ETH Zurich Institut für Theoretische Informatik Prof. Dr. Angelika Steger Prof. Dr. Emo Welzl

Prof. Dr. Peter Widmayer

## **Algorithms Lab**

## **Exercise** – Even pairs

You are part of a team to develop a new kind of pseudorandom number generator (PRNG). To gauge how good your algorithm is at producing random sequences of bits, you are running several different statistical tests.

For example, if  $x_0, \ldots, x_{n-1}$  was a truly random sequence of bits, then it would have the property that the sum  $x_i + \cdots + x_j$  is even for about half of the pairs  $0 \le i \le j < n$  (and odd for the other half).

To check whether this is the case if  $x_0, \ldots, x_{n-1}$  are generated by your PRNG, you need to be able to count the number of pairs  $1 \le i \le j \le n$  for which the sum is even.

**Input** The first line of the input contains the number  $t \le 30$  of test cases. Each of the t test cases is described as follows.

- It starts with a line that contains an integer n such that  $1 \le n \le 5 \cdot 10^4$ .
- The following line contains n integers  $x_0 \ldots x_{n-1}$ , separated by a space, such that  $x_i \in \{0,1\}$ , for all  $i \in \{0,\ldots,n-1\}$ .

**Output** For each test case output a single line containing the number of pairs  $0 \le i \le j < n$  such that the sum  $x_i + \cdots + x_j$  is even.

**Points** There are three groups of test sets, worth 100 points in total.

- 1. For the first group of test sets, worth 40 points, you may assume that  $1 \le n \le 200$ .
- 2. For the second group of test sets, worth 30 points, you may assume that  $1 \le n \le 5000$ .
- 3. For the third group of test sets, worth 30 points, there are no additional assumptions.

Corresponding sample test sets are contained in test i. in/out, for  $i \in \{1, 2, 3\}$ .

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