Midterm

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Section I - True (T) or False (F) (20 Points)

- 1. False: Principal Component Regression is unsupervised learning.
- 2. **False:** Collinearity increases the errors associated with the coefficients, causing them to worsen.
- 3. False: R-squared of 0 means the model explains none of the variation in response Y, not -1.
- 4. **False:** If the number of predictors is > the number of observations, unique least squares coefficient estimate is eliminated.
- 5. True
- 6. True
- 7. True
- 8. True
- 9. False: OLS cannot be used.
- 10. False: Last name is Wang, first name is Min.

Section II - Free Response Questions (25 Points)

Problem 1 (Total: 15 Points)

Explain whether each scenario is a classification or regression problem, and indicate whether we are most interested in inference or prediction. Finally, provide n and p.

1a) We collect a set of data on the top 500 firms in the US. For each firm we record profit, number of employees, industry, and the CEO salary. We are interested in understanding which factors affect CEO salary. (5 Points)

Since CEO salary is a continuous variable, this is a **regression** problem. The focus is on **inference** because we want to understand the relationship between CEO salary and the other variables. The number of observations (**n**) is 500 (i.e., the top 500 firms) and the number of features (**p**) is 3 (i.e., profit, number of employees, and industry).

1b) We are considering launching a new product and wish to know whether it will be a success or a failure. We collect data on 20 similar products that were previously launched. For each product we have recorded whether it was a success or failure, price charged for the product, marketing budget, competition price, and ten other variables. (5 Points)

Since the outcome is a categorical variable, this is a **classification** problem. The focus is on **prediction** because we want to predict the outcome of a new product launch. The number of observations (\mathbf{n}) is 20 (i.e., 20 products) and the number of features (\mathbf{p}) is 13.

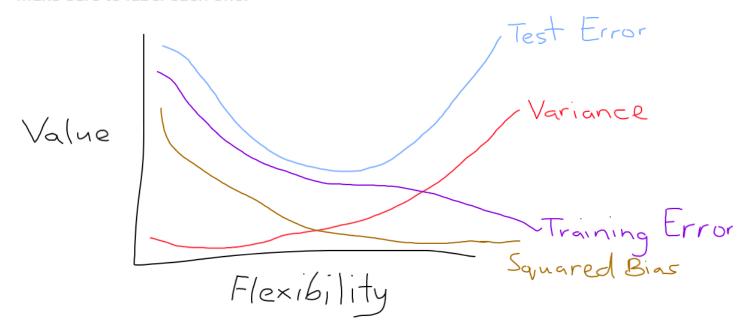
1c) We are interested in predicting the % change in the USD/Euro exchange rate in relation to the weekly changes in the world stock markets. Hence we collect weekly data for all of 2012. For each week we record the % change in the USD/Euro, the % change in the US market, the % change in the British market, and the % change in the German market. (5 Points)

Since the percentage change in the USD/Euro exchange rate is a continuous variable, this is a **regression** problem. The focus is on **prediction** because we want to predict future changes in the rate. The number of observations (\mathbf{n}) is 52 (i.e., 52 weeks of data) and the number of features (\mathbf{p}) is 3.

Problem 2 (Total: 10 Points)

In this class, we discussed the bias-variance trade-off. Answer the following questions.

2a) Provide a sketch of typical (squared) bias, variance, training error, test error curves, on a single plot, as we go from less flexible statistical learning methods towards more flexible approaches. The x-axis should represent the amount of flexibility in the method, and the y-axis should represent the values for each curve. There should be four curves. Make sure to label each one.



Statistical learning methods flexibility sketch

2b) Briefly explain why each of the four curves has the shape displayed in part (a).

Squared bias: Since more complex models can fit the training data better, this curve begins high and decreases as complexity increases. High squared bias means the model is too simple and underfitting the data, not identifying the underlying patterns.

Variance: Measures the difference between the model's predictions and actual values. Variance increases as the model becomes more complex due to random noise captured from the data, causing underfitting.

Training Error: Complex models fit the training data extremely well leading to lower training errors. As the model becomes simpler, the training error increases because simpler models cannot capture all of the data's complexity.

Test Error: The curve is U-shaped: starting high for simple models resulting from high bias, decreasing to a minimum, then increasing for models with high complexity due to higher variance.

Section III - Coding Questions (55 Points)

Problem 3 (Total: 18 Points - 3 points each)

