



# Stack and Queue - Part III

Course on Data Structure



# CS & IT Engineering

Data Structure  
Stack & Queue



Lecture Number- 16

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# Topics

*to be covered*

1

Stack



# stack permutation

$n=3$

1) 1, 2, 3

2) 1, 3, 2

3) 2, 1, 3

4) 2, 3, 1

5) 3, 1, 2

6) 3, 2, 1

}  $3!$  permutation.

(i) Insertion order is fixed

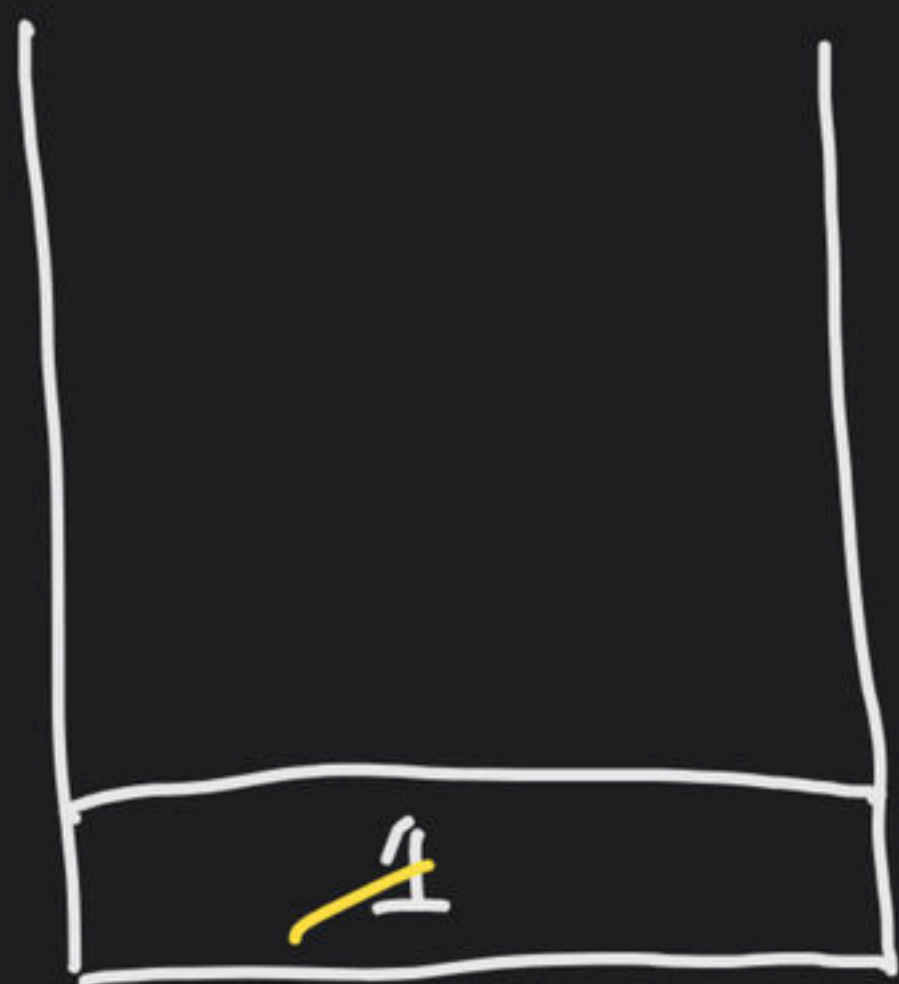
ex.

1, 2, 3  $\rightarrow$

but you can pop()  
any time.

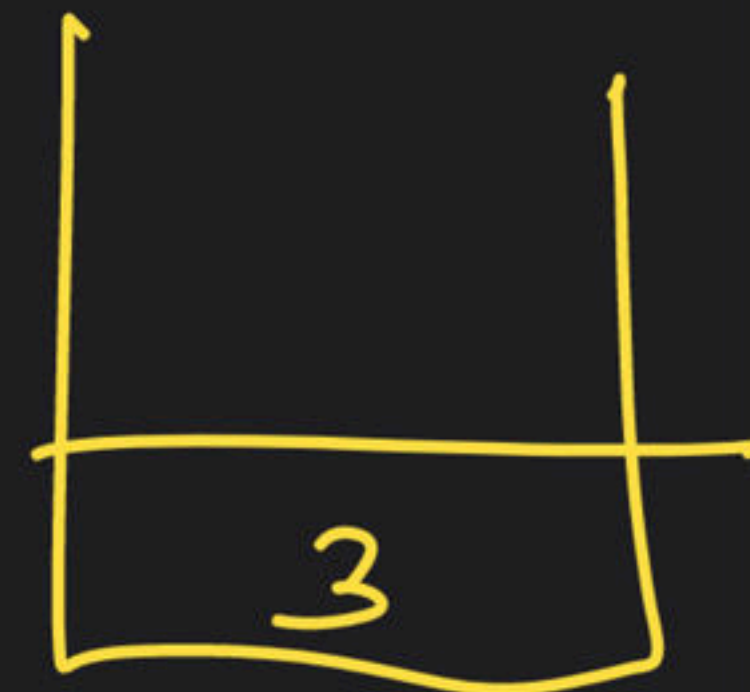
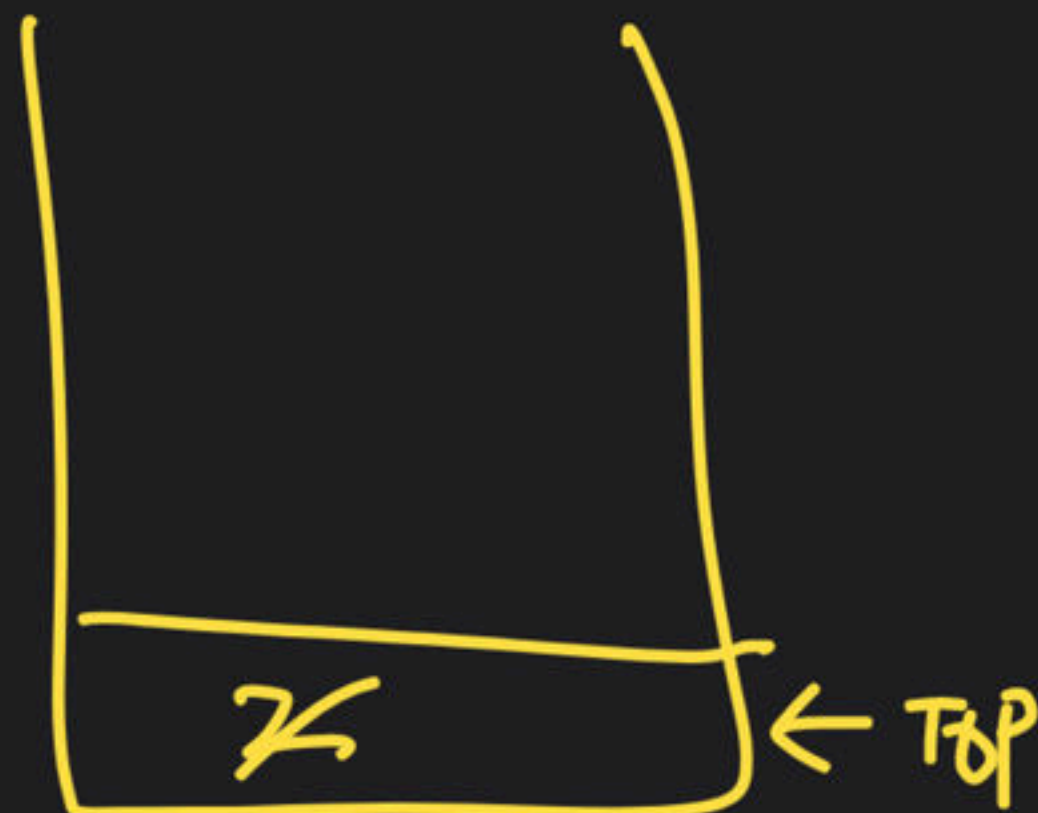
Insertion order : 1, 2, 3 →

