

# Procesamiento de señales, fundamentos

Maestría en sistemas embebidos

Universidad de Buenos Aires

MSE 5Co2020

## Clase 2 - CIAA<>Python

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```
0000 c0ff 0300 80ff 0100 c0ff 0400 4000 a.....@.
0500 0000 faff c0ff 0200 c0ff 0600 0000 .....
0200 c0ff 1100 0000 ffff 80ff 0200 c0ff .....
0000 6865 6164 6572 2000 0000 f2ff 0000 .....header.....
fcff 0000 0600 0000 0000 c0ff f6ff 0000 .....
fcff 4000 f6ff 0000 0d00 4000 feff 0000 .....@.....@.....
0400 c0ff 0200 0000 feff 0000 0800 c0ff .....
ffff 0000 0600 c0ff ffff 0000 fdff 0000 .....
0000 6865 6164 6572 2000 0000 ecff c0ff .....header.....
e8ff 0000 0100 c0ff 0300 c0ff edff c0ff .....
0c00 0000 f0ff 0000 0100 c0ff 0500 c0ff .....
0200 c0ff 0500 c0ff f6ff 0000 feff 0000 .....@.....
0600 4000 0900 0000 0a00 c0ff f8ff 0000 .....@.....@.....
0000 6865 6164 6572 2000 80ff f4ff 0000 .....header.....
0200 c0ff f9ff c0ff 0400 c0ff 0500 0000 .....
fcff 0000 f2ff 0000 0300 0000 0100 c0ff .....
f5ff c000 fcff 4000 0200 0000 fdff 0000 .....@.....
ffff 0000 f9ff 0000 0400 0000 f7ff 0000 .....
0000 6865 6164 6572 2000 c0ff e0ff 0000 .....header.....
fcff 0000 0a00 c0ff ffff 0000 f1ff c0ff .....
```

# Enuestas

## *Encuesta anónima clase a clase*

Propiciamos este espacio para compartir sus sugerencias, criticas constructivas, oportunidades de mejora y cualquier tipo de comentario relacionado a la clase.

### Encuesta anónima



<https://forms.gle/1j5dDTQ7qjVfRwYo8>

### Link al material de la material



[https://drive.google.com/drive/u/1/folders/1TIR2cgDPchL\\_4v7DxdpS7pZHtjKq38CK](https://drive.google.com/drive/u/1/folders/1TIR2cgDPchL_4v7DxdpS7pZHtjKq38CK)

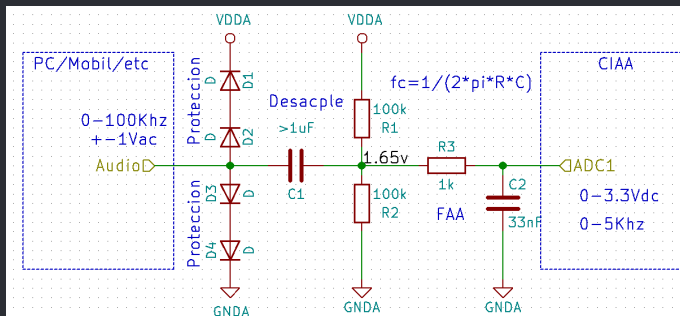
# Sampleo

## Acondicionamiento de señal



Acondicionar la señal de salida del dispositivo de sonido (en PC ronda  $\pm 1V$ ) al rango del ADC del hardware. En el caso de la CIAA sera de 0-3.3V.

Se propone el siguiente circuito, que minimiza los componentes sacrificando calidad y agrega en filtro anti alias de 1er orden.



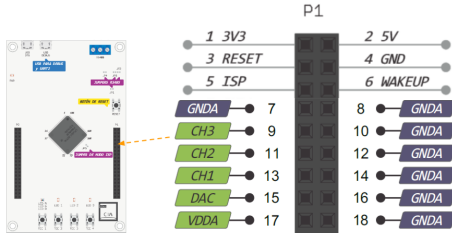


### Pinout de la CIAA para conectar el ADC/DAC

#### CIAA ADC y DAC en la EDU-CIAA-NXP

Maapeo de ADC y DAC en la biblioteca sAPI:

- 3 entradas analógicas nombradas CH1, CH2 y CH3 (ADC).
- 1 salida analógica nombrada DAC.



# Generación de audio con Python



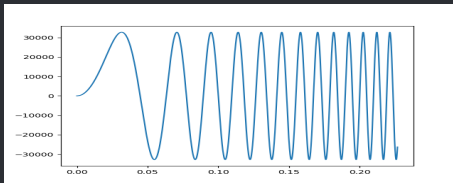
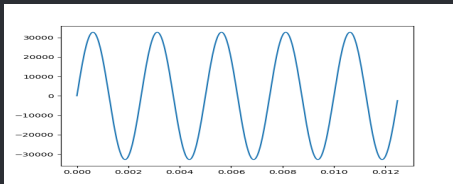
<https://simpleaudio.readthedocs.io/en/latest/installation.html>

Instalar el módulo simpleaudio (ver apéndice 6) para generar sonidos con python y utilizamos el siguiente código como base:

