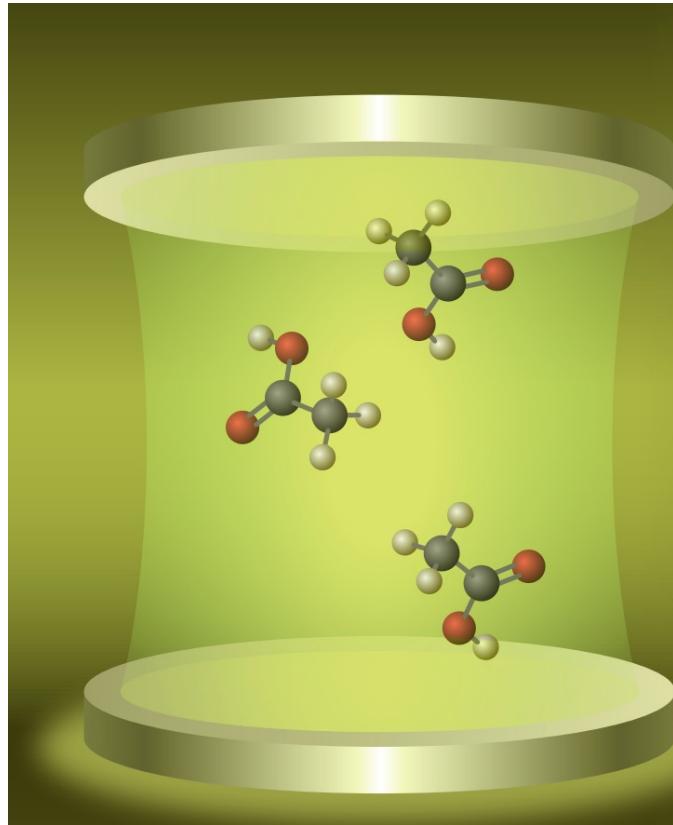


Jay Foley, Associate Professor
UNC Charlotte Department of Chemistry
<https://foleylab.github.io/>



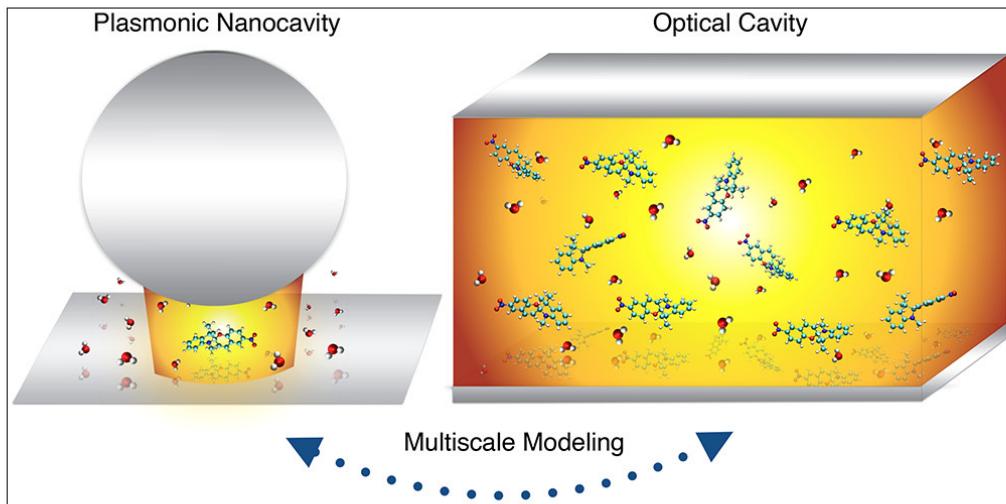
Many-Body Methods,
Spectroscopies, and
Dynamics for Molecular
Polaritonic Systems

Ingredients of polaritonic chemistry

Strong interaction between light and molecular excitations

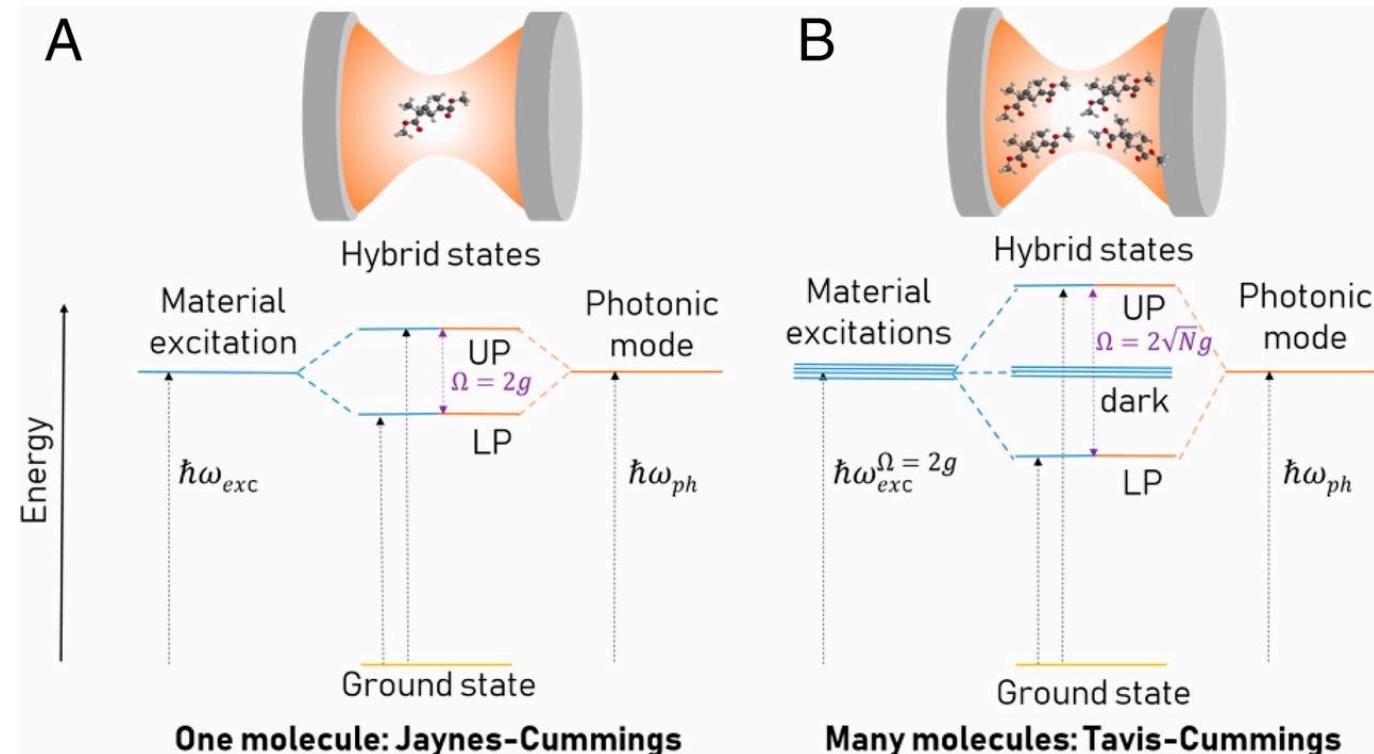
$\hbar g > \hbar\gamma \rightarrow$ Strong Coupling

