

Design and Analysis of Algorithms I

Data Structures

Insertion In A Red-Black Tree

High-Level Plan

Idea for In sert (Delete: proceed as in a normal bihary Search tree, then recolor and for perform rotations and invariants are restored.

Ingert (x): (Dinsert x as usual Choices x a leaf)

Dtry coloring x red

The first parent y is black, done.

The else y is red. => y has a black parent w

Insertion

Case 1

Case! He other child 2 st x's
grand parent w is also red.

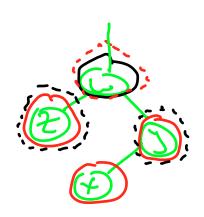


2) litter restores invariant (3) or propagates the double red upward

Can only happen oclog not times

L'A you reach the rost, recolor it black =>

preserves invariant (F)



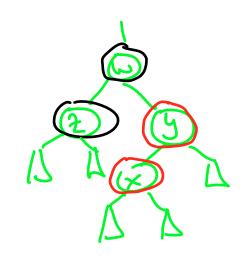
Case 2

Caxà: let xiy be the current double -red, x the deeper node.

Let w = x's grand parent.

Suppose w's other child (#y) is NULL

or is a black node 2.



Exercise (Case analysis (Attails omitted): Can eliminate double-red [=> all invariants satisfied) in O(1) time via 2-3 rotations + recolorings.