

Hashing

Course on Data Structure



CS & IT Engineering

Data Structure
Graphs



Lecture Number- 32

By- Pankaj Sir



Topics

to be covered

1 Representation of Graphs



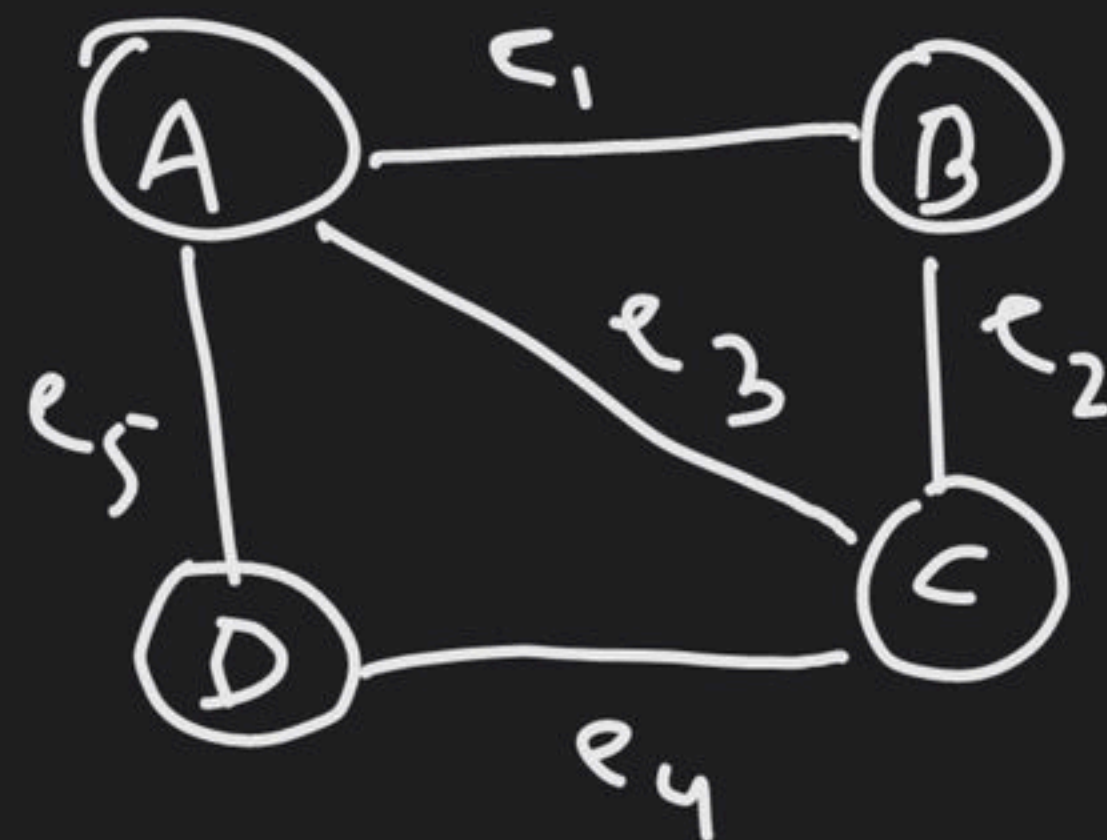
Graphs

Non linear data structure

$G(V, E)$

set of vertices

set of edges



$$V = \{A, B, C, D\}$$

$$E = \{e_1, e_2, e_3, e_4, e_5\}$$

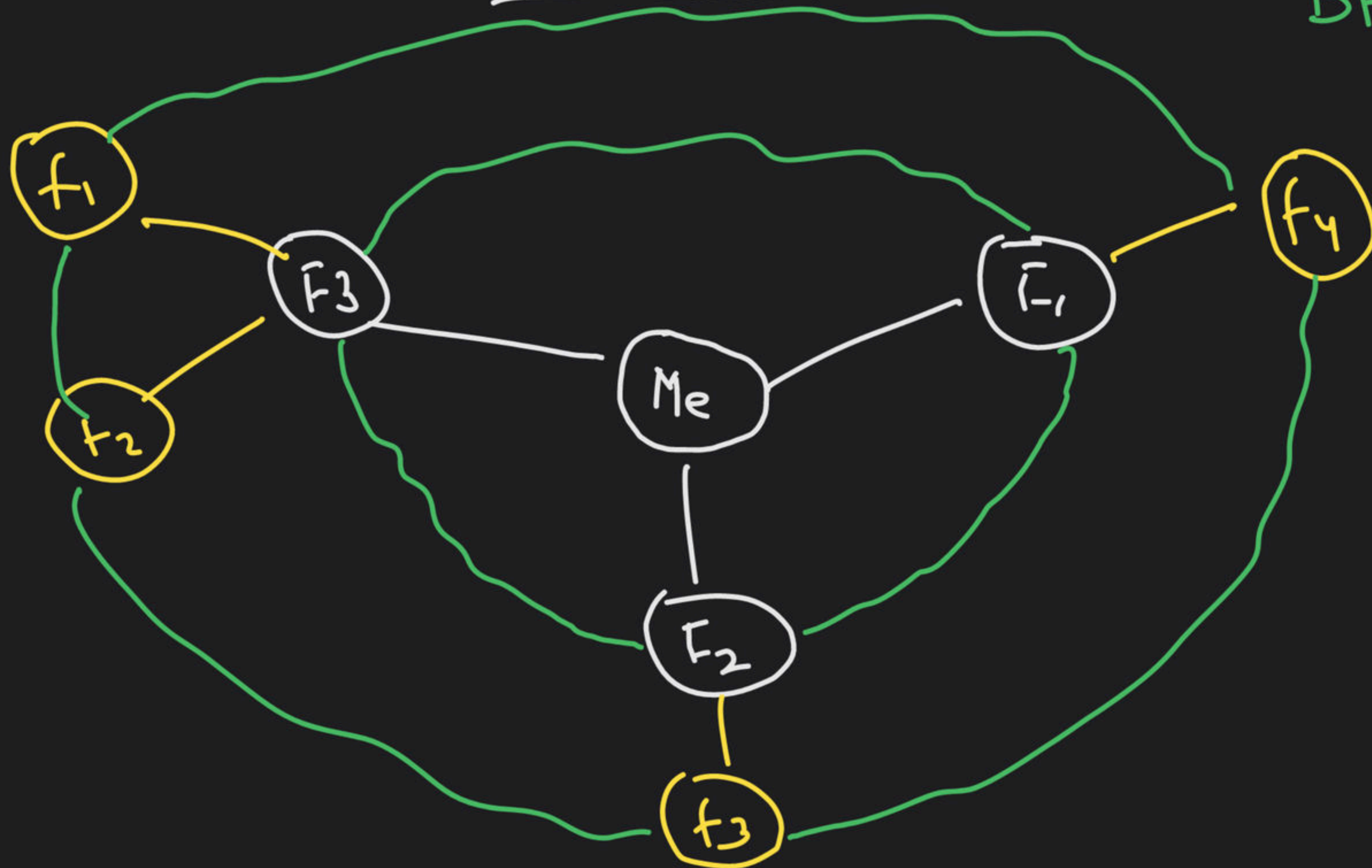
CS

wow



Social N/w

BFS



Graph Representation

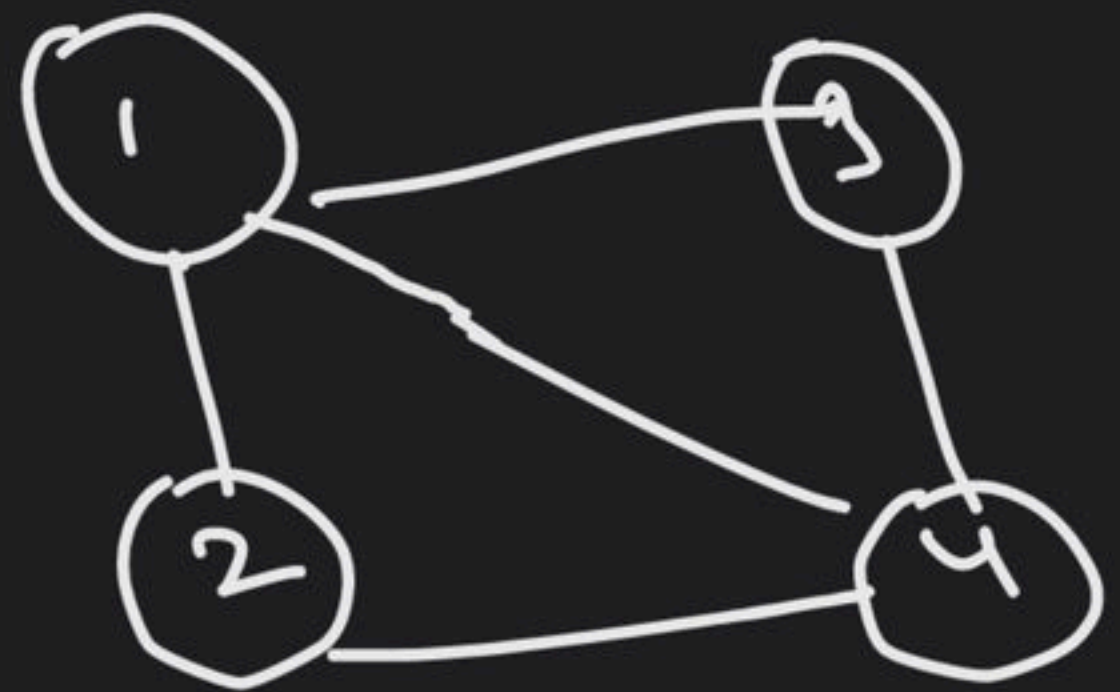
- 1) Adjacency Matrix
- 2) Adjacency List

