THE UNIVERSITY OF TEXAS AT AUSTIN
Department of Statistics and Data Sciences
College of Natural Sciences

SDS 385: Stat Models for Big Data

Lecture 11: Map reduce

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https://psarkar.github.io/teaching

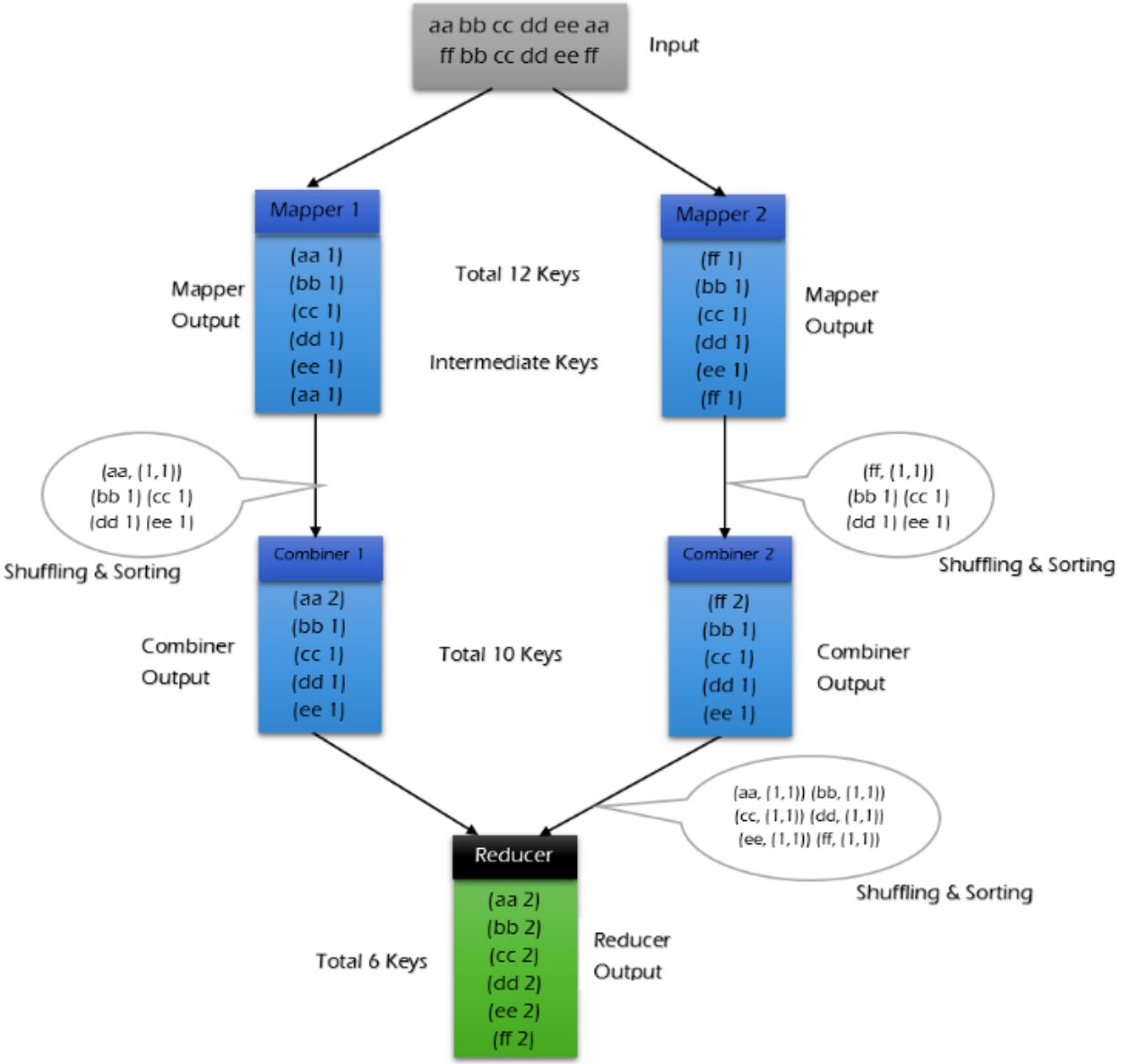
Map reduce framework

- Provides an easy framework for parallel computation
  - distributes data and takes care of synchronization
- But there are restrictions: only certain kinds of parallelisms are allowed