This exercise involves the Auto data set studied in the lab. Make sure that the missing values have been removed from the data. We may start R and use these commands to load the data:

```
library(ISLR)
library(dplyr)
library(rlist)
library(ggplot2)
library(corrplot)
library(tidyr)
library(caret)
data('Auto')
str(Auto)
'data.frame': 392 obs. of 9 variables:
$ mpg
        : num 18 15 18 16 17 15 14 14 14 15 ...
$ displacement: num 307 350 318 304 302 429 454 440 455 390 ...
$ horsepower : num 130 165 150 150 140 198 220 215 225 190 ...
         : num 3504 3693 3436 3433 3449 ...
$ weight
$ acceleration: num 12 11.5 11 12 10.5 10 9 8.5 10 8.5 ...
$ year
          : num 70 70 70 70 70 70 70 70 70 ...
$ origin
            : num 111111111...
$ name
             : Factor w/ 304 levels "amc ambassador brougham",..: 49 36 231 14 161 141 54
223 241 2 ...
# Convert numeric to factor: cylinders & origin
Auto$cylinders <- as.factor(Auto$cylinders)</pre>
Auto$origin <- as.factor(Auto$origin)</pre>
# Verify updated data types
str(Auto)
'data.frame': 392 obs. of 9 variables:
$ mpg
            : num 18 15 18 16 17 15 14 14 14 15 ...
$ displacement: num 307 350 318 304 302 429 454 440 455 390 ...
$ horsepower : num 130 165 150 150 140 198 220 215 225 190 ...
          : num 3504 3693 3436 3433 3449 ...
$ weight
$ acceleration: num 12 11.5 11 12 10.5 10 9 8.5 10 8.5 ...
$ year
             : num 70 70 70 70 70 70 70 70 70 ...
           : Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 1 1 1 ...
$ origin
           : Factor w/ 304 levels "amc ambassador brougham",..: 49 36 231 14 161 141 54
$ name
223 241 2 ...
```

```
### Check for missing values
Auto_missing_values <- sum(
    is.na(
        Auto
        )</pre>
```

```
print(
    paste0(
        "Missing values: ",
        Auto_missing_values
    )
)
```

[1] "Missing values: 0"

3a) Which of the predictors are quantitative, and which are qualitative?

```
# Quantitative predictors
quant_preds <- colnames(
    select_if(
        Auto,
        is.numeric
    )
)

# Qualitative predictors
qual_preds <- colnames(
    select_if(
        Auto,
        is.factor
    )
)</pre>
```

```
cat(
   "Quantitative predictor(s): ",
   paste0(
      quant_preds
   ),
   sep = "\n"
)
```

```
Quantitative predictor(s):
mpg
displacement
horsepower
weight
acceleration
year
```

```
cat(
    'Qualititative predictor(s): ',
    paste0(
        qual_preds
    ),
    sep = "\n"
)
```

```
Qualititative predictor(s):
cylinders
origin
name
```

```
# Create key values for dictionary for pretty printing
quant_preds_list <- list(</pre>
    colnames(
        select_if(
            Auto,
             is.numeric
        )
    )
)
quant_preds_keys <- c()
colon <- ": "
for (pred in quant_preds_list) {
    new_pred = paste(
        pred,
        colon,
        sep = ""
    quant_preds_keys = append(
        quant_preds_keys,
        new_pred
    )
}
names(quant_preds) <- cat(quant_preds_keys)</pre>
```

mpg: displacement: horsepower: weight: acceleration: year:

3b) What is the range of each quantitative predictor? You can answer this using the range() function.

```
quant_preds_range <- sapply(
    Auto[, quant_preds],
    range
)
cat(
    'Quantitative predictor ranges:',
    paste0(
        quant_preds_keys,
        quant_preds_range[1,],
        " _ ",
        quant_preds_range[2,]
    ),
    sep = "\n"
)</pre>
```

```
Quantitative predictor ranges:
mpg: 9 - 46.6
displacement: 68 - 455
horsepower: 46 - 230
```

```
weight: 1613 - 5140
acceleration: 8 - 24.8
year: 70 - 82
```

3c) What is the mean and standard deviation of each quantitative predictor?

```
quant_preds_mean <- round(</pre>
    sapply(
        Auto[, quant_preds],
    ),
    2
)
quant_preds_sd <- round(</pre>
    sapply(
        Auto[, quant_preds],
    ),
)
cat(
    'Quantitative predictor means:',
    paste0(
        quant_preds_keys,
        quant_preds_mean
    ),
    sep = "\n"
)
```

```
displacement: 194.41
horsepower: 104.47
weight: 2977.58
acceleration: 15.54
year: 75.98

cat(
    'Quantitative predictor standard deviations:',
    paste0(
        quant_preds_keys,
        quant_preds_sd
    ),
    sep = "\n"
)
```

```
Quantitative predictor standard deviations: mpg: 7.81 displacement: 104.64 horsepower: 38.49 weight: 849.4 acceleration: 2.76 year: 3.68
```

Quantitative predictor means:

mpg: 23.45

3d) Now remove the 20th through 80th observations. What is the range, mean, and standard deviation of each predictor in the subset of the data that remains?

```
# Create subset dataset, removing 20th through 80th observations
subset_Auto \leftarrow Auto[-c(20:80), ]
# Calucate new range
range_Auto_subset <- sapply(</pre>
    subset_Auto[, quant_preds],
    range
)
# Calucate new mean
mean_Auto_subset <- round(</pre>
    sapply(
    subset_Auto[, quant_preds],
    mean
    ),
)
# Calucate new standard deviation
sd_Auto_subset <- round(</pre>
    sapply(
    subset_Auto[, quant_preds],
    sd
    ),
)
```

```
cat(
    'Quantitative predictor subset ranges:',
    paste0(
        quant_preds_keys,
        range_Auto_subset[1,],
        " - ",
        range_Auto_subset[2,]
    ),
    sep = "\n"
)
```

```
displacement: 68 - 455
horsepower: 46 - 230
weight: 1649 - 4997
acceleration: 8 - 24.8
year: 70 - 82

cat(
    'Quantitative predictor subset means:',
    paste0(
        quant_preds_keys,
```