Interaction compared to energy dissipation

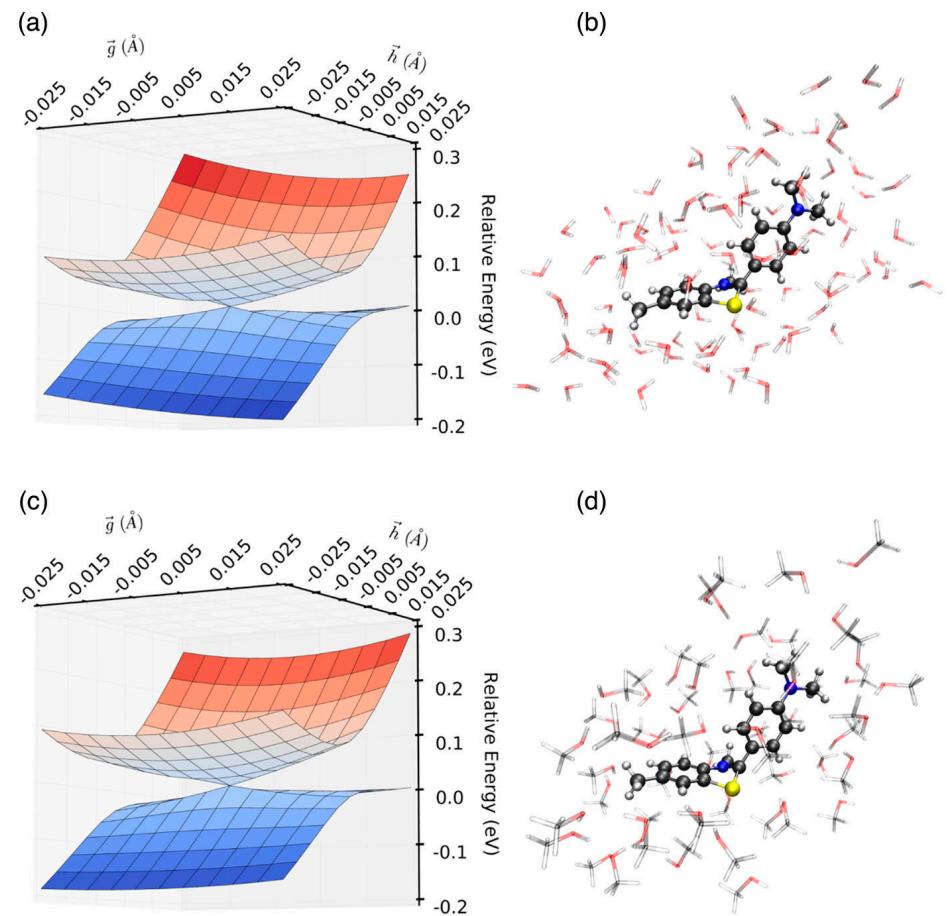
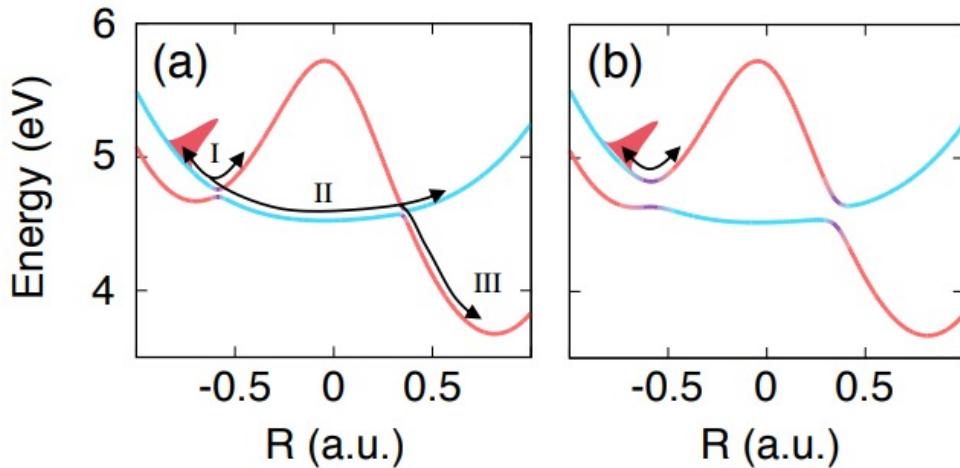
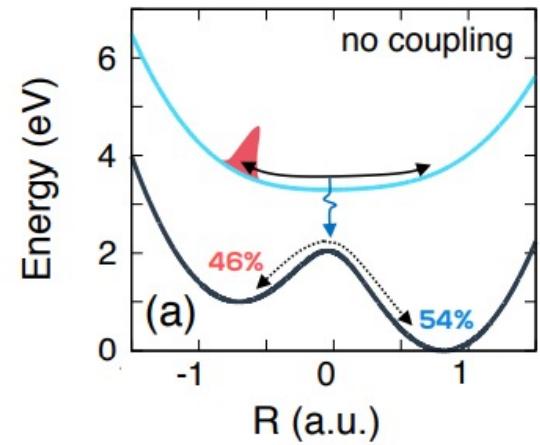


$\hbar g > \hbar\omega \rightarrow$ Ultra-strong Coupling

Interaction compared to excitation energies



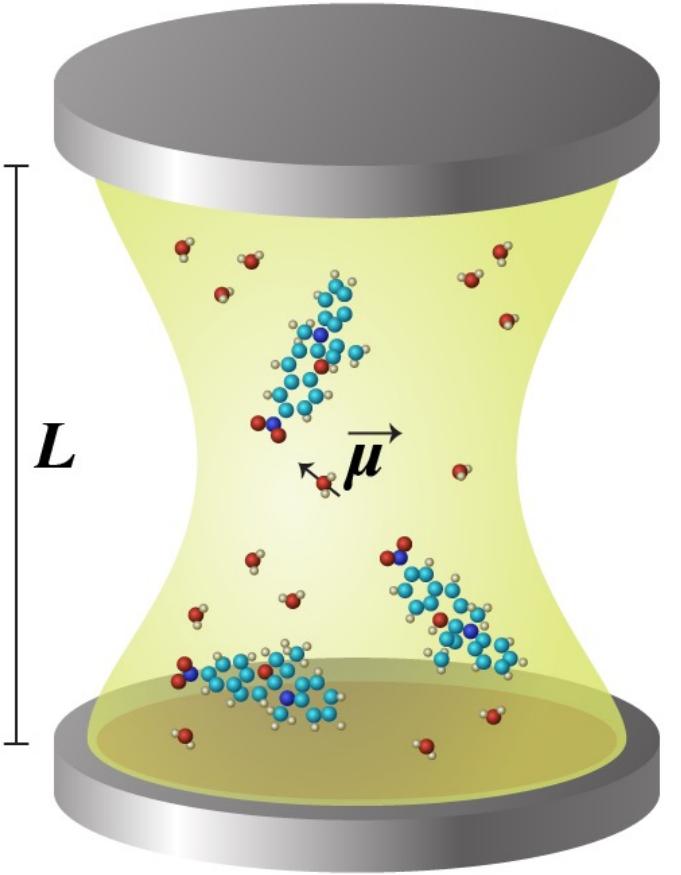
Quantum chemistry for polaritonic surfaces and couplings



J. Chem. Phys.. 2017;147(9) doi:10.1063/1.5000476

Pauli-Fierz Hamiltonian

$$\lambda = \sqrt{\frac{\hbar}{\epsilon_0 L^3}} \hat{\mathbf{e}}$$



$$\hat{H} = \hat{H}_e + \omega_{\text{cav}} \hat{b}^\dagger \hat{b} - \sqrt{\frac{\omega_{\text{cav}}}{2}} (\lambda \cdot \hat{\mu})(\hat{b}^\dagger + \hat{b}) + \frac{1}{2} (\lambda \cdot \hat{\mu})^2$$

ab initio
molecular
Hamiltonian Photonic
Hamiltonian Bilinear molecule-photon coupling Quadratic dipole self energy

Coherent state transformation

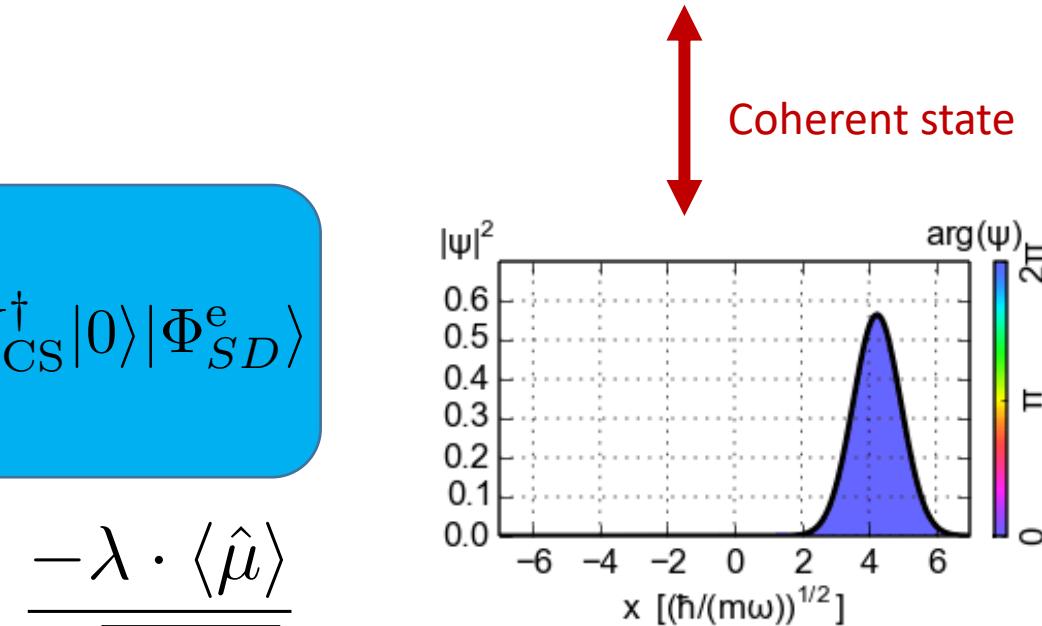
$$|0^p\rangle = \sum_n (\hat{b}^\dagger)^n |0\rangle c_n = \hat{U}_{\text{CS}}^\dagger |0\rangle$$