Map reduce basics

- Represent data as $\langle key, value \rangle$ pairs
  - Typically "key" is simple, e.g. the url of an webpage/ ID of a document
  - "value" is complex, can be contents of a webpage/ a document
- distributes data and takes care of synchronization
  - Data from the mapper is fed to the combiner, which is like a local reducer and reduces the amount of data transfer
- But there are restrictions: only certain kinds of parallelisms are allowed

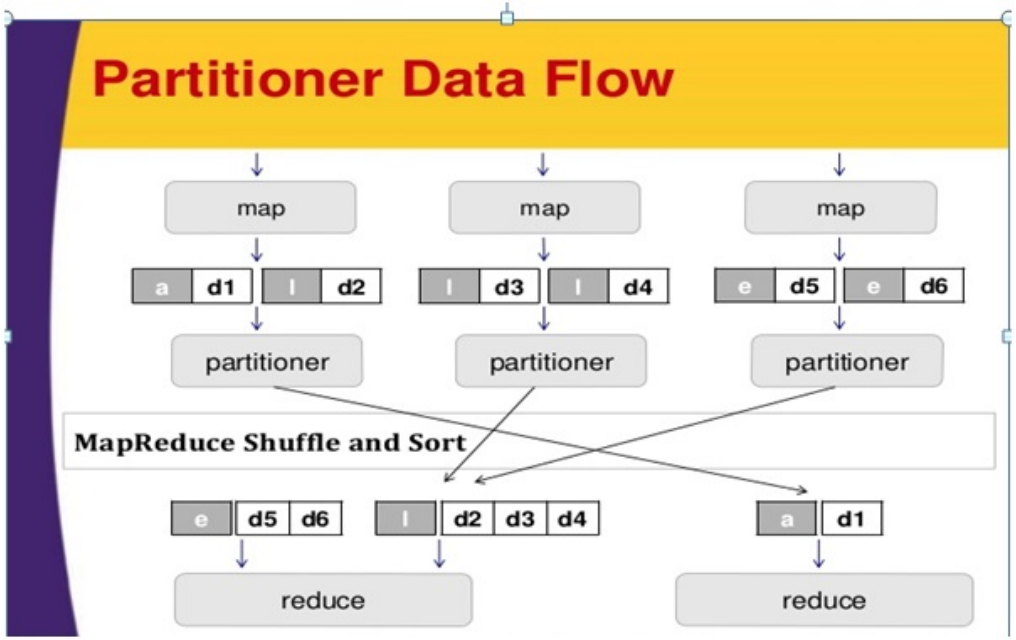
Map reduce basics



Map reduce basics - partitioner

- Runs on the same machine where the mapper had completed its execution by consuming the mapper output.
- Distributes how outputs from the map stage are send to the reducers.
- Controls the keys partition of the intermediate map-outputs.
- The key is used to derive the partition by a hash function.

Map reduce basics



Shuffle and sort

- The shuffling process starts right away as the first mapper has completed its task.
- Once the data is shuffled to the reducer node the intermediate output is sorted based on key before sending it to reduce task.
- The algorithm used for sorting at reducer node is Merge sort.