```
import numpy as np
import scipy.signal as sc
import simpleaudio as sa
import matplotlib.pyplot as plt

f = 400
fs = 44100
sec = 5
B = 600
t = np.arange(0, sec, 1/fs)
#note = (2**15-1)*np.sin(2 * np.pi * f * t) #sin
#note = (2**15-1)*sc.sawtooth(2*np.pi*f*t,0) #saw
note = (2**15-1)*np.sin(2 * np.pi * B*t/sec * t) #
    sweept

audio = note.astype(np.int16)
for i in range(1000):
    play_obj = sa.play_buffer(audio, 1, 2, fs)
    play_obj.wait_done()
```



# Captura de audio con la CIAA



CIAA->UART->picocom->log.bin

Utilizando picocom <https://github.com/npat-efault/picocom> o similar se graba en un archivo la salida de la UART para luego procesar como sigue

```
picocom /dev/ttyUSB1 -b 460800 -logfile=log.bin
```

```
#include "sapi.h"

#define LENGTH 512
int16_t adc [ LENGTH ];
uint16_t sample = 0;

int main ( void ) {
    boardConfig      (
        uartConfig    ( UART_USB, 460800 );
        adcConfig      ( ADC_ENABLE );
        cyclesCounterInit ( EDU_CIAA_NXP_CLOCK_SPEED );
        while(1) {
            cyclesCounterReset();
            uartWriteByteArray ( UART_USB ,(uint8_t* )&adc[sample] ,sizeof(adc[0])
            );
            adc[sample] = ((int16_t )adcRead(CH1)-512);
            if ( ++sample==LENGTH ) { //22.7hz para 512
                sample = 0;
                uartWriteByteArray ( UART_USB ,"header" ,6 );
                gpioToggle      ( LEDR );
            }
            while(cyclesCounterRead()< 20400) //clk 204000000
        }
}
}
Ing. Pablo Slavkin
```

