

CS202: Software Tools and Techniques for CSE

Lecture 8

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Memory Optimization

- Reuse memory / register wherever possible.
- z and y can reuse memory / register.

Live Ranges

x : (0,1), (3,4,5), (0,1,6,7,8)

y : (4,5,10), (7,8,9,10)

z : (0,1,2), (0,1,6,7)

```
0 int x = 2, y = 3, z = 1;
1 if (x == 2) {
2     y = z;
3     x = 9;
4     y = 7;
5     x = x - y;
6 } else {
7     y = x + z;
8     ++x;
9 }
10 printf("%d", y);
```

This optimization demands computation of live variables.

DFA for Live Variables

Domain	Sets of variables
Transfer function	$\text{in}(B) = \text{use}(B) \cup (\text{out}(B) \cap \text{def}(B))$ $\text{out}(B) = \bigcup \text{in}(S)$ where S is a successor of B
Direction	Backward
Meet / confluence operator	\cup
Initialization	$\text{in}(B) = \{ \}$

Definition: A variable v is **live** at a program point p if v is used along some path in the flow graph starting at p . Otherwise, the variable v is **dead**.

How to compute live variables?

Algorithm for Live Variable Analysis

```

for each basic block B
  compute  $\text{gen}(B)$  and  $\text{kill}(B)$ 
   $\text{out}(B) = \{ \}$ 
do {
  for each basic block B
     $\text{in}(B) = \bigcup \text{out}(P)$  where  $P \in \text{pred}(B)$ 
     $\text{out}(B) = \text{gen}(B) \cup (\text{in}(B) - \text{kill}(B))$ 
  } while  $\text{in}(B)$  changes for any basic block B
    
```

Algo for
**reaching
definitions**

Domain	Sets of variables
Transfer function	$\text{in}(B) = \text{use}(B) \cup (\text{out}(B) - \text{def}(B))$ $\text{out}(B) = \bigcup \text{in}(S)$ where S is a successor of B
Direction	Backward
Meet / confluence operator	\cup
Initialization	$\text{in}(B) = \{ \}$

Parameters
for **live
variable
analysis**

Direction and Confluence

	Forward	Backward
U	Reaching Definitions	Live Variables
n	Available Expressions	Very Busy Expressions

An expression is available at a program point P if the expression is computed along each path to P (from START) without getting invalidated.

An expression is very busy at a program point P if along each path from P (to END) the expression is computed without getting invalidated.

Data Flow Framework

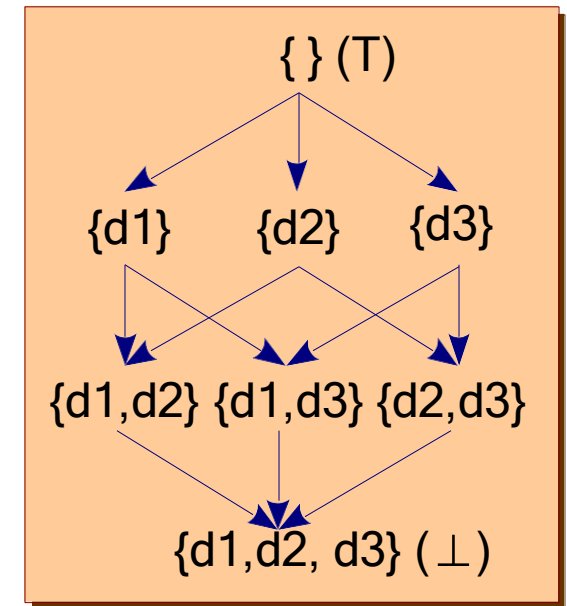
- Point: start or end of a basic block
- Information flow direction: forward / backward
- Transfer functions
- Meet / confluence operator
- One can define a transfer function over a path in the CFG $f_k(f_{k_1}(\dots f_2(f_1(f_0(T)))\dots))$ // small $k(\text{block})$
- $\text{MOP}(x) = \prod_K f_K(T)$ $K \in \text{Paths}(x)$ // capital K (path)

