

# A Structured Framework for Adaptively Incorporating External Evidence in Sequentially Monitored Clinical Trials

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- We present a structured framework for specifying monitoring priors and stoppage criteria for a Bayesian sequentially monitored clinical trial that is based on intuitive justification for the design quantities rather than being motivated by having pre-specified frequentist operating characteristics.

# Enthusiastic Monitoring Prior

- Consider again the hypotheses  $H_0 : \theta \leq \theta_0$  versus  $H_1 : \theta > \theta_0$  where  $\theta_0$  represents a treatment effect of interest and let  $\theta_1 > \theta_0$  represent a plausible, clinically meaningful effect.
- Define an enthusiastic prior, denoted as  $\pi_E(\theta)$ , as a prior consistent with  $\theta_1$  being the most likely value of  $\theta$  (i.e., the prior mode) and that reflects the belief of an observer who is *all but convinced* that  $H_1$  is true a priori.
- Formally, this is defined as satisfying (i)  $\operatorname{argmax}_{\theta} \pi_E(\theta) = \theta_1$  and (ii)  $P_E(\theta > \theta_0) = 1 - \epsilon$ , where the subscript  $E$  indicates that the probability is based on  $\pi_E(\theta)$ .

# Skeptical Monitoring Prior

- Similarly, define a skeptical prior, denoted as  $\pi_S(\theta)$ , as a prior consistent with  $\theta_0$  being the most likely value of  $\theta$  and that reflects the belief of an observer who is *all but convinced* that  $\theta < \theta_1$  is true a priori.
- Formally, this is defined as the prior  $\pi_S(\theta)$  satisfying (iii)  $\operatorname{argmax}_{\theta} \pi_S(\theta) = \theta_0$  and (iv)  $P_S(\theta < \theta_1) = 1 - \epsilon$ . In what follows we refer to (i) and (iii) as *mode value constraints* and (ii) and (iv) as *tail-probability constraints*, respectively.

# Generalized Normal Distribution

- The density for a generalized normal distribution  $\mathcal{GN}(\mu, \alpha, \beta)$  is

$$f(\theta) = \frac{\beta}{2\alpha\Gamma(1/\beta)} \exp \left\{ - \left( \frac{|\theta - \mu|}{\alpha} \right)^\beta \right\}$$

where  $\mu$  is a location parameter,  $\alpha > 0$  is a scale parameter, and  $\beta > 0$  is a shape parameter.

- A monitoring prior in the generalized normal family of distributions can have density at the mode equal to  $k \times \frac{1}{\sqrt{2\pi}\sigma}$ , with  $k < 1$  indicating a more flattened distribution and  $k > 1$  indicating a more peaked distribution at the mode, relative to the default normal distribution.

# Skeptical Monitoring Prior

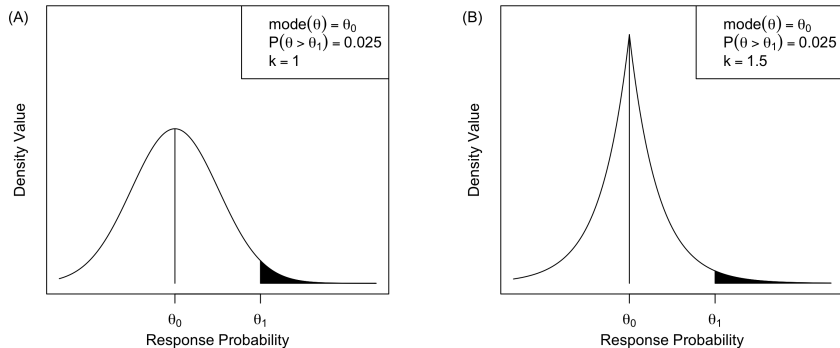


Figure: A, Default skeptical prior. B, Concentrated skeptical prior.

# Enthusiastic Monitoring Prior

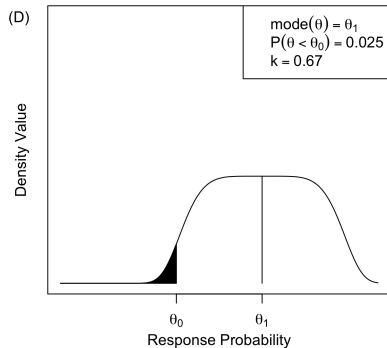
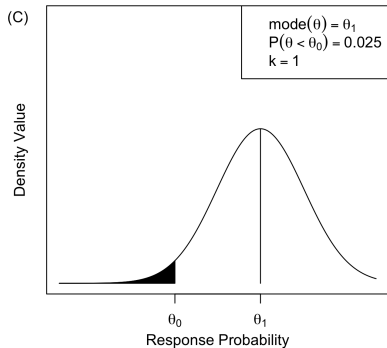


Figure: C, Default enthusiastic prior. D, Flattened enthusiastic prior.