```
0000 c0ff 0300 80ff 0100 c0ff 0400 4000 a.....
0500 0000 faff c0ff 0200 c0ff 0600 0000 .....
0200 c0ff 1100 0000 ffff 80ff 0200 c0ff .....
0000 6865 6164 6572 2000 0000 f2ff 0000 .....header.....
fcff 0000 0600 0000 0000 c0ff f6ff 0000 .....
fcff 4000 f6ff 0000 0d00 4000 feff 0000 .....@.....@.....
0400 c0ff 0200 0000 feff 0000 0800 c0ff .....
ffff 0000 0600 c0ff ffff 0000 fdff 0000 .....
0000 6865 6164 6572 2000 0000 ecff c0ff .....header.....
e8ff 0000 0100 c0ff 0300 c0ff edff c0ff .....
0c00 0000 f0ff 0000 0100 c0ff 0500 c0ff .....
0200 c0ff 0500 c0ff f6ff 0000 feff 0000 .....@.....
0600 4000 0900 0000 0a00 c0ff f8ff 0000 .....@.....@.....
0000 6865 6164 6572 2000 80ff f4ff 0000 .....header.....
0200 c0ff f9ff c0ff 0400 c0ff 0500 0000 .....
fcff 0000 f2ff 0000 0300 0000 0100 c0ff .....
f5ff c000 fcff 4000 0200 0000 fdff 0000 .....@.....
ffff 0000 f9ff 0000 0400 0000 f7ff 0000 .....
0000 6865 6164 6572 2000 c0ff e0ff 0000 .....header.....
fcff 0000 0a00 c0ff ffff 0000 f1ff c0ff .....
```

# Ancho de banda



$$USB \leftrightarrow UART_{maxbps} = 460800bps$$

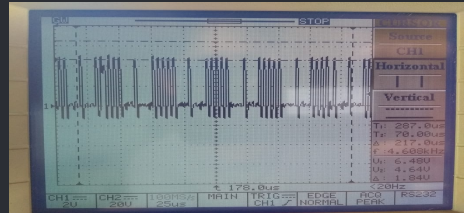
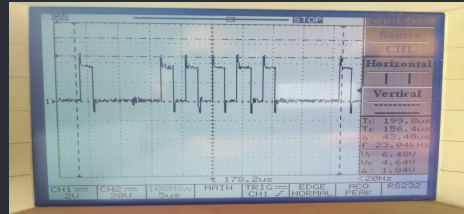
$$Eficacia = \frac{10b}{8b} = 0,8$$

$$bits_{muestra} = 16$$

$$Tasa_{efectiva} = \frac{460800_{bps} * 0,8}{16} = 23040$$

Máxima señal muestreable y reconstruible

11520hz



# Sampleo

## Calculo del filtro antialias 1er orden R-C

$$B = 10\text{kbps}$$

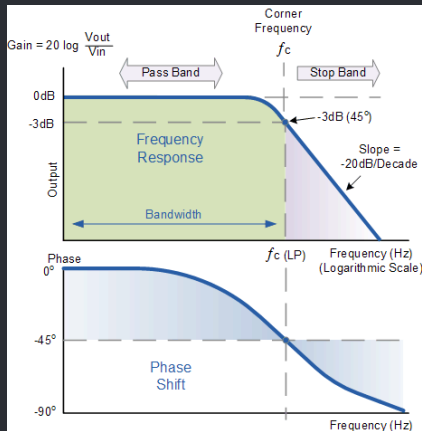
$$f_{\text{corte}} = \frac{1}{2 * \pi * R * C}$$

$$R = 1\text{k}\Omega$$

$$C = \frac{1}{f_{\text{corte}} * R * 2 * \pi} \approx 15\text{nF}$$

Máxima señal muestreable y reconstruible

11520hz





# Captura de audio con la CIAA

UART->Python



## Lectura de un log y visualización en tiempo real de los datos

```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.animation import
FuncAnimation
import os

length = 512
fs = 10000
header = b'header'
fig = plt.figure(1)
adcAxe = fig.add_subplot(1,1,1)
time = np.linspace(0,length/fs,length)
adcLn, = plt.plot([],[],'r')
adcAxe.grid(True)
adcAxe.set_ylim(-512,512)
adcAxe.set_xlim(0,length/fs)

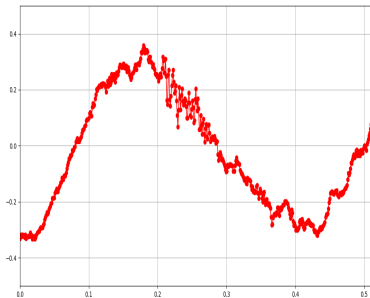
def findHeader(f):
    index = 0
    sync = False
    while sync==False:
        data=b''
        while len(data) <1:
            data = f.read(1)
        if data[0]==header[index]:
            index+=1
```

```
        if index>=len(header):
            sync=True
            print(sync)
        else:
            index=0
            print(sync)

def readInt4File(f):
    raw=b''
    while len(raw)<2:
        raw += f.read(1)
    return (int.from_bytes(raw[0:2],"
        little",signed=True))

def update(t):
    findHeader(logFile)
    adc = []
    for chunk in range(length):
        adc.append(readInt4File(logFile))
    adcLn.set_data(time,adc)
    return adcLn,