$$\langle \Phi_{SD}^e | \hat{H} | 0^p \Phi_{SD}^e \rangle = \langle \Phi_{SD}^e | \langle 0 | \hat{U}_{\text{CS}} \hat{H} \hat{U}_{\text{CS}}^\dagger | 0 \rangle | \Phi_{SD}^e \rangle$$

$$\hat{U}_{\text{CS}} = \exp \left(z(\hat{b}^\dagger - \hat{b}) \right) \quad z = \frac{-\lambda \cdot \langle \hat{\mu} \rangle}{\sqrt{2\omega_{\text{cav}}}}$$

Koch and co-workers, PRX **10**, 041043 (2020)

Foley, McTague, DePrince, *Chem Phys Rev*, **4**, 041301 (2023)



"It's just a state that, no matter what happens in life, can't be annihilated"

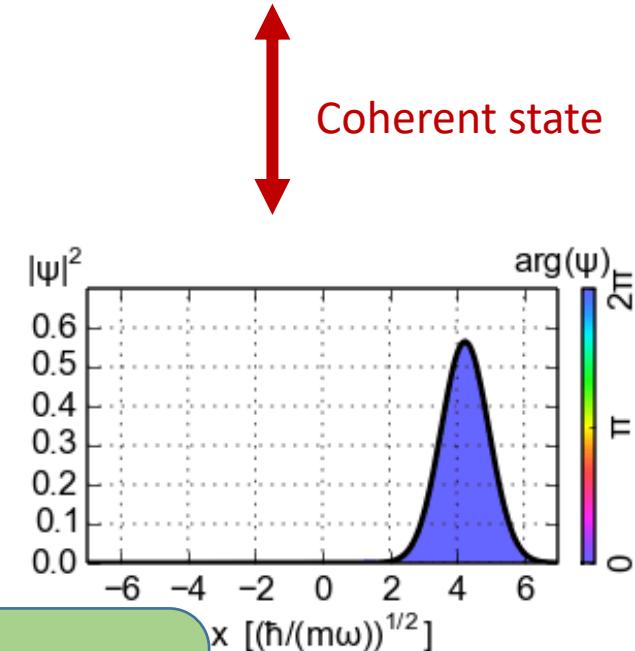
"It's just a state that, no matter what happens in life, never spreads"

Coherent state transformation and solution to QED-HF

$$|0^p\rangle = \sum_n (\hat{b}^\dagger)^n |0\rangle c_n = \hat{U}_{\text{CS}}^\dagger |0\rangle$$

$$\langle \Phi_{SD}^e | 0^p | \hat{H} | 0^p \Phi_{SD}^e \rangle = \langle \Phi_{SD}^e | \langle 0 | \hat{U}_{\text{CS}} \hat{H} \hat{U}_{\text{CS}}^\dagger | 0 \rangle | \Phi_{SD}^e \rangle$$

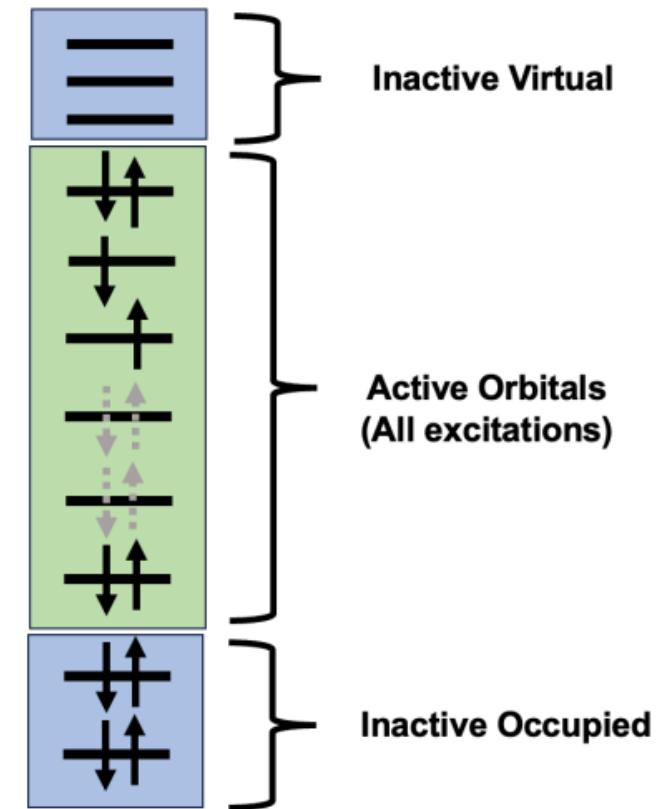
$$\hat{H}_{CS} = \hat{H}_e + \omega_{\text{cav}} \hat{b}^\dagger \hat{b} - \sqrt{\frac{\omega_{\text{cav}}}{2}} [\lambda \cdot (\hat{\mu} - \langle \hat{\mu} \rangle)] (\hat{b}^\dagger + \hat{b}) + \frac{1}{2} [\lambda \cdot (\hat{\mu} - \langle \hat{\mu} \rangle)]^2$$