# Box's $p$ -value

The prior-predictive distribution for data  $D$  (also called the marginal likelihood) reflects the probability of observing  $D$  given the assumed prior distribution for  $\theta$  and is defined formally as

$$p(D) = \int p(D|\theta)\pi(\theta)d\theta. \quad (1)$$

Let  $D_{\text{obs}}$  be the observed data at some point in time in an ongoing trial. *Box's  $p$ -value* is defined as the following:

$$\psi(D_{\text{obs}}) = \int p(D)1[p(D) \leq p(D_{\text{obs}})]d(D) \quad (2)$$

where  $1[A]$  is an indicator that the event  $A$  is true.



# Adaptive Monitoring Prior

- We define the *adaptive monitoring prior* for efficacy evaluations as the mixture distribution

$$\pi_{AE}(\theta) = \omega \cdot \pi_E(\theta) + (1 - \omega) \cdot \pi_S(\theta) \quad (3)$$

- Define the mixing weight  $\omega$  given to the *enthusiastic* prior as

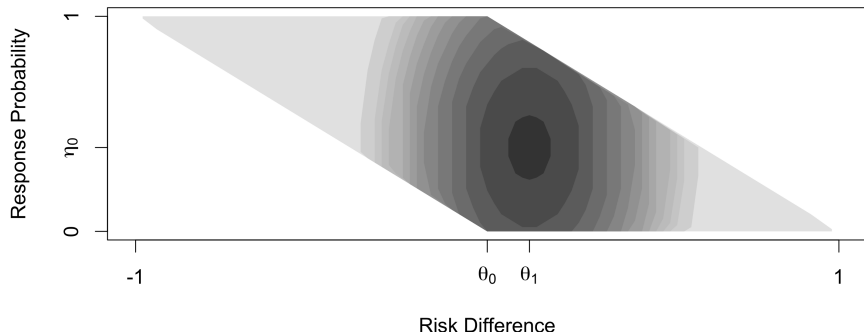
$$\omega = (1 - \delta) \cdot \psi^{(E)}(D_{\text{obs}}) \quad (4)$$

- This mixture weight achieves the goal of favoring the enthusiastic component if the trial data are compatible with that prior, and otherwise assigning a higher weight to the skeptical component.
- The minimum possible mixing weight  $\delta$  assigned to the *skeptical* prior is achieved when  $\psi^{(E)}(D_{\text{obs}}) = 1$  and is equal to  $\delta$ .
- Choices of  $\delta$  in  $\{0, 0.05, 0.10, 0.15, 0.20, 0.25\}$  are explored.

- We consider the trial “The Pediatric Lupus Trial of Belimumab Plus Background Standard Therapy (PLUTO)” (NCT01649765) which was conducted between September 2012 and January 2018 [?].
- The study population was comprised of patients ages 5 through 17 with active systemic lupus erythematosus (SLE), defined as a baseline SELENA SLEDAI score of 6 or above on a scale of 0-105, where higher scores indicate more severe disease activity.
- Patients were randomized to monthly dosing of either belimumab 10mg/kg or placebo, while continuing to receive standard of care therapy regardless of assignment.
- The primary endpoint was a dichotomous variable reflecting a 4-point or greater reduction in SELENA SLEDAI score from baseline to week 52.

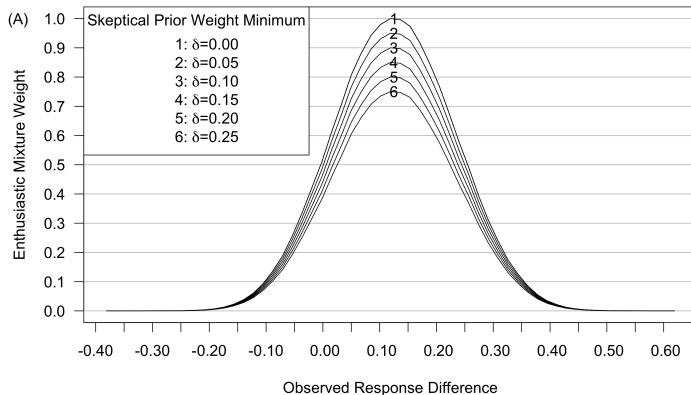
- An estimate for the pediatric response probability is denoted by  $\eta_0 = 0.39$  (i.e. the sample proportion of responders from the pooled adult studies), and for purposes of monitoring, a plausible, clinically meaningful difference in response probabilities is  $\theta_1 = 0.12$  (i.e. based on the pooled adult study's treatment response probability of 0.51).
- Using these values for the null and hypothesized response probabilities for the treatment group and assuming a response probability of 0.39 for the control group, a frequentist two-sided hypothesis test with confidence level 95% and 80% power would require 266 patients per group.