Quantitative predictor subset ranges:

mpg: 11 - 46.6

```
mean_Auto_subset
),
sep = "\n"
)
```

Quantitative predictor subset means:

mpg: 24.22

displacement: 189.44 horsepower: 101.86 weight: 2935.02 acceleration: 15.61

year: 76.85

```
cat(
    'Quantitative predictor subset standard deviations:',
    paste0(
        quant_preds_keys,
        sd_Auto_subset
    ),
    sep = "\n"
)
```

Quantitative predictor subset standard deviations:

mpg: 7.82

displacement: 101.76 horsepower: 36.6 weight: 805.48 acceleration: 2.76

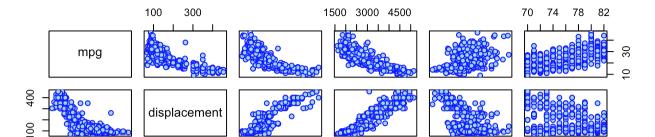
year: 3.32

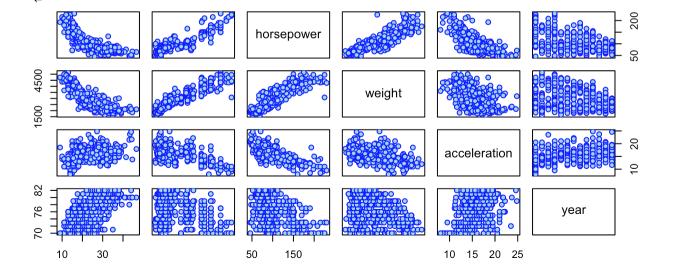
3e) Using the full data set, investigate the predictors graphically, using scatterplots or other tools of your choice. Create some plots highlighting the relationships among the predictors. Comment on your findings.

Scatterplot Correlation

```
plot(~mpg+displacement+horsepower+weight+acceleration+year,
    data=Auto,
    main="Investigate Potential Variable Correlation",
    col='blue',
    bg='lightblue',
    pch = 21)
```

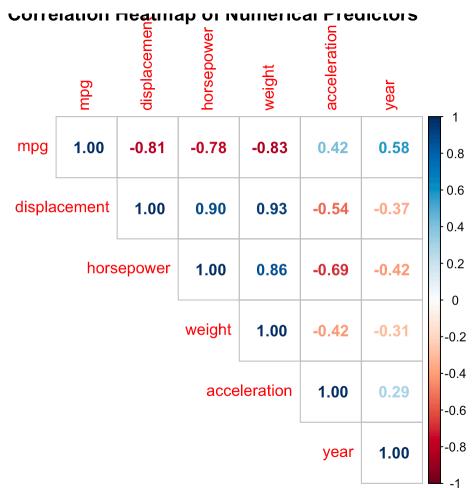
Investigate Potential Variable Correlation





Heatmap Correlation

```
Auto %>%
  select_if(is.numeric) %>%
  cor() %>%
  corrplot(
    method = "number",
    title = 'Correlation Heatmap of Numerical Predictors',
    type = 'upper')
```

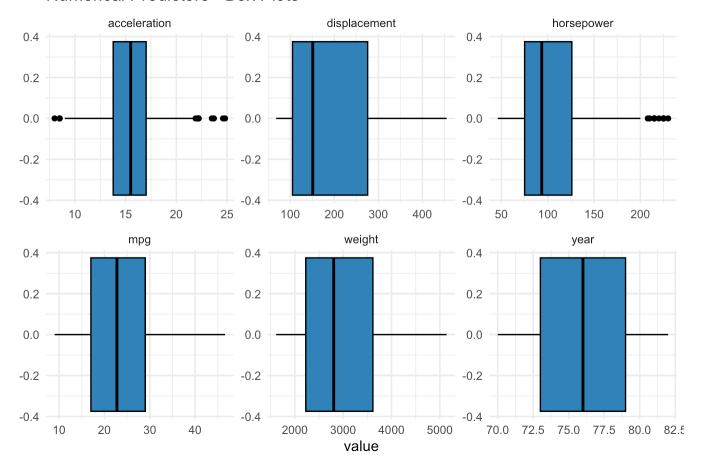


Day Dlate

DOX PIOU

```
Auto %>%
  select_if(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  geom_boxplot(color='black', fill='steelblue') +
  facet_wrap(~key, scales = 'free') +
  ggtitle(("Numerical Predictors - Box Plots")) +
  theme_minimal()
```

Numerical Predictors - Box Plots

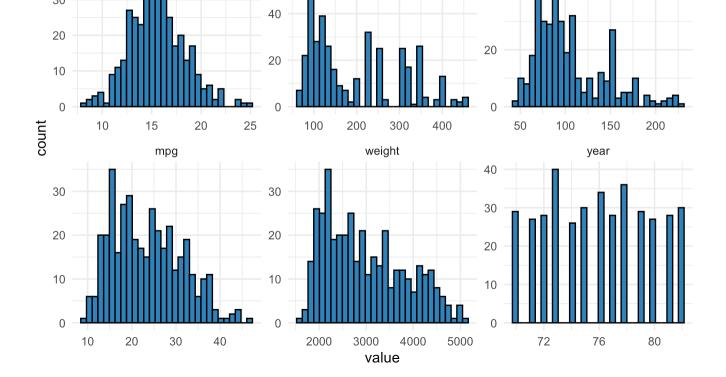


Histogram Plots

```
Auto %>%
  select_if(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
  geom_histogram(color='black', fill='steelblue') +
  facet_wrap(~key, scales = 'free') +
  ggtitle(("Numerical Predictors - Histograms")) +
  theme_minimal()
```

Numerical Predictors - Histograms





Comments on predictor relationships: Based on our scatterplots and heatmap, mpg has a strong negative relationship with displacement, horsepower, and weight as well as a moderate positive relationship with year. Horsepower has a moderately strong negative relationship with acceleration, and a strong positive relationship with weight. Displacement has a strong positive relationship with horsepower and weight, and a moderate negative relationship with acceleration.

