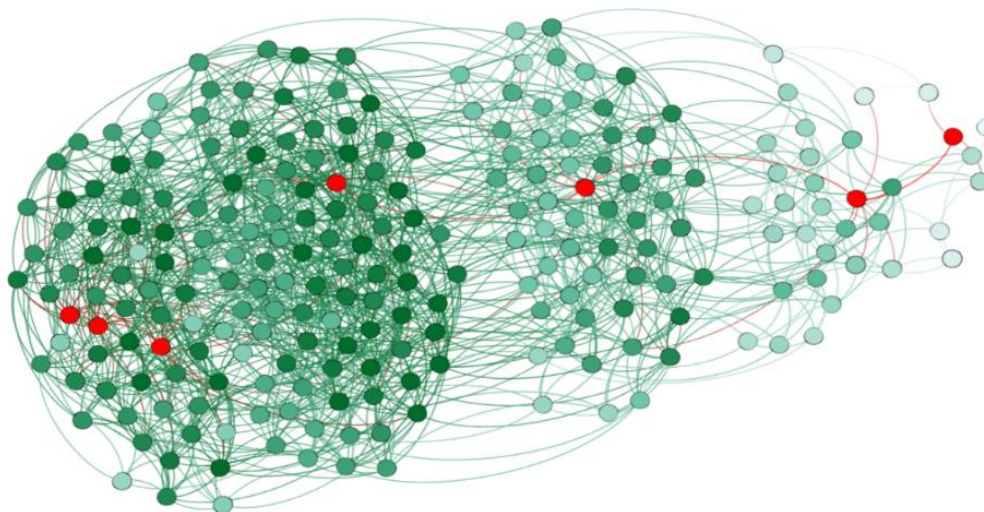


# Genetic Algorithm

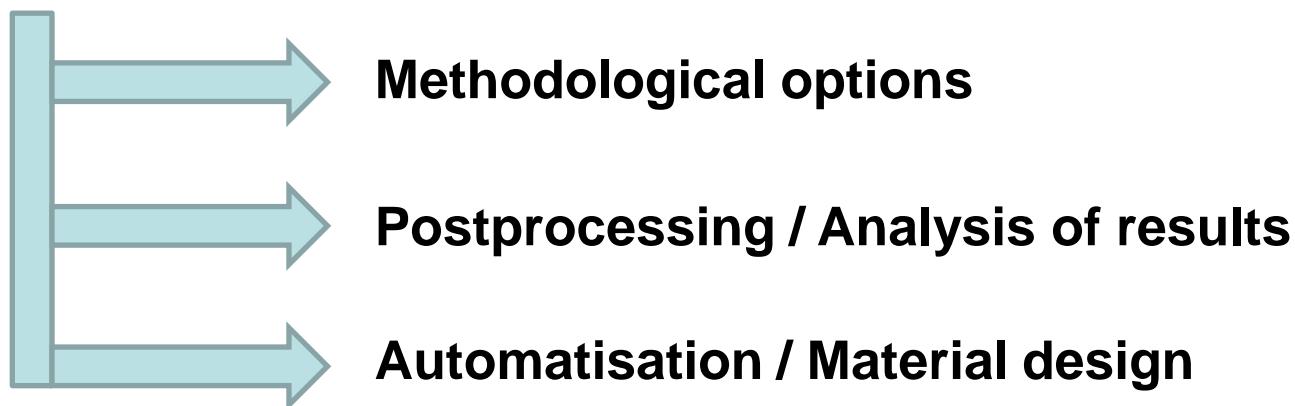
-

## Simulating Materials from first principles



# Scope of This Exercise

**Electronic Structure Theory is more than pressing buttons**



## Educational Targets:

- Identify challenges
- Assess solutions
- Present results

Structure Search  
as a simple-to-implement  