1.) Pop-Order: 1, 2, 3 ✓✓✓



Push(1)  
 Pop() → 1  
 Push(2)  
 Pop() → 2  
 ← TOP

Push(3)  
 Pop()





1.)

pop-order

1, 2, 3



Stack permutation.

Push(1)

Pop()

Push(2)

Pop()

Push(3)

Pop()

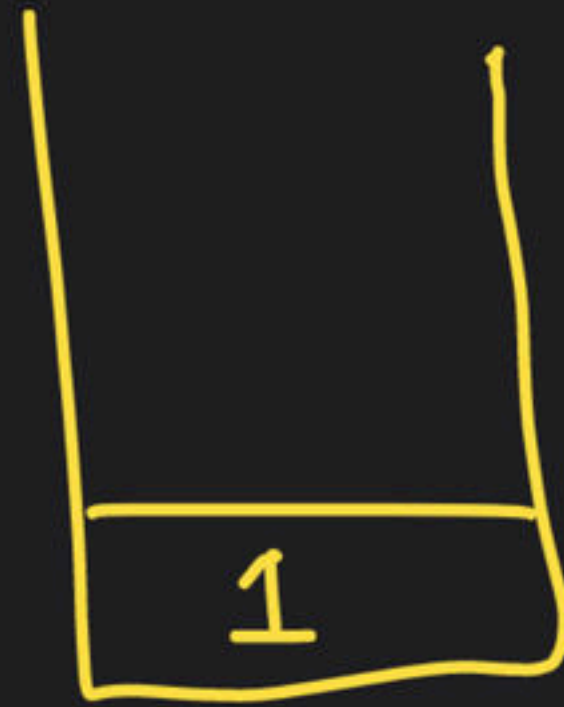
2.)  $1, 3, 2$  (pop-seq.)

$\overrightarrow{1, 2, 3}$

a)



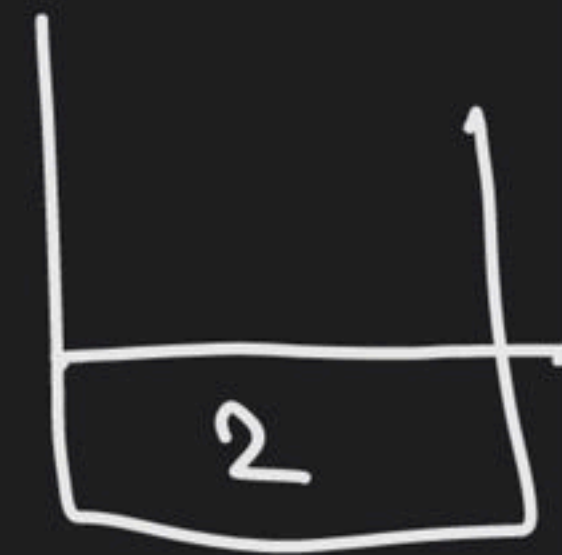
Push(1)



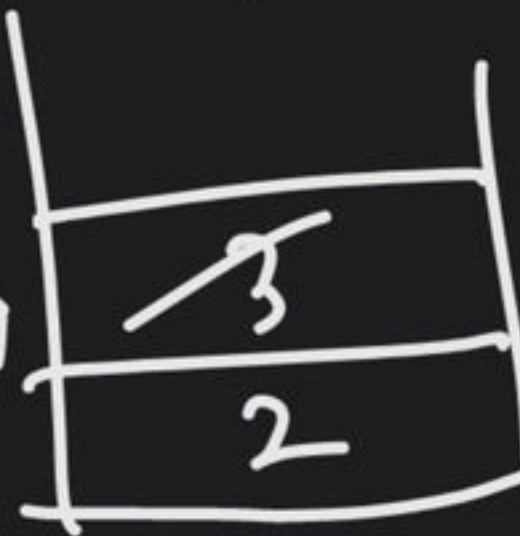
↑  
Pop



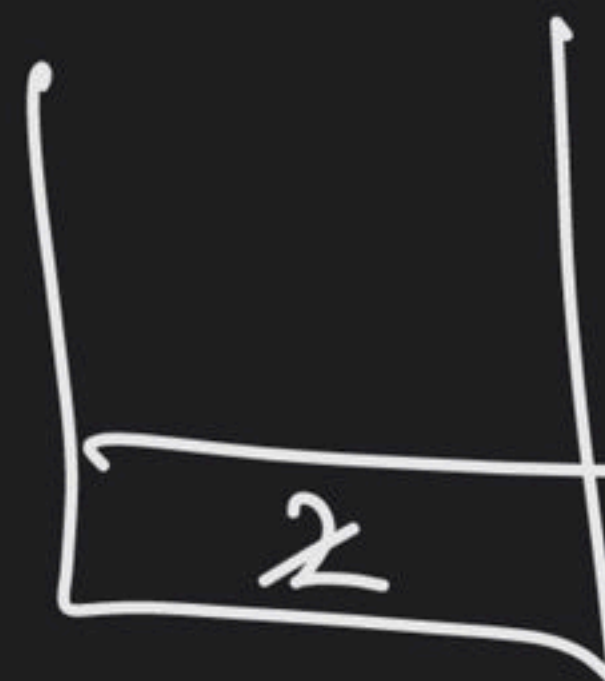
Push(2)