Meet over all paths

Path enumeration is expensive

Structure in Data Flow Framework

- A **semilattice** L with a binary meet operator \sqcap , such that $a, b, c \in L$
 - **Idempotency**: $a \sqcap a = a$
 - **Commutativity**: $a \sqcap b = b \sqcap a$
 - **Associativity**: $a \sqcap (b \sqcap c) = (a \sqcap b) \sqcap c$
- \sqcap imposes an order on L
 - $a \geq b \Leftrightarrow a \sqcap b = b$
- L has a **bottom** element \perp , $a \sqcap \perp = \perp$
- L has a **top** element \top , $a \sqcap \top = a$



Reaching Definitions Lattice

Analysis Dimensions

An analysis's precision and efficiency is guided by various design decisions.

- Flow-sensitivity
- Context-sensitivity
- Path-sensitivity
- Field-sensitivity



How many hands are required to know the time precisely?

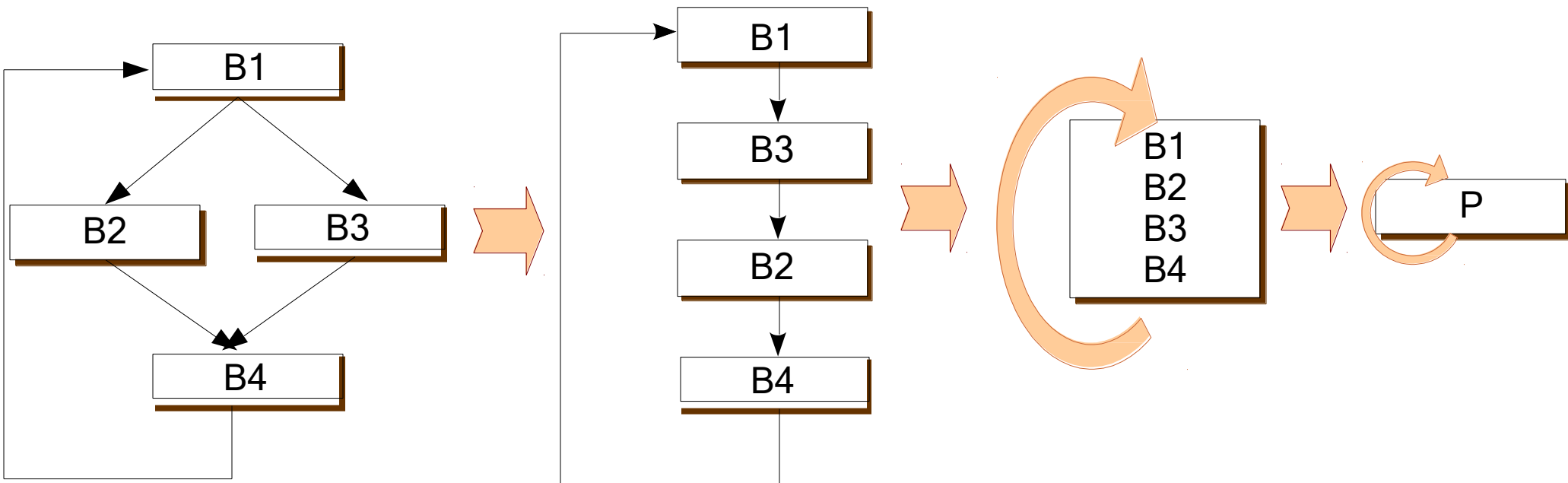
Flow-sensitivity

L0: $a = 0$;
L1: $a = 1$;
L2: ...

Flow-sensitive solution: *at L1 a is 0, at L2 a is 1*

Flow-insensitive solution: *in the program a is in $\{0, 1\}$*

Flow-insensitive analyses ignore the control-flow in the program.