QED-CI for multiple polaritonic states

$$|\Psi\rangle = \sum_n \sum_I C_{I,n} |\Phi_I^e\rangle |n^p\rangle$$

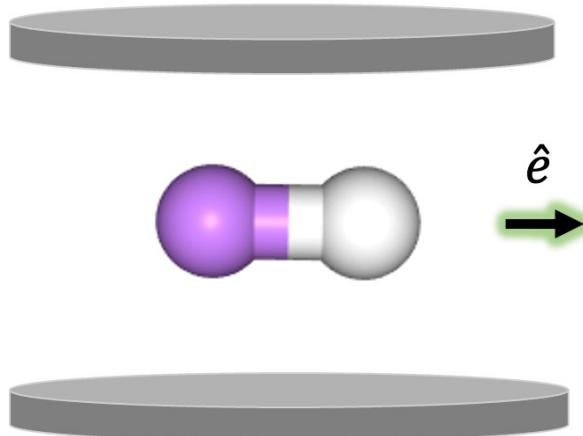
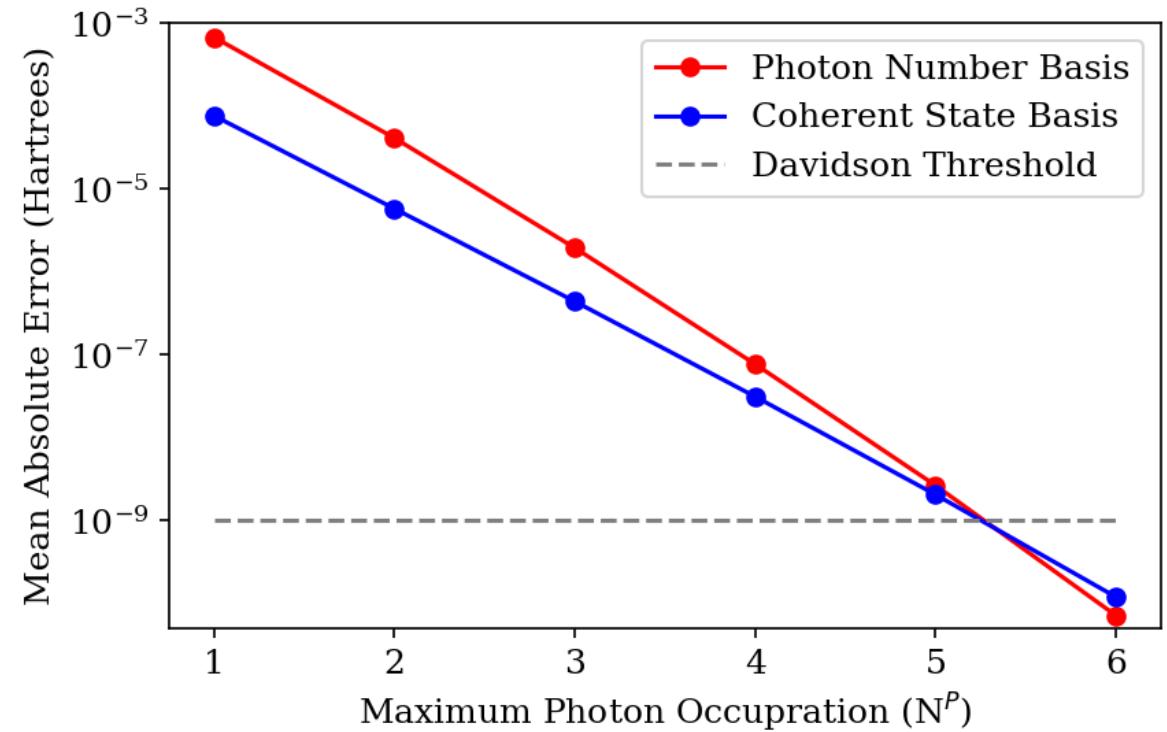
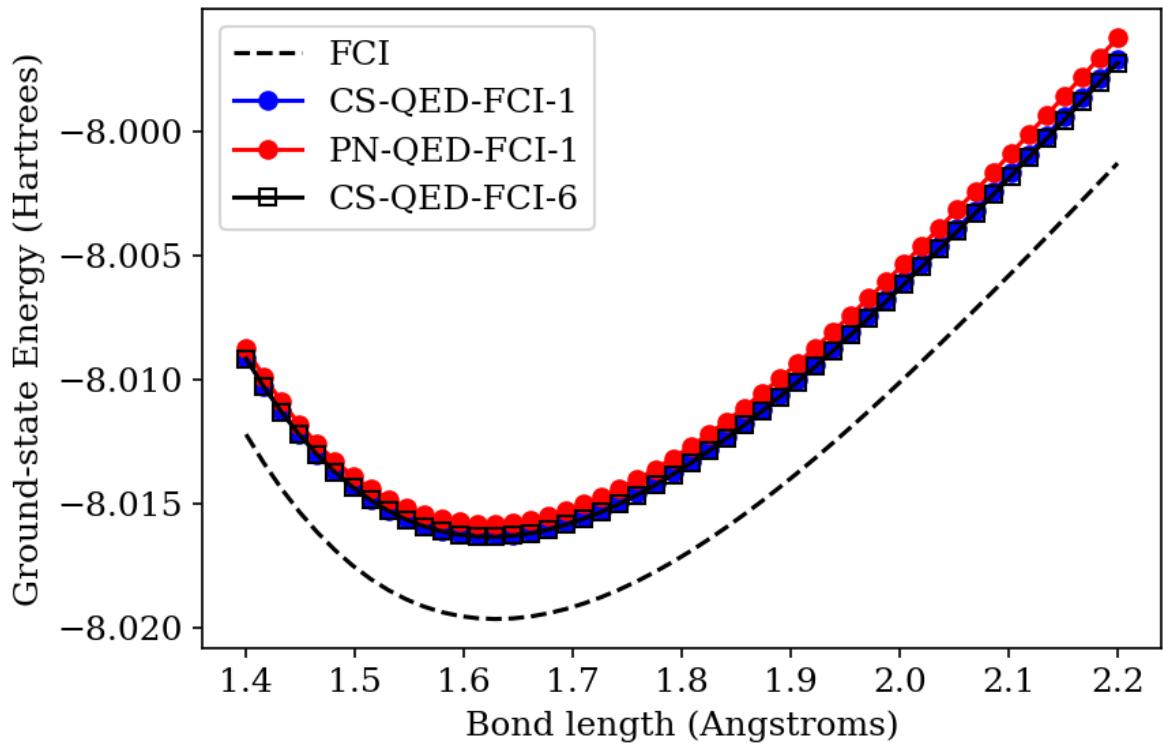
$$\mathbf{H} = \begin{bmatrix} \mathbf{A} + \Delta & \mathbf{G} & 0 & \dots & 0 & 0 \\ \mathbf{G} & \mathbf{A} + \Delta + \Omega & \sqrt{2}\mathbf{G} & \dots & 0 & 0 \\ 0 & \sqrt{2}\mathbf{G} & \mathbf{A} + \Delta + 2\Omega & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & \mathbf{A} + \Delta + (N^p - 1)\Omega & \sqrt{N^p}\mathbf{G} \\ 0 & 0 & 0 & \dots & \sqrt{N^p}\mathbf{G} & \mathbf{A} + \Delta + N^p\Omega \end{bmatrix}$$