↓  
Push(3)



↑  
Pop



↑  
Pop

top →



3) 2, 1, 3 ✓

a) push(1)

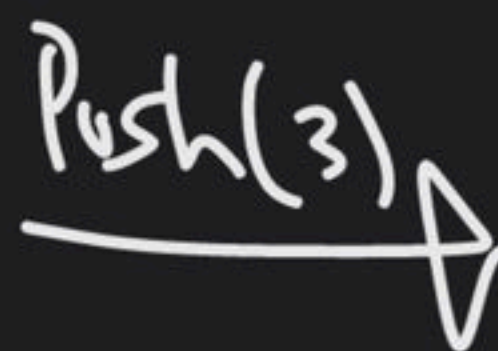
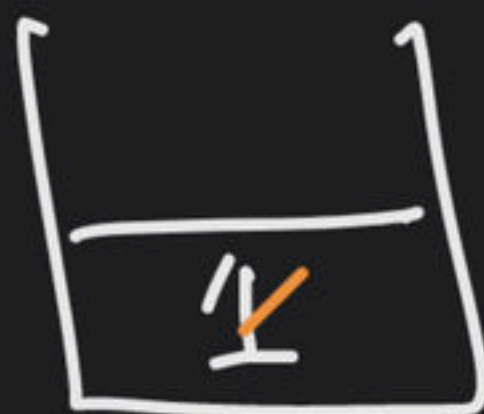
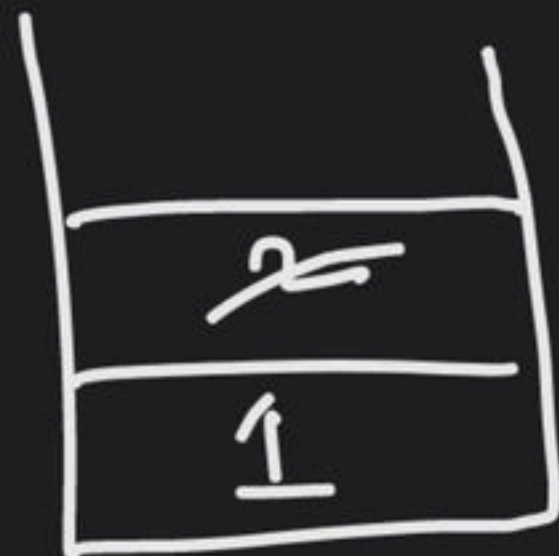
b) push(2)

c) pop()

d) pop()

e) push(3)

f) pop()



3  
4



4) 2, 3, 1 ✓ ✓

→ valid pop seq.     

Push(1)

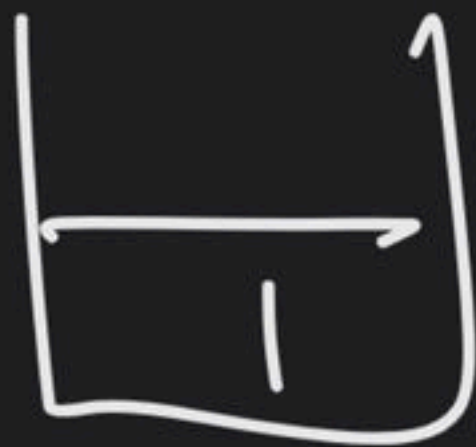
Push(2)

Pop() → 2

Push(3)

Pop()

Pop()