logFile=open("log.bin","w+b")
ani=FuncAnimation(fig,update,10,None,blit=
    True,interval=10,repeat=True)
plt.draw()
plt.show()
```

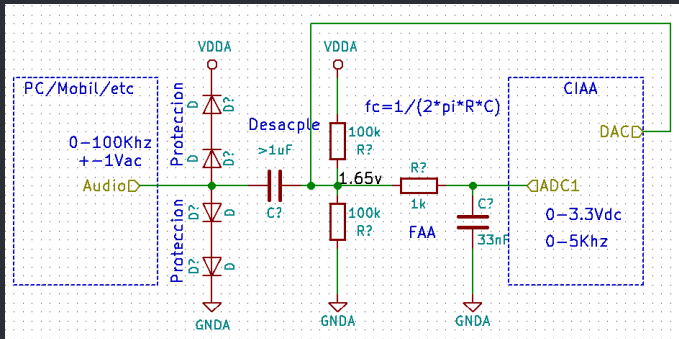


# Reconstrucción

## Acondicionamiento de señal



Se realiza un loop del DAC al ADC permitiendo sumar a la señal de entrada ya existente



# Generación de audio con el DAC de la CIAA

ARM CMSIS-DSP lib [https://www.keil.com/pack/doc/CMSIS/DSP/html/group\\_\\_sin.html](https://www.keil.com/pack/doc/CMSIS/DSP/html/group__sin.html)



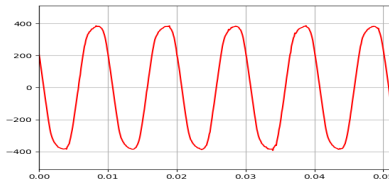
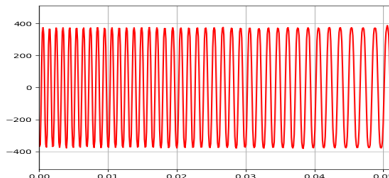
Con arm\_sin\_f32 se genera un tono y se convierte a analógico con el DAC

```
#include "sapi.h"
#include "arm_math.h"

#define LENGTH 512
#define FS 10000
int16_t adc[ LENGTH ];
uint16_t sample = 0 ;
uint32_t tick = 0 ;
uint16_t f = 100 ;
uint16_t B = 5000;
uint16_t swept = 1;
float t = 0;

int main ( void ) {
    boardConfig ( );
    uartConfig ( UART_USB
        ,460800 );
    adcConfig (
        ADC_ENABLE );
    dacConfig (
        DAC_ENABLE );
```

```
cyclesCounterInit ( EDU_CIAA_NXP_CLOCK_SPEED
    );
while(1) {
    cyclesCounterReset();
    uartWriteByteArray ( UART_USB ,(uint8_t* )
        &adc[sample] ,sizeof(adc[0]) );
    adc[sample] = adcRead(CH1)-512;
    t=((tick%(swept*FS))/(float)FS);
    //dacWrite( DAC, 512*arm_sin_f32 (t*B*(t/
        swept)*2*PI)+512); //swept
    dacWrite( DAC, 512*arm_sin_f32 (t*f*2*PI)
        +512); //tono
    if ( ++sample==LENGTH ) {
        sample = 0;
        uartWriteByteArray ( UART_USB ,"header"
            ,6 );
        gpioToggle ( LEDG );
    }
    tick++;
    while(cyclesCounterRead()<
        EDU_CIAA_NXP_CLOCK_SPEED/FS) //clk
        204000000
    ;
}
```



# Documentación

ARM CMSIS-DSP lib [https://www.keil.com/pack/doc/CMSIS/DSP/html/group\\_\\_sin.html](https://www.keil.com/pack/doc/CMSIS/DSP/html/group__sin.html)

The screenshot shows the CMSIS-DSP Version 1.8.0 documentation page. The top navigation bar includes tabs for General, Core(A), Core(M), Driver, DSP (selected), NN, RTOS v1, RTOS v2, and Pa. Below this is a sub-navigation bar with Main Page, Usage and Description, and Reference. The left sidebar lists various functions, with 'Root mean square (RMS)' expanded to show 'arm\_rms\_f32', 'arm\_rms\_q15' (highlighted), and 'arm\_rms\_q31'. The main content area displays the function signature: `void arm_rms_q15 ( const q15_t* pSrc, uint32_t blockSize, q15_t* pResult )`. It also includes the 'Returns' section (none), 'Parameters' section (describing pSrc, blockSize, and pResult), and 'Scaling and Overflow Behavior' section.

**CMSIS-DSP** Version 1.8.0  
CMSIS DSP Software Library

General Core(A) Core(M) Driver **DSP** NN RTOS v1 RTOS v2 Pa

Main Page Usage and Description Reference

Mean  
Minimum  
Power  
Root mean square (RMS)  
arm\_rms\_f32  
**arm\_rms\_q15**  
arm\_rms\_q31  
Standard deviation  
Variance  
arm\_entropy\_f32  
arm\_entropy\_f64  
arm\_kullback\_leibler\_f32  
arm\_kullback\_leibler\_f64  
arm\_logsumexp\_dot\_prod\_f32  
arm\_logsumexp\_f32  
Support Functions  
Interpolation Functions

[out] **pResult** root mean square value returned here

**Returns**  
none

