

Procesamiento de señnales, fundamentos

Maestría en sistemas embebidos MSE2020 Universidad de Buenos Aires

Clase 2 - Euler | Fourier Ing. Pablo Slavkin





2.7182818284590450907955982984276488423347473144

• f(t) = t

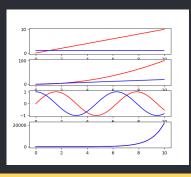
• f'(t) = 1

• $f(t) = t^2$

• f'(t) = 2 * t

• $f(t) = \sin(t)$

 $f'(t) = \cos(t)$



La derivada es igual a la funcion

$$f(t) = e^t \implies f'(t) = e^t$$

 $f(t) = e^{kt} \implies f'(t) = ke^{kt}$

Euler

Pero que pasa con e^{jt}?

La derivada es igual a la funcion

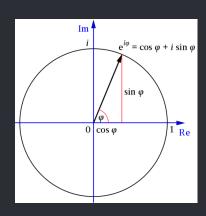
$$f(t) = e^{jt} \implies f'(t) = je^{jt}$$

$$e^{jt} = \cos(t) + j\sin(t)$$

$$e^{j\pi} = -1$$

$$e^{\frac{\pi}{2}} = i$$

$$e^{\frac{j3\pi}{2}} = i$$

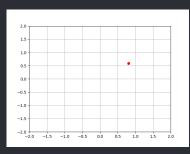




e^{j2πt} e^{j2πt} animado



```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.animation import FuncAnimation
           = plt.figure()
fia
fs
           = 10
           = 10
circleAxe = fig.add subplot(1,1,1)
circleLn, = plt.plot([],[],'ro')
circleAxe.grid(True)
circleAxe.set xlim(-2,2)
circleAxe.set ylim(-2,2)
circleFrec = \overline{1}
circle = lambda c,f,n: c*np.exp(-1j*2*np.pi*f*n*1/fs)
def update(n):
    circleLn.set data(np.real(circle(1.circleFrec.n)).
                      np.imag(circle(1.circleFrec.n)))
    return circleLn.
ani=FuncAnimation(fig,update,N,interval=100 ,blit=False,repeat=True)
plt.show()
```



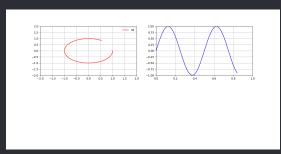


$e^{j2\pi t}$ y $\sin(t)$ animados independientemente

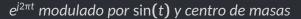


```
import numpy as no
import matplotlib.pyplot as plt
from matplotlib.animation import FuncAnimation
           = plt.fiqure()
circleAxe = fig.add subplot(2,2,1)
circleLn, = plt.plot([],[],'r-')
circleAxe.grid(True)
circleAxe.set xlim(-2.2)
circleAxe.set ylim(-2,2)
circleFrec = 1
circleData=[]
circle = lambda c.f.n: c*np.exp(-1i*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalLn. = plt.plot([1.[1.'b-')
signalAxe.grid(True)
signalAxe.set xlim(θ,N/fs)
signalAxe.set ylim(-1,1)
signalFrec = 2
signalData=[]
signal = lambda f,n: np.cos(2*np.pi*f*n*1/fs)
tData=[]
def init():
def update(n):
    global circleData, signalData, tData
    circleData.append(circle(1,circleFrec,n))
    circleLn.set data(np.real(circleData).
                      np.imag(circleData))
    signalData.append(signal(signalFrec,n))
    tData.append(n/fs)
    signalLn.set data(tData.signalData)
    if n==N-1:
        circleData=[]
        signalData=[]
        tData=[]
    circleLn.set label(n)
    circleAxe.legend()
```

return circleLn.circleAxe.signalLn



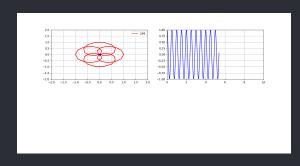






```
import matplotlib pyplot as plt
from matplotlib.animation import FuncAnimation
circleAxe = fig.add subplot(2,2,1)
circleLn,promLn = plt.plot([],[],'r-',[],[],'bo')
circleAxe.set xlim(-2,2)
circleAxe.set vlim(-2.2)
          = lambda c,f,n: c*np.exp(-lj*2*np.pi*f*n*l/fs)
signalAxe = fig.add subplot(2.2.2)
signalAxe.set vlim(-1.1)
signal = lambda f.n: np.cos(Z*np.pi*f*n*1/fs)
   circleData.append(circle(1.circleFrec.n)*signal(signalFrec.n))
   prom=np.average(circleData)
   promLn.set data(np.real(prom),
   circleLn.set_data(np.real(circleData)
                      np.imag(circleData))
   signalData.append(signal(signalFrec.n))
    tData.append(n/fs)
   signalLn.set data(tData,signalData)
   prom = 0
circleLn.set label(n)
   circleAxe.legend()
```

return circleIn,circleAxe,signalLn,promLn ani=FuncAnimation(fig.update.N.init.interval=10 .blit=True.repeat=True)

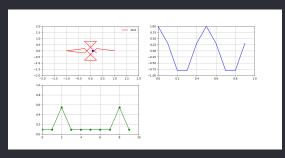




e^{j2πt} modulado por sin(t) y centro de masas en f



```
signalin, = plt.plst([],[],'b-')
signalAxe.grid(True)
fourierAxe.grid(True)
fourierAxe.set_xlim(0,fs)
            circletxe.legecd()
wrm circlein,circletxe,cignalin,promin,fourierin
```

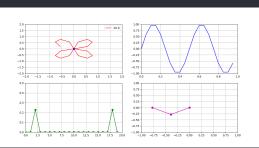




$e^{j2\pi t}$ del centro de masas de vuelta a sin(t)



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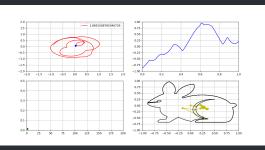




Señales complejas, conejo



```
prom-np.average(circlebata)
promin.oet_data(np.real(prom)
```



Bibliografia

Libros, links y otro material

- [1] Steven W. Smith. The Scientist and Engineer's Guide to Digital Signal Processing. Second Edition, 1999.
- [2] Interactive Mathematics Site Info.
- [3] Grant Sanderson https://youtu.be/spUNpyF58BY