Adjacency Matrix: $n \times n$ matrix, $n \Rightarrow$ no. of vertices

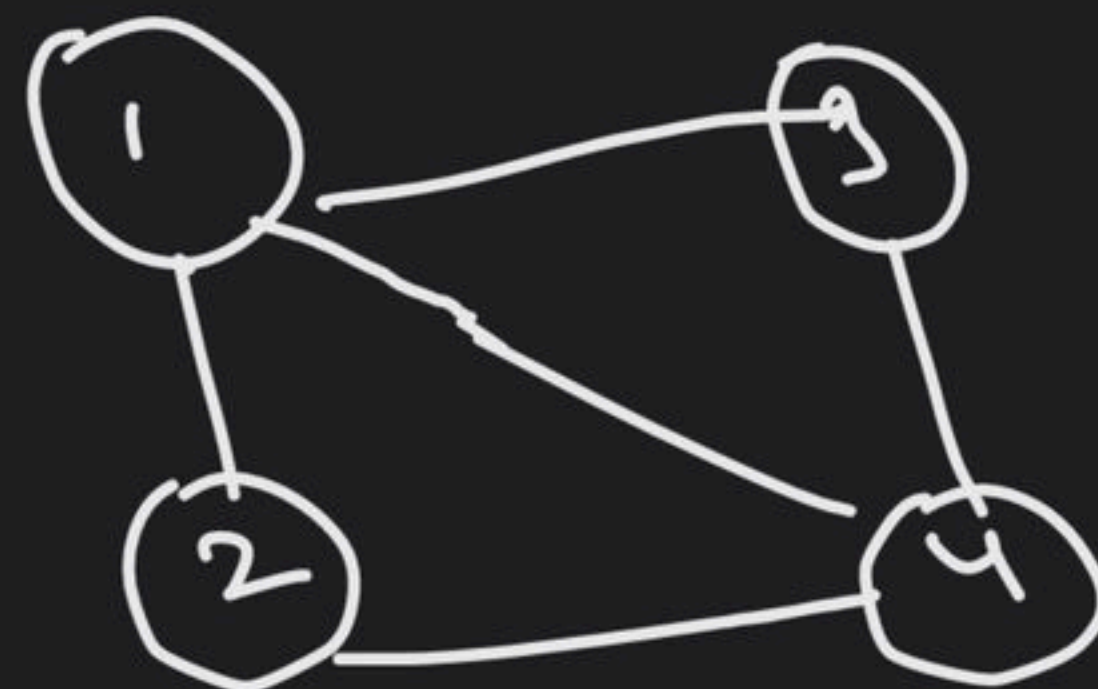
Each entry $\begin{matrix} \nearrow i \\ \searrow j \end{matrix}$

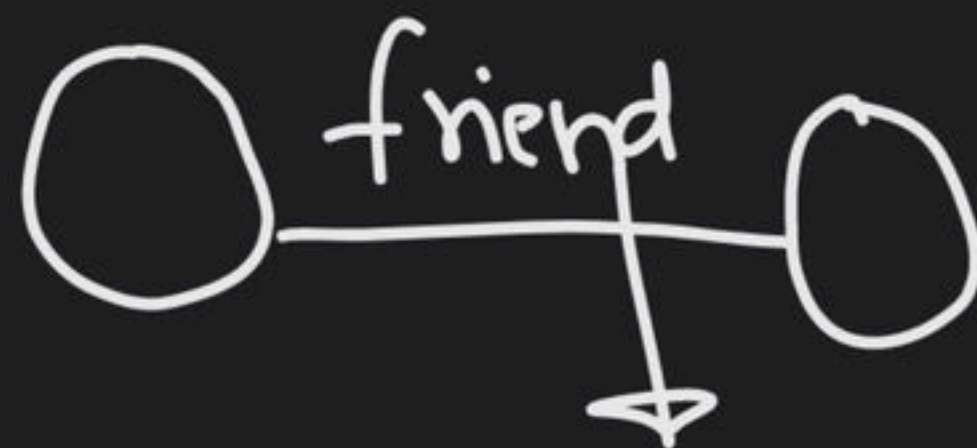
$$A_{ij} = 1$$

when node i is
adjacent to node
 j



$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

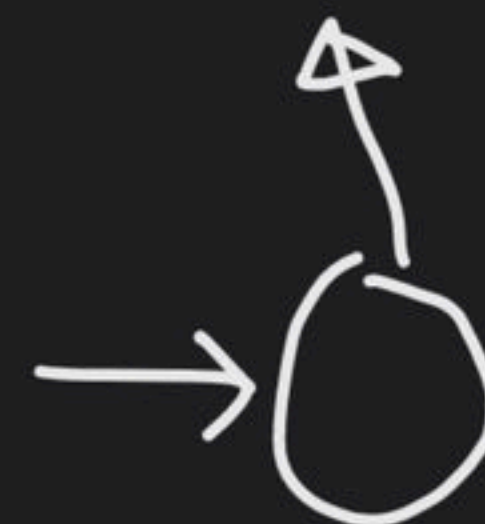
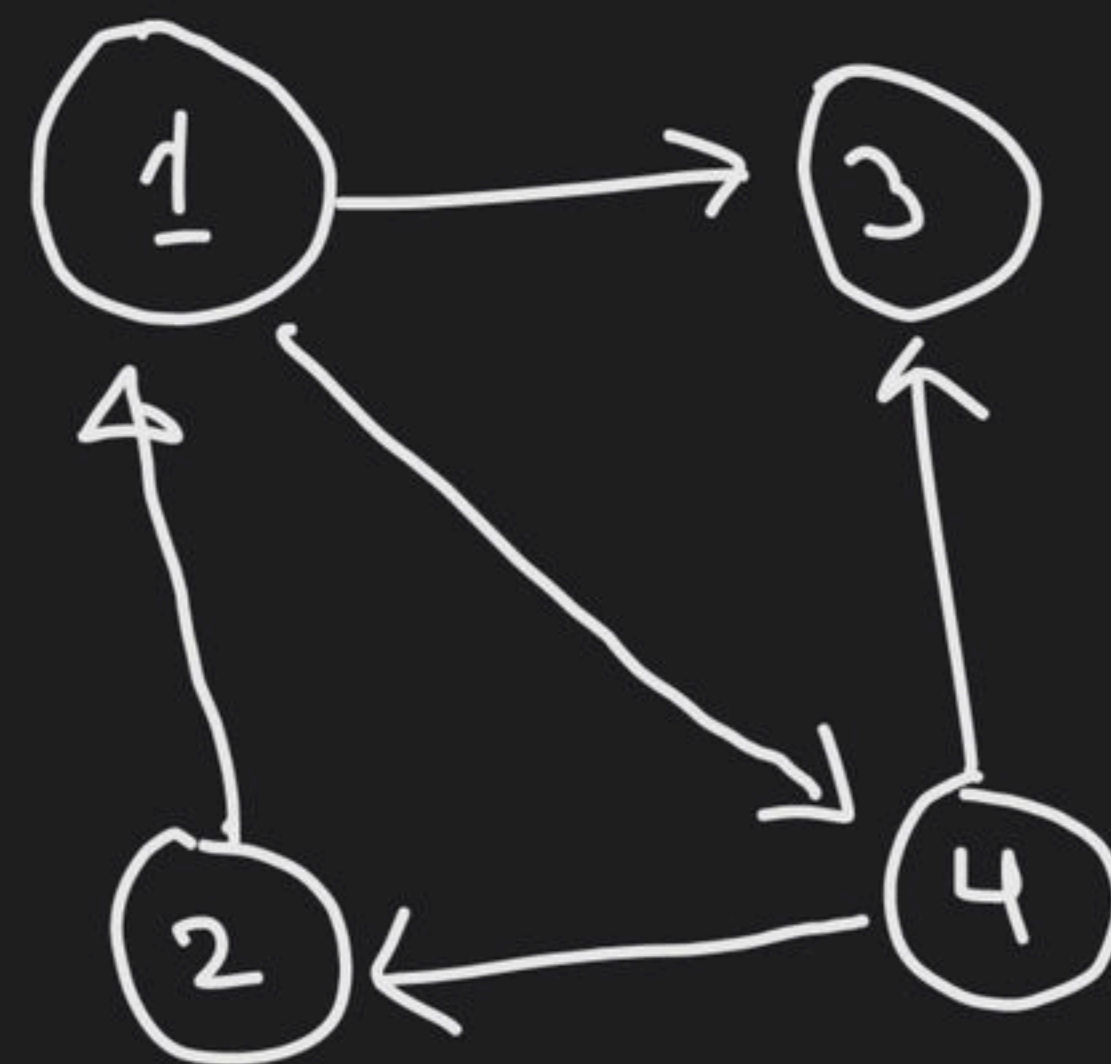