Example

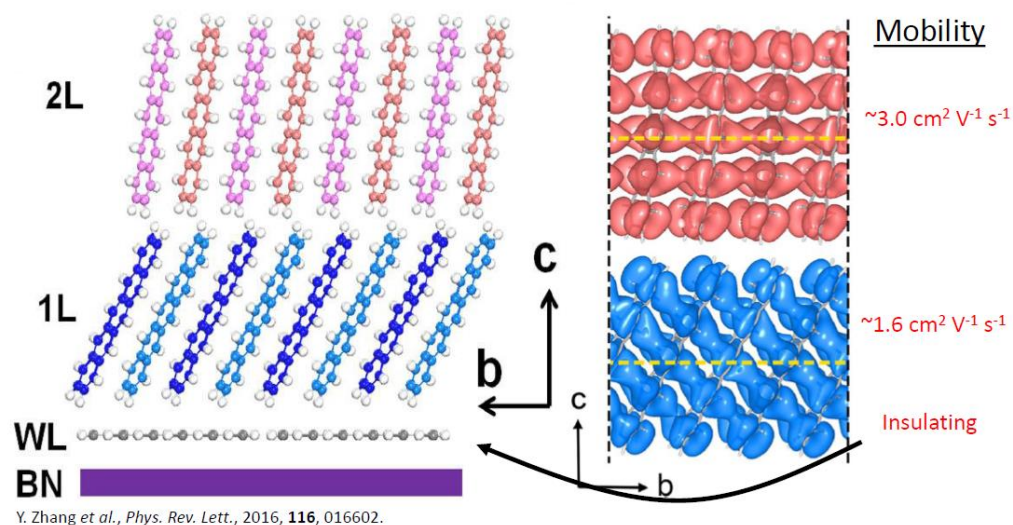
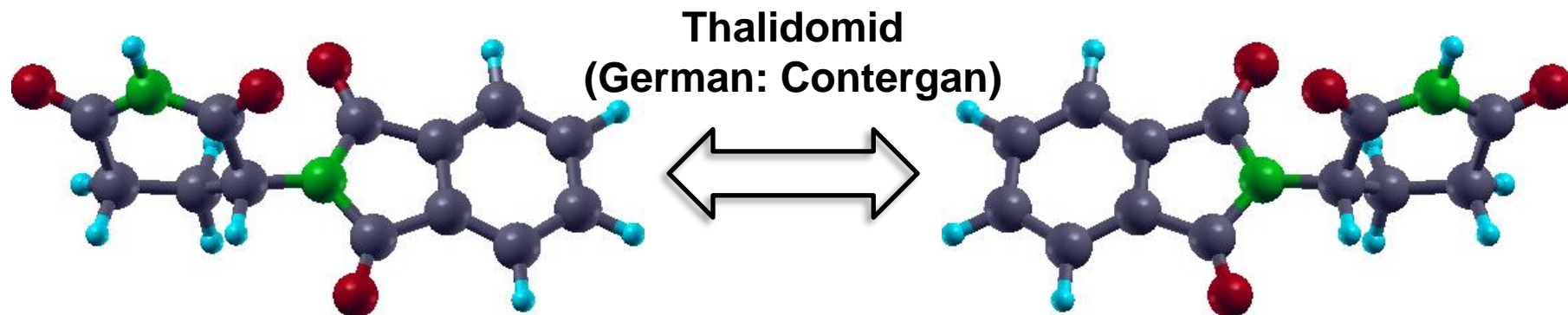
# Structure Search Relevance in Practise



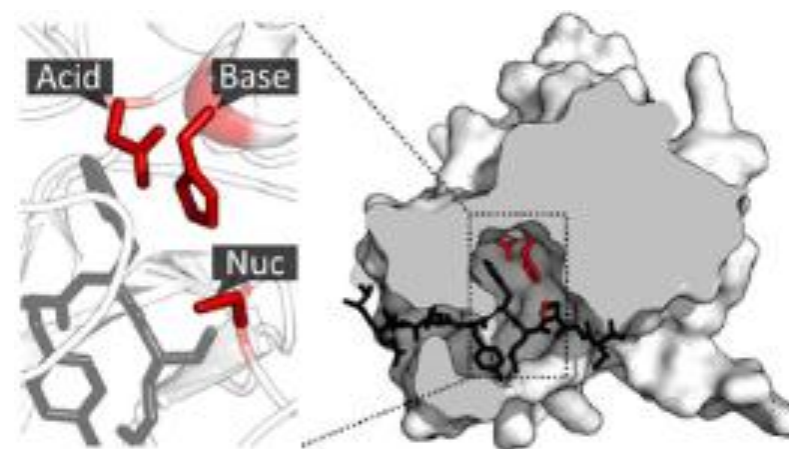
## Thermal Barrier Coatings

*Image by April Gocha <http://ceramics.org/ceramic-tech-today/new-ceramic-thermal-barrier-coating-is-long-strong-and-down-to-get-the-friction-on>*

