

Procesamiento de señales, fundamentos

Maestría en sistemas embebidos Universidad de Buenos Aires MSE 5Co2O2O

Clase 3 - Euler | Fourier

Ing. Pablo Slavkin slavkin.pablo@gmail.com wapp:011-62433453

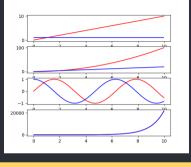




2.7182818284590450907955982984276488423347473144

- f(t) = t
 - f'(t) = 1
- $f(t) = t^2$ • $f(t) = \sin(t)$

• f'(t) = 2 * t• f'(t) = cos(t)



La derivada es igual a la funcion

$$f(t) = e^t \implies f'(t) = e^t$$

 $f(t) = e^{kt} \implies f'(t) = ke^{kt}$

Euler

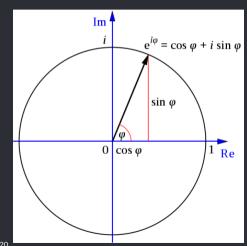
Pero que pasa con e^{jt}?

La derivada es igual a la funcion

$$f(t) = e^{jt} \implies f'(t) = je^{jt}$$

$$e^{jt} = \cos(t) + j\sin(t)$$

 $e^{j\pi} = -1$
 $e^{\frac{j\pi}{2}} = j$
 $e^{\frac{j3\pi}{2}} = -j$



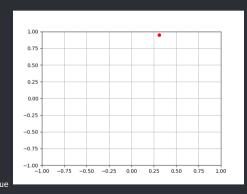
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$e^{j2\pi ft}$ animado



```
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.animation import FuncAnimation
fiq
           = plt.figure()
fs
           = 20
= 20
circleAxe = fig.add subplot(1,1,1)
circleLn, = plt.plot([],[],'ro')
circleAxe.grid(True)
circleAxe.set xlim(-1,1)
circleAxe.set_vlim(-1.1)
circleFrec = \overline{1}
def circle(c,f,n):
    return c*np.exp(-1i*2*np.pi*f*n*1/fs)
def init():
    return circleLn.
def update(n):
    circleLn.set data(np.real(circle(1.circleFrec.n)).
                       np.imag(circle(1,circleFrec,n)))
    return circleLn.
ani=FuncAnimation(fig.update,N,init,interval=100 ,blit=False,repeat=True
```



plt.show()

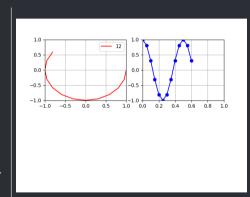


$e^{j2\pi ft}$ y Sin(t) animados independientemente



```
import numpy as np
import mathlotlib nyplot as plt
from matplotlib.animation import FuncAnimation
           = plt.figure()
circleAxe = fig.add subplot(2.2.1)
circleLn. = plt.plot([].[].'r-')
circleAxe.grid(True)
circleAxe.set xlim(-1.1)
circleAxe.set vlim(-1.1)
circleIn.set Tabel(0)
circleLg=circleAxe.legend()
circleFrec = 1
circleData = []
def circle(f.n):
    return np.exp(-1j*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalLn. = plt.plot([].[].'b-o')
signalAxe.grid(True)
signalAxe.set xlim(0.N/fs)
signalAxe.set ylim(-1,1)
signalFrec = 2
signalData=[]
```

```
signalData=[]
def signal(f.n):
    return np.cos(2*np.pi*f*n*1/fs)
tData=np.arange(0.N/fs.1/fs)
def init():
    return circleLn.circleLg.signalLn.
def update(n):
    global circleData.signalData
    circleData.append(circle(circleFrec,n))
    circleLn.set data(np.real(circleData),
                      np.imag(circleData))
    signalData.append(signal(signalFrec.n))
    signalLn.set data(tData[:n+1],signalData)
    if n==N-1:
        circleData=[]
        signalData=[]
    circleIn.set label(n)
    circleLg=circleAxe.legend()
    return circleLn.circleLg.signalLn.
ani=FuncAnimation(fig.update.N.init.interval=100 .
       blit=True.repeat=True)
plt.show()
```