```
void arm_rms_q15 ( const q15_t* pSrc,  
                  uint32_t    blockSize,  
                  q15_t*      pResult  
                  )
```

**Parameters**  
[in] **pSrc** points to the input vector  
[in] **blockSize** number of samples in input vector  
[out] **pResult** root mean square value returned here

**Returns**  
none

**Scaling and Overflow Behavior**  
The function is implemented using a 64-bit internal accumulator.

# Sistemas de números

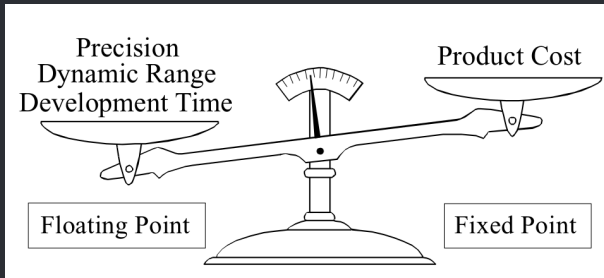
## *Punto fijo vs punto flotante*

### Punto fijo:

- Cantidad de patrones de bits= 65536
- Gap entre números constante
- Rango dinámico 32767, -32768
- Gap 10 mil veces mas chico que el numero

### Punto flotante:

- Cantidad de patrones de bits= 4,294,967,296
- Gap entre números variable
- Rango dinámico  $\pm 3,4e10^{38}$ ,  $\pm 1,2e10^{-38}$
- Gap 10 millones de veces mas chico que el numero



# Sistemas de números

## Sistema Q

Qm.n:

- m: cantidad de bits para la parte entera
- n: cantidad de bits para la parte decimal

Q1.15:

$$1000\ 0000\ 0000\ 0000 = -1$$

$$0111\ 1111\ 1111\ 1111 = 1/2 + 1/4 + 1/8 + \dots + 1/2^{15} = 0,99$$

Q2.14:

$$1010\ 0000\ 0000\ 0000 = -1.5$$

$$0101\ 0000\ 0000\ 0000 = 1.25$$

# Sistemas de números

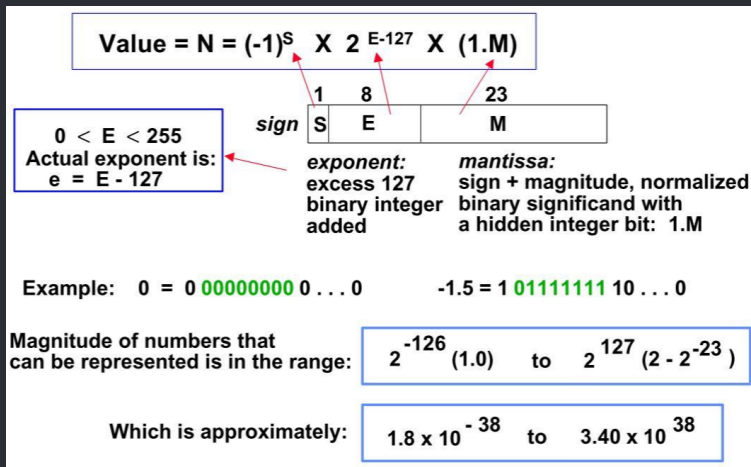
## Tabla de ejemplos Q1.2 y Q2.1 signado y no signado

| UQ3.0   | UQ2.1               | UQ1.2                    |
|---------|---------------------|--------------------------|
| 011 = 3 | 01.1 = $1+1/2= 1.5$ | 0.11 = $0+1/2+1/4= 0.75$ |
| 010 = 2 | 01.0 = $1+0/2= 1.0$ | 0.10 = $0+1/2+0/4= 0.5$  |
| 001 = 1 | 00.1 = $0+1/2= 0.5$ | 0.01 = $0+0/2+1/4= 0.25$ |
| 000 = 0 | 00.0 = $0+0/2= 0.0$ | 0.00 = $0+0/2+0/4= 0.0$  |
| 111 = 7 | 11.1 = $3+1/2= 3.5$ | 1.11 = $1+1/2+1/4= 1.75$ |
| 110 = 6 | 11.0 = $3+0/2= 3.0$ | 1.10 = $1+1/2+0/4= 1.5$  |
| 101 = 5 | 10.1 = $2+1/2= 2.5$ | 1.01 = $1+0/2+1/4= 1.25$ |
| 100 = 4 | 10.0 = $2+0/2= 2.0$ | 1.00 = $1+0/2+0/4= 1.0$  |

| SQ3.0   | SQ2.1                | SQ1.2                     |
|---------|----------------------|---------------------------|
| 011 =+3 | 01.1 = $1+1/2=+1.5$  | 0.11 = $0+1/2+1/4=+0.75$  |
| 010 =+2 | 01.0 = $1+0/2=+1.0$  | 0.10 = $0+1/2+0/4=+0.5$   |
| 001 =+1 | 00.1 = $0+1/2=+0.5$  | 0.01 = $0+0/2+1/4=+0.25$  |
| 000 =+0 | 00.0 = $0+0/2=+0.0$  | 0.00 = $0+0/2+0/4=+0.0$   |
| 111 =-1 | 11.1 = $-1+1/2=-0.5$ | 1.11 = $-1+1/2+1/4=-0.25$ |
| 110 =-2 | 11.0 = $-1+0/2=-1.0$ | 1.10 = $-1+1/2+0/4=-0.5$  |
| 101 =-3 | 10.1 = $-2+1/2=-1.5$ | 1.01 = $-1+0/2+1/4=-0.75$ |
| 100 =-4 | 10.0 = $-2+0/2=-2.0$ | 1.00 = $-1+0/2+0/4=-1.0$  |

# Sistemas de números

## Float32 IEEE 754





# Calculo de propiedades temporales

## ARM CMSIS-DSP lib



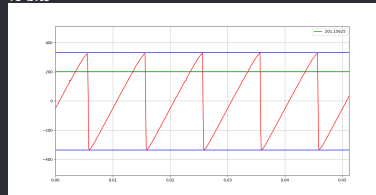
Calculamos max, min y rms con la CIAA