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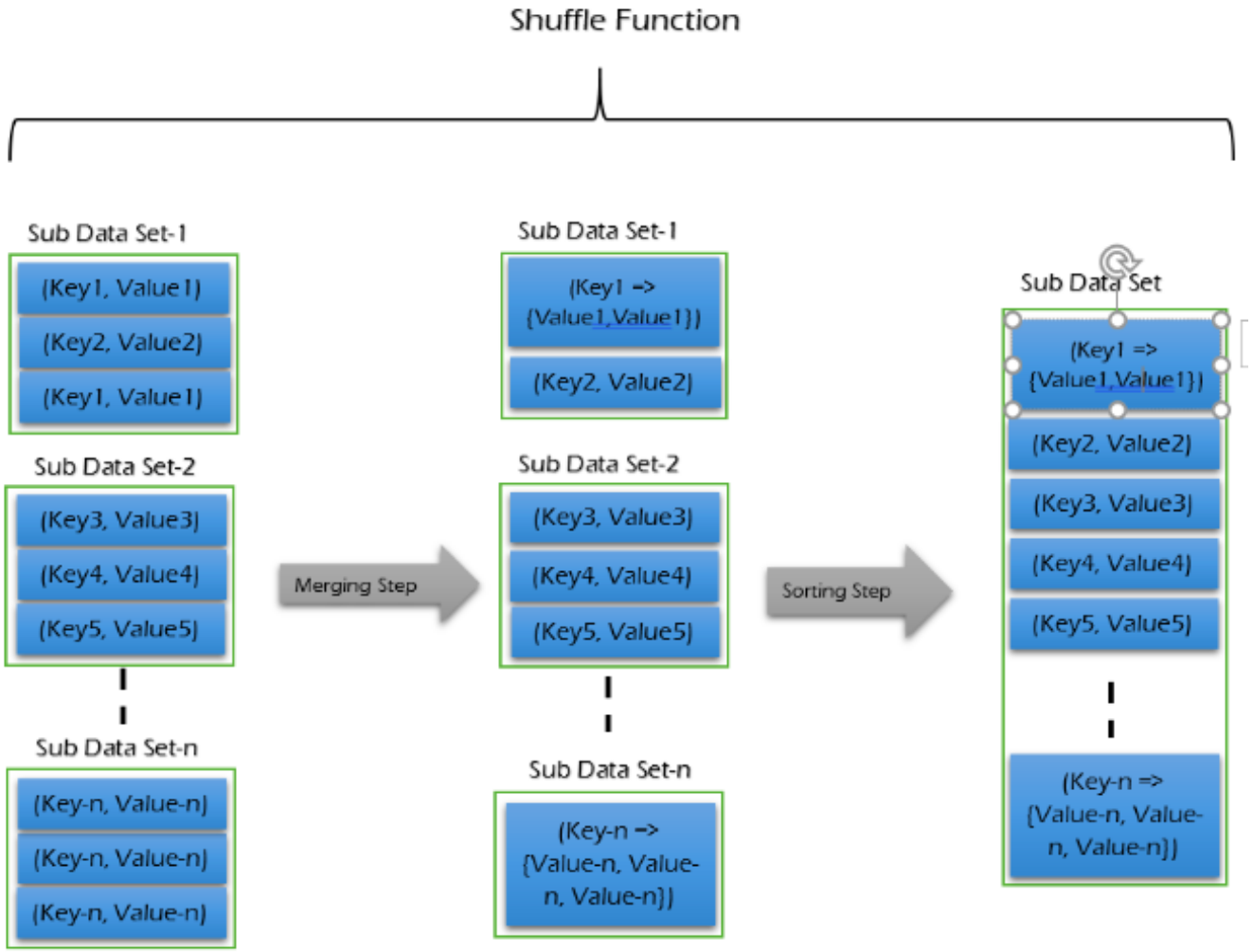