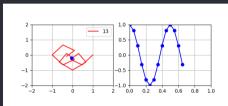


$e^{j2\pi ft}$ modulado por sin(t) y centro de masas



```
import numpy as np
import mathlotlib nyplot as plt
from matplotlib.animation import FuncAnimation
           = plt.figure()
           = 20
circleAxe = fig.add subplot(2.2.1)
circleLn. = plt.plot([].[].'r-')
circleAxe.grid(True)
circleAxe.set xlim(-1.1)
circleAxe.set vlim(-1,1)
circleIn.set Tabel(0)
circlel g=circleAxe.legend()
circleFrec = 1
circleData = []
def circle(f.n):
    return np.exp(-1j*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalLn, = plt.plot([],[],'b-o')
signalAxe.grid(True)
signalAxe.set xlim(0.N/fs)
signalAxe.set vlim(-1.1)
signalFrec = 2
signalData=[]
def signal(f.n):
    return np.cos(2*np.pi*f*n*1/fs)
```

```
def signal(f,n):
    return np.cos(2*np.pi*f*n*1/fs)
tData=np.arange(0.N/fs.1/fs)
def init():
    return circleLn, circleLg, signalLn.massLn
def update(n):
    global circleData, signalData
    circleData.append(circle(circleFrec.n)*signal(
            signalFrec.n))
    mass=np.average(circleData)
    massLn.set data(np.real(mass).
                    np.imag(mass))
    circleLn.set data(np.real(circleData),
                      np.imag(circleData))
    signalData.append(signal(signalFrec.n))
    signall n.set_data(tData[:n+1].signalData)
    if n==N-1:
        circleData = []
        signalData = []
    circleLn.set label(n)
    circleLg=circleAxe.legend()
    return circleLn.circleLg.signalLn.massLn
ani=FuncAnimation(fig.update.N.init.interval=10 .
       blit=True.repeat=True)
plt.show()
```







$e^{j2\pi ft}$ modulado por Sin(t) y centro de masas en f, DFT?

```
import numpy as np
import matplotlib.pyplot as plt
from mathlotlib animation import FuncAnimation
           = nlt.figure()
           = 28
circleAxe = fig.add subplot(2.2.1)
circleLn.massLn = plt.plot([],[],'r-',[],[],'bo')
circleAxe.grid(True)
circleAxe.set xlim(-1.1)
circleAxe.set vlim(-1.1)
circleFrec = np.arange(-fs/2,fs/2,fs/N)
circlein set label(circleFrec[0])
circleLg = circleAxe.legend()
circleData = []
    return np.exp(-1j*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalLn. = plt.plot([1.[1.'b-o')
signalAxe.grid(True)
signalAxe.set xlim(0,N/fs)
signalAve set vlim(-1.1)
signalFrec = 2
signalData=[]
def signal(f.n):
    return nn sin(2*nn ni*f*n*1/fs)
prom\Delta ve = fig. add. subplot(2.2.3)
promRLn.promILn.promMagLn.promPhaseLn = plt.plot([],[],'b-o'
promAxe.grid(True)
promAxe.set xlim(-fs/2.fs/2)
promAxe.set vlim(-1.1)
promData=np.zeros(N.dtvpe=complex)
```

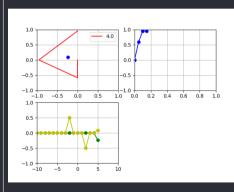
tData=np.arange(0,N/fs,1/fs)
Ing Pahlo Slavkin

```
tData=np.arange(0.N/fs.1/fs)
dof init():
    return circleLn.circleLq.signalLn.massLn.promRLn.promILn
    global circleData.signalData.promData.frecIter.circleFrec.
   circleData.append(circle(circleFrec[frecIter].n)*signal(
             signalFrec.n))
   mass=np.average(circleData)
   massLn.set data(np.real(mass),
                   np.imag(mass))
   circleIn set data(nn real(circleData).
                      np.imag(circleData))
   signalData.append(signal(signalFrec.n))
   signalLn.set data(tData[:n+1].signalData)
   promData[frecIter]=mass
   promRLn.set data(circleFrec[:frecIter+1],np.real(promData[:
             frecIter+11))
   promILn.set data(circleFrec[:frecIter+1].np.imag(promData[:
             frecTter+11))
    promMagLn.set data(circleFrec[:frecIter+1].np.abs(promData
   promPhaseln.set_data(circleFrec[:frecIter+11.np.angle(
         promData[:frecIter+1])/np.pi)
   if n==N-1:
       circleData = []
       signalData = []
       circleLn.set label(circleFrec[frecIter])
       circleLa=circleAxe.legend()
        if frecIter == N-1:
           ani.repeat=False
           frecIter+=1
   return circleLn.circleLq.signalLn.massLn.promRLn.promILn.
             promMagin.promPhasein.
```

ani=FuncAnimation(fig.update.N.init.interval=10 .blit=True.

