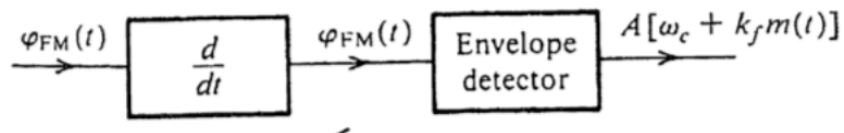
$\Delta f = 5000$



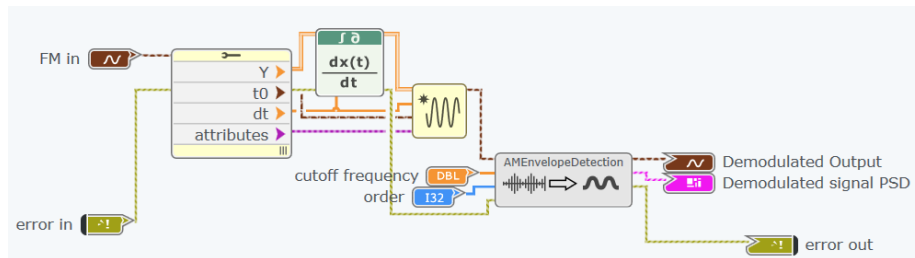
- As Δf increases, you can more easily see the variations in frequency of the FM signal.
- In the frequency domain, you can see the message signal spread across a larger bandwidth.

Exercise 2: FM Demodulator

- Theory is that the derivative provides a sinusoidal signal which has amplitude proportional to the message signal.
- This is just like AM modulation, so the envelope detection method works to retrieve the signal from the differentiated signal.
- Coherent detection would not work because we do not know the phase of the resultant signal

