Solutions Lecture 1 (Sections 3.1-3.5)

Make sure to import Numpy to be able to use all its functionality.

```
import numpy as np
```

Do not use for- or while-loops when answering the questions below.

Question 1

Create a 3×2 array M of ones. Make sure the elements have data type int.

```
# If you don't specify the dtype, then the array will have
# dtype 'float64' (You can check this with the command: x.dtype)
x = np.ones((3,2),dtype=int)
print(x)
```

[[1 1] [1 1]

[1 1]]

Question 2

Create the array x=[2,4,6,8,...,100] once with np.arange(), and once with np.linspace().

```
# With arange()
x = np.arange(2,101,2)
print(x)

# With linspace()
x = np.linspace(2,100,50)
print(x)
```

```
10
                        12
                                16
                                     18
                                          20
                                              22
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                                                       26
                                                           28
                                                                    32
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 58.
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            62.
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                        66.
                             68.
                                   70.
                                        72.
                                              74.
                                                   76.
                                                         78.
                                                              80.
                                                                    82.
                                                                         84.
```

```
86. 88. 90. 92. 94. 96. 98. 100.]
```

Create the array $x = [-1, -0.9, \dots, -0.1, 0, 0.1, \dots, 0.9, 1].$

```
# With arange()
x = np.arange(-1,1.1,0.1)
print(x)

# With linspace()
x = np.linspace(-1,1,21)
print(x)

[-1.00000000e+00 -9.00000000e-01 -8.00000000e-01 -7.00000000e-01
-6.00000000e-01 -5.00000000e-01 -4.00000000e-01 -3.00000000e-01
-2.00000000e-01 -1.00000000e-01 -2.22044605e-16 1.0000000e-01
2.00000000e-01 3.00000000e-01 4.0000000e-01 5.00000000e-01
6.00000000e-01 7.00000000e-01 8.0000000e-01 9.0000000e-01
1.00000000e+00]
[-1. -0.9 -0.8 -0.7 -0.6 -0.5 -0.4 -0.3 -0.2 -0.1 0. 0.1 0.2 0.3
```

Question 4

Consider the two-dimensional array below and answer the questions below.

```
M = np.array([[1,1,1,1,1],[2,1,2,1,2],[2,1,2,1,2],[2,1,2,1,2],[2,1,2,1,2],[1,1,1,1,1]])
print(M)
```

```
[[1 1 1 1 1]

[2 1 2 1 2]

[2 1 2 1 2]

[2 1 2 1 2]

[2 1 2 1 2]

[1 1 1 1 1]]
```

a) Index/access the odd-numbered rows of M.

0.4 0.5 0.6 0.7 0.8 0.9 1.]

```
M_odd = M[1::2]
print(M_odd)
```

```
[[2 1 2 1 2]
[2 1 2 1 2]
[1 1 1 1 1]]
```

b) Index/access the rows and columns that form the submatrix consisting of elements equal to 2.

```
M_2 = M[1:5,0::2]

print(M_2)

[[2 2 2]
      [2 2 2]
      [2 2 2]
      [2 2 2]]

c) Return the submatrix consisting of the rows 0,1,5 and columns 1,3,4.

i = [0,1,5]
      j = [1,3,4]

print(M[np.ix_(i,j)])

[[1 1 1]
      [1 1 2]
      [1 1 1]]
```

Consider the following array.

```
x = np.array([3,6,4,5,5,5,1,4,2,9,6,7,11,10])
print(x)
```

[3 6 4 5 5 5 1 4 2 9 6 7 11 10]

a) Use a Boolean mask to access all element whose value is smaller or equal than 4.

```
mask = x <= 4
print(x[mask])</pre>
```

[3 4 1 4 2]

b) Use a Boolean mask to access all element whose value is in the interval [5, 10].

```
mask = (x >= 5) & (x <= 10)
print(x[mask])</pre>
```

[655596710]

c) Use a Boolean mask to access all element whose value is in the interval [2,4] or [6,9].

```
mask = ((x \ge 2) & (x \le 4)) | ((x \ge 6) & (x \le 9))
print(x[mask])
```

```
[3 6 4 4 2 9 6 7]
```

Take the array x = [0, 1, 2, 3] and convert it to

$$\begin{bmatrix} 0 & 1 & 2 & 3 & 0 & 1 & 2 & 3 \\ 0 & 1 & 2 & 3 & 0 & 1 & 2 & 3 \end{bmatrix}.$$

```
x = np.arange(0,4)
y = np.tile(x,(2,2))
print(y)
```

```
[[0 1 2 3 0 1 2 3]
[0 1 2 3 0 1 2 3]]
```

Question 7

Construct the following matrix M using appropriate NumPy functions starting from the array [1, 2, 4]:

$$\begin{bmatrix} 1 & 1 & 2 & 2 & 4 & 4 \\ 1 & 1 & 2 & 2 & 4 & 4 \end{bmatrix}.$$

```
x = np.array([1,2,4])
x_repeat = np.repeat(x,2)

M = np.tile(x_repeat,(2,1))
print(M)
```

```
[[1 1 2 2 4 4]
[1 1 2 2 4 4]]
```

Question 8

Write a function blocks(m,n) that, for given inputs n and m, returns an $(m+n)\times(m+n)$ matrix that contains an $m\times m$ block of ones on the top left, and an $n\times n$ block of ones on the bottom right (and zeros elsewhere). Use np.hstack() and np.vstack() in your solution.

For m=2 and n=3, this results in the matrix

```
\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 \end{bmatrix}
```

```
def blocks(m,n):
    X1 = np.ones((m,m),dtype='int')
    X2 = np.ones((n,n),dtype='int')
    Y1 = np.zeros((m,n),dtype='int')
    Y2 = np.zeros((n,m),dtype='int')
    return np.vstack((np.hstack((X1,Y1)),np.hstack((Y2,X2))))
#Testing
print(blocks(2,3))
```

```
[[1 1 0 0 0]

[1 1 0 0 0]

[0 0 1 1 1]

[0 0 1 1 1]
```

Write a function checkerboard(n) that returns a checkerboard pattern of zeros and ones of size $n \times n$ (see examples below; the top-left element is always a 1).

For n = 5 and n = 6, the matrix should look like this

$$\begin{bmatrix} 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 \end{bmatrix} \text{ and } \begin{bmatrix} 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 \end{bmatrix}.$$

```
def checkerboard(n):
    x = np.zeros((n,n),dtype=int)
    x[0::2,0::2] = 1
    x[1::2,1::2] = 1
    return x

#Testing
n = 5
print(checkerboard(n))
```

```
n = 6
print(checkerboard(n))
```

```
[[1 0 1 0 1]

[0 1 0 1 0]

[1 0 1 0 1]

[0 1 0 1 0]

[1 0 1 0 1]]

[1 0 1 0 1 0]

[0 1 0 1 0 1]

[1 0 1 0 1 0]

[0 1 0 1 0 1]

[1 0 1 0 1 0]

[0 1 0 1 0 1]
```

Compute the anti-diagonal of the matrix

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 5 & 6 & -7 \\ -9 & 10 & 11 \end{bmatrix}$$

using np.rot90(). The anti-diagnoal is obtained by going from the bottom-left to the top-right element, i.e., [-9,6,3] in this case (and not [3,6,-9]). Have a look at the documentation of np.rot90() for details of how this function works.

```
A = np.array([
    [1, 2, 3],
    [5, 6, -7],
    [-9, 10, 11]])

# We first rotate the matrix 3*90 = 270 degrees
# and then take the diagonal.
d = np.diag(np.rot90(A,k=3))
print(d)
```

[-9 6 3]