bidirectional



directed
edge / undirected
edge

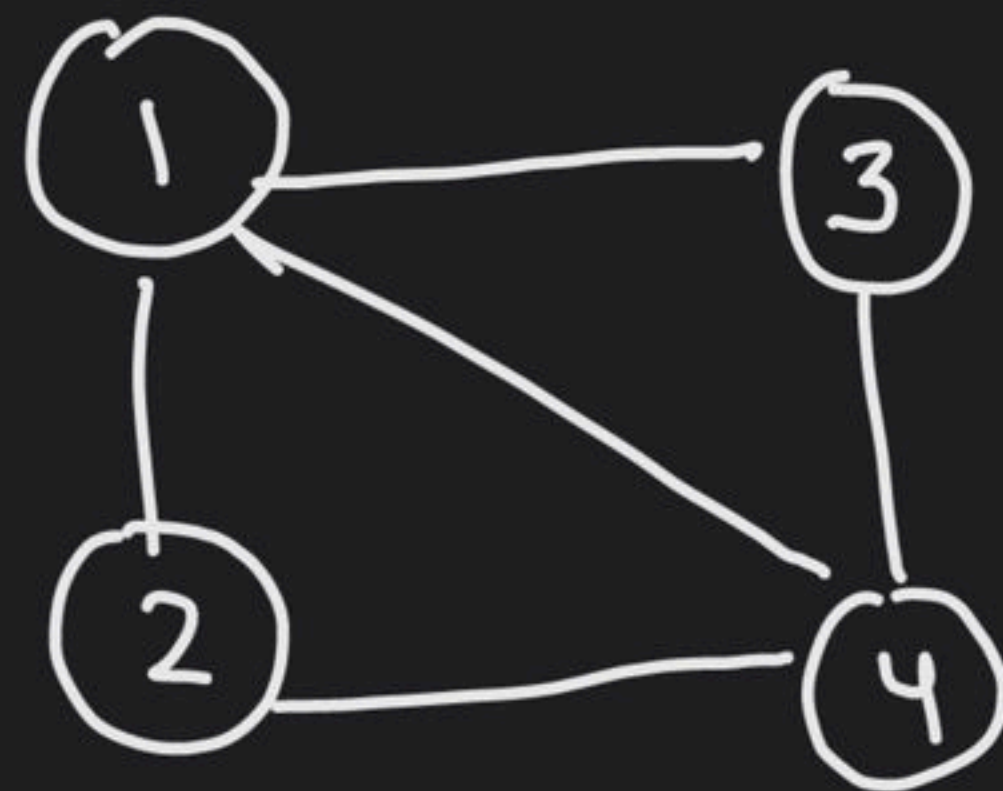
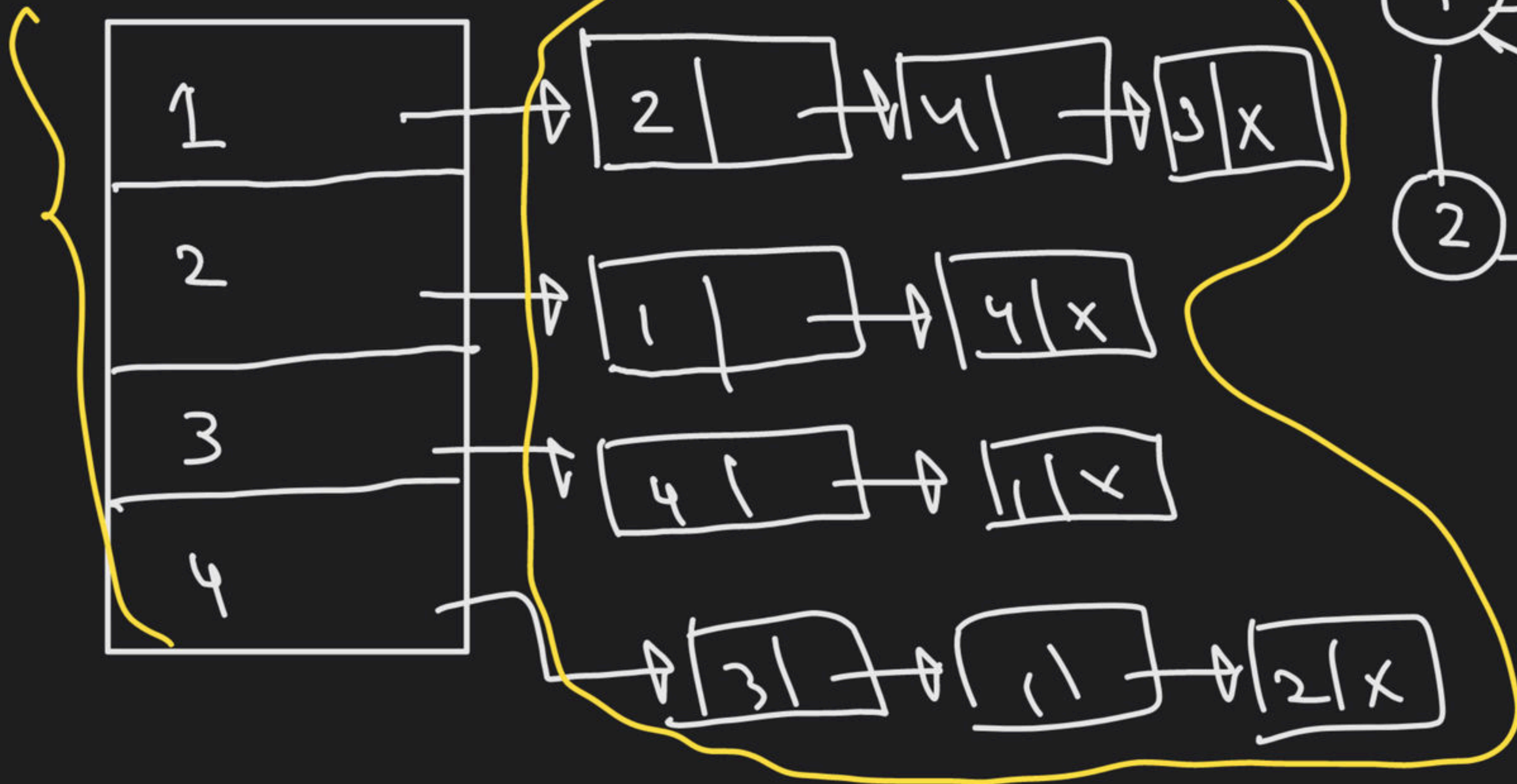
$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$


Adjacency List

$|V|$

$2|E|$

$|V| + 2|E|$

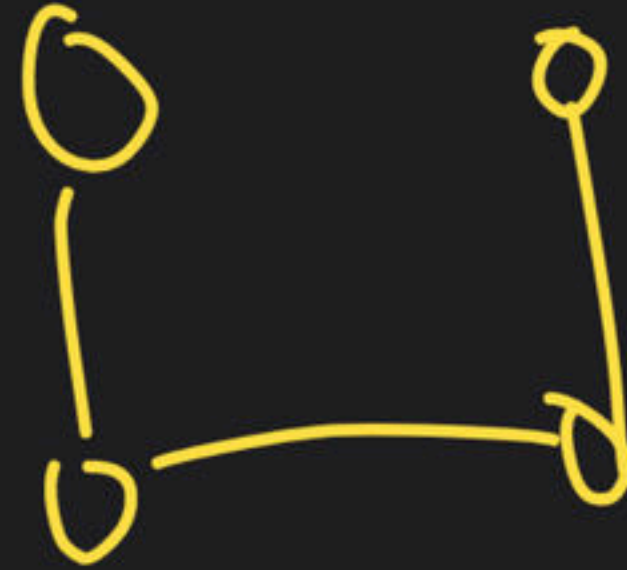
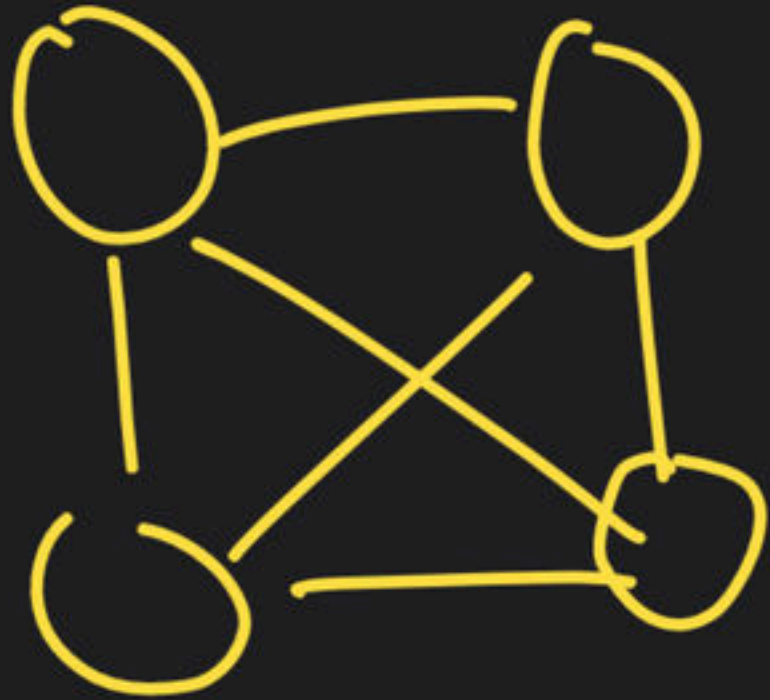