3f) Suppose that we wish to predict gas mileage (mpg) on the basis of the other variables. Do your plots suggest that any of the other variables might be useful in predicting mpg? Justify your answer.

The correlation coefficients for variables displacement, horsepower, and weight are -0.81, -0.78, and -0.83, respectively. Since the magnitudes of these coefficients fall between the range -0.9 and -0.7, these variables have a strong negative correlation with mpg: - As engine displacement (inches) increases, the car gets less mpg. - As horsepower increases, mpg decreases. - As vehicle weight increases (lbs), mpg decreases. Additionally, mpg has a moderate positive correlation (coeff = 0.58) with the model year of the vehicle, indicating that newer cars get better gas mileage. Considering our observations, these four variables might serve as useful predictors for building a model to predict mpg.

Problem 4 (Total: 15 Points)

We will predict the number of applications received using the other variables in the College data set available in the R package ISLR, which can be accessed as follows.

```
library(ISLR)
library(e1071)
library(nnet)
library(earth)
data(College)
#data basic information
head(College)
```

Abilene Christian University	Yes	1660	1232	721		23	52
Adelphi University	Yes	2186	1924	512		16	29
Adrian College	Yes	1428	1097	336		22	50
Agnes Scott College	Yes	417	349	137		60	89
Alaska Pacific University	Yes	193	146	55		16	44
Albertson College	Yes	587	479	158		38	62
	F.Under	grad F	P.Underg	rad Ou	tstate	Room.Board	Books
Abilene Christian University	2	2885		537	7440	3300	450
Adelphi University	2	2683	1	227	12280	6450	750
Adrian College	-	1036		99	11250	3750	400
Agnes Scott College		510		63	12960	5450	450
Alaska Pacific University		249		869	7560	4120	800
Albertson College		678		41	13500	3335	500
	Persona	l PhD	Termina	l S.F.	Ratio	perc.alumni	Expend
Abilene Christian University	2200	70	7	8	18.1	12	7041
Adelphi University	1500	29	3	0	12.2	16	10527
Adrian College	1165	5 53	6	6	12.9	30	8735
Agnes Scott College	875	5 92	9	7	7.7	37	19016
Alaska Pacific University	1500	76	7	2	11.9	2	10922
Albertson College	675	5 67	7	3	9.4	11	9727
	Grad.Rat	te					
Abilene Christian University	(50					
Adelphi University		56					
Adrian College		54					
Agnes Scott College		59					
Alaska Pacific University	1	15					
Albertson College	į	55					

dim(College)

[1] 777 18

The column Apps is the response variable, and others may be treated as predictors. #For instance, for linear regression model in R, you may use $lm(Apps\sim.,data=College)$

Call:

lm(formula = Apps ~ ., data = College)

Coefficients:

Top25perc	Top10perc	Enroll	Accept	PrivateYes	(Intercept)
-14.23448	49.92628	-0.88069	1.58581	-494.14897	-445.08413
Personal	Books	Room.Board	Outstate	P.Undergrad	F.Undergrad
0.03110	0.02090	0.15103	-0.08587	0.04445	0.05739
Grad.Rate	Expend	perc.alumni	S.F.Ratio	Terminal	PhD
8.66763	0.07790	0.17867	15.38961	-3.33066	-8.67850

4a) Appropriately split the data set into a training set (80%) and a test set (20%). [3 points]

Split the data
set.seed(123)

```
train_index <- createDataPartition(College$Apps, p = 0.8, list = FALSE)
train_data <- College[train_index, ]
test_data <- College[-train_index, ]</pre>
```

4b) Fit a support vector machine (SVM) model with the radial basis function function model using least squares on the training set. Clearly report the test error obtained. [3 points]

```
# Fit SVM-RBF model
svm_mod <- svm(Apps ~ ., train_data, kernel = "radial")

# Predict test data
svm_preds <- predict(svm_mod, test_data)

# Calcuate MSE (Mean Squared Error)
svm_mse <- round(mean((svm_preds - test_data$Apps)^2),2)
cat("SVM MSE:", paste0(svm_mse))</pre>
```

SVM MSE: 622415.53

4c) Fit a neural network model on the training set by creating an appropriate grid for tuning parameters. Clearly report the test error obtained. [3 points]

```
# Neural network tuning grid
grid_neural_network <- expand.grid(size = c(5, 10), decay = c(0.1, 0.5))
# Fit neural network model
set.seed(123)
model_neural_network <- train(</pre>
  Apps ~ .,
  data = train_data,
  method = "nnet",
  trControl = trainControl(method = "cv", number = 5),
 tuneGrid = grid_neural_network,
  trace = FALSE
)
# Predict test data
preds_neural_network <- predict(model_neural_network, test_data)</pre>
# Calculate the MSE
neural_network_mse <- round(mean((preds_neural_network - test_data$Apps)^2),2)</pre>
cat("Neural Network MSE:", paste0(neural_network_mse))
```