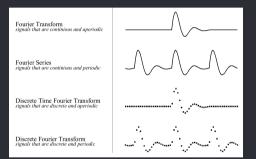
repeat=True)

nlt.show()



Transformada de Fourier

Diferentes tipos segun la señal



Time Duration		
Finite	Infinite	
Discrete FT (DFT)	Discrete Time FT (DTFT)	discr.
$X(k) = \sum_{n=0}^{N-1} x(n)e^{-j\omega_k n}$	$X(\omega) = \sum_{n=-\infty}^{+\infty} x(n)e^{-j\omega n}$	time
$k=0,1,\ldots,N-1$	$\omega \in [-\pi, +\pi)$	n
Fourier Series (FS)	Fourier Transform (FT)	cont.
$X(k) = \frac{1}{F} \int_0^P x(t)e^{-j\omega_k t} dt$	$X(\omega) = \int_{-\infty}^{+\infty} x(t)e^{-j\omega t}dt$	time
$k = -\infty, \dots, +\infty$	$\omega \in (-\infty, +\infty)$	t
discrete freq. k	continuous freq. ω	

$$X_k = \sum_{n=0}^{N-1} x_n e^{-rac{2\pi i}{N}kn} \qquad k=0,\ldots,N-1$$

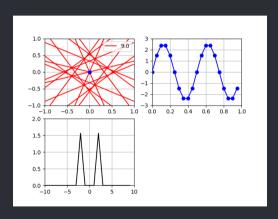
DFT

Densidad de potencia espectral



$$P_{sin} = \frac{}{2}$$
 $P_{sin} = \frac{2,5^2}{2}$
 $P_{sin} = 3,125W$
 $P = 1,56 + 1,56$

P = 3.125W

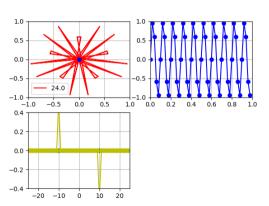


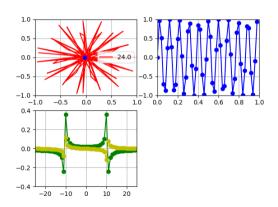
DFT

Fuga espectral (Spectral leakage)



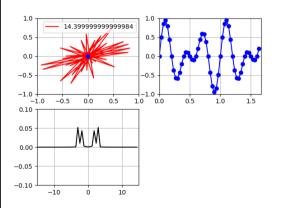




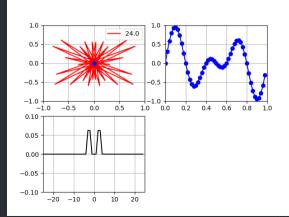


Resolucion espectral





f1=2 f2=3 fs = 50 N = 50



DFTDFT Zero padding



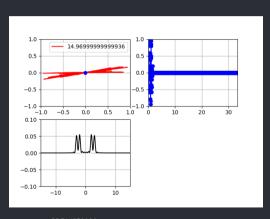
$$f1 = 2$$

$$f2 = 3$$

$$fs = 10$$

$$N = 50$$

$$Z = 950$$



DFT

Acelerada



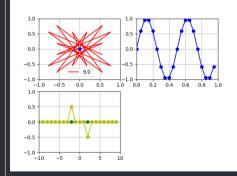
```
import numby as no
from matplotlib.animation import FuncAnimation
circleAxe = fig.add subplot(2.2.1)
circleLn.massLn = plt.plot([].[].'r-'.[].[].'bo')
circleAxe.grid(True)
circleAxe.set vlim(-1.1)
circleLo = circleAxe.legend()
   return np.exp(-11*2*np.pi*f*n*1/fs)
signalAxe.set vlim(-1.1)
   return np.sin(2*np.pi*f*n*1/fs)
promAxe = fig.add subplot(2.2.3)
promRin.promIin.promMagin.promPhasein = plt.plot([],[],'b-o',[],[],'r-o',[],[],'k-'
promAxe.grid(True)
promAxe.set xlim(-fs/2.fs/2)
prompataenn zeros(N. dtype=complex)
tData=np.arange(0.N/fs.1/fs)
   return circleLn.circleLq.signalLn.massLn.promRLn.promILn
   global circleData,signalData,promData,frecIter,circleFrec.circleLo
```

```
circlestes | 1
signalitis = | 1
signalitis = | 1
for n.in rego(N)
signalitis appendix policitatis
signali
```

frectter==1
return circletn,circletg,signalln,massin,promRin,promRin,promMagin,promPhaseln,
ami=Funchimation(fin undate N.imit.interval=100.blit=True_recent=True)

ani repeat=False

nlt.show()