Dense

Sparse

①

complete
graph



$n \times n$ →

$$f_B \rightarrow 10^{10} \quad n = 10^{10}$$

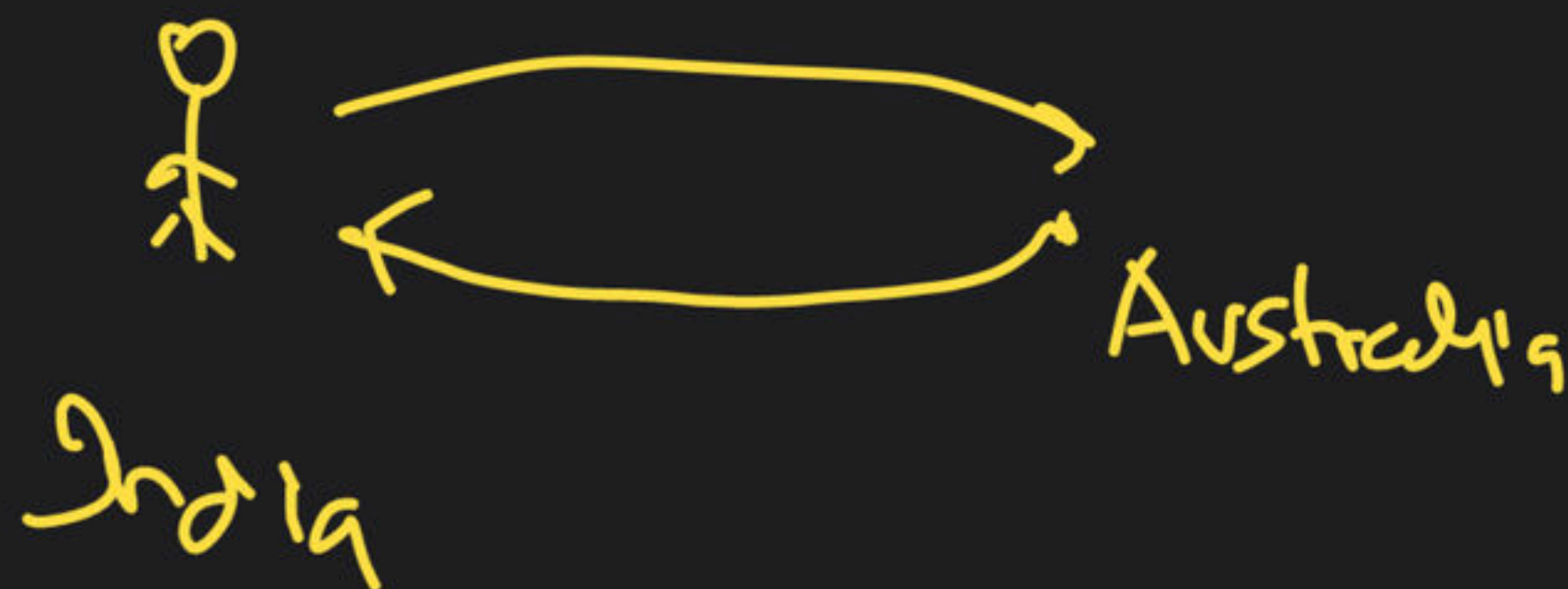
$$\text{Adj. Matrix} \Rightarrow 10^{10} \times 10^{10}$$

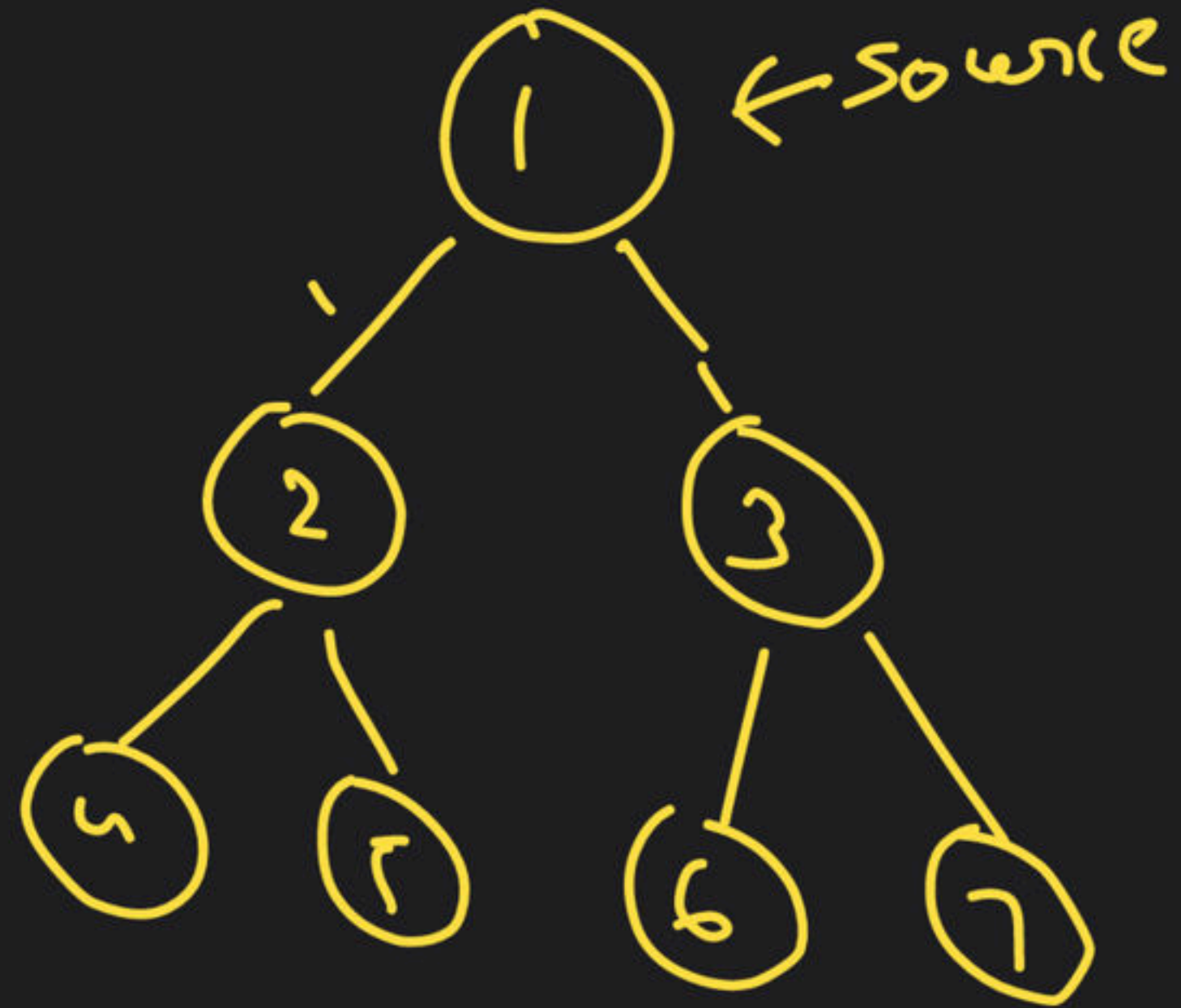


5000



- (i) visit
- (ii) Explore





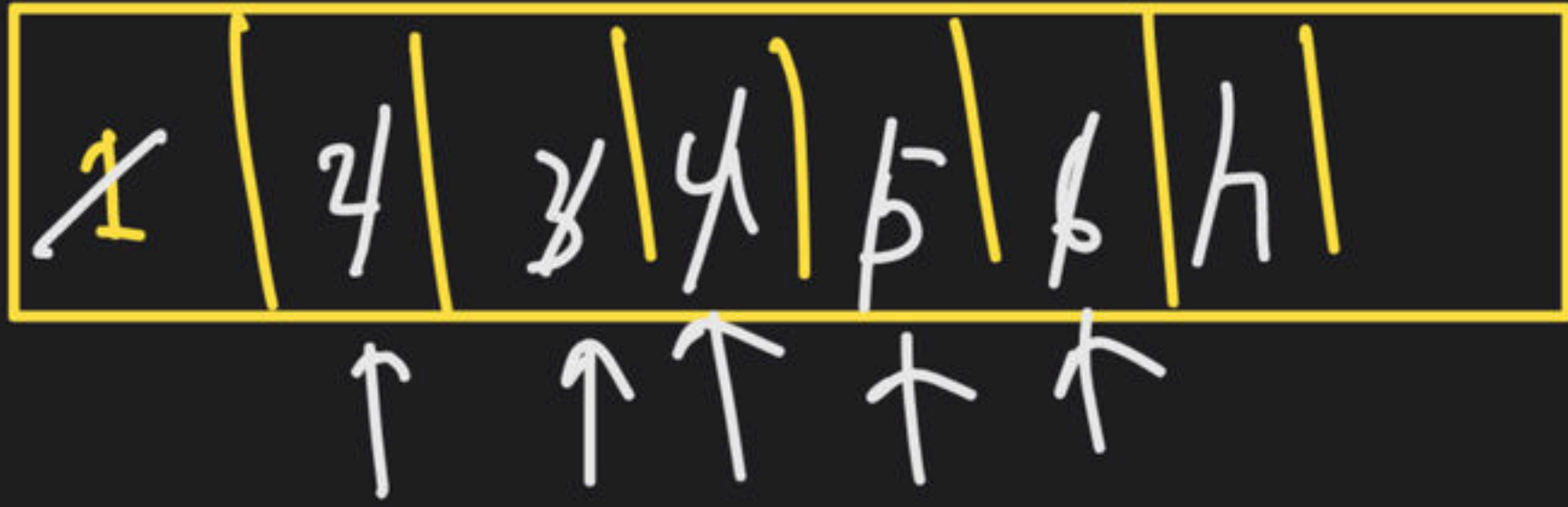
BFS

1 → {2, 3} → {4, 5, 6, 7}
 1 2

Queue:

Stack:

Queue



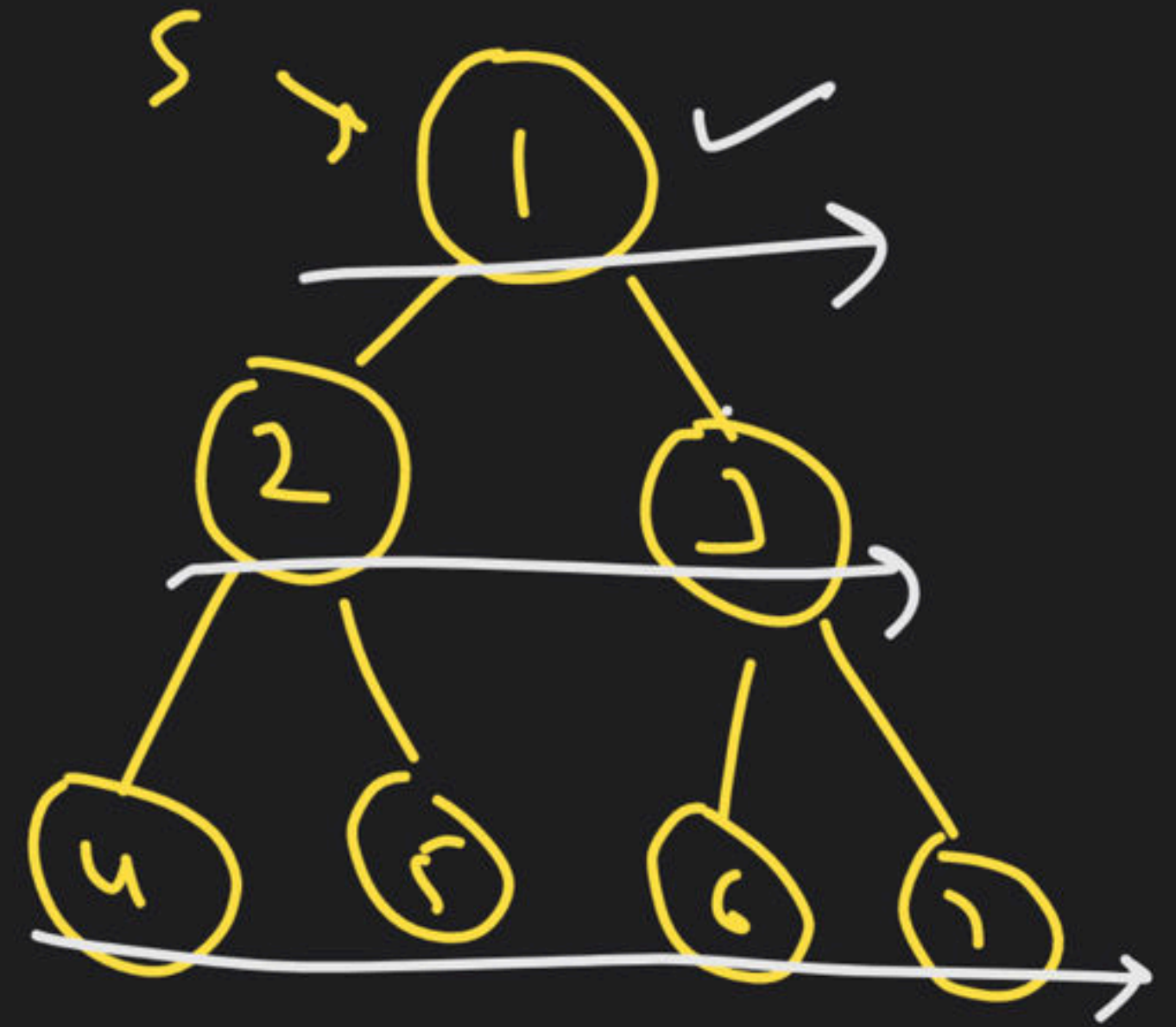
while (q is not empty)

{
u = dequeue();

print(u);

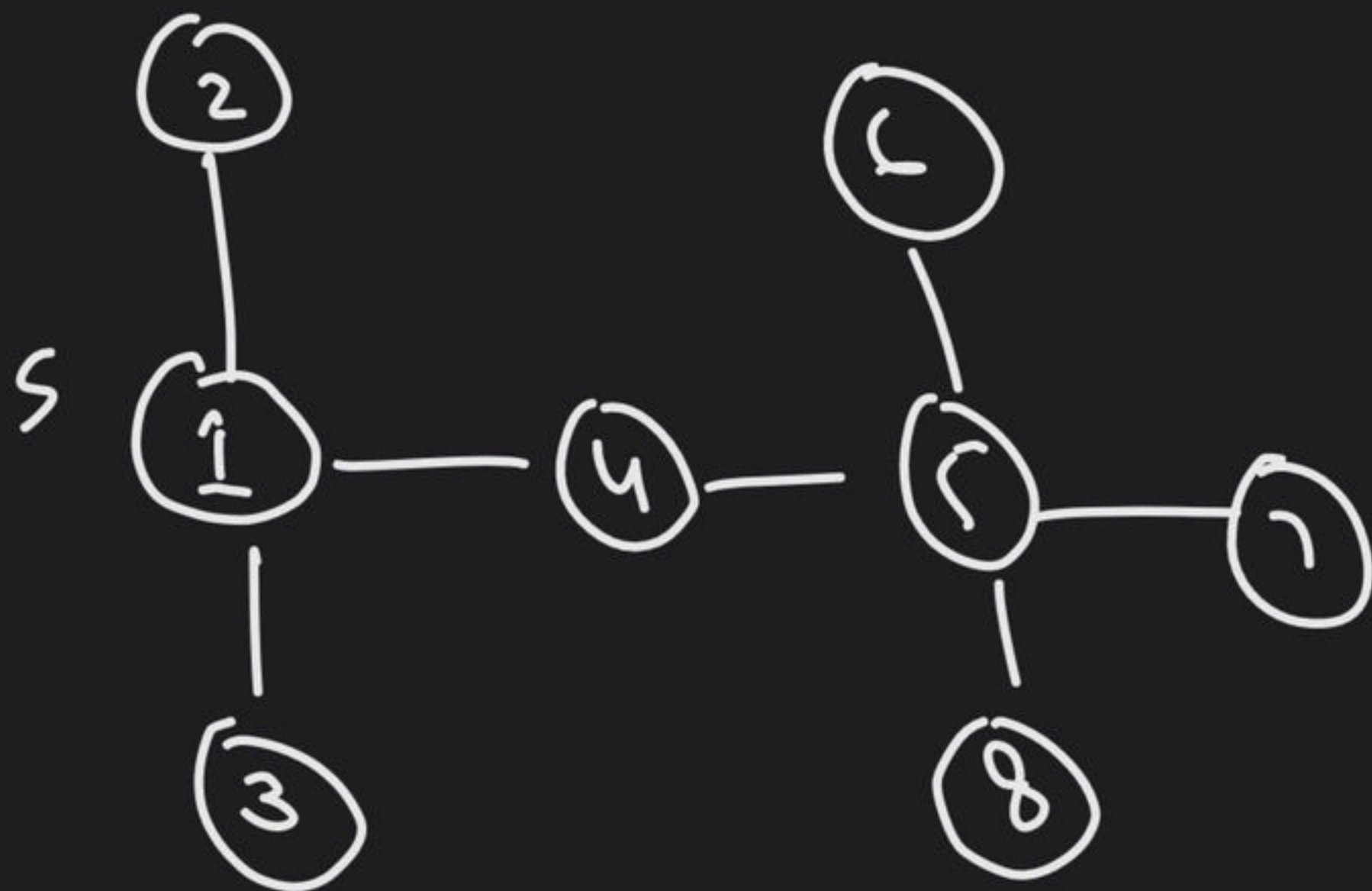
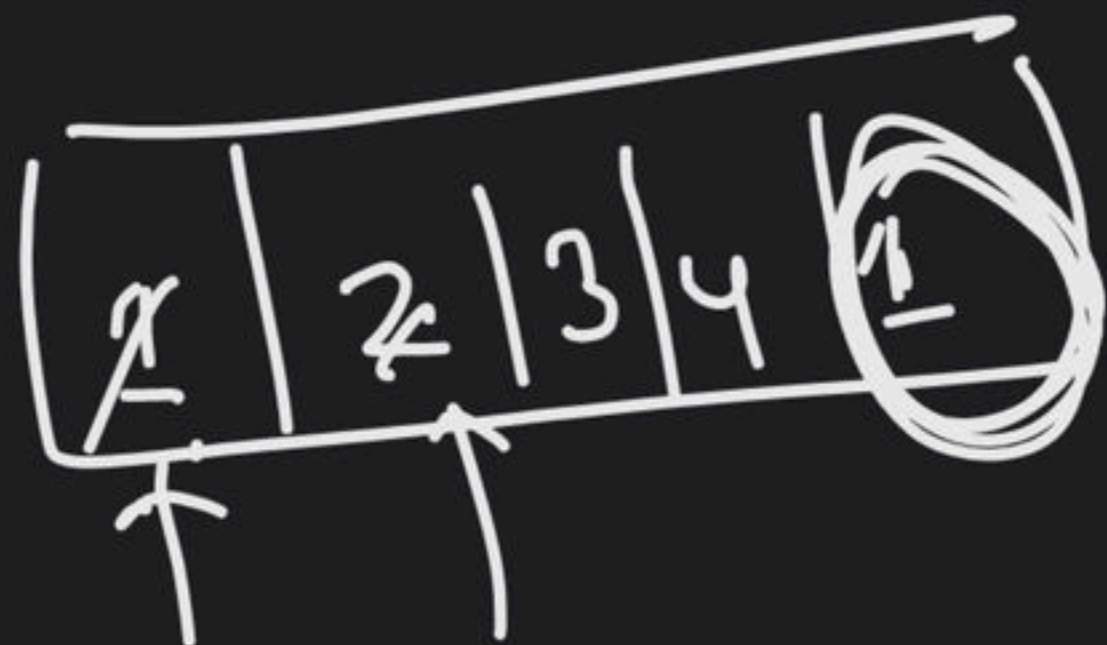
q.push(q->left);

q.push(q->right);



not
complete
code.