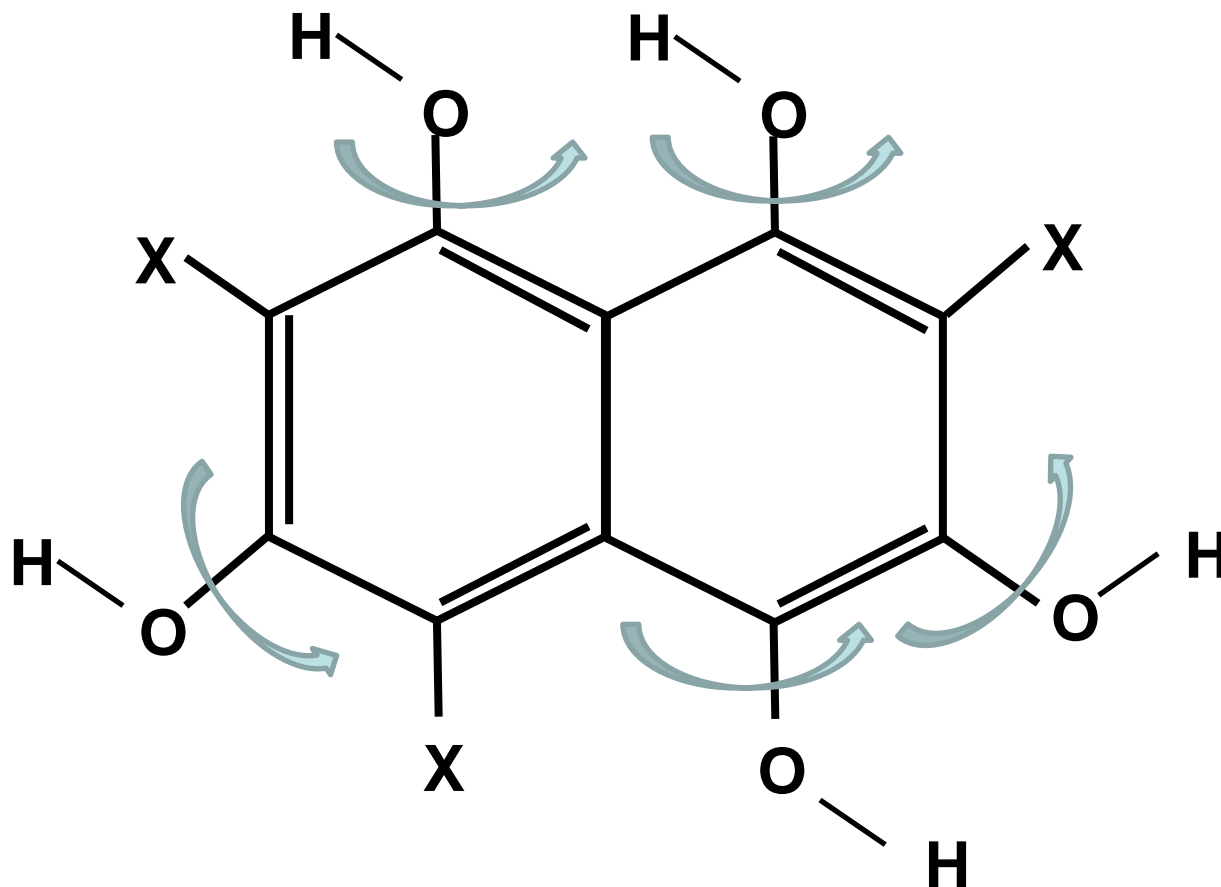
# Structure Determines Function



**Mobilities in Pentacene**



**Catalytic Triade**



**Find the OH-orientations that give the best energy**

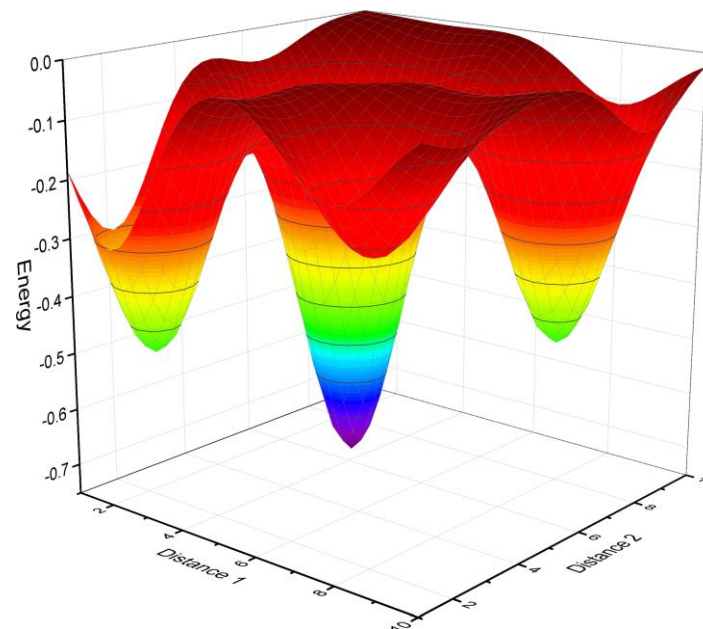
X choose random mixture of: H, F, Cl, CH<sub>3</sub>, NO<sub>2</sub>

# Definitions

**Potential Energy Surface (PES):** result of Born-Oppenheimer approximation. Energy is a function of nuclear coordinates

**On the PES:**

- Local Minima
- Global Minimum
- Transition States



**Attactor Basin:** all points leading to the same minimum with a local geometry optimization

# Structure Determines Function

Thalidomid  
(German: Contergan)