3



1

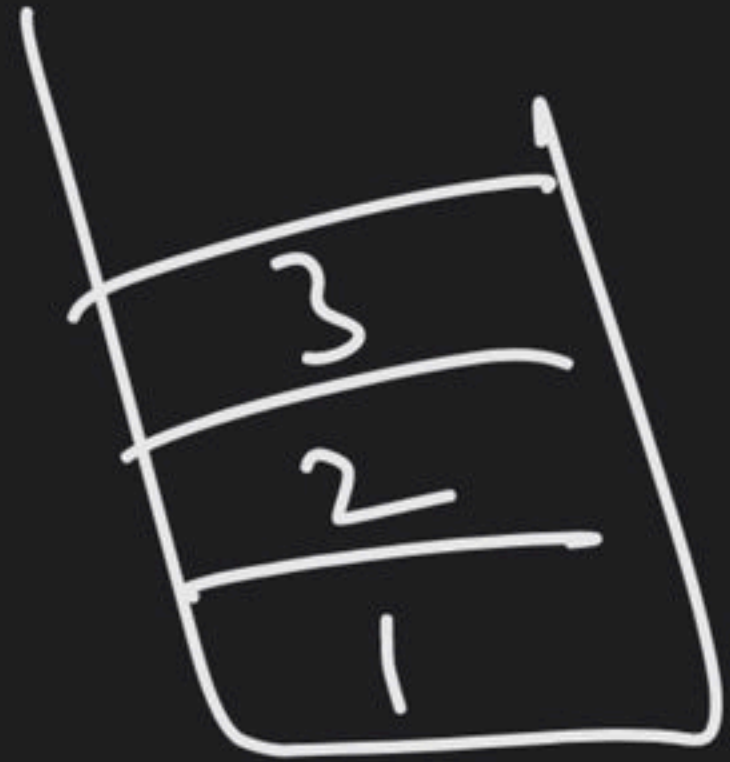
5) 3, 1, 2

→ not a valid stack permutation

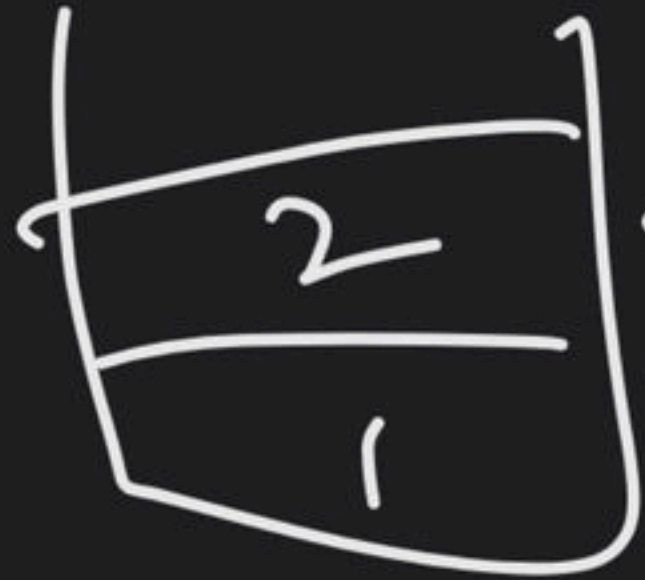
Push(1)

Push(2)

Push(3)



Pop()



← TOP



6) 3, 2, 1 ✓

Push(1)

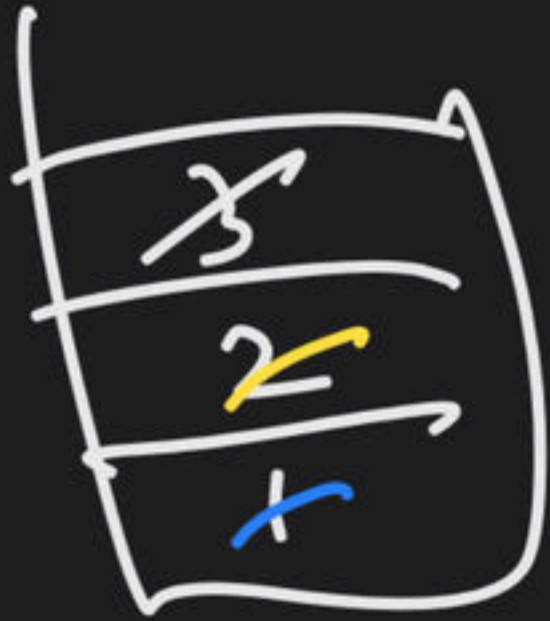
Push(2)

Push(3)

Pop()

Pop() ✓

Pop() ✓



$1, 2, 3$ 

Total no. of permutation = 6

Out of 6 possible permutation  $\Rightarrow 5$  are valid stack permutations.

Total valid stack permutation =  $\frac{{}^2P_n C_n}{n+1}$  Catalan number



# operator Infix, prefix, postfix

infix:

2 + 3

operand

operand

Postfix:

Operators comes  
after operands

2 3 +

Prefix:

operator comes before operands

+ 2 3

Why Postfix? Eyes

i/p:  $3 + 4 \times 6 / 3^2$

left to right

$3 + 4 \times 6 / 9$

multiple scans

T.C.

Applications  
of  
stack.

infix Expression Evaluated?

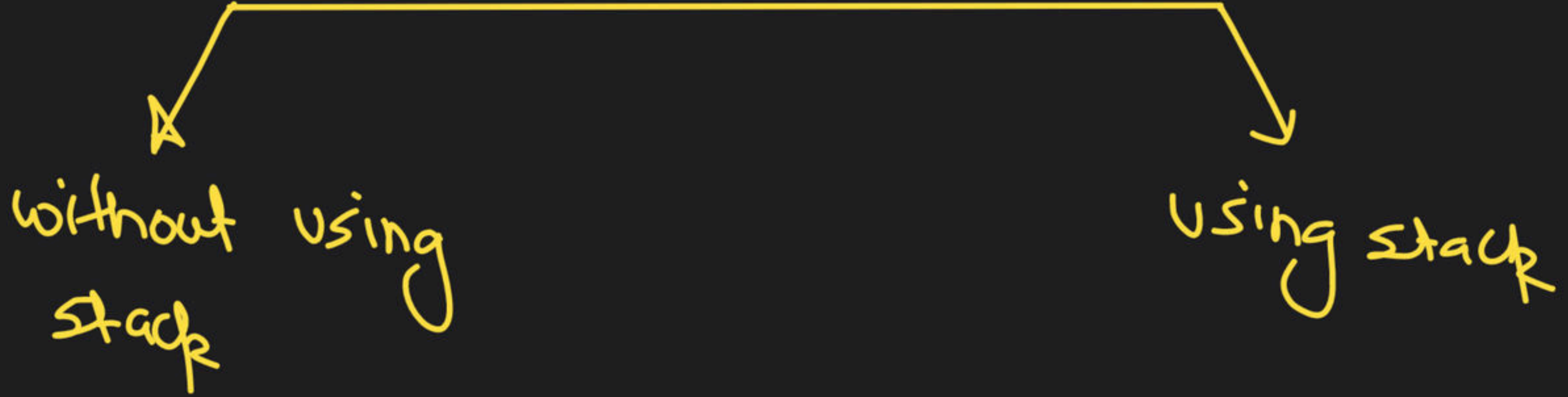
1.) infix  $\longrightarrow$  Postfix

2.) Evaluate postfix Expression



Priority  
Associativity.

infix to postfix conversion



Ex1.