The CI space can be FCI, truncated CI, or CASCI

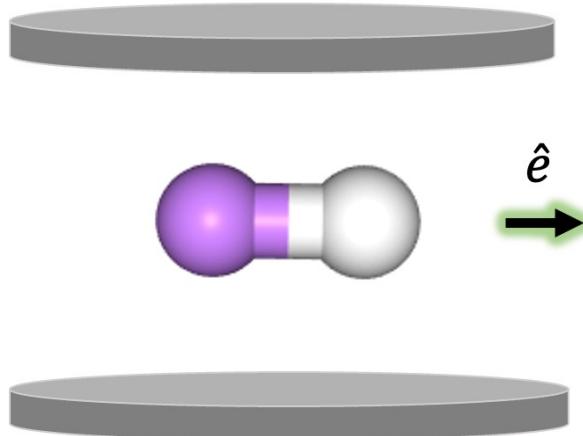
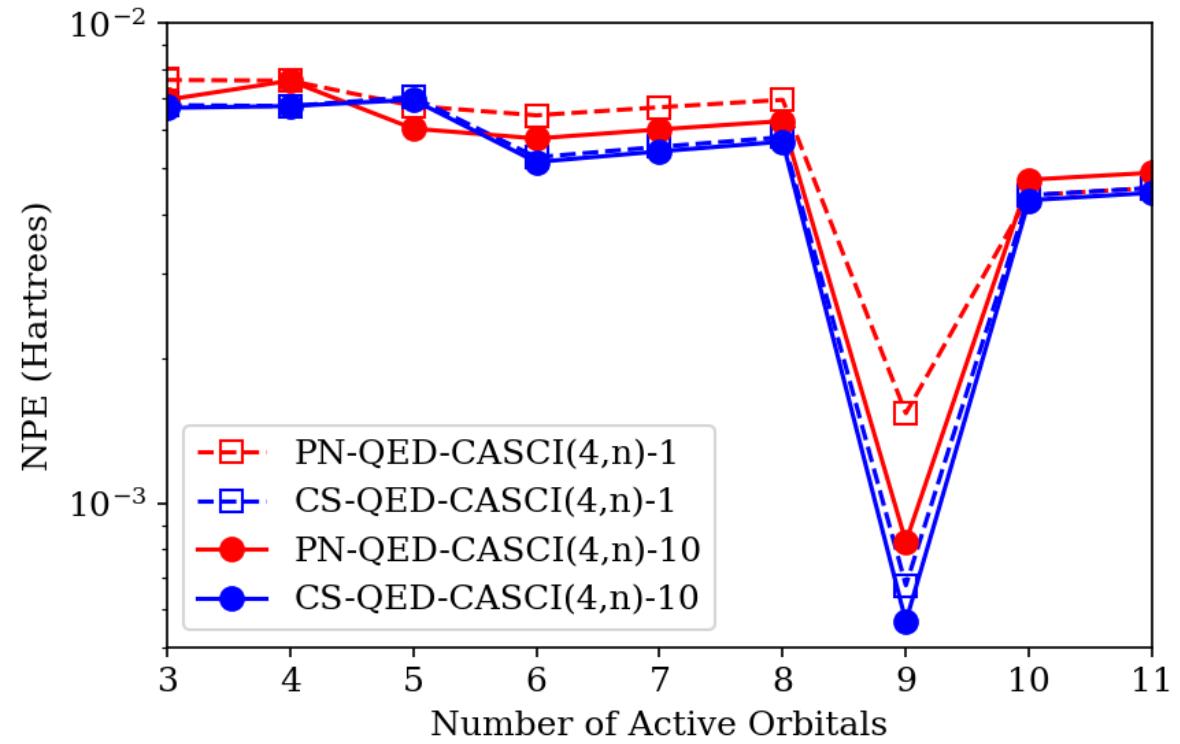
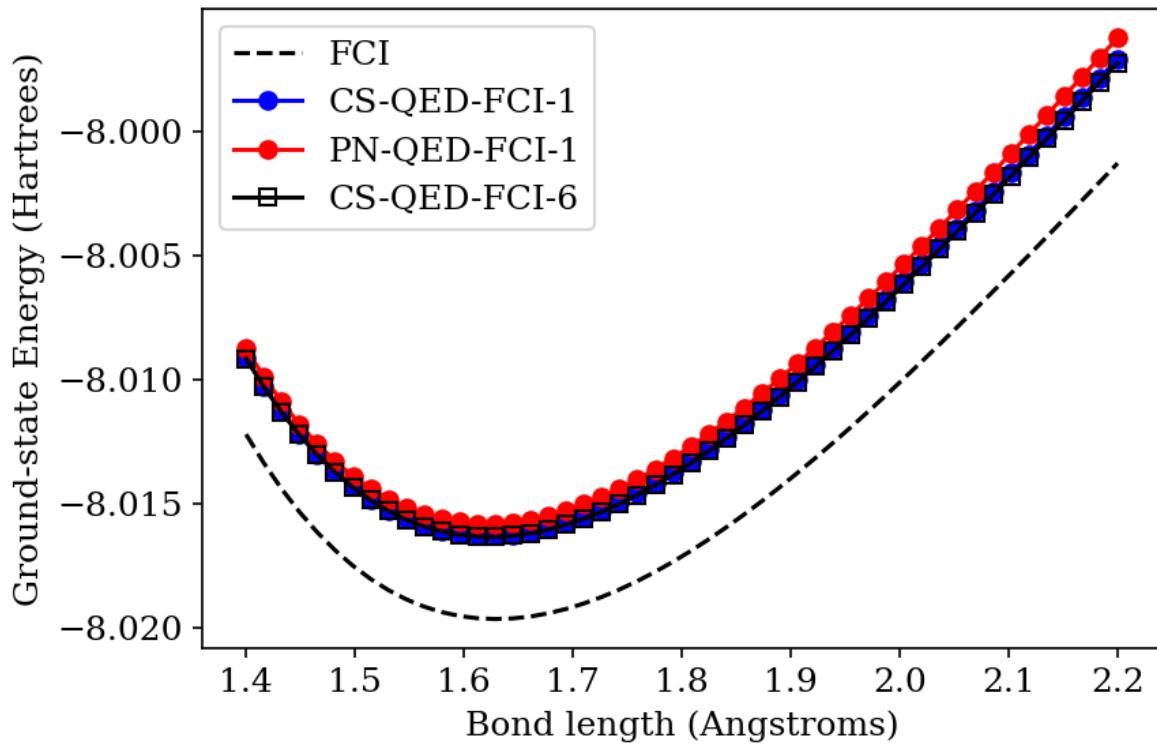
$$\hbar\omega = 3.29 \text{ eV}, \lambda = (0, 0, 0.05) \text{ a.u.}$$

QED-FCI in Coherent State vs Photon Number State – LiH/6-311G



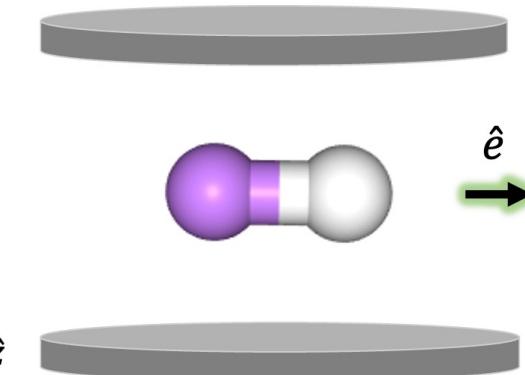
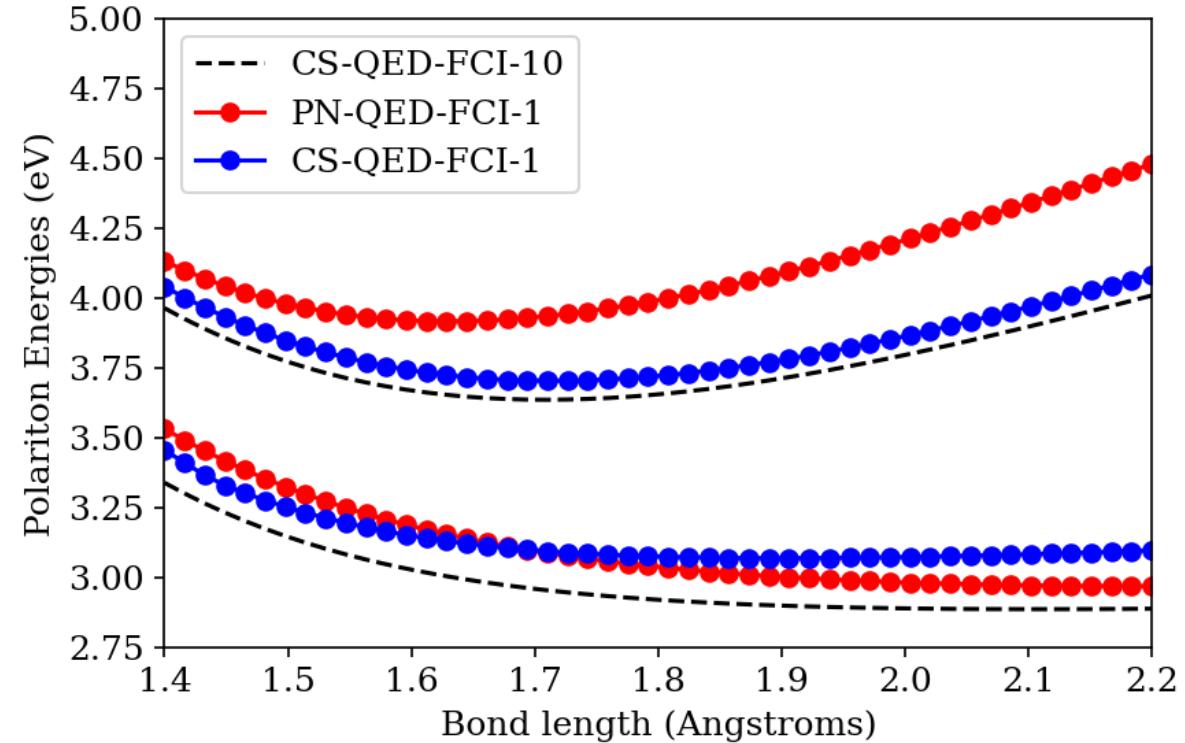
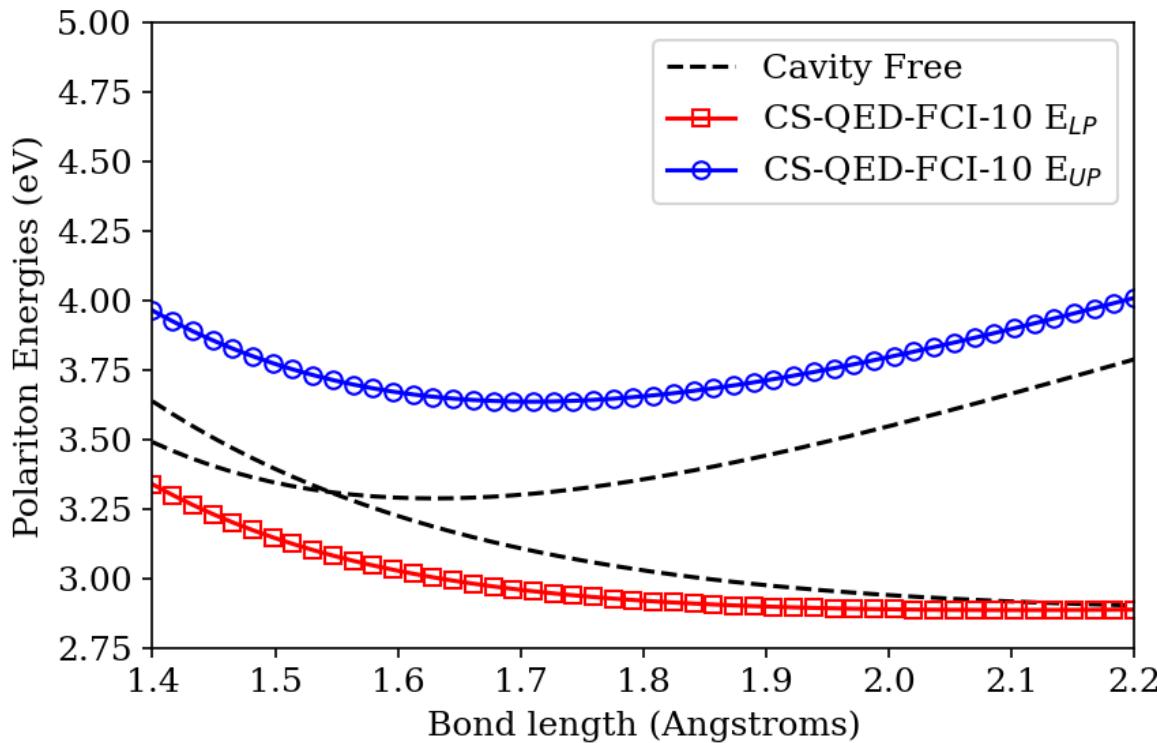
$$\hbar\omega = 3.29 \text{ eV}, \lambda = (0, 0, 0.05) \text{ a.u.}$$