**Global Structure Search  
(of some kind)  
is always the first calculation  
you do**

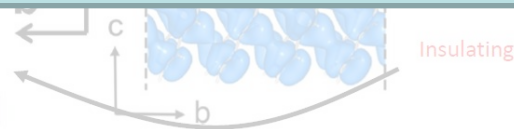
2L

1L

WL

BN

Y. Zhang et al., *Phys. Rev. Lett.*, 2016, **116**, 016602.



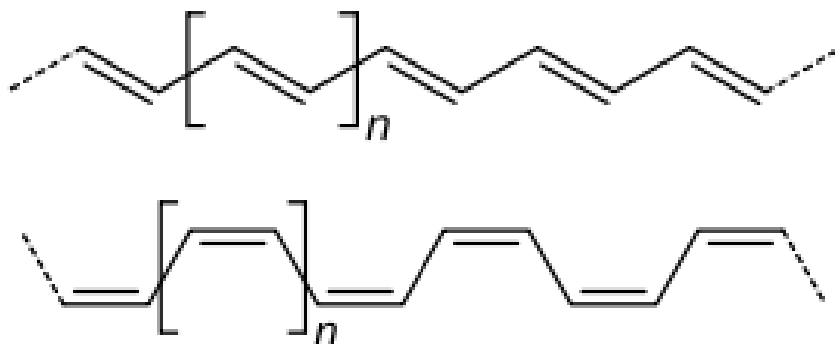
Mobilities in Pentacene

Catalytic Triade



# Why Is This a Hard Problem?

## Simple Example: Polyacetylene



2 options for each double bond:  
*cis* or *trans*



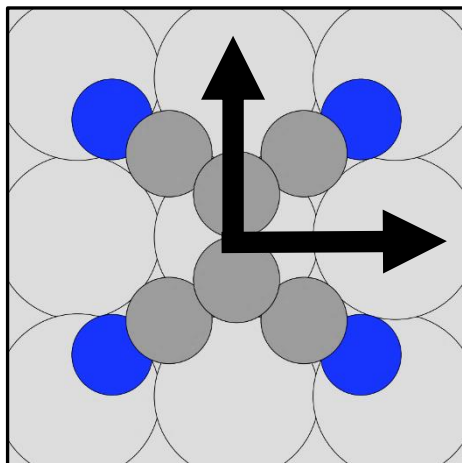
$2^n$  stable geometries

N	# geometries
2	4
4	16
6	64
8	256
10	1024
12	4096
14	16384

**„Configurational  
Explosion“**



# Non-independent DoF



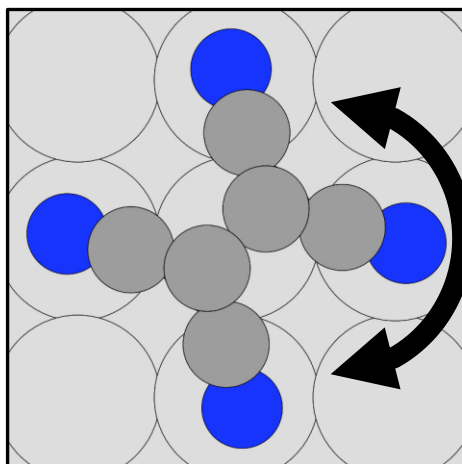
For each molecule:

Translation x:  $\sim 10$  steps

Translation y:  $\sim 10$  steps

Rotation:  $\sim 10$  steps

3 mol.:  $(10 \times 10 \times 10)^3 = \mathbf{1 \text{ billion}}$

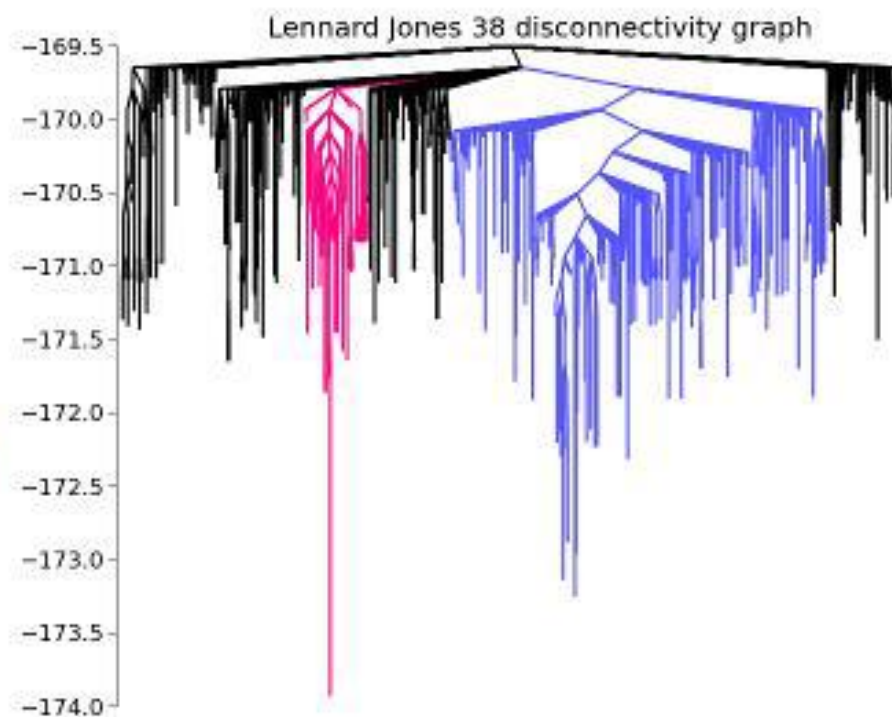


Q: Assuming we can do 1 calc / s,  
how long would it take?