```
#include "sapi.h"
#include "arm_math.h"

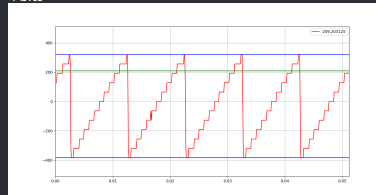
#define LENGTH 512
#define FS 10000
uint16_t adc[ LENGTH ];
uint16_t sample = 0;
uint32_t maxIndex,minIndex = 0;
q15_t maxValue,minValue,rms = 0;

int main ( void ) {
    boardConfig ( );
    uartConfig ( UART_USB ,460800 );
    adcConfig ( ADC_ENABLE );
    dacConfig ( DAC_ENABLE );
    cyclesCounterInit ( EDU_CIAA_NXP_CLOCK_SPEED );
    while(1) {
        cyclesCounterReset();
        uartWriteByteArray ( UART_USB ,(uint8_t* )&adc[sample] ,sizeof(adc[0]) );
        adc[sample] = ((adcRead(CH1)-512)>>6)<<12;
        if ( ++sample==LENGTH ) {
            arm_max_q15 ( adc, LENGTH, &maxValue,&maxIndex );
            arm_min_q15 ( adc, LENGTH, &minValue,&minIndex );
            arm_rms_q15 ( adc, LENGTH, &rms );
            uartWriteByteArray ( UART_USB ,(uint8_t* )&maxValue ,2 );
            uartWriteByteArray ( UART_USB ,(uint8_t* )&minValue ,2 );
            uartWriteByteArray ( UART_USB ,(uint8_t* )&rms ,2 );
            sample = 0;
            uartWriteByteArray ( UART_USB ,"header" ,6 );
            gpioToggle ( LEDG );
        }
        while(cyclesCounterRead()< EDU_CIAA_NXP_CLOCK_SPEED/FS) //clk 204000000
            ;
    }
}
```

10 bits



4 bits



# Cálculo de propiedades temporales

## ARM CMSIS-DSP lib



Visualizamos max, min y rms con Python

```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.animation import FuncAnimation
import os

N = 512
fs = 10000
header = b'header'
fig = plt.figure(1)
adcAxe = fig.add_subplot(1,1,1)
time = np.linspace(0,N/fs,N)
adcLn, maxLn, minLn, rmsLn, \
= plt.plot([],[],'r',[],[],'b',[],[],'b',[],[],'g')
adcAxe.grid(True)
adcAxe.set_ylim(-512,512)
adcAxe.set_xlim(0,N/fs)

def findHeader(f):
    index = 0
    sync = False
    while sync==False:
        data=b''
        while len(data) <1:
            data = f.read(1)
        if data[0]==header[index]:
            index+=1
            if index>=len(header):
```