1 2 3 4 5 6 7
1 2
dist did-

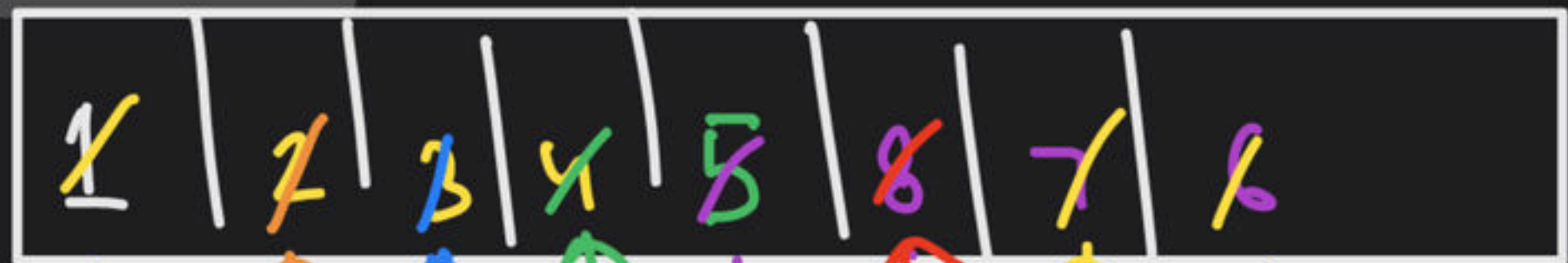


Another d.s.

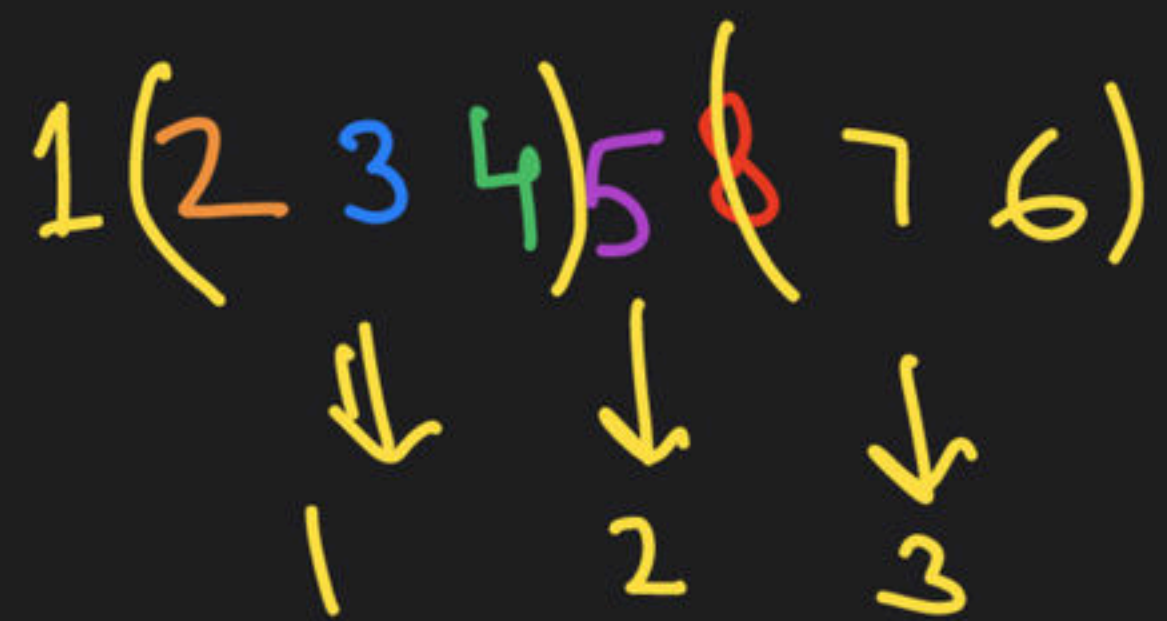
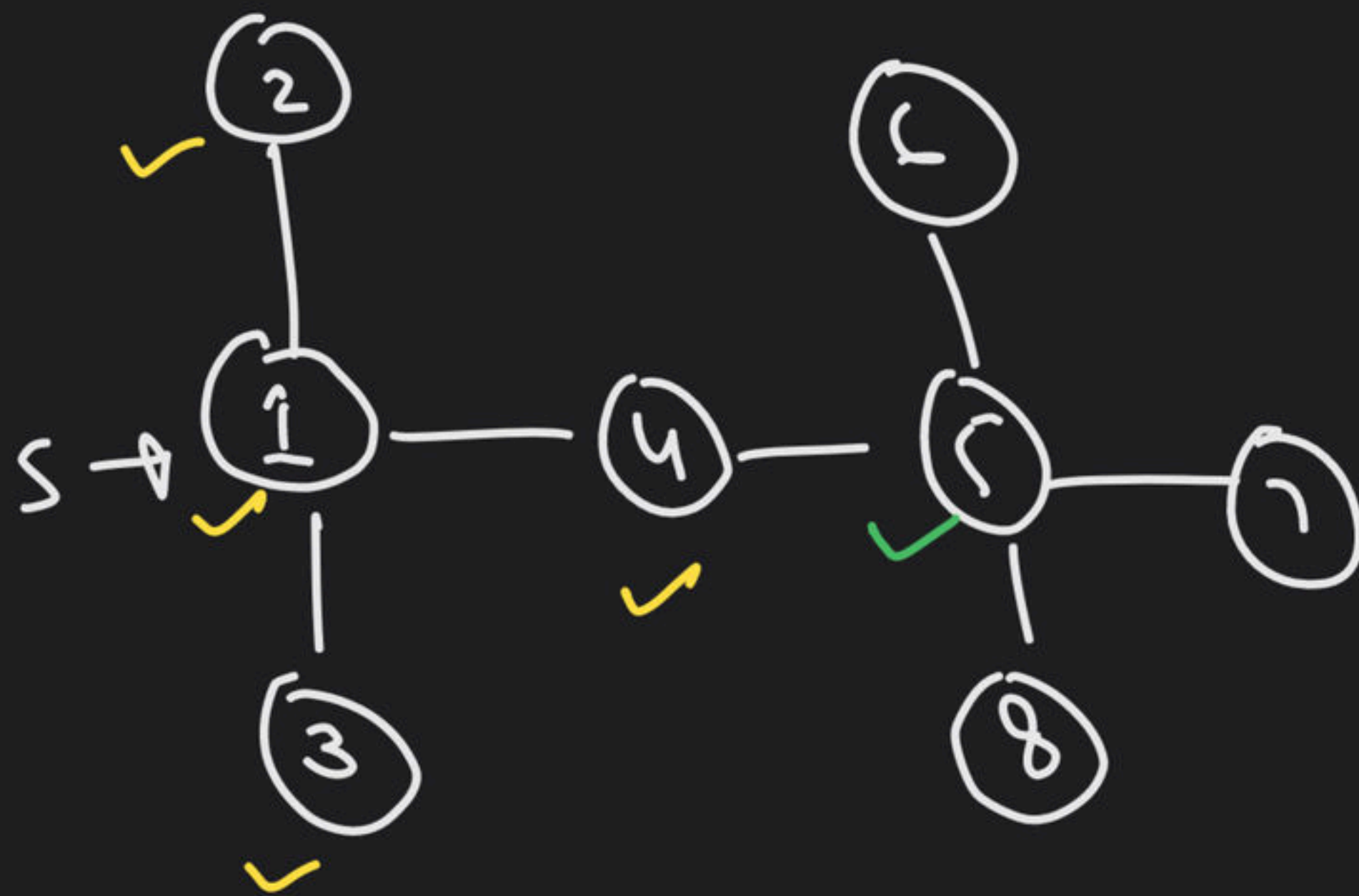
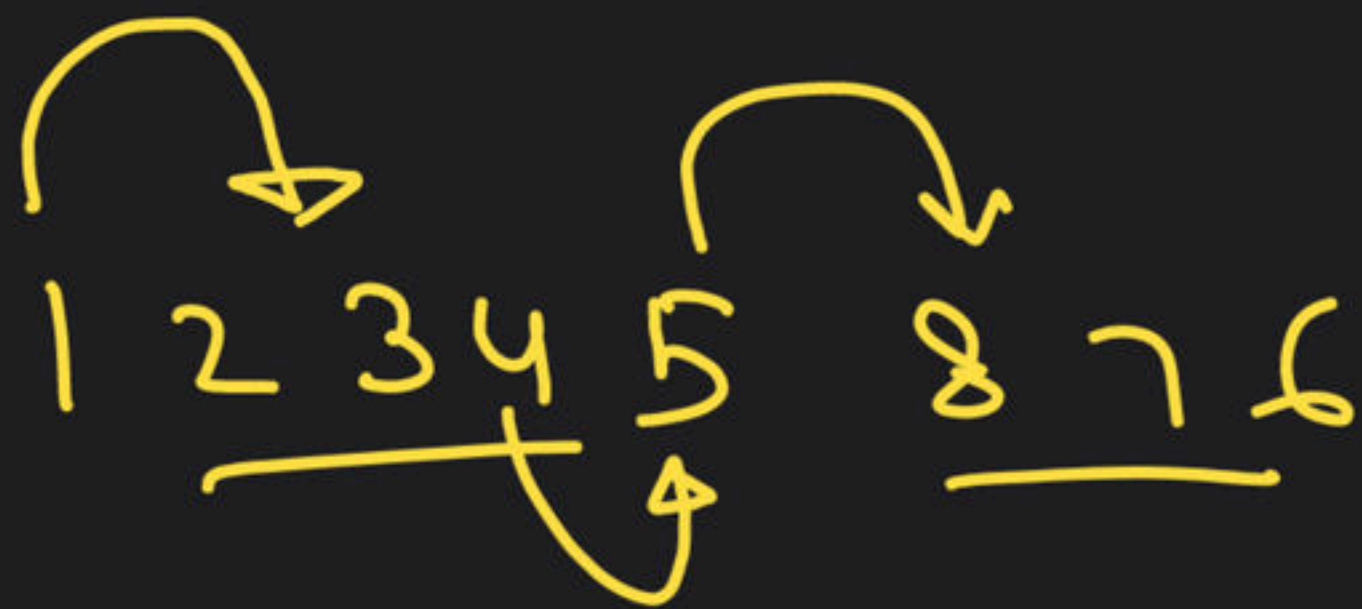
⇒ visited []