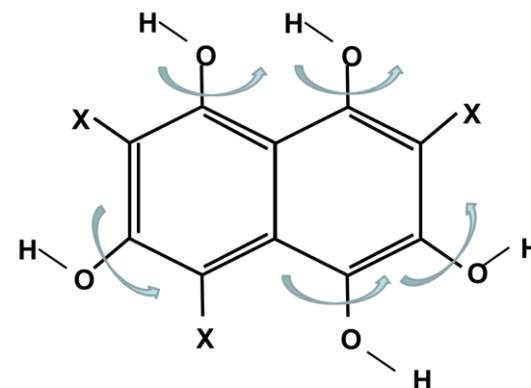
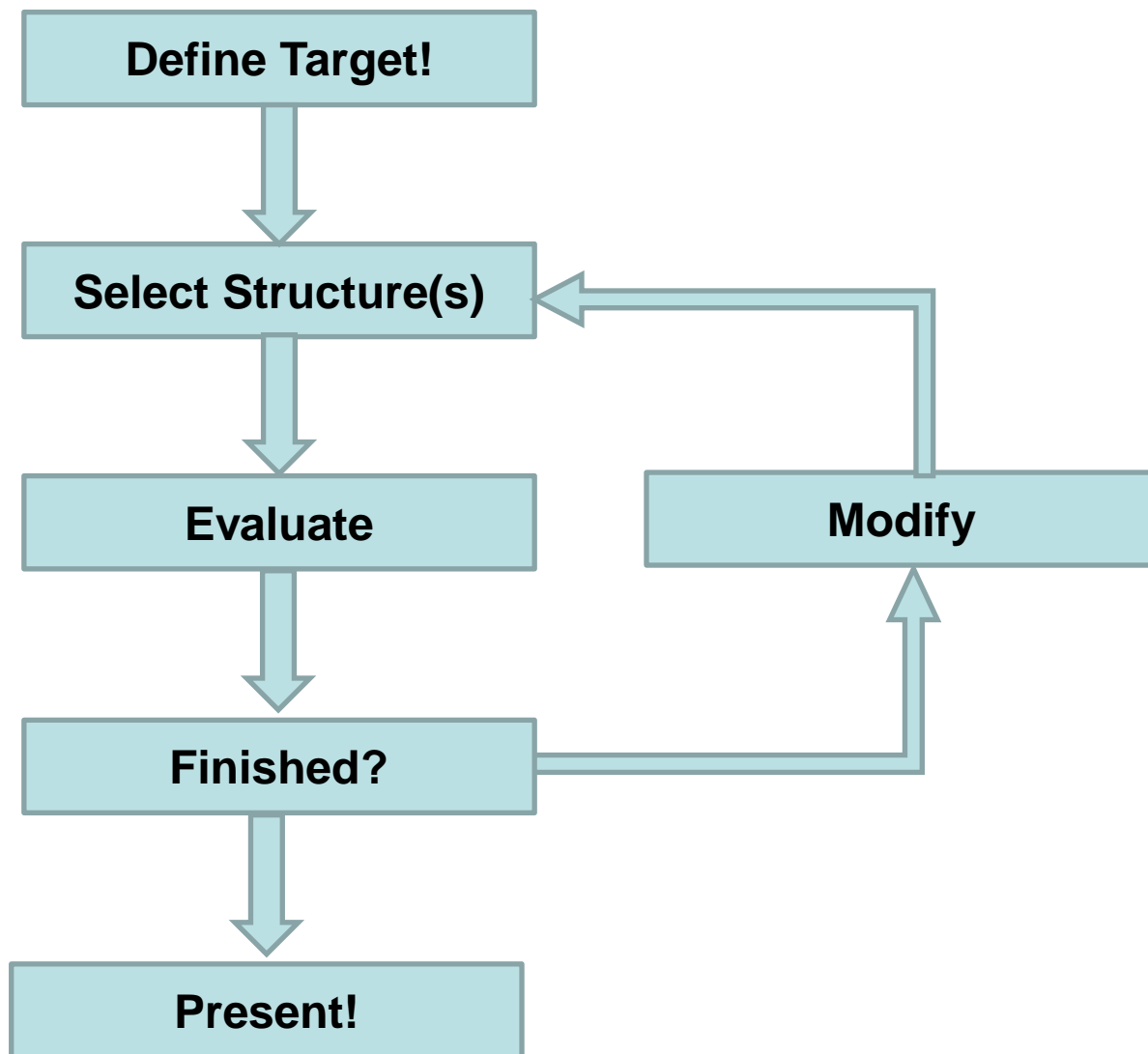
A:  $>100$  years

# Starting points or local minima?

## More Complicated Example: Lennard-Jones Cluster



*Structure and Energy Disconnectivity Graph for a 38 atom Lennard-Jones Cluster. Taken from <https://pele-python.github.io/pele/>*



Define Target!

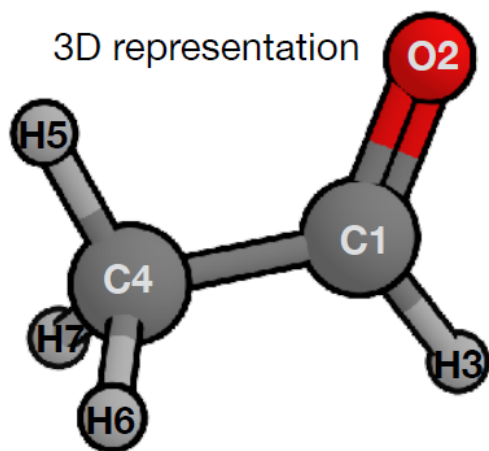
Select Structure(s)

## Initialization:

- Random?
- All oriented the same?
- Mixture?