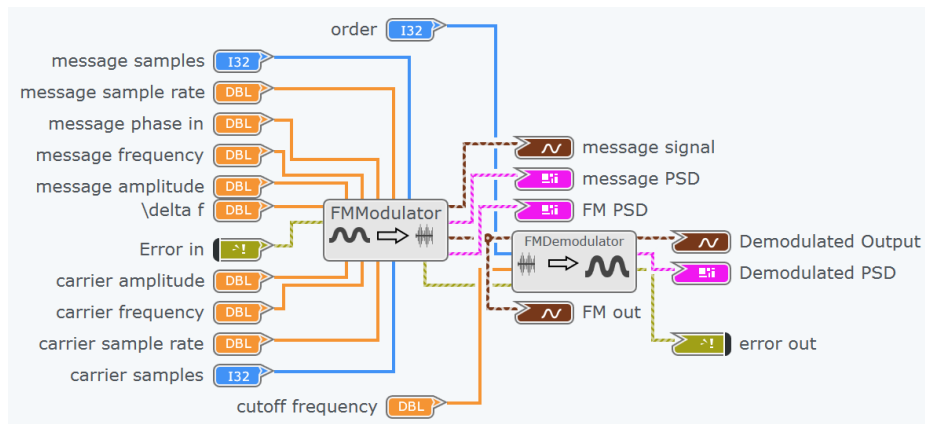


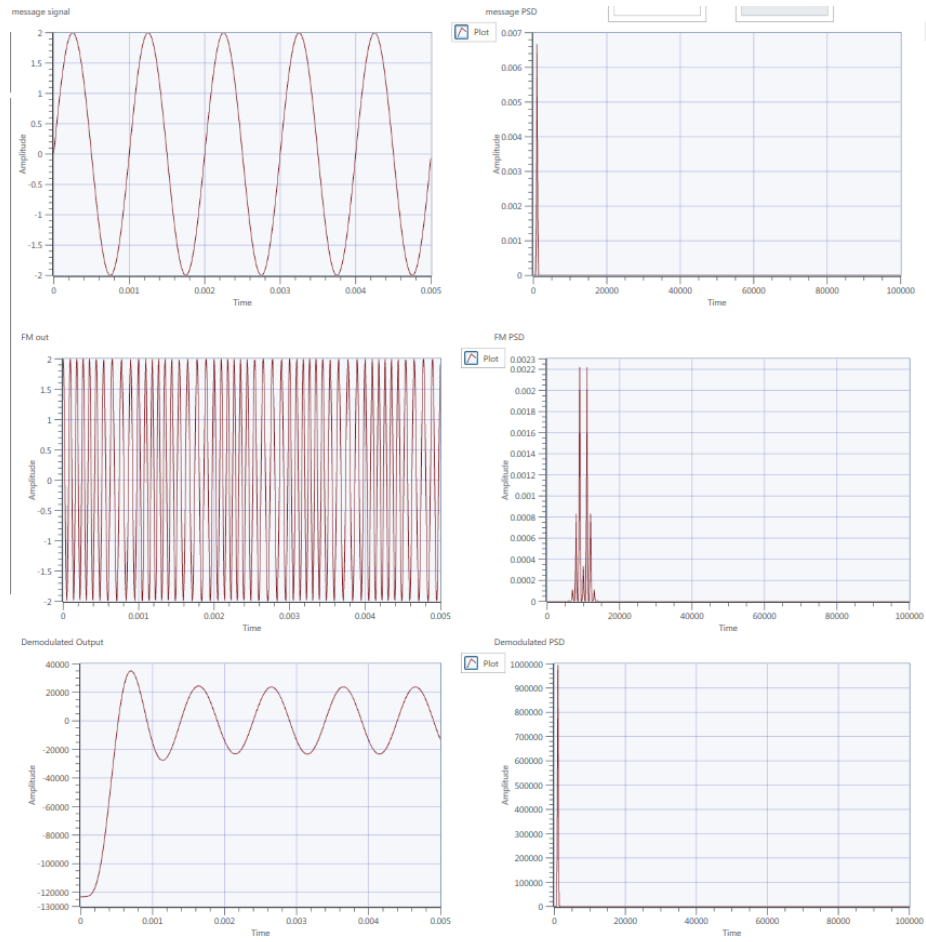
Envelope Detection



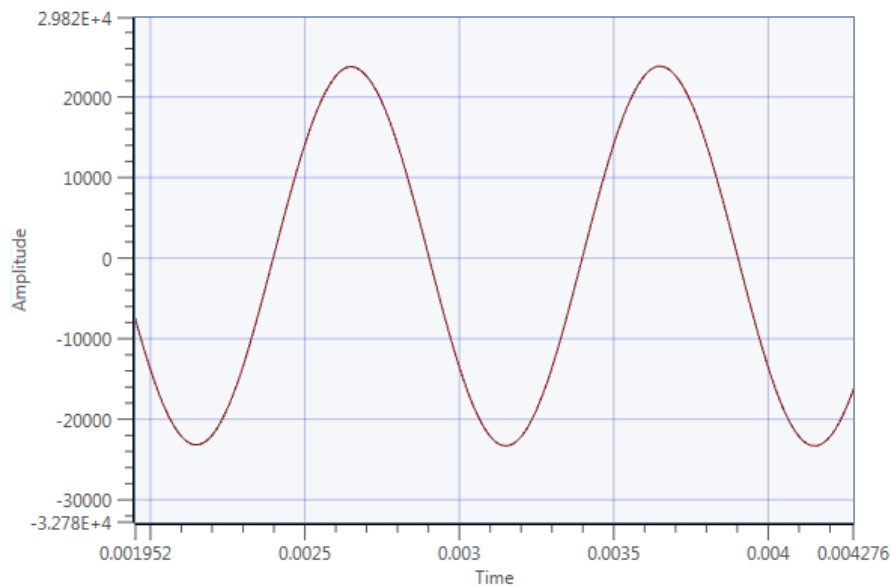
Exercise 3: FM Simulation

Top level Diagram



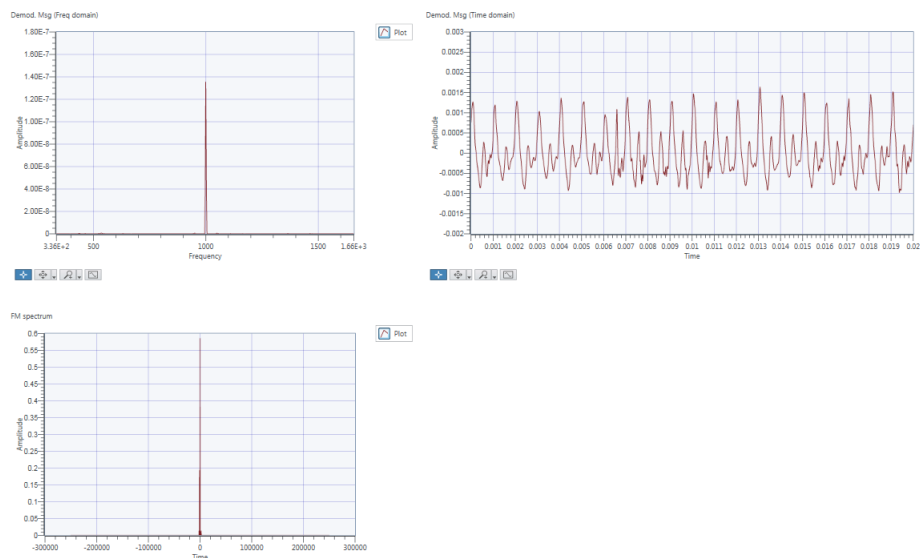


Demodulated Output

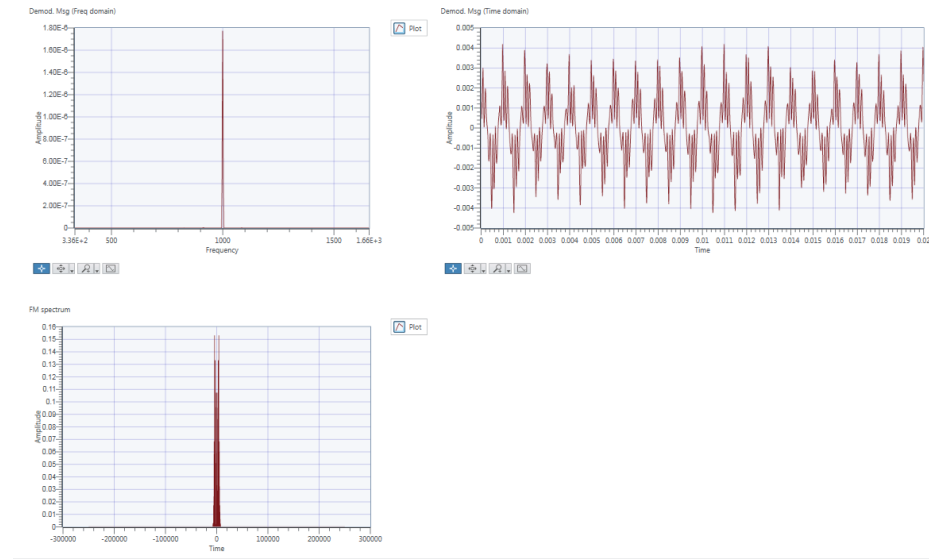


Exercise 4: FM USRP