# Joint Enthusiastic Monitoring Prior



**Figure:** Joint prior  $\pi(\theta, \eta) = \pi(\theta) \times \pi(\eta|\theta)$  truncated based on the conditions  $-1 < \theta < 1$  and  $0 < \theta + \eta < 1$ .

# Enthusiastic Prior Mixing Weight $\omega$



**Figure:** A, Enthusiastic prior mixing weight  $\omega$  associated with skeptical prior weight minimum  $\delta$  in (??) by observed response difference between IP and PC groups, when the PC response rate is fixed at 38% (16/42 responses).

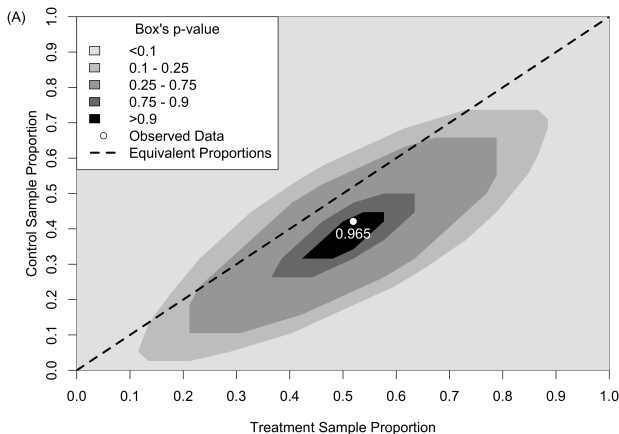
- Ultimately, 93 patients were enrolled over approximately 52.5 months (approximately 1 patient enrolled per 17 days).
- Clinical response was observed in 28 of 53 (52.8%) of patients randomized to belimumab and in 17 of 40 (43.6%) of patients randomized to placebo (95% CI [-0.1122, 0.2962])

# Re-analysis of PLUTO trial

**Table:** Summary characteristics of re-analysis of PLUTO trial. SS = Sample Size, I/F = Interim/Final,  $\psi^{(E)}(D_{\text{obs}})$  = Box's  $p$ -value using enthusiastic prior,  $\omega$  = Enthusiastic mixing weight in adaptive monitoring prior, Efficacy Post Prob = Posterior probability of treatment efficacy.

| $\delta$ | SS (I/F) | $\psi^{(E)}(D_{\text{obs}})$ (I/F) | $\omega$ (I/F) | Efficacy Post Prob (I/F) |
|----------|----------|------------------------------------|----------------|--------------------------|
| 0.00     | 62 / 90  | 0.914 / 0.965                      | 0.914 / 0.965  | 0.980 / 0.979            |
| 0.05     | 64 / 92  | 0.876 / 0.934                      | 0.833 / 0.887  | 0.976 / 0.962            |
| 0.10     | 76 / 92  | 0.941 / 0.934                      | 0.847 / 0.841  | 0.975 / 0.951            |
| 0.15     | 92 / 92  | 0.934 / 0.934                      | 0.794 / 0.794  | 0.940 / 0.940            |
| 0.20     | 92 / 92  | 0.934 / 0.934                      | 0.747 / 0.747  | 0.928 / 0.928            |
| 0.25     | 92 / 92  | 0.934 / 0.934                      | 0.701 / 0.701  | 0.917 / 0.917            |

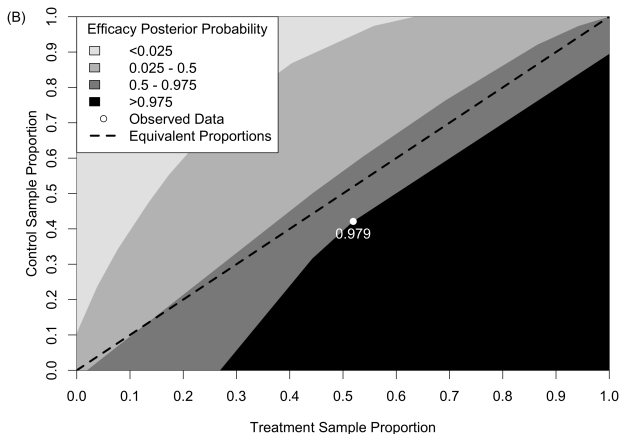
# Box's $P$ -value Using Enthusiastic Prior $\psi^{(E)}(D_{\text{obs}})$



**Figure:** A, Box's  $p$ -value by control and treatment sample proportions at the final analysis with 90 subjects when  $\delta = 0$  is used (??) for the adaptive monitoring prior.



# Posterior Probability of Treatment Efficacy



**Figure:** B, Posterior probability of efficacy by control and treatment sample proportions.