Neural Network MSE: 14683008.9

4d) Fit a Multivariate Adaptive Regression Splines (MARS) model on the training set with tuning parameters chosen by cross-validation. Clearly report the test error obtained, along with the importance of each predictor. estimates. [3 points]

```
# Fit MARS model with cross-validation
set.seed(123)
```

```
mars_mod <- train(
   Apps ~ .,
   data = train_data,
   method = "earth",
   trControl = trainControl(method = "cv", number = 5),
   tuneLength = 5
)

# Predict test data
mars_preds <- predict(mars_mod, test_data)

# Calculate the MSE
mars_mse <- round(mean((mars_preds - test_data$Apps)^2),2)
cat('MARS MSE:', paste0(mars_mse))</pre>
```

MARS MSE: 822261.73

```
# Variable importance
variable_importance <- varImp(mars_mod)
variable_importance</pre>
```

earth variable importance

Overall
Accept 100.000
Top10perc 16.090
Enroll 3.688
F.Undergrad 0.000

4e) Comment on the results obtained. Is there much difference among the test errors resulting from these three nonparametric approaches? [3 points]

SVM Results

```
call:
svm(formula = Apps ~ ., data = train_data, kernel = "radial")

Parameters:
    SVM-Type: eps-regression
SVM-Kernel: radial
    cost: 1
    gamma: 0.05555556
    epsilon: 0.1
```

Number of Support Vectors: 278

```
cat("SVM MSE: ", svm_mse)
```

SVM MSE: 622415.5

Neural Network Results

```
model_neural_network
```

Neural Network

624 samples17 predictor

No pre-processing

Resampling: Cross-Validated (5 fold)

Summary of sample sizes: 499, 500, 497, 500, 500 Resampling results across tuning parameters:

size	decay	RMSE	Rsquared	MAE
5	0.1	5069.826	0.0005407588	3091.989
5	0.5	5069.826	NaN	3091.989
10	0.1	5069.826	0.0706531705	3091.989
10	0.5	5069.826	0.0893022018	3091.989

RMSE was used to select the optimal model using the smallest value. The final values used for the model were size = 5 and decay = 0.5.

```
cat("Neural Network MSE: ", neural_network_mse)
```

Neural Network MSE: 14683009

MARS Results

mars_mod

Multivariate Adaptive Regression Spline

624 samples 17 predictor

No pre-processing

Resampling: Cross-Validated (5 fold)

Summary of sample sizes: 499, 500, 497, 500, 500

Resampling results across tuning parameters:

nprune RMSE Rsquared MAE

nprune	RMSE	Rsquared	MAE
2	1594.315	0.8500763	699.0368
4	1270.057	0.9178074	548.5028
6	1251.483	0.9218557	557.1920
8	1286.650	0.9170281	597.1205
10	1311.021	0.9134643	608.1759

Tuning parameter 'degree' was held constant at a value of 1 RMSE was used to select the optimal model using the smallest value.

The final values used for the model were nprune = 6 and degree = 1.

```
cat("MARS MSE: ", mars_mse)
```

MARS MSE: 822261.7

Conclusion: There is much difference among the test errors resulting from these three nonparametric approaches. The neural network approach calculated the largest test error. Additionally, it did not calculate decent R-squared values. The MARS model had the second highest test error, but the model produced R-squared values greater than 85%, indicating that it explains the variance of the data well. The support vector machine with the radial basis function calculated the lowest test error.

Problem 5 (Total: 22 Points)

A chemical manufacturing process for a pharmaceutical product was discussed in Sect.
1.4 of the textbook. In this problem, the objective is to understand the relationship between biological measurements of the raw materials (predictors), measurements of the manufacturing process (predictors), and the response of product yield. Biological predictors cannot be changed but can be used to assess the quality of the raw material before processing. On the other hand, manufacturing process predictors can be changed in the manufacturing process. Improving product yield by 1% will boost revenue by approximately one hundred thousand dollars per batch. We may start R and use these commands to load the data:

```
library(AppliedPredictiveModeling)
library(ggplot2)
library(dplyr)
library(caret)
library(e1071)
data("ChemicalManufacturingProcess")
```

The matrix processPredictors contains the 57 predictors (12 describing the input biological material and 45 describing the process predictors) for the 176 manufacturing runs, yield contains the percent yield for each run.