QED-FCI in Coherent State vs Photon Number State – LiH/6-311G

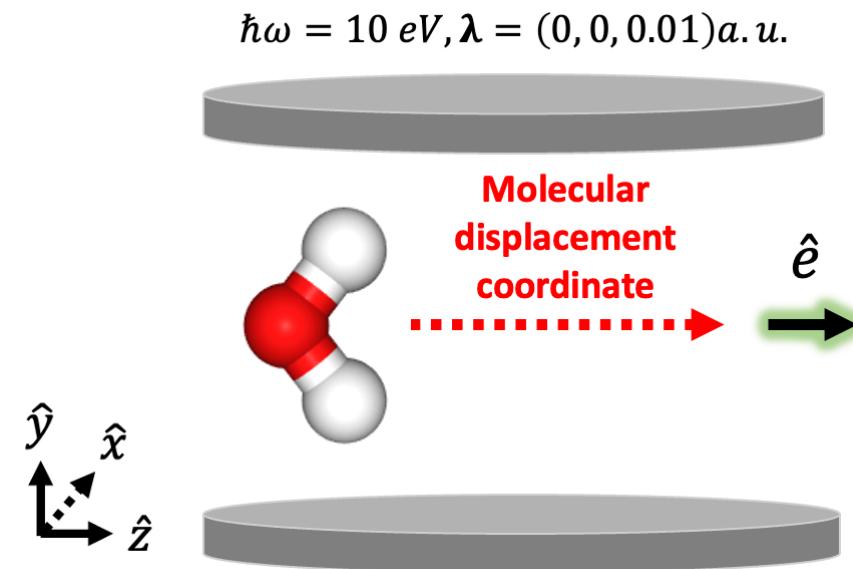
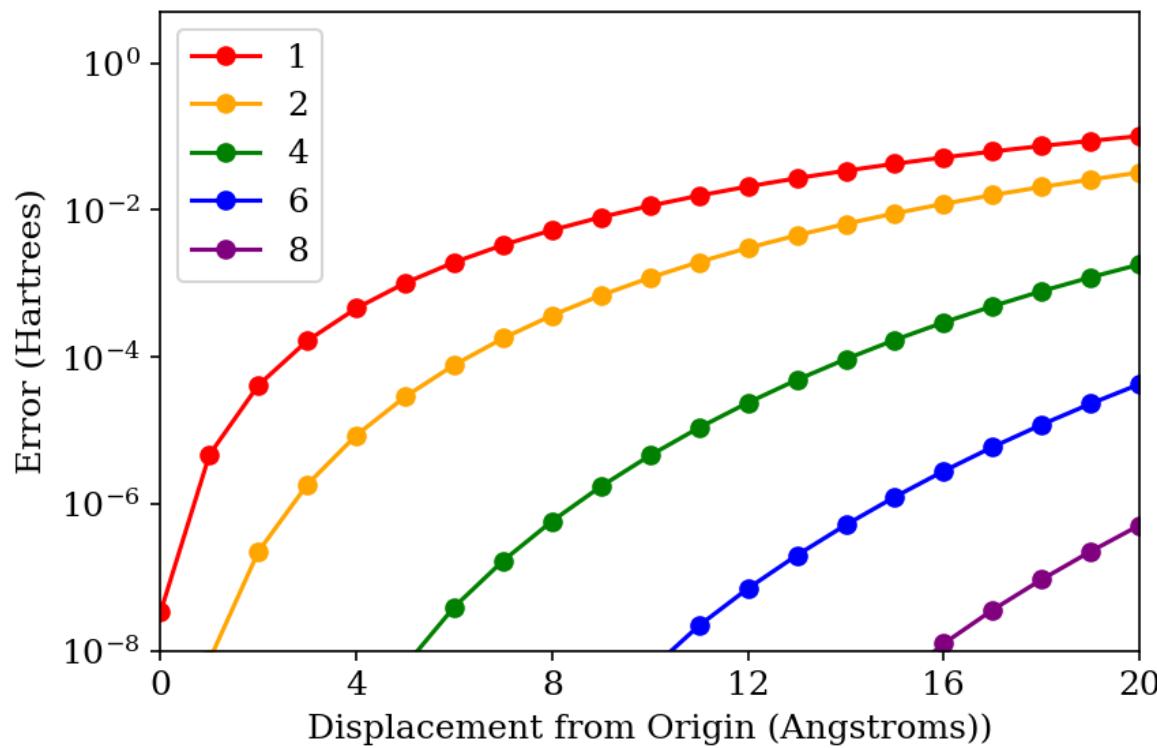