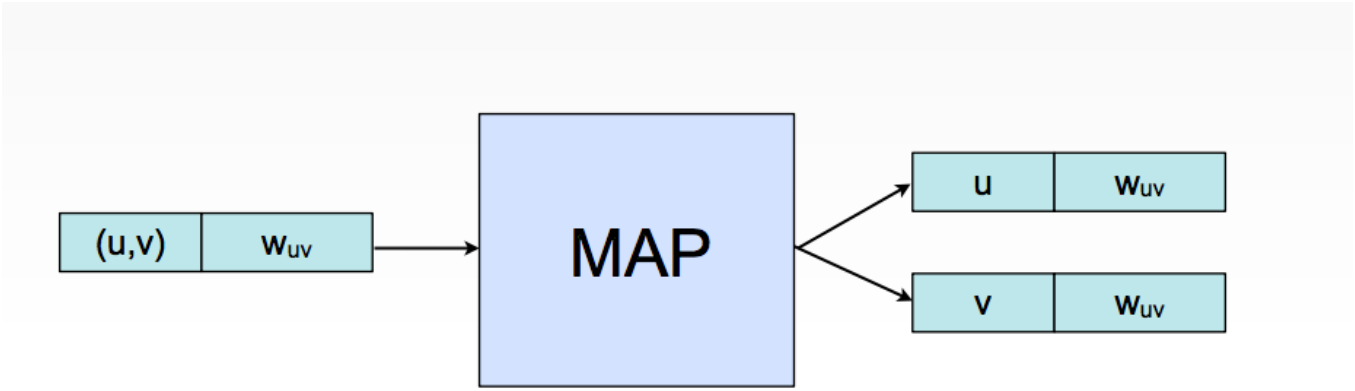
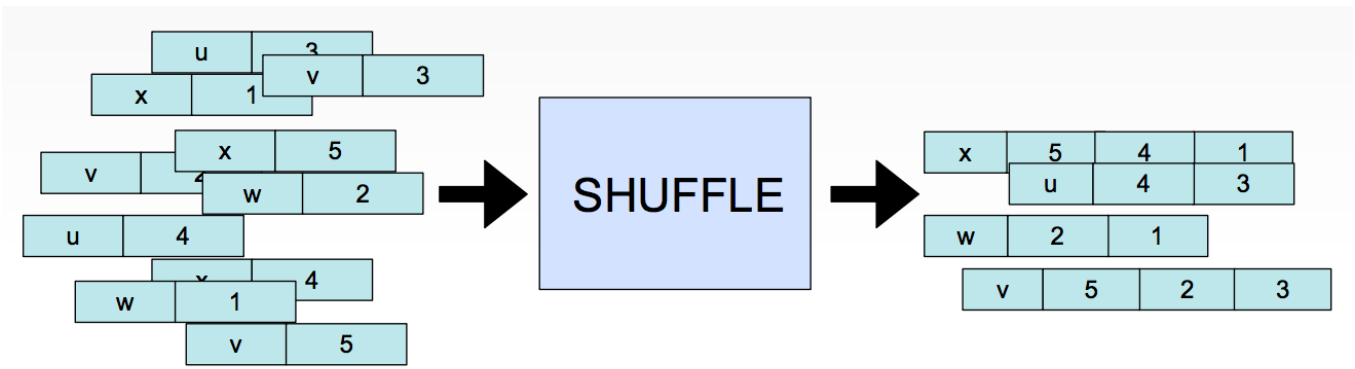