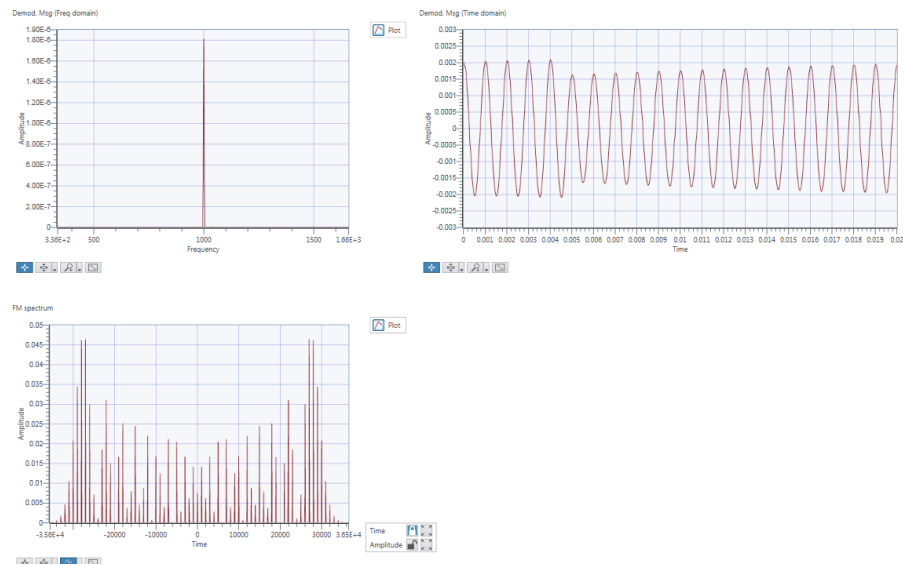
$\Delta f = 1\text{kHz}$



$\Delta f = 5\text{kHz}$



$\Delta f = 30\text{kHz}$



- Note that the bandwidth of this signal is 62kHz, which agrees with Carsons rule for $\Delta f = 30\text{kHz}$ and $B = 1\text{kHz}$:

$$B_{FM} \cong 2(\Delta f + B) = 62\text{kHz}.$$