

Then we just need to verify that $GF = EF$. From (2),

$$\begin{aligned}
 GF &= BC \cdot \frac{AH - EF}{AH} = \frac{BC}{AH} \cdot (AH - EF) \\
 &= \frac{BC}{AH} \cdot \left(AH - \frac{BC \cdot AH}{BC + AH} \right), \quad \text{from (1)} \\
 &= \frac{BC}{AH} \cdot \frac{AH^2}{BC + AH} \\
 &= \frac{BC \cdot AH}{BC + AH} = EF
 \end{aligned} \tag{3}$$

The construction logic is derived from the GF expression (1), assuming that $GF = FE$. The expression gives hint to construct the square $CJKI$.