

### Computer Programming

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Session: Representing Floating Point Numbers

# Quick Recap of Relevant Topics



- Architecture of a simple computer
- Representation of integers

#### **Overview of This Lecture**

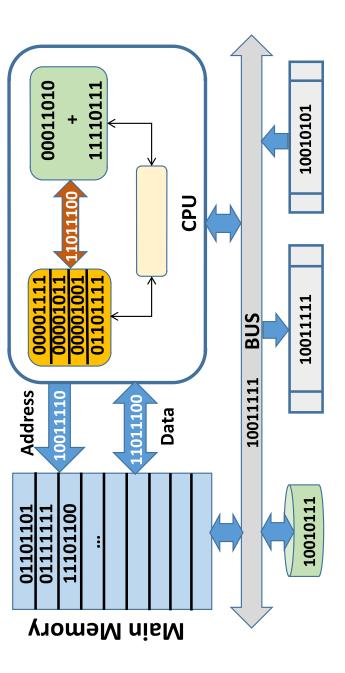


- A computer's internal representation of numbers
- Floating point numbers
- C++ declarations of floating point variables

## Recap from Earlier Lecture



Snapshot:



• How do we represent numbers like 3.14 x 10<sup>-23</sup> in a computer?

# Representing Floating Point Numbers



- Numbers with fractional values, very small or very large numbers cannot be represented as integers
- Floating point number



• Mantissa =  $-(3 \times 10^{0} + 1 \times 10^{-1} + 2 \times 10^{-2} + 3 \times 10^{-3})$ 

• Binary:  $-1.1101 \times 2^{110}$ 

• Mantissa =  $-(1 \times 2^0 + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4}) = -1.8125$ 

• Exponent =  $(1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0) = 6$ 

# Representing Floating Point Numbers



- Normalized mantissa: single non-0 digit to left of radix point
- $0.02345 \times 10^{12} = 2.345 \times 10^{10}$
- $110.101 \times 2^{110} = 1.10101 \times 2^{1000}$
- Binary: Implicit 1 always on left of radix point; need not be stored
- Floating point numbers represented by allocating fixed number of bits for mantissa and exponent
- Cannot represent all real numbers
- Finite precision artifacts
- What is  $0.101 \times 2^{111} + 1$  if we have only 3 bits to represent mantissa?

## Floating Point Numbers in C++



float and double data types

float

• 32 bits (4 bytes): 1 sign, 8 exponent, 23 mantissa

ullet Approximate range of magnitude:  $10^{-44.85}$  to  $10^{34.83}$ 

double

64 bits (8 bytes): 1 sign, 11 exponent, 52 mantissa

 $\bullet$  Approximate range of magnitude:  $10^{\text{-}323.3}\,\text{to}\ 10^{\text{3}08.3}$ 

 Special bit patterns reserved for 0, infinity, NaN (not-anumber: result of 0/0), ... C++ declarations: float temperature; double verticalSpeed;

## Floating Point Numbers in C++



- Floating point constants can be specified in C++ programs as
- 23.572 (can have non-normalized mantissa in programs)
- 2357.2e-2 or 2357.2E-2 (scientific notation)
- $2357.2 \times 10^{-2}$  (base 10)
- C++ constant floating point declaration
- const float pi = 3.1415
- const double e = 2.7183
- Values of pi and e cannot change during program execution



#### Summary

- Binary representation of floating point numbers
- Sign, mantissa and exponent
- C++ declarations