Síntesis

Como reconstruyo la señal en el tiempo



```
import numby as no
import mathlotlib nyplot as plt
from matplotlib.animation import FuncAnimation
          = plt.figure()
          = 100
          = 100
circleAxe = fig.add subplot(2.2.1)
circleLn.massLn. = plt.plot([].[].'r-'.[].[].'bo')
circleAxe.grid(True)
circleAxe.set xlim(-1.1)
circleAve.set vlim(-1.1)
circleFrec = np.arange(-fs/2,fs/2,fs/N)
circleLn.set label(circleFrec[0])
circleLg=circleAxe.legend()
circleData = []
frecIter = A
    return np.exp(-1i*2*np.pi*f*n*1/fs)
    return c*np.exp(-1i*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalln. = plt.plot([].[].'b-')
signalAxe.grid(True)
signalAxe.set xlim(0.N/fs)
signalAxe.set vlim(-1.1)
signalFrec = 2
signalData=[]
def signal(f,n):
```

return np.sin(2*np.pi*f*n*1/fs)

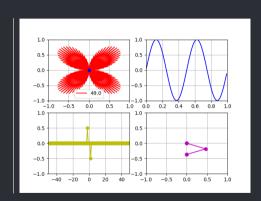
```
return np.sin(2*np.pi*f*n*1/fs)
promAxe = fig.add subplot(2.2.3)
promRLn, promILn, = plt.plot([],[],'q-o',[],[],'y-o')
promAxe.grid(True)
promAxe.set xlim(-fs/2,fs/2)
promAxe.set ylim(-1,1)
promData=np.zeros(N.dtyne=complex)
                  = fig.add subplot(2.2.4)
inversaLn, = plt.plot([],[],'m-o')
inversaAxe.grid(True)
inversaAxe.set xlim(-1.1)
inversalize set vlim(-1.1)
inversaData = []
tData=np.arange(0.N/fs.1/fs)
    return circleLn,circleLq,signalLn,massLn,promRLn,promILn,inversaLn
def undateF(n):
    global promData,fData,inversaData,frecIter
    if aniT.repeat==True:
        return inversaln.
    inversaData=[0]
        inversaData.append(inversaData[-1]+circleInv(circleFrec[f].frecIter.promData[f]))
    inversaln.set data(np.imag(inversaData).np.real(inversaData))
    frecIter+=1
    if frecTter==N:
        frecTter=A
    return inversaln.
```

Síntesis

Como reconstruyo la señal en el tiempo



```
def updateT(nn):
   global circleData.signalData.promData.frecIter.circleFrec.circleLo
   circleData = []
   signalData = []
       circleData.append(circle(circleFrec[frecIter],n)*signal(signalFrec,n))
       mass=np.average(circleData)
       signalData.append(signal(signalFrec.n))
       promData[frecIter]=mass
   massLn.set data(np.real(mass)
                   np.imag(mass))
   circleLn.set data(np.real(circleData),
                     np.imag(circleData))
   signalLn.set data(tData[:n+1].signalData)
   promRLn.set data(circleFrec[:frecIter+1],np.real(promData[:frecIter+1]))
   promILn.set data(circleFrec[:frecIter+1].np.imag(promData[:frecIter+1]))
   circleLn.set label(circleFrec[frecIter])
   circleLg=circleAxe.legend()
   if frecIter == N-1:
        aniT.repeat=False
        frecIter+=1
   return circleLn.circleLg.signalLn.massLn.promRLn.promILn.
aniT=FuncAnimation(fig.updateT.N.init.interval=10 .blit=True.repeat=True)
aniF=FuncAnimation(fig.updateF.N.init.interval=30 .blit=True.repeat=True)
nlt.show()
```



$$x_n = rac{1}{N} \sum_{k=0}^{N-1} X_k e^{rac{2\pi i}{N} k n} \qquad n = 0, \dots, N-1.$$

Señales complejas como entrada?