5a) A small percentage of cells in the predictor set contain missing values. Use an appropriate imputation function to fill in these missing values. [3 points]

```
# Identify missing values
missing_vals <- sum(is.na(ChemicalManufacturingProcess))
print(paste0("Pre-imputation missing values: ", missing_vals))</pre>
```

[1] "Pre-imputation missing values: 106"

```
# Impute missing values with k-NN
pre_process <- preProcess(ChemicalManufacturingProcess, c("knnImpute"))
df <- predict(pre_process, ChemicalManufacturingProcess)

# Double check successful imputation (i.e., 0 missing values)
impute miss <- sum(is na(pre process))</pre>
```

```
print(paste0("Post-imputation missing values: ", impute_miss))
```

- [1] "Post-imputation missing values: 0"
- 5b) Split the data into a training and a test set, pre-process the data, and build at least four different models from Chapter 6. For those models with tuning parameters (e.g., ENET), what are the optimal values of the tuning parameter(s)? [8 points]

```
# Create variables to separate predictors and response
proc_preds <- df[, -1]</pre>
resp <- df[, 1]
# Split the data
train_index <- createDataPartition(resp, p = 0.8, list = FALSE)</pre>
train_data <- proc_preds[train_index, ]</pre>
train_resp <- resp[train_index]</pre>
test_data <- proc_preds[-train_index, ]</pre>
test_resp <- resp[-train_index]</pre>
# Data normalization - center and scale
pre_process_range <- preProcess(train_data, method = c("center", "scale"))</pre>
train_transformed <- predict(pre_process_range, train_data)</pre>
test_transformed <- predict(pre_process_range, test_data)</pre>
# Create list for model training
models <- list(</pre>
  ENET = trainControl(method = "cv", number = 5),
  Ridge = trainControl(method = "cv", number = 5),
  PCR = trainControl(method = "cv", number = 5),
  PLS = trainControl(method = "cv", number = 5)
)
# Tuning grids
tuning_grids <- list(</pre>
  ENET = expand.grid(alpha = seq(0, 1, length = 10), lambda = 10^seq(4, -4, length = 100)),
  Ridge = expand.grid(alpha = 0, lambda = 10^s eq(4, -4, length = <math>100)),
  PLS = expand.grid(ncomp = 1:10)
)
# Train the four models
set.seed(123)
enet_mod <- train(train_transformed, train_resp, method = "glmnet", trControl = models$ENET,</pre>
ridge_mod <- train(train_transformed, train_resp, method = "glmnet", trControl = models$Ridge</pre>
pls_mod <- train(train_transformed, train_resp, method = "pls", trControl = models$PLS, tuneG</pre>
pcr_mod <- train(train_transformed, train_resp, method = "pcr", trControl = models$PCR, tuneG</pre>
# Optimal tuning parameters
enet_mod$bestTune
```

```
alpha lambda
940 1 0.1417474
```

ridge mod\$bestTune

```
alpha lambda
59 0 4.862602

pls_mod$bestTune

ncomp
3 3

pcr_mod$bestTune

ncomp
10 10

5c) Which model has the best predictive ability? Is any model significantly better or worse than the others? You need to conduct a hypothesis testing to justify your choice if necessary. [5 points]
```

```
# Predict test set
enet_preds <- predict(enet_mod, test_transformed)
ridge_preds <- predict(ridge_mod, test_transformed)
pls_preds <- predict(pls_mod, test_transformed)
pcr_preds <- predict(pcr_mod, test_transformed)

# Calculate MSE (Mean Squared Error)
test_err_enet <- mean((enet_preds - test_resp)^2)
test_err_ridge <- mean((ridge_preds - test_resp)^2)
test_err_pls <- mean((pls_preds - test_resp)^2)
test_err_pcr <- mean((pcr_preds - test_resp)^2)
# Print MSE
cat("ENET Test Error: ", test_err_enet)</pre>
```

ENET Test Error: 0.4927384

```
cat("Ridge Test Error: ", test_err_ridge)
```

Ridge Test Error: 0.6256541

```
cat("PLS Test Error: ", test_err_pls)
```

PLS Test Error: 0.3802276

```
cat("PCR Test Error: ", test_err_pcr)
```

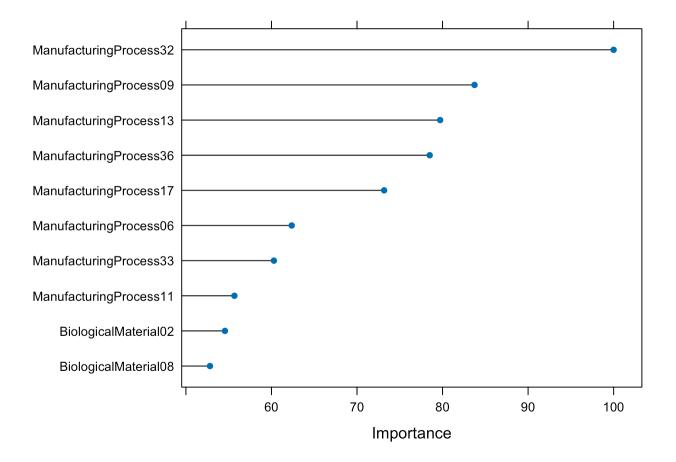
PCR Test Error: 0.4212739

Since our PLS model has the lowest test error, it has the best predictive ability among our four models.