## Representation:

**Cartesian or Internal Coordinates?**  
**Reflect symmetries?**



atom name	atom connect	distance	angle connect	angle	torsion connect	torsion angle
C1	0	0.00	0	0.0	0	0.0
O2	1	1.20	0	0.0	0	0.0
H3	1	1.10	2	120.0	0	0.0
C4	1	1.50	2	120.0	3	180.0
H5	4	1.10	1	110.0	2	0.0
H6	4	1.10	1	110.0	2	120.0
H7	4	1.10	1	110.0	2	-120.0

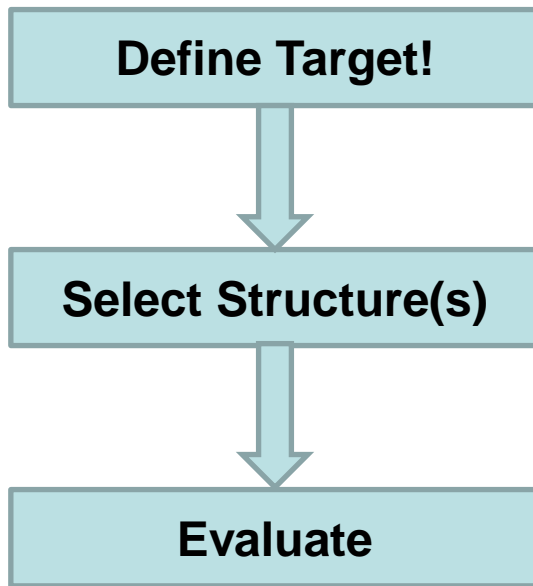
## Cartesian Coordinates:

- Easy to implement
- Straightforward to connect to external code
- Reasonable choice for non-covalent bonds
- Perturbations easily create bogus structure

versus

## Internal Coordinates:

- Requires (some) more thought
- Smoother potential energy surface
- Easier to modify (esp. for genetic algorithm)
- Freezing of DOFs more straightforward



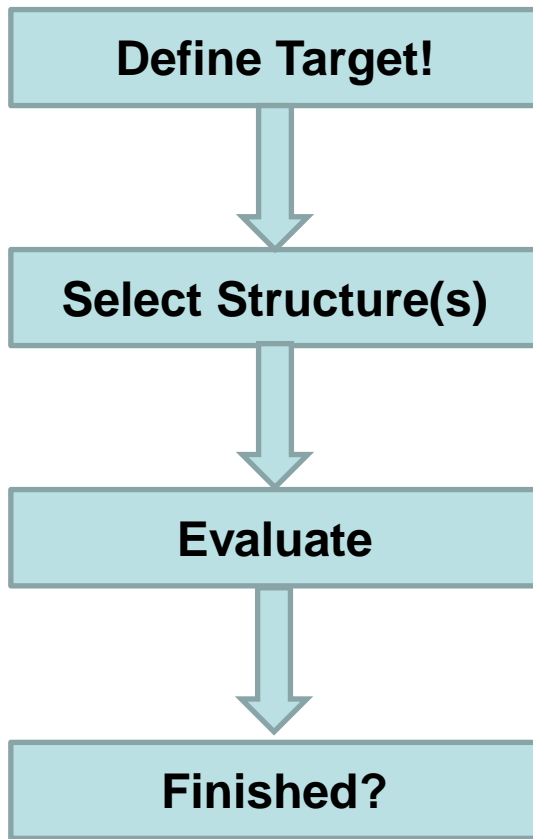
## Select Level Of Theory:

- Connect to Electronic Structure Code (PySCF, FHI-aims, Gaussian, VASP)

→ Low Level Theory will be fast  
(Basis set? Method?)