Example - calculate degree in weighted graph

- Data: (src,dst, weight)
- Key (src,dst) value weight





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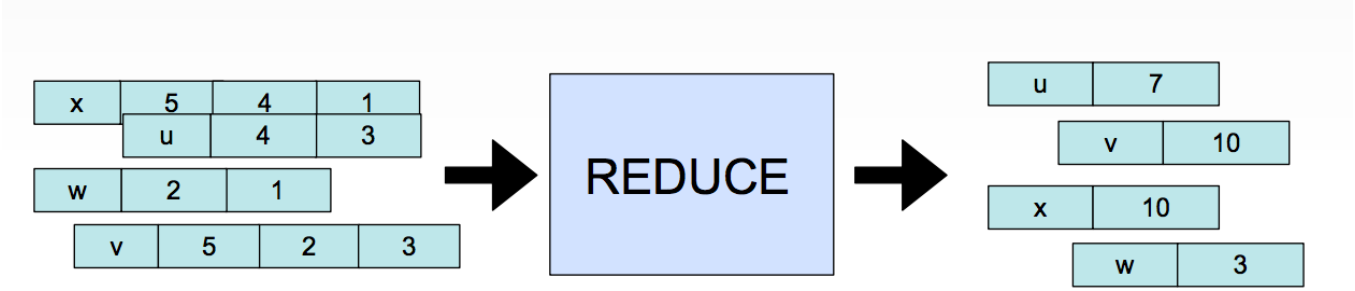
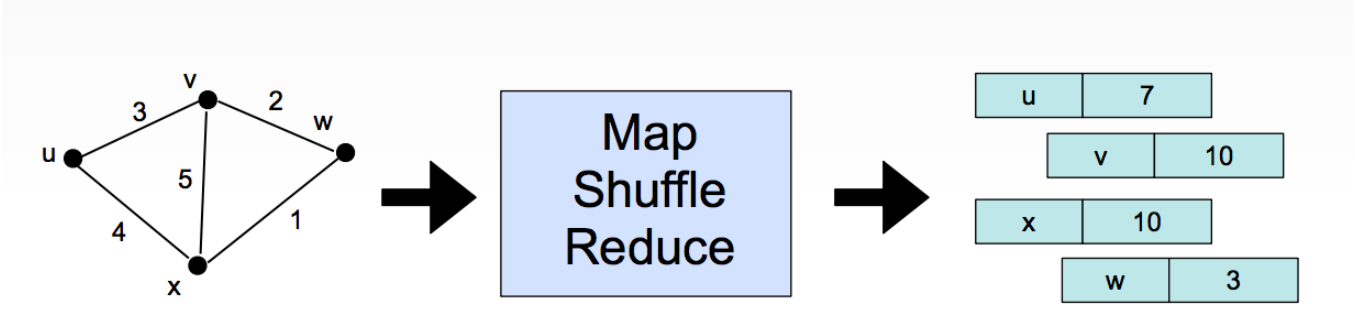




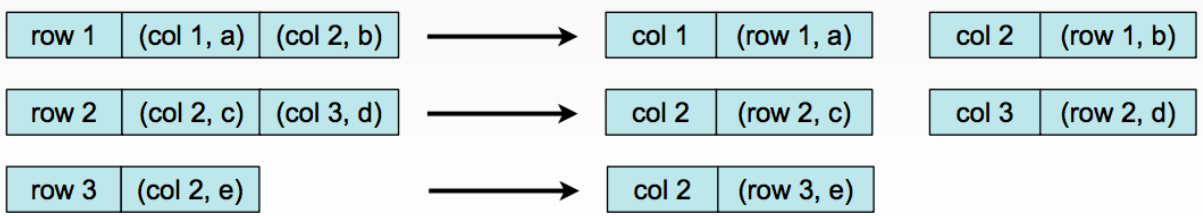
Example - transpose of a giant matrix

- Input: sparse matrix in row major order
- Output: sparse matrix in column major order

Map:

- Input: <row i, (col_{i1}, val_{i1}), (col_{i2}, val_{i2}), ... >
- Output: <col_{i1}, (row i, val_{i1})>
- <col_{i2}, (row i, val_{i2})>
- ....

a	b	
	c	d
	e	



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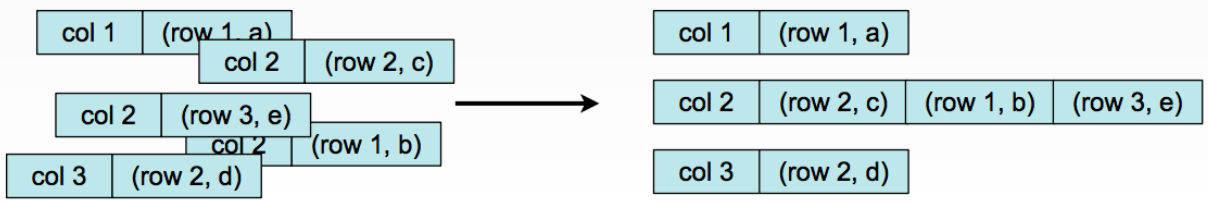

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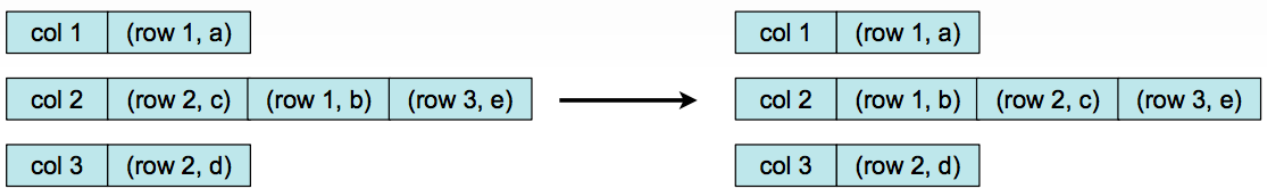
Shuffle