5d) Which predictors are most important in the model you have trained? Do either the

biological of process predictors dominate the list is points.

```
# Variable Importance - PLS
variable_importance <- varImp(pls_mod)
plot(variable_importance, top = 10)</pre>
```



top_preds <- rownames(variable_importance\$importance)[order(variable_importance\$importance[,1
cat("Top 10 predictors: ", paste0(top_preds), sep = "\n")</pre>

Top 10 predictors:

ManufacturingProcess32

ManufacturingProcess09

ManufacturingProcess13

ManufacturingProcess36

ManufacturingProcess17

ManufacturingProcess06

ManufacturingProcess33

ManufacturingProcess11

BiologicalMaterial02

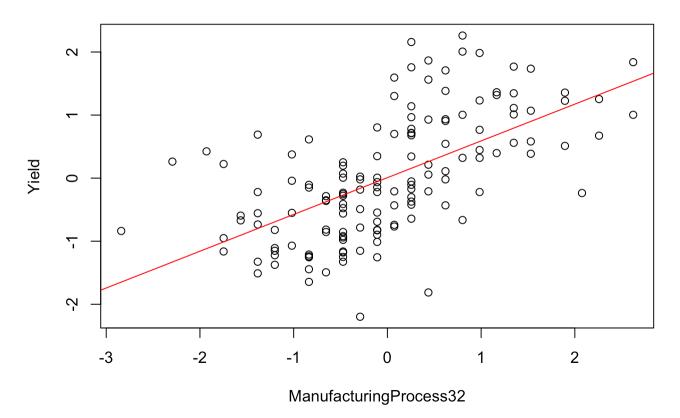
BiologicalMaterial08

The top 10 predictors (listed above) are all process predictors.

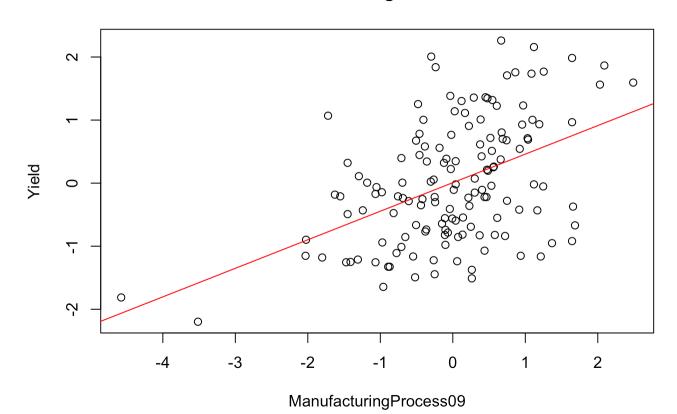
5e) Explore the relationships between each of the top predictors and the response. How could this information be helpful in improving yield in future runs of the manufacturing process? [3 points]

```
for (pred in top_preds) {
  plot(train_transformed[, pred], train_resp, main = pred, xlab = pred, ylab = "Yield")
  abline(lm(train_resp ~ train_transformed[, pred]), col = "red")
}
```