$$\hbar\omega = 3.29 \text{ eV}, \lambda = (0, 0, 0.05) \text{ a.u.}$$

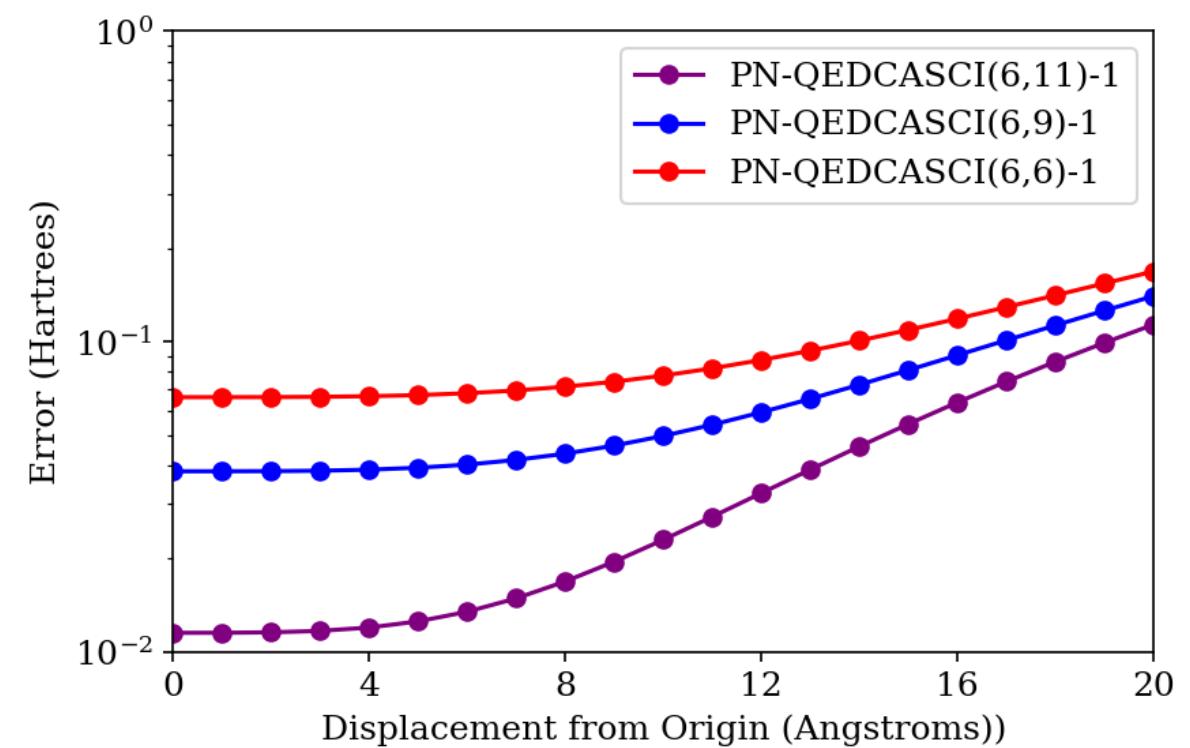
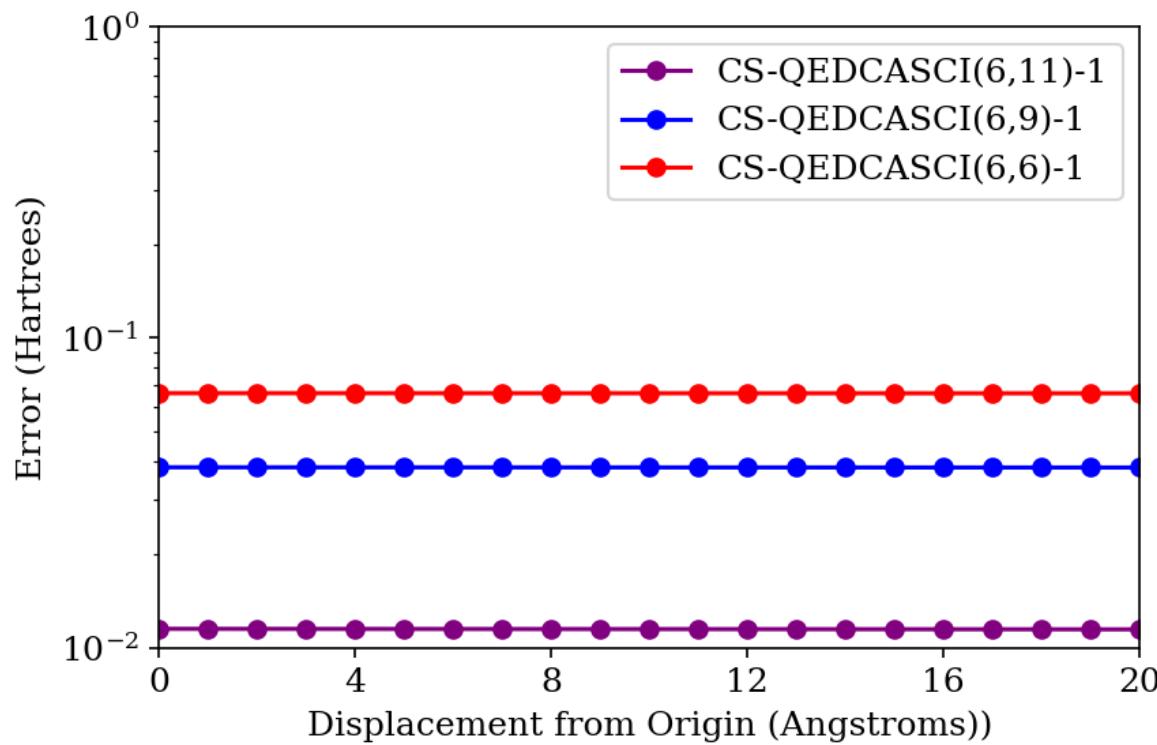
QED-FCI in Coherent State vs Photon Number State



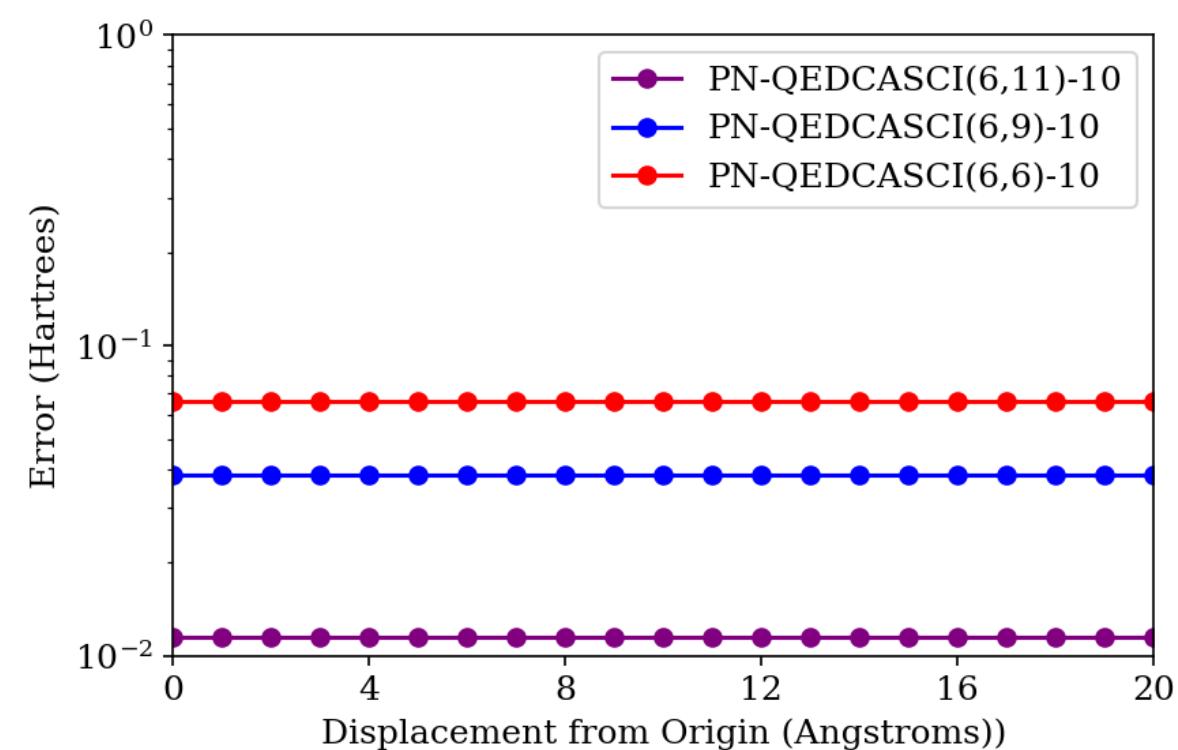
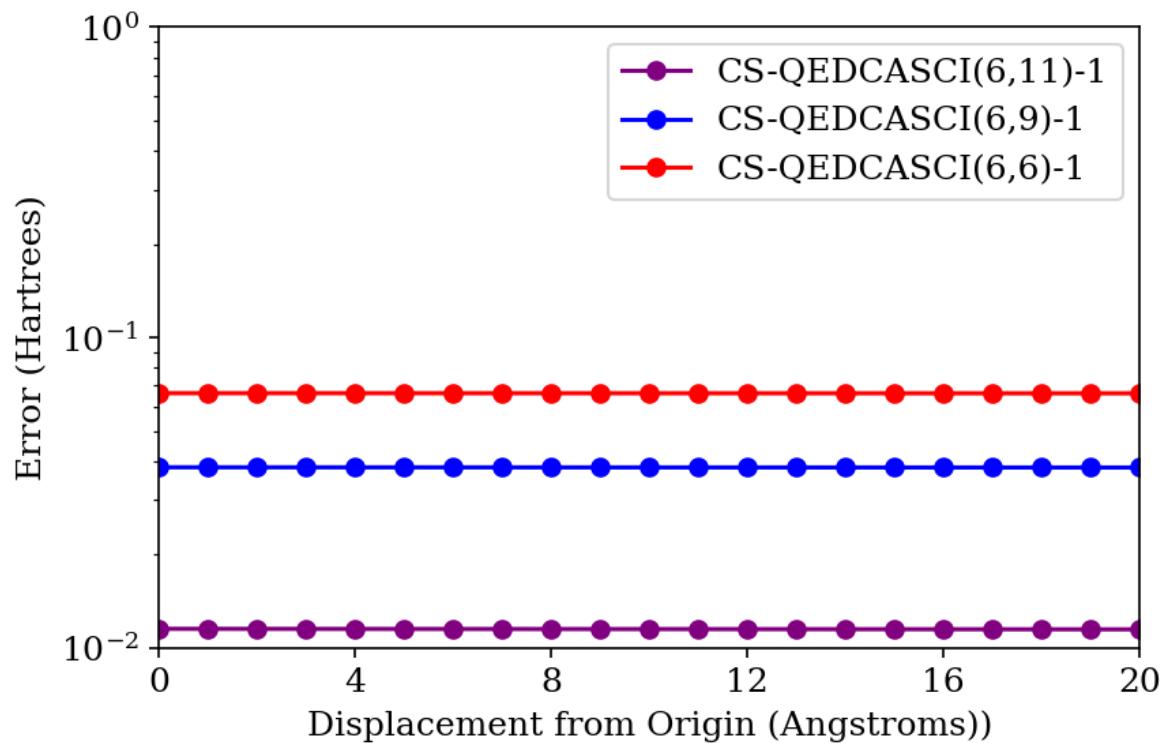
QED-FCI in Coherent State vs Photon Number State