1 2

Q



visited 1 2 3 4 5 6 7 8



$1 \rightarrow \{2, 4, 3\} \rightarrow \{5\} \rightarrow \{7, 6, 8\}$ ✓

1 2 4 3 5 7 6 8

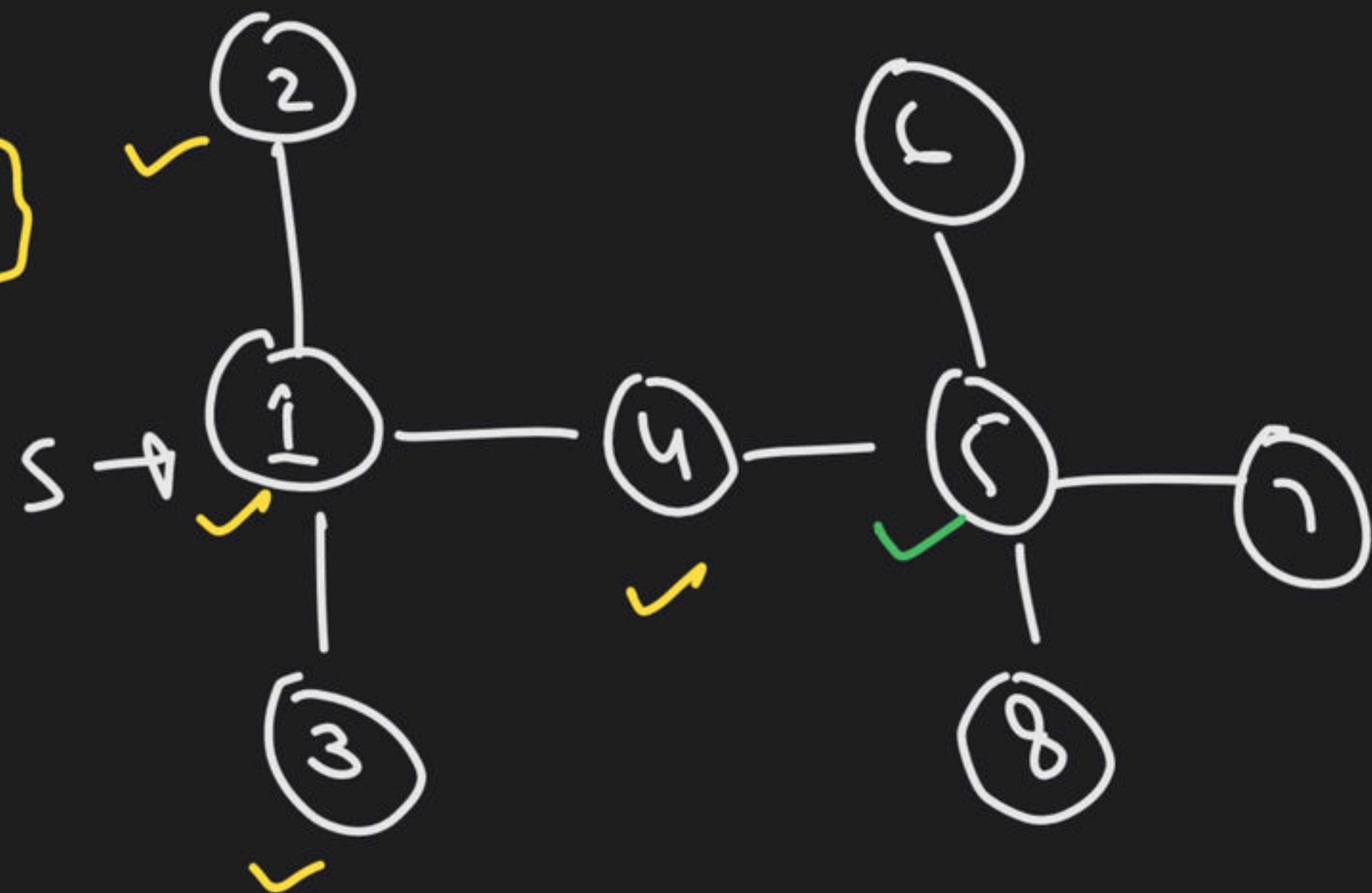
1 2 4 3 5 6 7 8

1 2 4 3 5 6 8 7

1 2 4 3 5 7 8 6

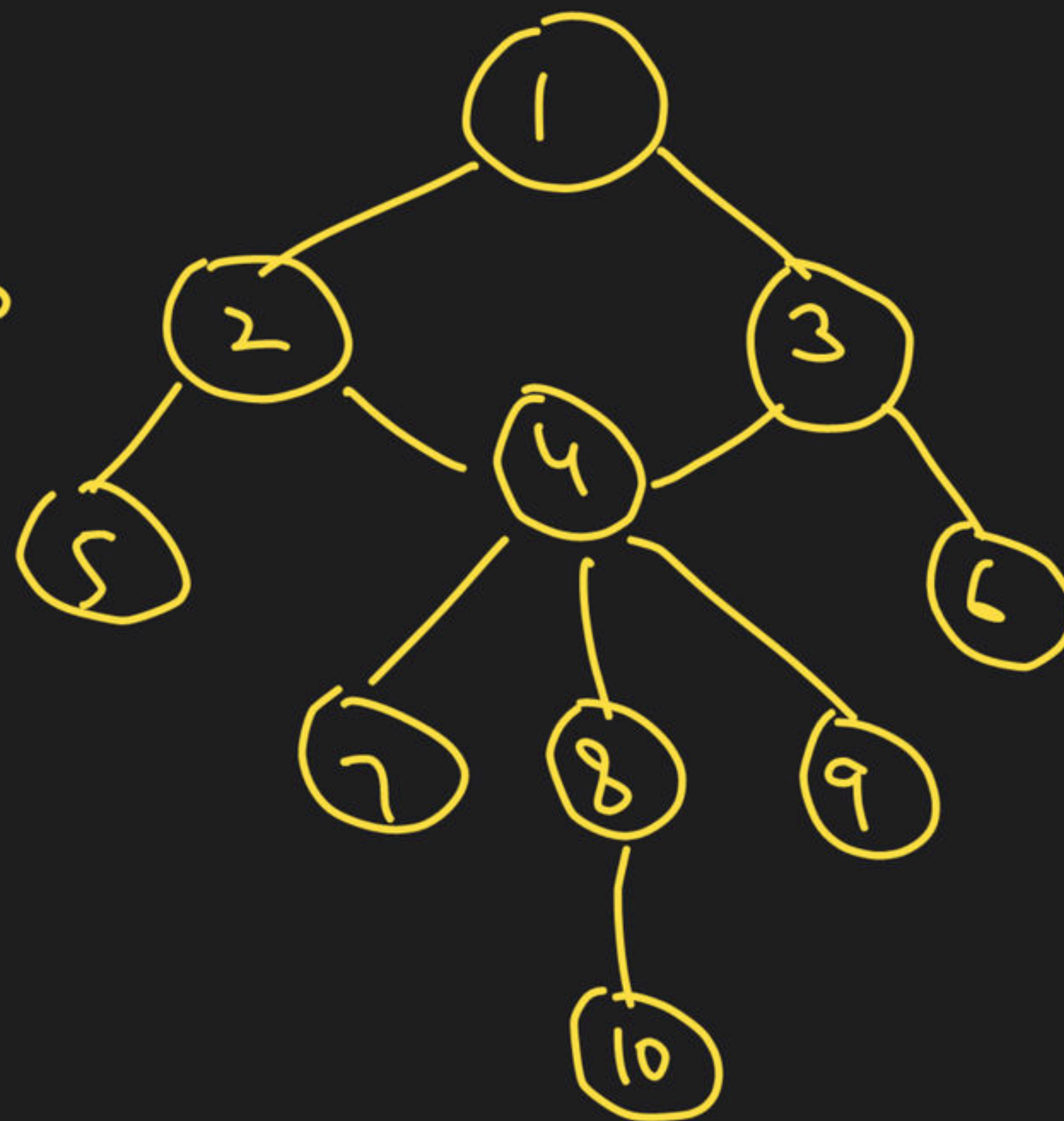
1 2 4 3 5 8 6 7

1 2 4 3 5 8 7 6