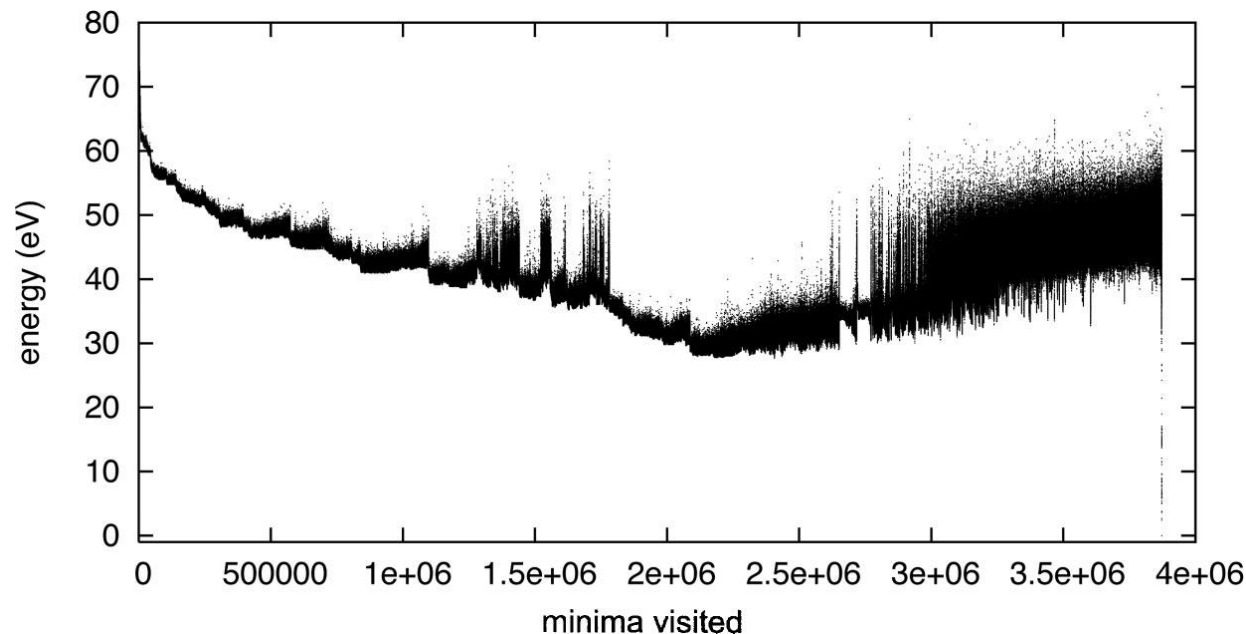
## Obtain energy

- Just single point
- Local Geometry Optimization
- Think about thresholds (energy, forces)

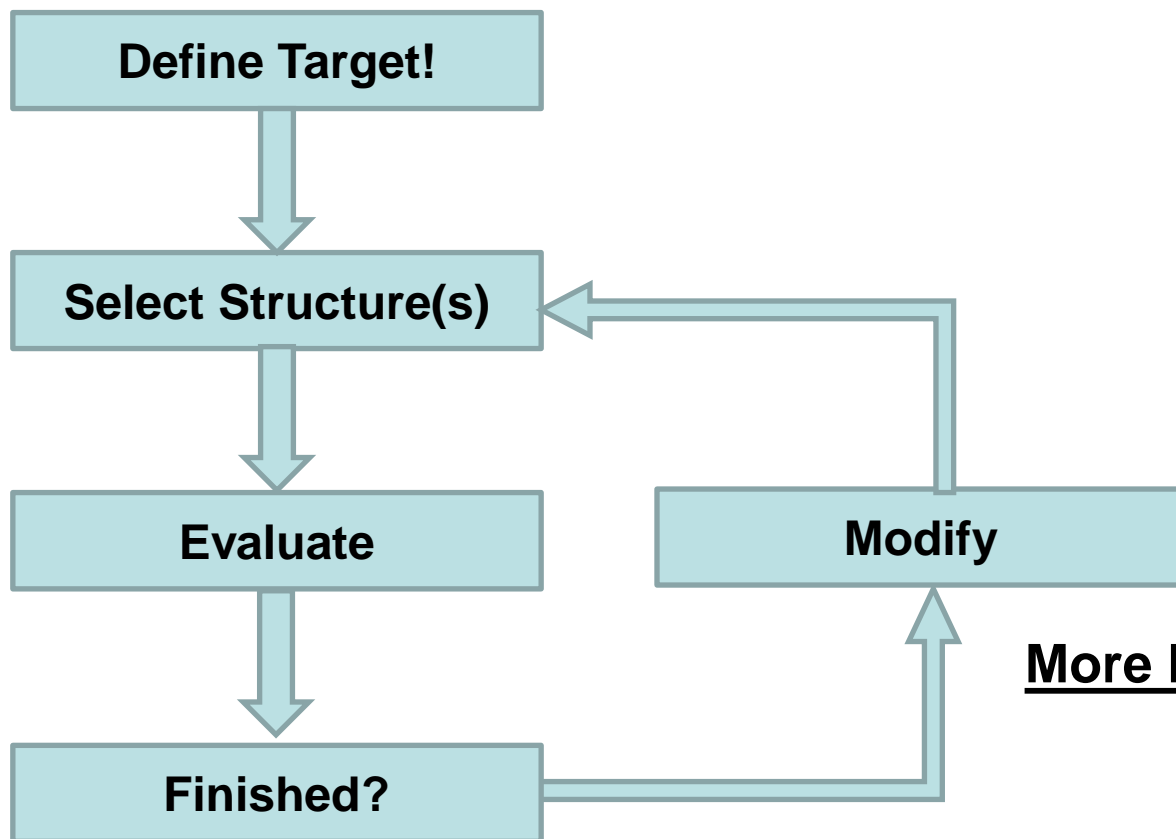


## Convergence

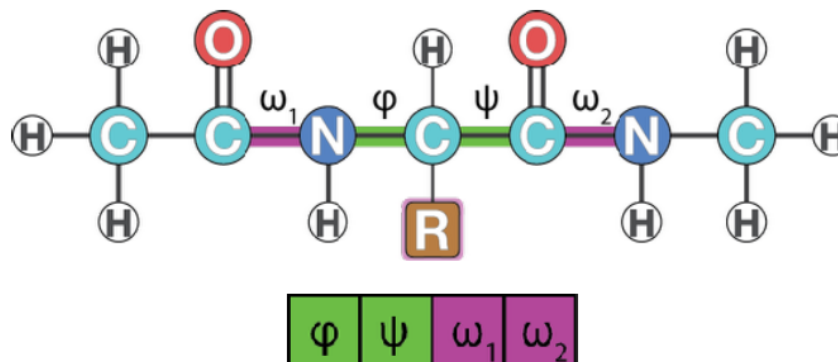
- Run for fixed number of steps
- Run maximum time
- Stop if no better structure is found long enough



