



Random Numbers



100 X



-1













Can't go below step o

0.1 % chance of falling down the stairs

Bet: you'll reach step 60







How to solve?

- Analytical
- Simulate the process
 - Hacker statistics!



Random Generators

```
In [1]: import numpy as np
                                   Pseudo-random numbers
In [2]: np.random.rand()
Out[2]: 0.9535543896720104
                                   Mathematical formula
                                   Starting from a seed
In [3]: np.random.seed(123)
In [4]: np.random.rand()
Out[4]: 0.6964691855978616
In [5]: np.random.rand()
                                   Same seed: same random numbers!
Out[5]: 0.28613933495037946
                                   Ensures "reproducibility"
In [6]: np.random.seed(123)
In [7]: np.random.rand()
Out[7]: 0.696469185597861
In [8]: np.random.rand()
Out[8]: 0.28613933495037946
```



Coin Toss

```
import numpy as np
np.random.seed(123)
coin = np.random.randint(0,2)
print(coin)
Randomly generate o or 1
```

```
Output:
```

0



Coin Toss

```
game.py
import numpy as np
np.random.seed(123)
coin = np.random.randint(0,2)
print(coin)
if coin == 0:
    print("heads")
else:
    print("tails")
```

```
Output:
heads
```





Let's practice!



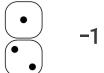


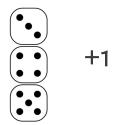
Random Walk



Random Step







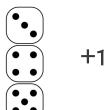


Random Walk

100 X



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Known in Science

- Path of molecules
- Gambler's financial status



Heads or Tails

```
import numpy as np
np.random.seed(123)
outcomes = []
for x in range(10):
    coin = np.random.randint(0, 2)
    if coin == 0:
        outcomes.append("heads")
    else:
        outcomes.append("tails")
print(outcomes)
```

```
Output:
['heads', 'tails', 'heads', 'heads', 'heads',
'heads', 'heads', 'tails', 'heads']
```



Heads or Tails: Random Walk

```
import numpy as np
np.random.seed(123)
tails = [0]
for x in range(10):
    coin = np.random.randint(0, 2)
    tails.append(tails[x] + coin)
print(tails)
```

```
Output:
[0, 0, 1, 1, 1, 1, 1, 2, 3, 3]
```



Step to Walk

outcomes

```
['heads', 'tails', 'heads', 'heads',
'heads', 'heads', 'tails', 'heads']
```

tails

```
Output:
[0, 0, 1, 1, 1, 1, 1, 2, 3, 3]
```





Let's practice!





Distribution





100 X



Each random walk has an end point

Simulate 10,000 times: 10,000 end points



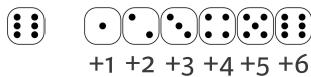
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Distribution!



Calculate chances!





Random Walk

```
import numpy as np
np.random.seed(123)
tails = [0]
for x in range(10):
    coin = np.random.randint(0,2)
    tails.append(tails[x] + coin)
```



100 runs

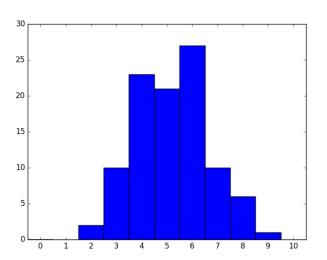
```
import numpy as np
np.random.seed(123)
final_tails = []
for x in range(100) :
    tails = [0]
    for x in range(10) :
        coin = np.random.randint(0,2)
        tails.append(tails[x] + coin)
    final_tails.append(tails[-1])
print(final_tails)
```

```
Output:
[3, 6, 4, 5, 4, 5, 3, 5, 4, 6, 6, 8, 6, 4, 7, 5, 7, 4, 3, 3, 4, 5, 8, 5, 6, 5, 7, 6, 4, 5, 8, 5, 8, 4, 6, 6, 3, 4, 5, 4, 7, 8, 9, 4, 3, 4, 5, 6, 4, 2, 6, 6, 5, 7, 5, 4, 5, 5, 6, 7, 6, 6, 6, 3, ..., 7]
```



Histogram, 100 runs

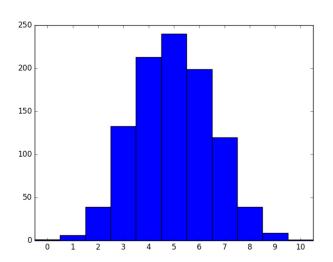
```
distribution.py
import numpy as np
import matplotlib.pyplot as plt
np.random.seed(123)
final_tails = []
for x in range (100):
    tails = [0]
    for x in range(10):
        coin = np.random.randint(0,2)
        tails.append(tails[x] + coin)
    final_tails.append(tails[-1])
plt.hist(final_tails, bins = 10)
plt.show()
```





Histogram, 1.000 runs

```
import numpy as np
import matplotlib.pyplot as plt
np.random.seed(123)
final_tails = []
for x in range(1000):
    tails = [0]
    for x in range(10):
        coin = np.random.randint(0,2)
        tails.append(tails[x] + coin)
    final_tails.append(tails[-1])
plt.hist(final_tails, bins = 10)
plt.show()
```

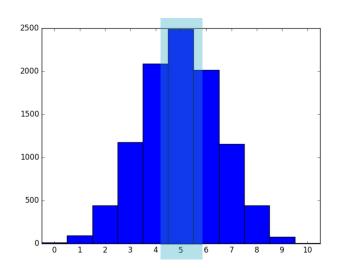






Histogram, 10.000 runs

```
import numpy as np
import matplotlib.pyplot as plt
np.random.seed(123)
final_tails = []
for x in range(10000):
    tails = [0]
    for x in range(10):
        coin = np.random.randint(0,2)
        tails.append(tails[x] + coin)
    final_tails.append(tails[-1])
plt.hist(final_tails, bins = 10)
plt.show()
```







Let's practice!