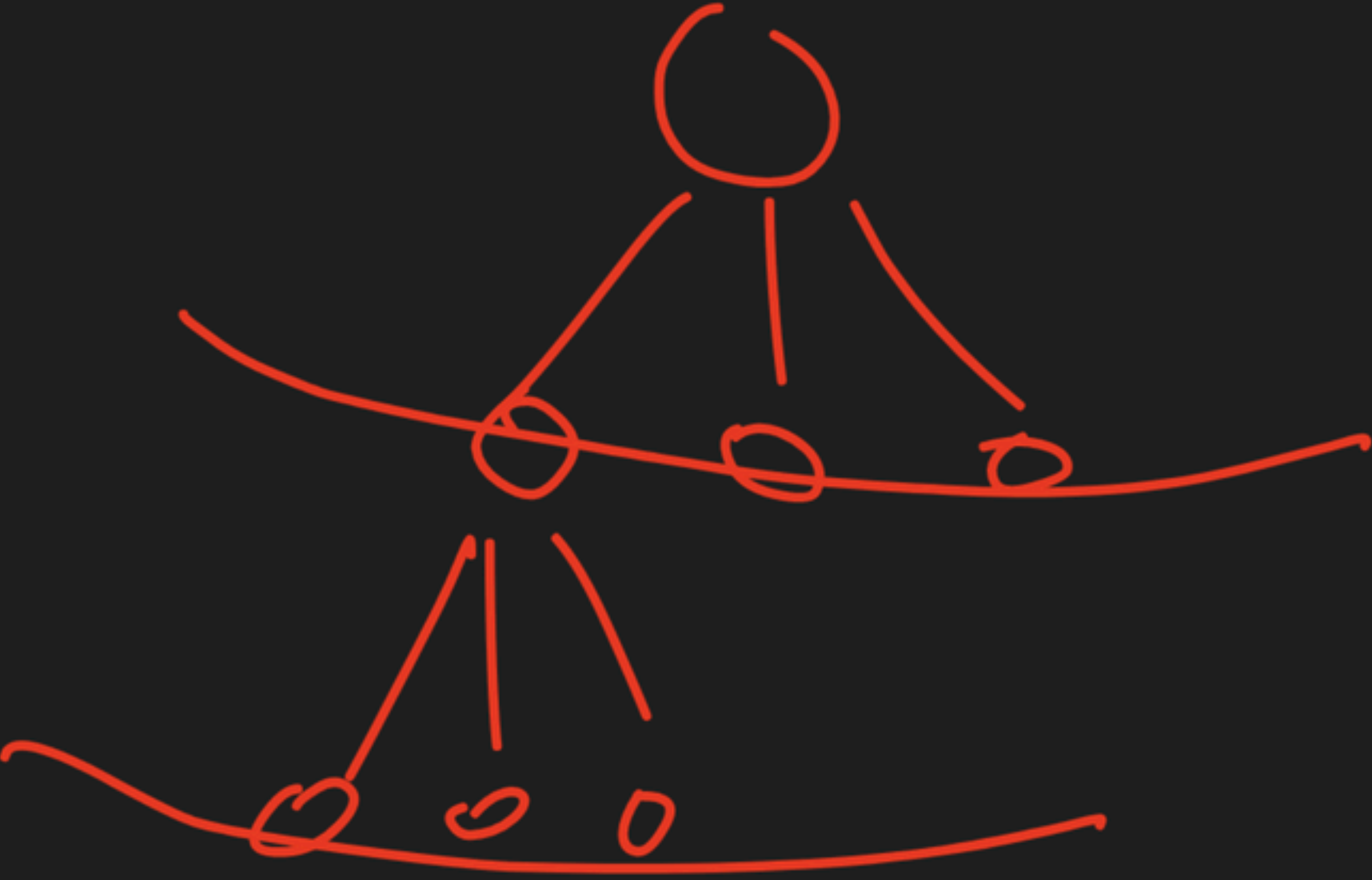
1 2 3 6 4 5 7 8 9 10

A red box highlights the numbers 2 and 3. A red arrow points from the box to the number 4.



4 5 ✓

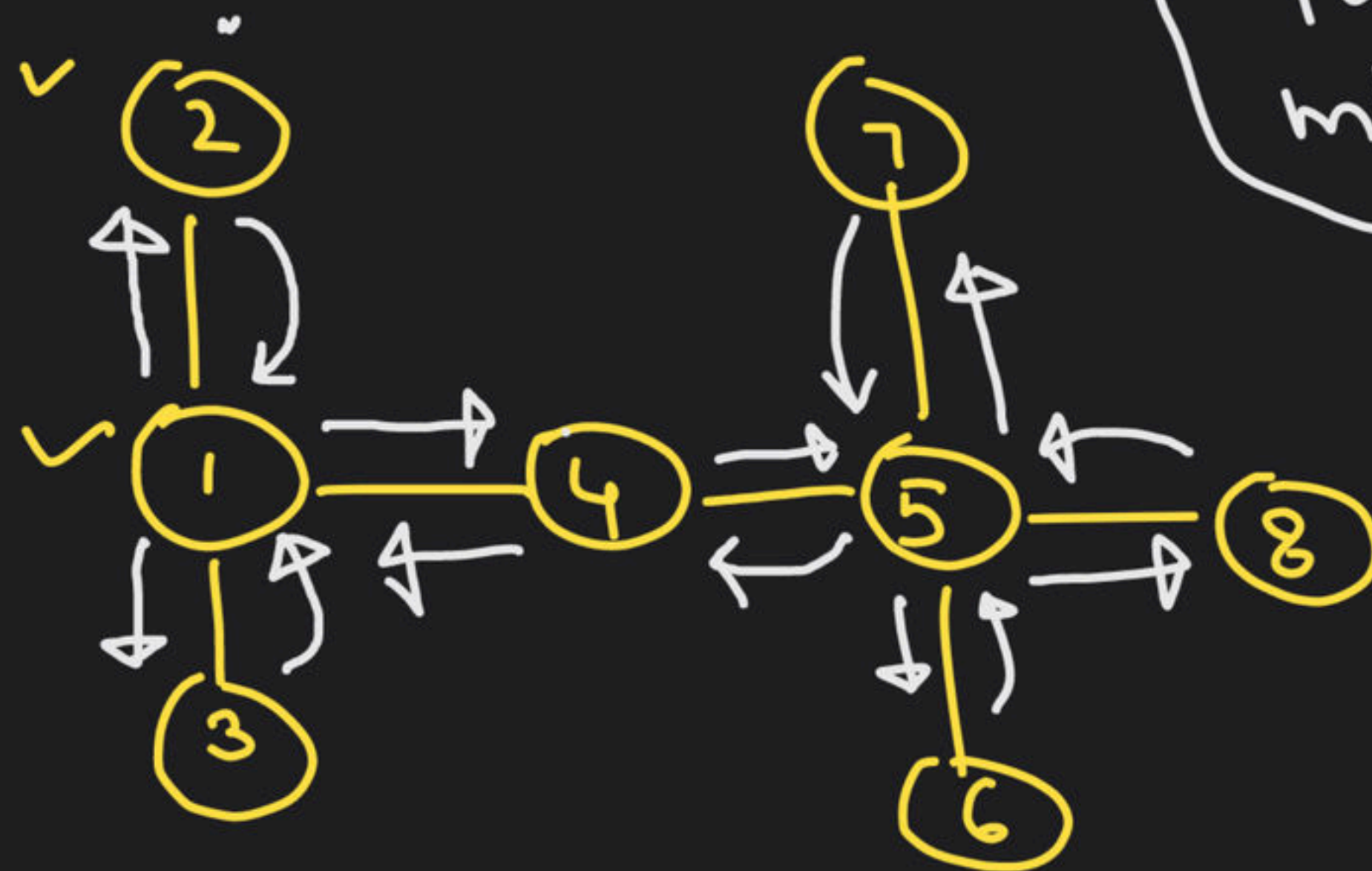
5 4 ✓



[illegible]

1 2 3 4 5 7 8 6

DFS



40-50
min



THANK YOU!

Here's to a cracking journey ahead!