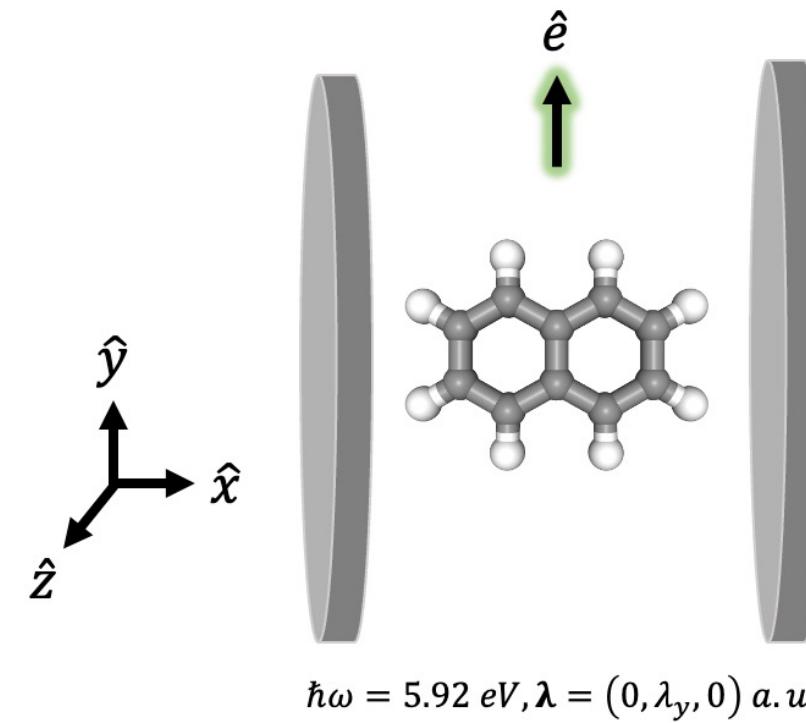
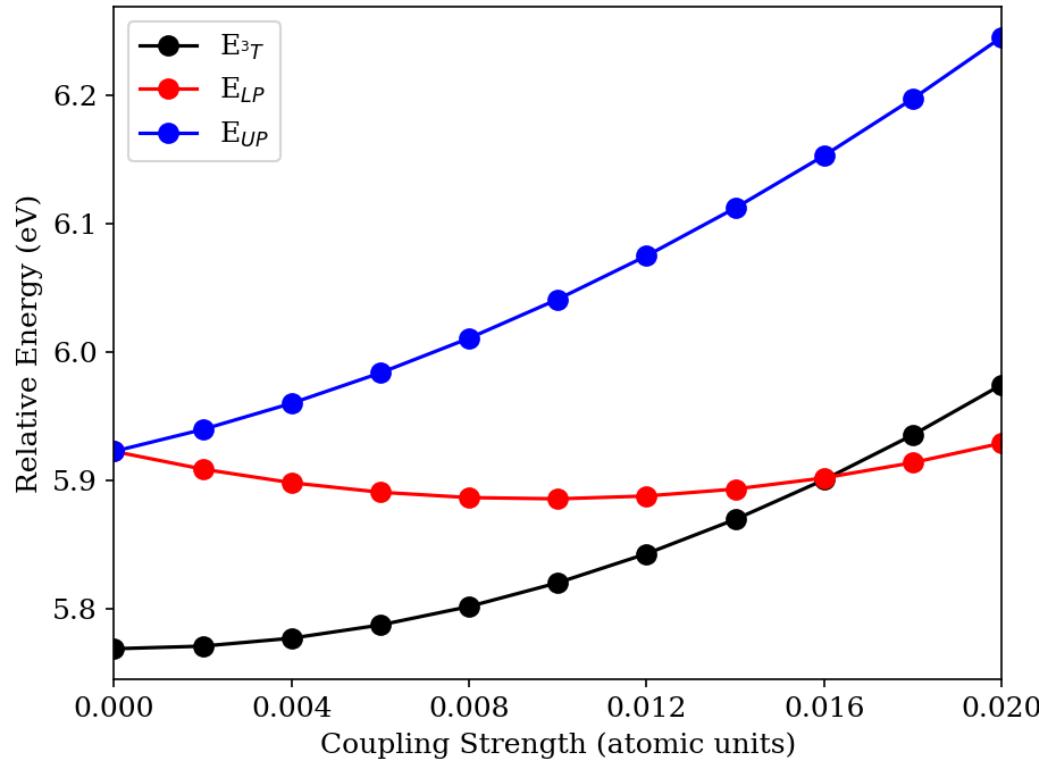
QED-CASCI in Coherent State vs Photon Number State



QED-FCI in Coherent State vs Photon Number State



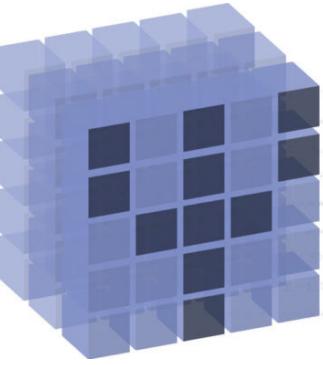
QED-FCI in Coherent-state vs Photon Number State basis



5 roots for a (12,12) active space with 100 photon states takes < 4 hours in our reference implementation!

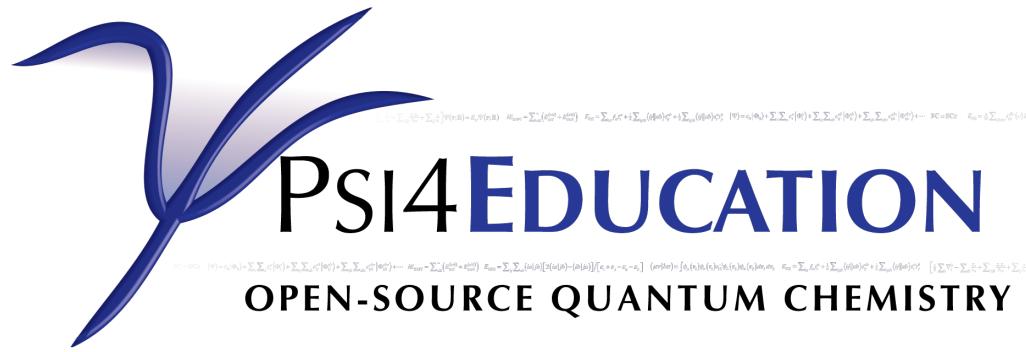


ExaChem



PSI4NUMPY

INTERACTIVE QUANTUM CHEMISTRY



- Reference implementations for QED-HF, QED-CIS-1 available in Psi4Numpy repo; QED-CIS Prism, QED-CASCI, QED-FCI available in group repos
- Psi4Education Module -> MolSSI-MAPOL-Charlotte Workshop
- Tutorials for QED-HF and QED-CIS Prism available
- Production implementations in EXACHEM coming soon
- High-order response, (non)adiabatic forces from automatic differentiation within 3 years

Nam Vu, Peyton Roden, Lane Tolley, Jay, Ruby Manderna

