

MASARYK UNIVERSITY  
FACULTY OF INFORMATICS



**«title»**

BACHELOR'S THESIS

**«author»**

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## **Declaration**

Hereby I declare that this paper is my original authorial work, which I have worked out on my own. All sources, references, and literature used or excerpted during elaboration of this work are properly cited and listed in complete reference to the due source.

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# **Abstract**

«abstract»

## Keywords

«keywords»





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# **1 Introduction**





## 2 Preliminaries

### 2.1 Büchi Automaton

A nondeterministic Büchi automaton (BA) is a tuple  $A = (\Sigma, Q, q_0, \Delta, \Gamma)$ , where

- $\Sigma$  is a finite alphabet
- $Q$  is finite set of states
- $q_0 \in Q$  is the initial state
- $\Delta \subseteq Q \times \Sigma \times Q$  are transitions
- $\Gamma \subseteq \Delta$  is the transition-based acceptance condition

**run** A run  $r$  of  $A$  on  $w \in \Sigma^\omega$  is an  $\omega$ -word  $r_0, w_0, r_1, w_1, \dots$  in  $(Q \times \Sigma)^\omega$  such that  $r_0 = q_0 \wedge \forall i > 0, (r_{i-1}, w_{i-1}, r_i) \in \Delta$  and  $w_i = w_i$ .

**inf(r)** We write  $\text{inf}(r) \subseteq \Delta$  for the set of transitions that appear infinitely often in the run  $r$ .

**accepting run** A run  $r$  is accepting if  $\text{inf}(r) \cap \Gamma \neq \emptyset$

**language** The language  $L_A \subseteq \Sigma^\omega$  is recognized by  $A$ .  
 $\forall w \in L_A \exists r$  on  $w$  such that  $r$  is accepting.

**$\omega$ -regular language** A language is  $\omega$ -regular if it is accepted by BA.

**deterministic automaton**  $A = (\Sigma, Q, q_0, \Delta, \Gamma)$  is deterministic if  
 $(q, \rho, q'), (q, \rho, q'') \in \Delta \implies q' = q''$

**complete automaton**  $A$  is complete if,  $\forall w \in \Sigma, \forall q \in Q, \exists (q, w, q') \in \Delta$ . A word in  $\Sigma^\omega$  has exactly one run in a deterministic, complete automaton.

## 2.2 Markov Decision Processes

A Markov decision process (MDP)  $M$  is a tuple  $(S, A, T, \Sigma, L)$ , where

- $S$  is a finite set of states
- $A$  is a finite set of actions
- $T : S \times A \rightarrow D(S)$ , where  $D(S)$  is set of probability distributions over  $S$ , is the probabilistic transition (partial) function
- $\Sigma$  is an alphabet
- $L : S \times A \times S \rightarrow \Sigma$  is the labeling function of the set of transitions. For a state  $s \in S$ ,  $A(s)$  denotes the set of actions available in  $s$ .

**run** A run of  $M$  is an  $\omega$ -word  $s_0, a_1, \dots \in A = S \times (A \times S)^\omega$  such that  $Pr(s_{i+1} | s_i, a_{i+1}) > 0$  for all  $i \geq 0$ . A finite run is a finite such sequence.

**labeled run** We define labeled run as  $L(r) = L(s_0, a_1, s_1), L(s_1, a_2, s_2), \dots \in \Sigma^\omega$ .

## 2.3 to be defined

$\omega$ -word?,

### 2.3.1 xd

'' GF MDP, model checking

## 2.4 Algorithms

BP + both slim

## **3 Implementation**

### **3.1 Technologies**

### **3.2 Implementation inside Seminotor**



## **4 Evaluation**

### **4.1 Alternative Algorithm**

### **4.2 Different Implementation - ePMC**

### **4.3 Semi-deterministic Automata**



## 5 Conclusion