Q/p:  $2 + 3 \times 5$

postfix

operand  $2 + [3 \ 5 \times]$   
 $\downarrow$   
 operand 2

postfix

$2 \ 3 \ 5 \times +$

Ex 2

i/p:  $3 + 5 \times 6 / 2^4$

$\Downarrow$

i/p:  $3 + 5 \times 6 / [2^4]$

$3 + \underbrace{[5 \ 6 \ X]}_{op_1} / \underbrace{[2 \ 4 \ ^]}_{op_2}$

$op_1$   
 $3 + \underbrace{[ \underbrace{5 \ 6 \ X}_{op_2} \ 2 \ 4 \ ^ ]}_{op_1} \Rightarrow$

Theorited

- ①  $\wedge$  R to L  
②  $X, /$  L to R  
③  $+ -$

$\uparrow$

Postfix

$3 \ 5 \ 6 \ X \ 2 \ 4 \ ^ \ / \ +$





Ex3 infix:  $(a+b) \times c/d - e^{\wedge} f^{\wedge} g/h$

^ R to L  
 x, / L to R  
 +, - L to R

$$[ab+] \times c/d - e^{\wedge} f^{\wedge} g/h$$

$$[ab+] \times c/d - e^{\wedge} [fg^{\wedge}] / h$$

$$[ab+] \times c/d - [efg^{\wedge}] / h$$

$$[ab+cx] / d - [efg^{\wedge}] / h$$