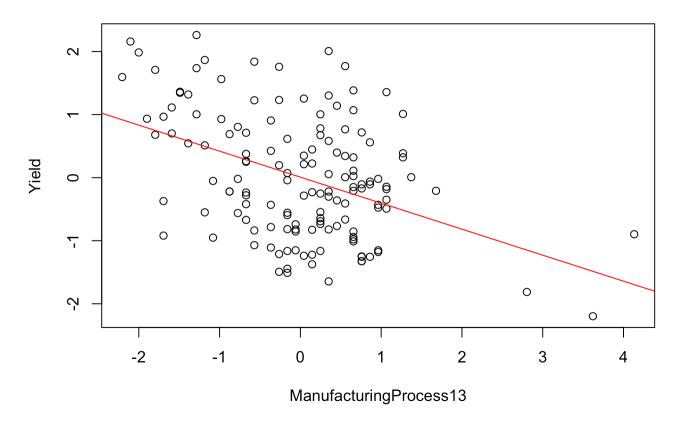
ManufacturingProcess32



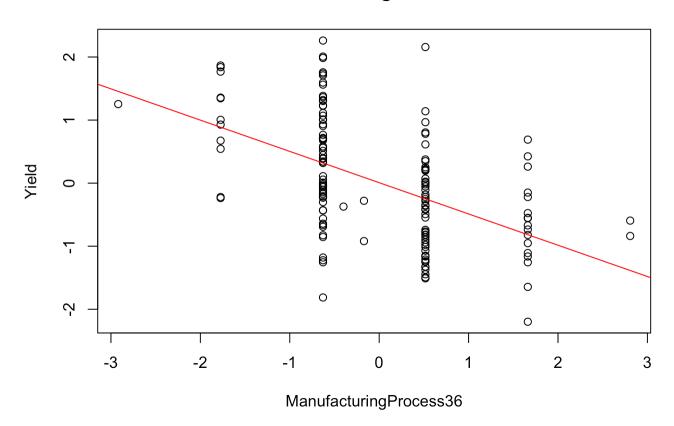
ManufacturingProcess09



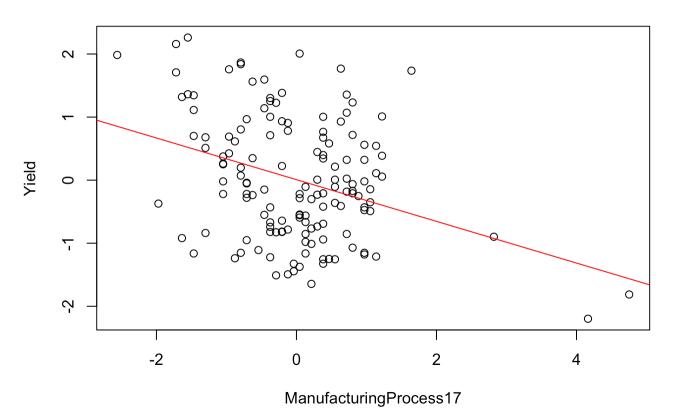
ManufacturingProcess13



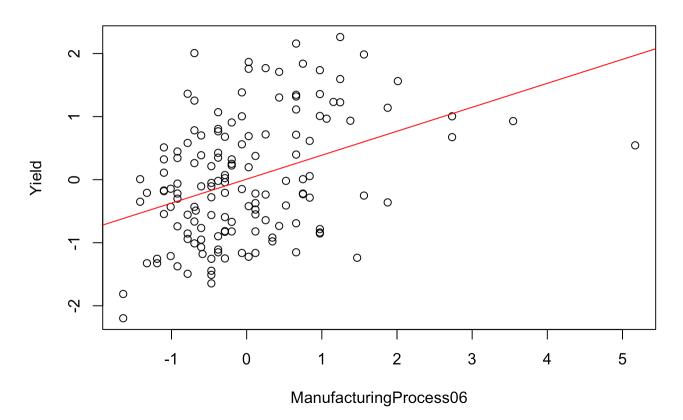
ManufacturingProcess36



ManufacturingProcess1/



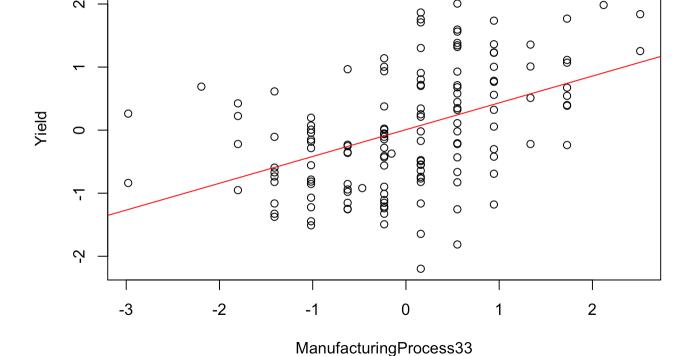
ManufacturingProcess06



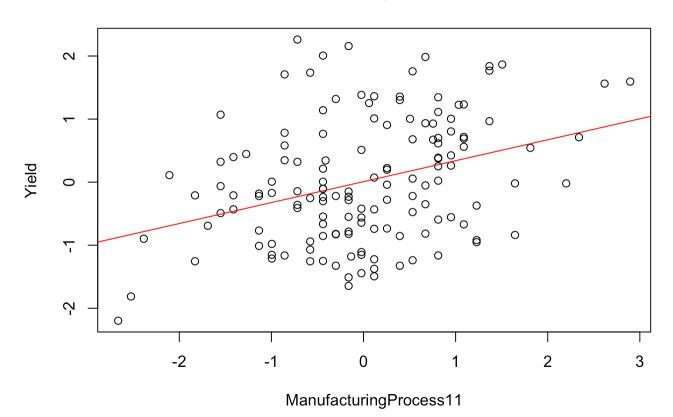
ManufacturingProcess33

0

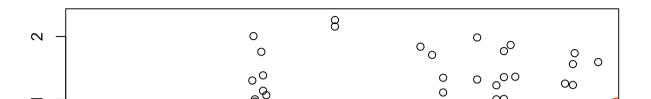
0

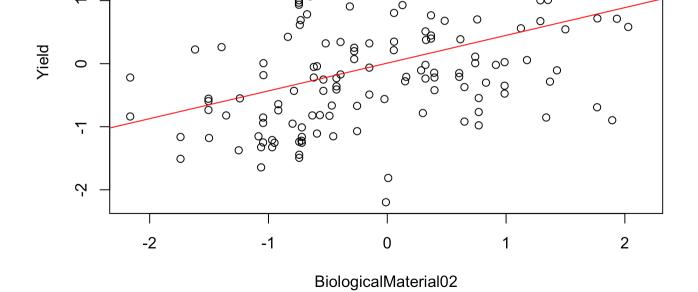


ManufacturingProcess11

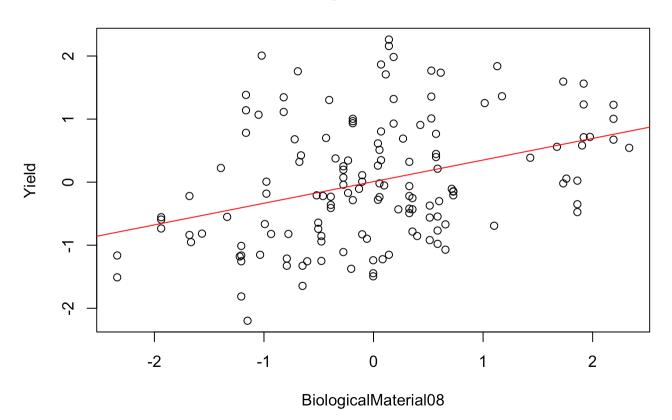


BiologicalMaterial02





BiologicalMaterial08



The relationships between our top predictors and the response variable (Yield) indicate that the process predictors are pretty evenly split between positive and negative linear relationships. By identifying these relationships between individual predictors and the response variable, the manufacturers have the opportunity to optimize their processes and potentially increase Yield.