```
                sync=True
                print(sync)
        else:
            index=0
            print(sync)

def readInt4File(f):
    raw=b''
    while len(raw)<2:
        raw += f.read(1)
    return (int.from_bytes(raw[0:2],"little",signed=True))

def update(t):
    findHeader(logFile)
    adc = []
    for chunk in range(N):
        adc.append(readInt4File(logFile)/2**6)
    adcLn.set_data(time,adc)
    maxLn.set_data(time,np.full(N,readInt4File(logFile)/2**6))
    minLn.set_data(time,np.full(N,readInt4File(logFile)/2**6))
    rmsValue=readInt4File(logFile)/2**6
    rmsLn.set_data(time,np.full(N,rmsValue))
    rmsLn.set_label(rmsValue)
    rmsLg = adcAxe.legend()
    return adcLn, maxLn, minLn, rmsLn,rmsLg

logFile=open("log.bin","w+b")
ani=FuncAnimation(fig,update,10,None,blit=True,interval=10,repeat=True)
plt.draw()
plt.show()
```

# Bibliografía

## *Libros, links y otro material*

- [1] *Numeracion Q.*  
[https://en.wikipedia.org/wiki/q\\_\(number\\_format\)](https://en.wikipedia.org/wiki/q_(number_format))
- [2] *Calculador float on-line.*  
[https://www.binaryconvert.com/result\\_float.html?decimal=048046053](https://www.binaryconvert.com/result_float.html?decimal=048046053)
- [3] *Calculando numeros Q.*  
<https://www.rfwireless-world.com/calculators/floating-vs-fixed-point-converter.html>

# Apéndice

## Instrucciones para usar simpleaudio

Docs » Installation

### Installation

Make sure you have pip installed. For Linux, this is usually done with the distro package manager (example: `sudo apt-get install python3-pip`). For Windows and macOS, have a look at the [pip documentation](#).

#### Note

The actual `pip` command may vary between platforms and Python versions. Substitute the correct one for usages in these examples. Some common variants for Python 3.x are: `pip3`, `pip3.x`, and `pip-3.x`.

Also, in some cases you may need to manually add pip's location to the 'path' environment variable.

Upgrade pip and setuputils:

```
pip install --upgrade pip setuputils
```

Install with:

```
pip install simpleaudio
```

### Linux Dependencies

The Python 3 and ALSA development packages are required for pip to build the extension. For Debian variants (including Raspbian), this will usually get the job done:

```
sudo apt-get install -y python3-dev libasound2-dev
```

Docs » Short Tutorial

### Short Tutorial

#### Import

Import the `simpleaudio` module:

```
import simpleaudio as sa
```

#### Playing audio directly

The simplest way to play audio is with `play_buffer()`. The `audio_data` parameter must be an object which supports the buffer interface: `bytes` objects, Python arrays, and `Numpy` arrays all qualify:

```
play_obj = sa.play_buffer(audio_data, 2, 2, 64100)
```

The `play_obj` object is an instance of `PlayObject` which could be viewed as a 'handle' to the audio playback initiated by the `play_buffer()` call. This can be used to stop playback of the audio clip:

```
play_obj.stop()
```

It can be used to check whether a sound clip is still playing:

```
if play_obj.is_playing():  
    print("still playing")
```

It can also be used to wait for the audio playback to finish. This is especially useful when a script or program would otherwise exit before playback is done (stopping the playback thread and consequently the audio):

```
play_obj.wait_done()  
# script exits
```

### WaveObject's

In order to facilitate cleaner code, the `WaveObject` class is provided which stores a reference to the object containing the audio as well as a copy of the playback parameters. These can be instantiated like so:

```
wave_obj = sa.WaveObject(audio_data, 2, 2, 64100)
```

Playback is started with `play()` and a `PlayObject` is returned as with `play_buffer()`:

```
play_obj = wave_obj.play()
```

A class method exists in order to conveniently create `WaveObject` instances directly from WAV files on disk:

```
wave_obj = sa.WaveObject.from_wave_file(path_to_file)
```

Similarly, instances can be created from `Wave_read` objects returned from `wave.open()` from the Python standard library:

```
wave_read = wave.open(path_to_file, 'r')  
wave_obj = sa.WaveObject.from_wave_read(wave_read)
```

### Using Numpy

`Numpy` arrays can be used to store audio but there are a few crucial requirements. If they are to store stereo audio, the array must have two columns since each column contains one channel of audio data. They must also have a signed 16-bit integer dtype and the sample amplitude values must consequently fall in the range of -32768 to 32767. Here is an example of a simple way to 'normalize' the audio (making it cover the whole amplitude range but not exceeding it):