$$[ab+cx/d] - [efg^{\wedge}] / h$$

$$[ab+cx/d] - [efg^{\wedge}h/]$$

Postfix:  $ab+cx/d/efg^{\wedge}h/-$

# Infix to postfix using stack

Infix:  $2 + 3$  →

Postfix:  $2 3 +$  →

Prefix:  $+ 2 3$  →

Infix:  $2 + 3 \times 4$  →

Postfix:  $2 3 4 \times +$  →

Prefix:  $+ 2 \times 3 4$  →



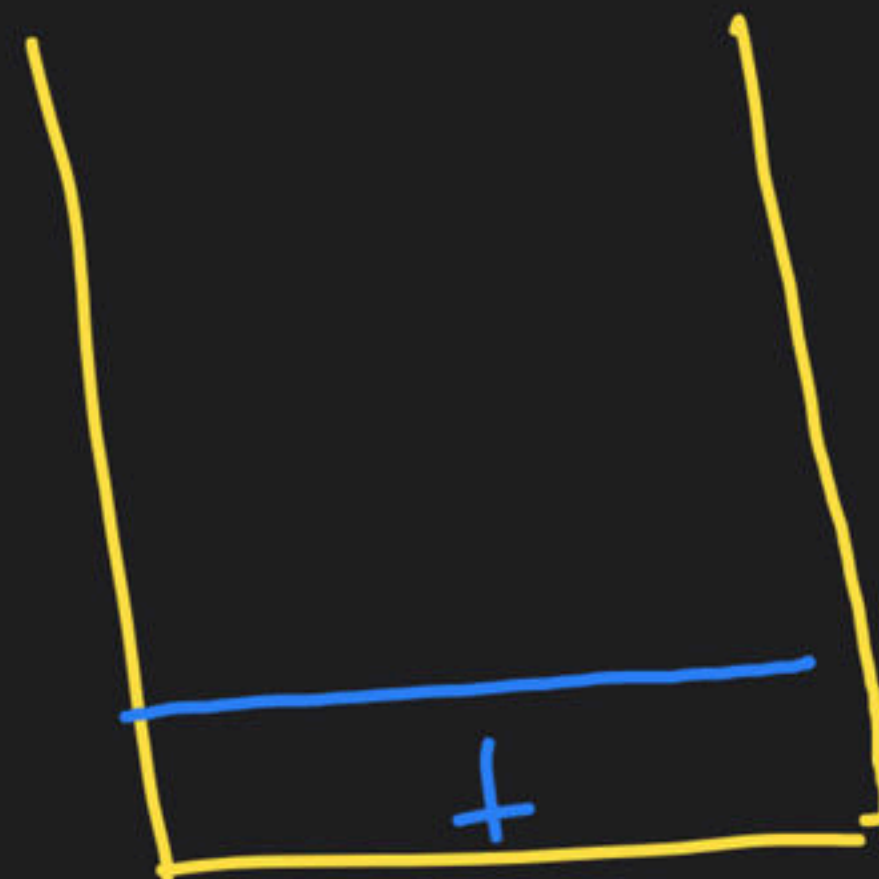
Ex 1. infix: 2+3

o/p: 2



Ex 1. infix: 2+3

o/p: 2



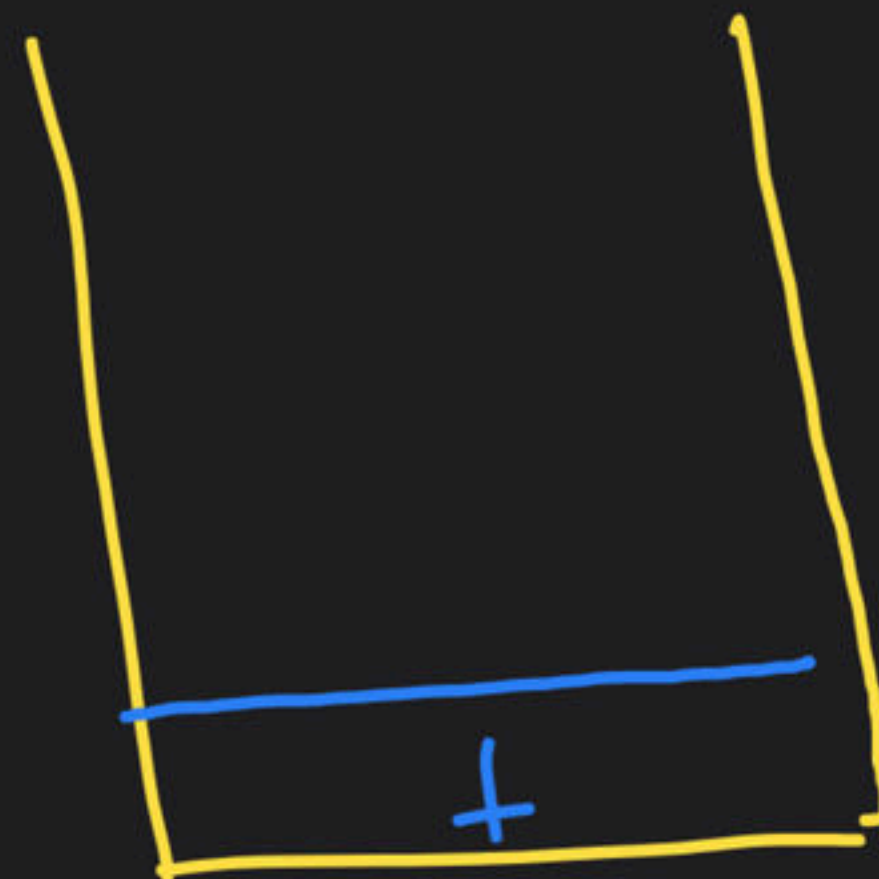
Scanned element  
is operator

⇒ And Stack  
is Empty

Push

Ex 1. infix: 2+3

o/p: 23



Scanned element  
is operator

⇒ And Stack  
is Empty

Push

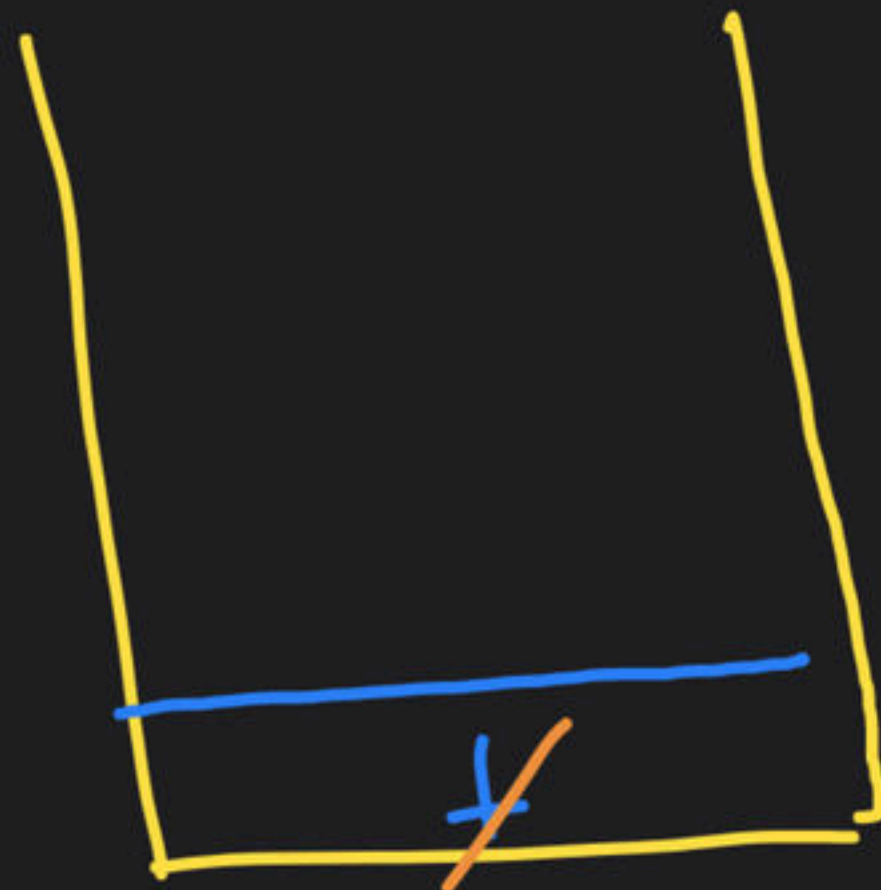


infix: 2+3 End

o/p: 23

Scanned element  
is operator

⇒ And Stack  
is Empty



← Top

Pop every  
thing from  
stack and add to  
o/p (one by one)