Context-sensitivity

```
main() {  
  L0: fun(0);  
  L1: fun(1);  
}
```

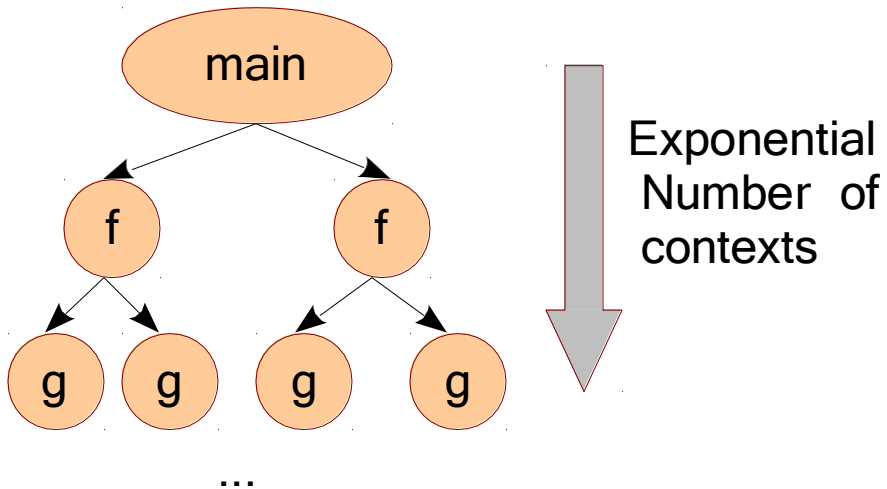
```
fun(int x) {  
  y = x;  
}
```

Context-sensitive solution:

y is 0 along L0, y is 1 along L1

Context-insensitive solution:

y is in {0, 1} in the program



Along main-f1-g1, ...
Along main-f1-g2, ...
Along main-f2-g1, ...
Along main-f2-g2, ...

Exponential time requirement

Exponential storage requirement

Context-sensitivity

<pre>main() { L0: fun(0); L1: fun(1); }</pre>	<pre>fun(int x) { y = x; }</pre>
---	--

Context-sensitive solution:
y is 0 along L0, y is 1 along L1

Context-insensitive solution:

Inter-procedural	→	<i>y is in {0, 1} in the program</i>
intra-procedural	→	<i>y is in $\{-\infty, +\infty\}$ in the program</i>

Path-sensitivity

```
if (a == 0)
    b = 1;
else
    b = 2;
```

Path-sensitive solution:

b is 1 when a is 0, b is 2 when a is not 0

Path-insensitive solution:

b is in {1, 2} in the program

```
if (c1)
    while (c2) {
        if (c3)
            ...
        else
            for (; c4; )
                ...
    }
else
    ...
```

```
c1 and c2 and c3, ...
c1 and c2 and !c3 and c4, ...
c1 and c2 and !c3 and !c4, ...
c1 and !c2, ...
!c1 ...
...
```

Field-sensitivity

```
struct T s;
```

```
s.a = 0;
```

```
s.b = 1;
```

Field-sensitive solution:

s.a is 0, s.b is 1

Field-insensitive solution:

s is in {0, 1}

Aggregates are collapsed into a single variable.
e.g., arrays, structures, unions.

This reduces the number of variables tracked during the analysis and reduces precision.

Texts, References, and Acknowledgements

Online:

- Continuous Integration and Delivery (**CircleCI**: <https://circleci.com>)
- <http://www.cse.iitm.ac.in/~rupesh/teaching/pa/jan19>

Textbook:

- Sharp, J. (2022). *Microsoft Visual C# Step by Step*, 10th edition, Microsoft Press.
- Watson, K., Nagel, C., Pedersen, J. H., Reid, J. D., & Skinner, M. (2008). *Beginning Microsoft Visual C# 2008*. John Wiley & Sons.
- Mark J. Price (2024). *C# 13 and .NET 9 – Modern Cross-Platform Development Fundamentals*, 9th edition, Packt Publishing Ltd.

Reference:

- Soni, M. (2016). *DevOps for Web Development*. Packt Publishing Ltd.
- Yusuf Sulistyo Nugroho, Hideaki Hata, and Kenichi Matsumoto. 2020. *How different are different diff algorithms in Git? Use --histogram for code changes*. Empirical Softw. Engg. 25, 1 (Jan 2020), 790–823.