```
audio_array *= 32767 / max(abs(audio_array))
```

And here is an example of converting it to the proper data type (note that this should always

# Apéndice

## Instrucciones para usar simpleaudio

be done after normalization or other amplitude changes:

```
audio_array = audio_array.astype(np.int16)
```

Here is a full example that plays a few sinewave notes in succession:

```
import numpy as np
import simpleaudio as sa

# calculate note frequencies
A_freq = 440
Csh_freq = A_freq * 2 ** (4 / 12)
E_freq = A_freq * 2 ** (7 / 12)

# get timesteps for each sample, T is note duration in seconds
sample_rate = 44100
T = 0.25
t = np.linspace(0, T, T * sample_rate, False)

# generate sine wave notes
A_note = np.sin(A_freq * t * 2 * np.pi)
Csh_note = np.sin(Csh_freq * t * 2 * np.pi)
E_note = np.sin(E_freq * t * 2 * np.pi)

# concatenate notes
audio = np.hstack([A_note, Csh_note, E_note])
# normalize to 16-bit range
audio *= 32767 / np.max(np.abs(audio))
# convert to 16-bit data
audio = audio.astype(np.int16)
```

In order to play stereo audio, the **Numpy** array should have 2 columns. For example, one second of (silent) stereo audio could be produced with:

```
silence = np.zeros((44100, 2))
```

We can then use addition to layer additional audio onto it - in other words, 'mixing' it together. If a signal/audio clip is added to both channels (array columns) equally, then the audio will be perfectly centered and sound just as if it were played in mono. If the proportions vary between the two channels, then the sound will be stronger in one speaker than the other, 'panning' it to one side or the other. The full example below demonstrates this:

```
import numpy as np
import simpleaudio as sa

# calculate note frequencies
A_freq = 440
Csh_freq = A_freq * 2 ** (4 / 12)
E_freq = A_freq * 2 ** (7 / 12)

# get timesteps for each sample, T is note duration in seconds
sample_rate = 44100
T = 0.5
t = np.linspace(0, T, T * sample_rate, False)

# generate sine wave notes
A_note = np.sin(A_freq * t * 2 * np.pi)
Csh_note = np.sin(Csh_freq * t * 2 * np.pi)
E_note = np.sin(E_freq * t * 2 * np.pi)

# mix audio together
audio = np.zeros((44100, 2))
n = len(t)
offset = 0
audio[0 + offset:n + offset, 0] += A_note
offset = 1000
audio[0 + offset:n + offset, 0] += 0.5 * A_note
audio[0 + offset:n + offset, 1] += 0.5 * Csh_note
offset = 11000
audio[0 + offset:n + offset, 0] += 0.5 * Csh_note
audio[0 + offset:n + offset, 1] += E_note

# normalize to 16-bit range
audio *= 32767 / np.max(np.abs(audio))
# convert to 16-bit data
audio = audio.astype(np.int16)
```

24-bit audio can be also be created using **Numpy** but since **Numpy** doesn't have a 24-bit integer dtype, a conversion step is needed. Note also that the max sample value is different for 24-bit audio. A simple (if inefficient) conversion algorithm is demonstrated below, converting an array of 32-bit integers into a **bytes** object which contains the packed 24-bit audio to be played:

```
import numpy as np
import simpleaudio as sa

# calculate note frequencies
A_freq = 440
Csh_freq = A_freq * 2 ** (4 / 12)
E_freq = A_freq * 2 ** (7 / 12)

# get timesteps for each sample, T is note duration in seconds
sample_rate = 44100
T = 0.5
t = np.linspace(0, T, T * sample_rate, False)

# generate sine wave tone
tone = np.sin(440 * t * 2 * np.pi)

# normalize to 24-bit range
tone *= 8388607 / np.max(np.abs(tone))

# convert to 20-bit data
tone = tone.astype(np.int32)

# convert from 32-bit to 24-bit by building a new byte buffer, skipping every fourth bit
# note: this also works for 2-channel audio
i = 0
byte_array = []
for b in tone.tobytes():
    if i % 4 != 3:
        byte_array.append(b)
    i += 1
audio = bytearray(byte_array)

# start playback
play_obj = sa.play_buffer(audio, 1, 3, sample_rate)

# wait for playback to finish before exiting
play_obj.wait_done()
```