Push

o/p: 23+

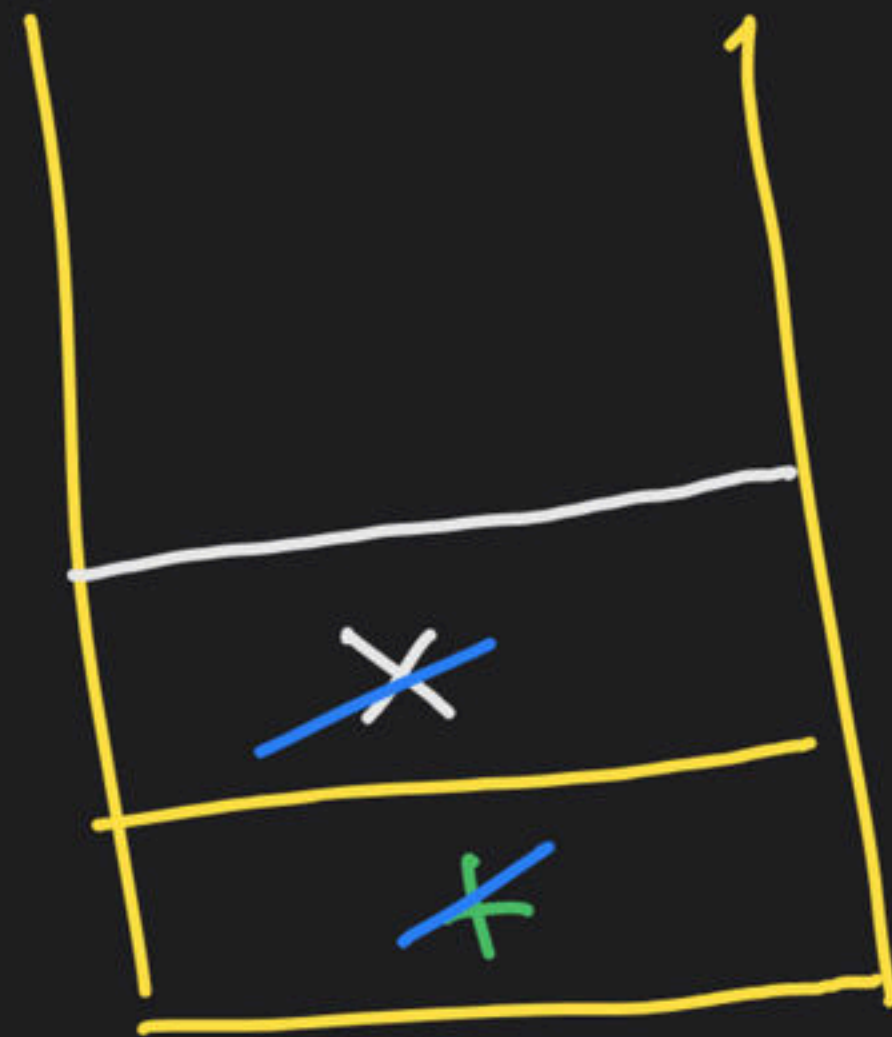
unacademy  
ex 2. i/p: 2 1 3 x 4

o/p: 23



unacademy  
ex 2. i/p: 2 1 3 X 4 End

o/p: 2 3 4 X +

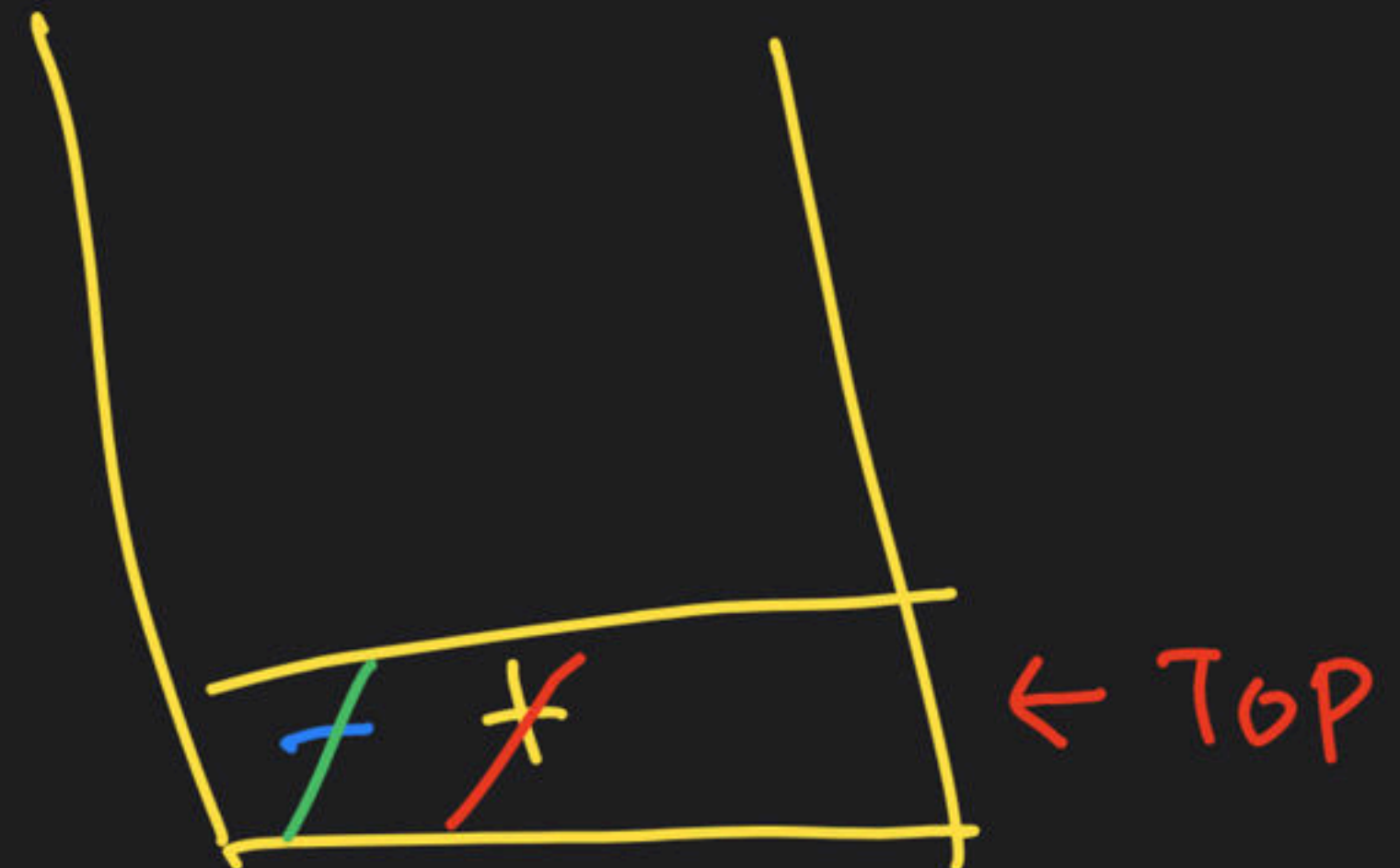




unacademy  
i/p:  $a + b - c$  end

o/p:  $ab + c -$

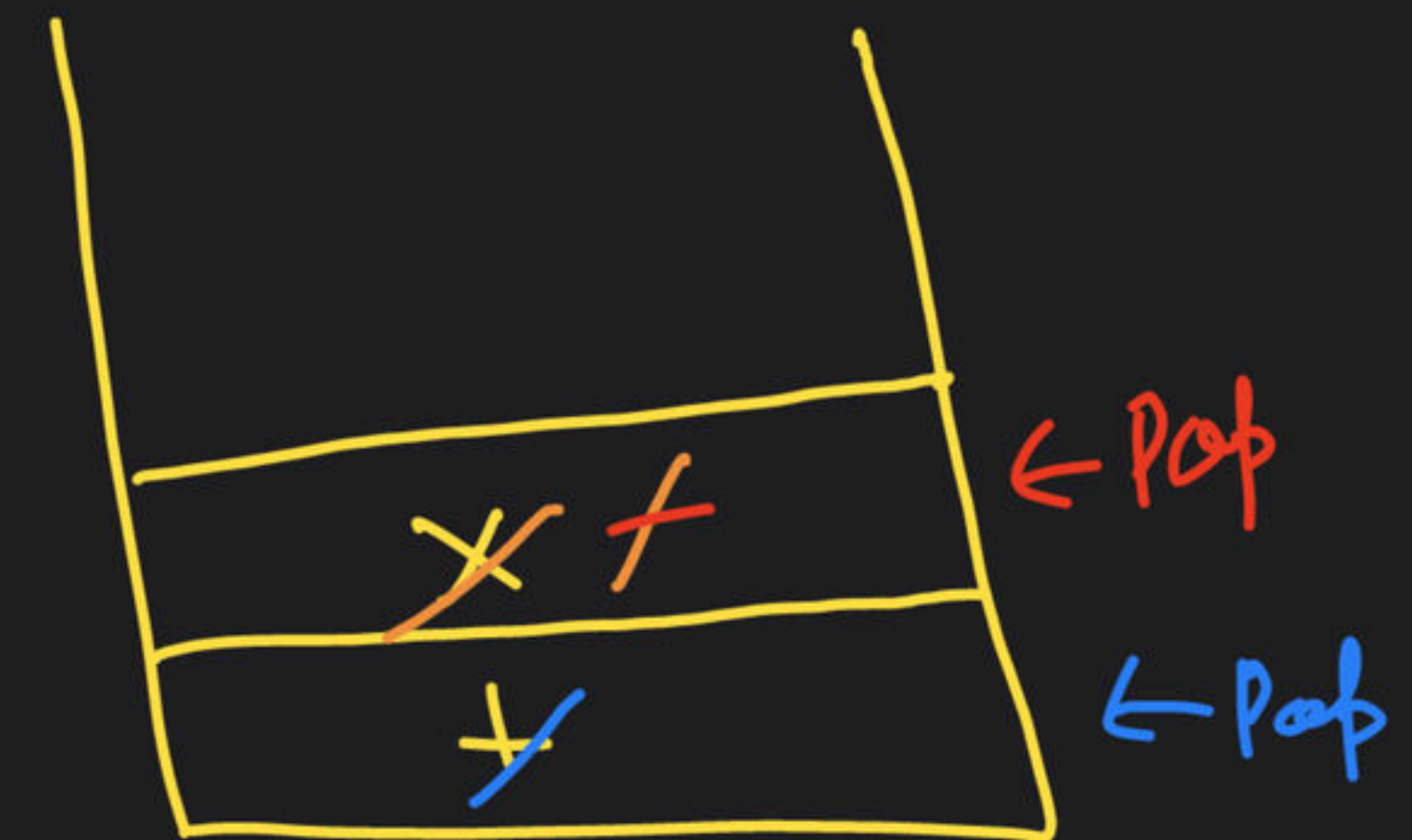
$a + b - c$   
→



Ex 4 unacademy i/p :

a + b x c / d End

o/p : a b c x d / +



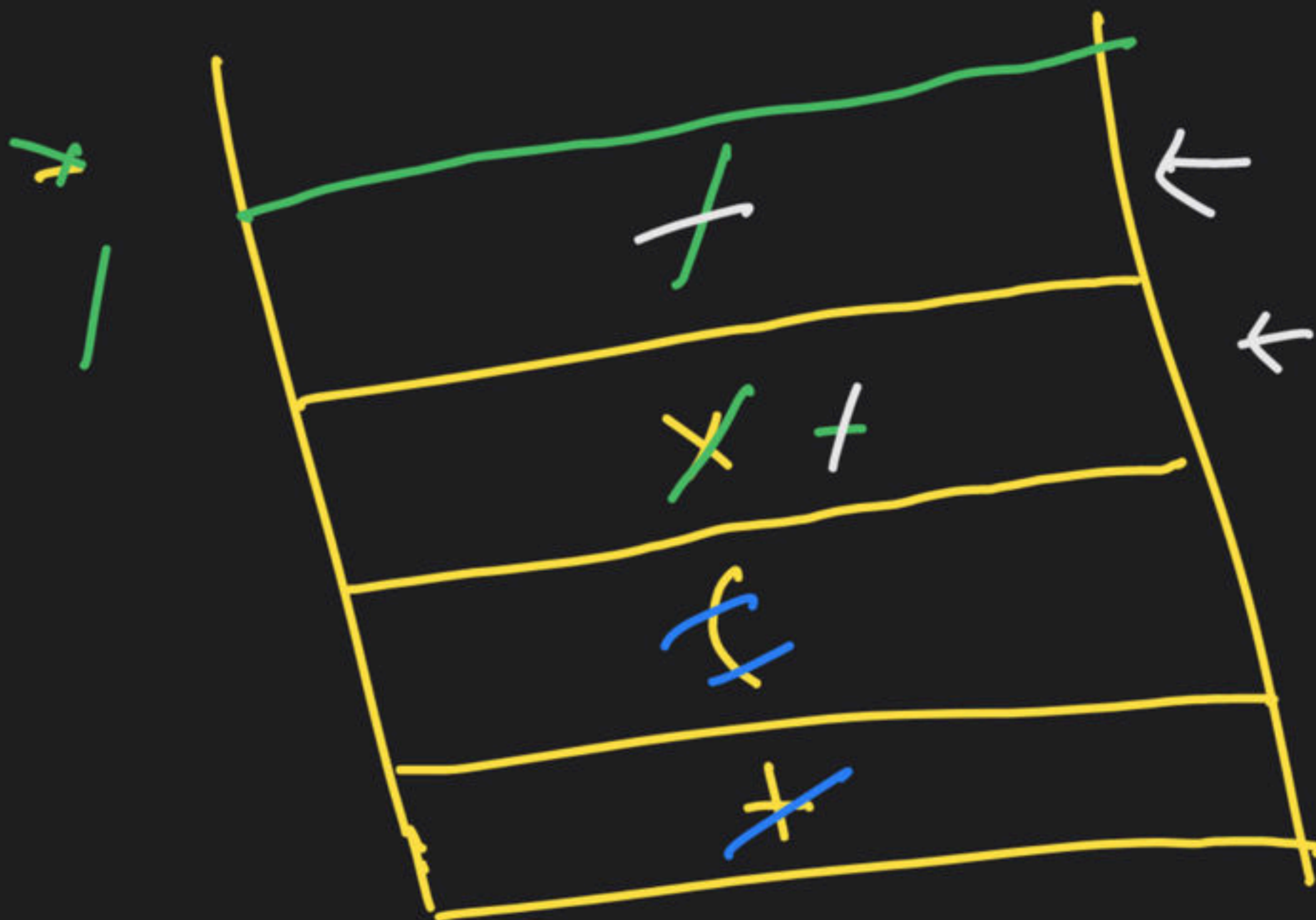
unacademy

i/p:  $2 + (3 \times 4 - 6 / 2)$

o/p:  $2\ 3\ 4\ \times\ 6\ 2\ /\ - +$

left (  $\Rightarrow$  Push

)  $\Rightarrow$  repeatedly Pop  
 & add to o/p  
 (one by one)  
 until (   
 is encountered



(  $\Rightarrow$  Pop() & discard



Ex 6

→ new concept



▲ 1 • Asked by Deepraj

sir postfix me ^ operator ko hamesha power operator  
samjhekya cos ^ to bitwise xor bhi hota hein na



# THANK YOU!

Here's to a cracking journey ahead!