Reduce:

- Sort by row number



Example - linear regression

- Data is $x_i = (x_{i1}, \ldots, x_{ip})$
- response variable y_i
- Want to compute $w = (X^T X)^{-1} X^T \boldsymbol{y}$

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- Output: two keys
  - K_1 - for $X^T X$ (calculated over subgroup), Value is a $p+1 \times p+1$ matrix
  - K_2 - for $X^T I; y$ (calculated over subgroup), Value is a $p+1 \times 1$ vector

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- Reducer
  - Sum the (K_1, Value) pairs to get $X^T X$
  - Sum the (K_2, Value) pairs to get $X^T \boldsymbol{y}$
  - Calculate $w = (X^T X)^{-1} X^T \boldsymbol{y}$

Example - Naive Bayes

- Data $x = (x_1, \ldots, x_p)$, discrete
- Response variable y_i, in $1, \ldots, K$
- Prediction for datapoint $(a_1, \ldots, a_p)$:
  $y^* = \arg\max_k P(y = k) \prod_j P(x_j = a_j | y = k)$

Example - Naive Bayes

- Map:
  - Input: $\langle k, \{\boldsymbol{x}_i, y_i\}_{i \in \text{subgroup}k} \rangle$
  - Output: three types of keys
    - $K_1 = (j, a_j, k)$, and Value1 $\sum_{subgroup} 1(x_j = a_j, y = k)$
    - $K_2 = (k)$ and Value2 $\sum_{subgroup} 1(y = k)$
    - K_3 and Value3 $\sum_{subgroup} 1$

Example - Naive Bayes

- Reduce
  - Estimate $P(x_j = a_j | y = k)$ by $\frac{\sum_{K_1=(j,a_j,k)} Value1}{\sum_{K_2=k} Value2}$
  - Estimate $P(y = k)$ by $\frac{\sum_{K_2=k} Value2}{\sum_{K_3} Value3}$

Example - K-means

- Data $x = (x_1, \ldots, x_p)$
- Goal: find clustering that minimizes sum of squares error.
- At any step, we do:
  - Update $y_i^{(t+1)} \leftarrow$ label of the closest center.
  - Update $\mu_k^{(t+1)} \leftarrow \frac{\sum_{i:y_i^{(t+1)}=k} x_i}{\sum_{i:y_i^{(t)}=k} 1}$

Example - K-means

- Map:
  - Input x
  - $k = argmin_j \|x - \mu_j^{(t)}\|$
  - Output $(k, x, 1)$

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- Map:
  - Input x
  - $k = \mathit{argmin}_j \|x - \mu_j^{(t)}\|$
  - Output $(k, x, 1)$
- Reduce:
  - Reduce into k values of the form: $(j, \underbrace{\sum_{key=j} value_1}_{N_j}, \underbrace{\sum_{key=j} value_2}_{D_j})$
  - Estimate $\mu_k^{(t+1)}$ by $\frac{N_k}{D_k}$

Seems like we can do anything

- Any ML algorithm that has an inner step with sum over matrices or vectors concerning n datapoints can be parallelized.

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- Any ML algorithm that has an inner step with sum over matrices or vectors concerning n datapoints can be parallelized.
- Works well when p is small, since then the communication overhead is relatively small
- Since we are invoking MR framework over each iteration of an algorithm (like GD), for large p things are pretty bad.
- So, how to reduce communication?

Acknowledgment

- https://www.tutorialscampus.com/tutorials/map-reduce/shuffle-and-sort.htm
- Sergei Vassilvitskii's notes
- Modeling with Hadoop - KDD 2011 tutorial
- Map-Reduce for Machine Learning on Multicore - NIPS 2007 paper by Chu et al.