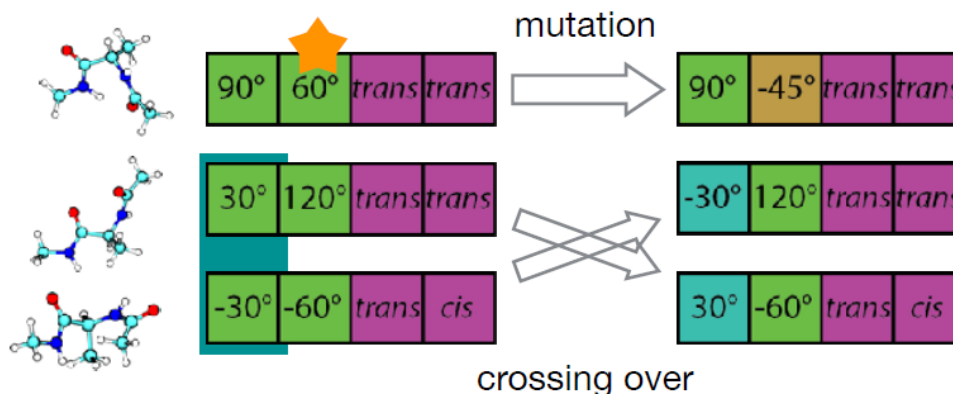




More Fun: Genetic Algorithm



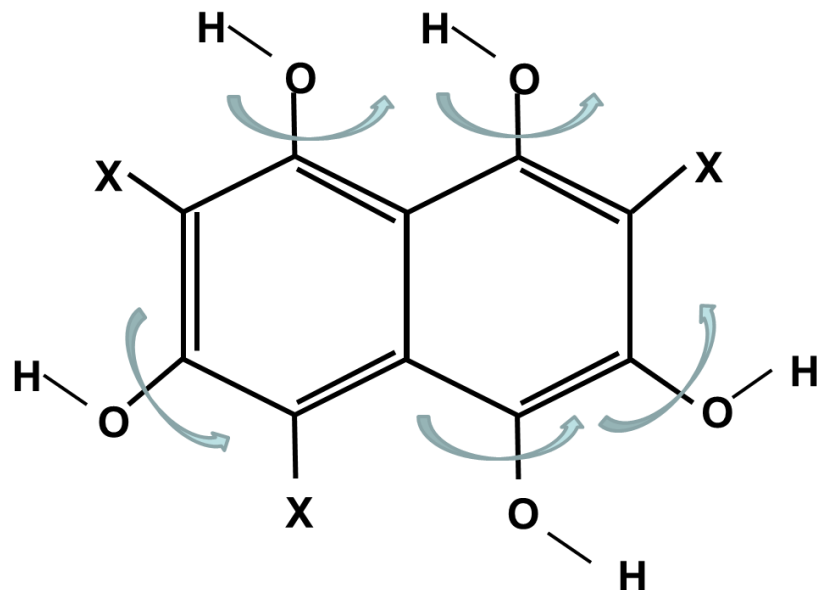
.....



Work by A. Supady

## Select sensible „genes“:

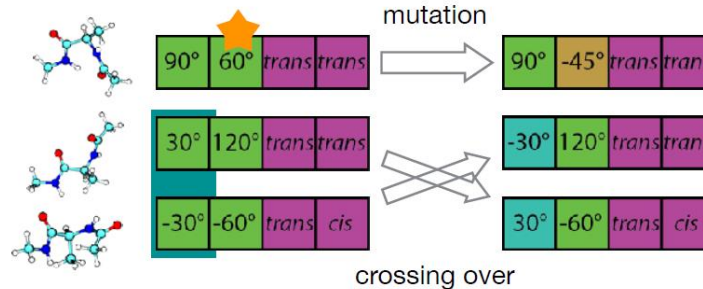
- Internal coordinates, including connection to different atoms



**Select sensible „genes“:**

- Here: Only C-C-O-H torsions
- Single points: Use 6-fold discretization: 0,60,120,180,240,300 °
- Geometry optimization: Darwin or Lamark

Select (pairs of) parents to mate and form offspring



Work by A. Supady

## Mating:

- Mutation: Change gene in sensible range
- Crossover:
  - Set of genes from M1
  - ***complimentary*** set of genes from M2

## Selections:

- Roulette Wheel: full population, weigh probably to mate by fitness
  - Inverse Roulette Wheel: full population, less fit members are more likely to mate
  - Tournament: randomly select subset, fittest mate
- Remember to keep some parents in the pool

A

Lamarck



B

Darwin



# Present Results

- **Chosen Molecule**
- **Level of Theory**
- **Other choices (population size, mutation rate, ..)**
- **Outcome**
  - **Best Geometry**
  - **Energy spread of explored geometries**
  - **Success rate**
  - **Time to find global minimum**

# Target Exercise

- **Write a global optimization program**
  - Select a system (cluster or molecule)
  - Make methodological choices and justify them
  - Explore parameters, report impact
  - Report results from the search. What could be relevant questions?

**Note: The performance will not be graded!**

## Questions:

**Contact me ([o.hofmann@tugraz.at](mailto:o.hofmann@tugraz.at))**