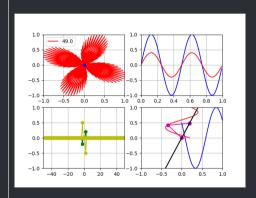
```
import numby as no
import matplotlib.pvplot as plt
from matplotlib.animation import FuncAnimation
           = plt.figure()
          = 100
circleAxe = fig.add subplot(2,2,1)
circleLn.massLn. = plt.plot([],[],'r-',[],[],'bo')
circleAxe.grid(True)
circleAxe.set xlim(-1.1)
circleAxe.set vlim(-1.1)
circleFrec = np.arange(-fs/2.fs/2.fs/N)
circleLn.set label(circleFrec[0])
circleLg=circleAxe.legend()
circleData = []
frecIter = 0
def circle(f.n):
    return np.exp(-1j*2*np.pi*f*n*1/fs)
    return c*np.exp(-1i*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalRLn.signalILn = plt.plot([],[],'b-',[],[],'r-')
signalAxe.grid(True)
signalAxe.set xlim(0.N/fs)
signalAxe.set vlim(-1.1)
signal Frec = 2
signalData=[]
def signal(f.n):
    return np.sin(2*np.pi*f*n*1/fs)+0.4i*np.sin(2*np.pi*f*n*1/fs)
```

```
return np.sin(2*np.pi*f*n*1/fs)+0.4i*np.sin(2*np.pi*f*n*1/fs)
promAxe = fig.add subplot(2.2.3)
promRLn.promILn. = plt.plot([].[].'g-o'.[].[].'v-o')
promaxe.grid(True)
promAxe.set xlim(-fs/2.fs/2)
promAxe.set vlim(-1.1)
promData=np.zeros(N.dtype=complex)
                  = fig.add subplot(2.2.4)
inversaln.penIn.penIln.penIln = plt.plot([],[],'m-o',[],[],'k-',[],[],'b-',[],[],'r-')
inversalize grid(True)
inversaAxe.set xlim(-1.1)
inversaAxe.set vlim(-1.1)
inversaData, penData= [],[]
tData=np.arange(θ,N/fs,1/fs)
    return circleln.circlelg.signalRLn.signalILn.massLn.promRLn.promILn.inversaLn.penILn.penRLn.
def undateF(n):
    global promData,fData,vectorData,frecIter,penData
    if aniT.repeat==True:
        return inversaln.
    vectorData=[0]
        vectorData.append(vectorData[-1]+circleInv(circleFrec[f].frecIter.promData[f]))
    inversaln.set data(np.imag(vectorData).np.real(vectorData))
   penData.insert(0.vectorData[-1])
   traceData=penData[0:N//2]
    t=np.linspace(θ.1.len(traceData))
   penRLn.set data(t.np.real(traceData))
   penILn.set_data(np.imag(traceData).t)
```

Señales complejas como entrada?



```
penILn.set data(np.imag(traceData).t)
   penLn.set data(np.imag(penData),np.real(penData))
   frecIter+=1
   if frecTter==N:
       frecIter=0
   return inversal n. penl n. penTl n. penRl n.
def updateT(nn):
   global circleData.signalData.promData.frecIter.circleFrec.circleLg
   circleData = []
   signalData = []
       circleData.append(circle(circleFrec[frecIter],n)*signal(signalFrec.n))
       mass=np.average(circleData)
       signalData.append(signal(signalFrec,n))
       promData[frecIter]=mass
   massLn.set data(np.real(mass),
                    np.imag(mass))
   circleLn.set data(np.real(circleData).
                     np.imag(circleData))
   signalRLn.set data(tData[:n+1].np.real(signalData))
   signalILn.set data(tData[:n+1].np.imag(signalData))
   promRLn.set data(circleFrec[:frecIter+1],np.real(promData[:frecIter+1]))
   promILn.set data(circleFrec[:frecIter+1].np.imag(promData[:frecIter+1]))
   circleLn.set label(circleFrec[frecIter])
   circleLa=circleAxe.legend()
   if frecTter == N-1:
        aniT.repeat=False
        frecIter+=1
   return circleLn.circleLn.signalRLn.signalILn.massLn.promRLn.promILn.
aniT=FuncAnimation(fig,updateT,N,init,interval=10 ,blit=True,repeat=True)
aniF=FuncAnimation(fig.updateF.N.init.interval=30 .blit=True.repeat=True)
nlt.show()
```



Un conejo como entrada?



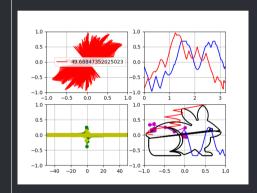
```
import numpy as no
import mathlotlib nymlot as nlt
from mathlotlib animation import FuncAnimation
           = plt.figure()
           = 180
conejo=np.load("conejo.npy")[::1]
def signal(f.n):
circleAxe = fig.add subplot(2,2,1)
circleLn, massLn, = plt.plot([],[],'r-',[],[],'bo')
circleAxe.grid(True)
circleAxe.set xlim(-1,1)
circleAxe.set ylim(-1,1)
circleFrec = np.arange(-fs/2,fs/2,fs/N)
circleLn.set label(circleFrec[0])
circleLa=circleAxe.legend()
circleData = []
frecIter = 0
    return np.exp(-1i*2*np.pi*f*n*1/fs)
def circleInv(f.n.c):
    return c*np.exp(-1i*2*np.pi*f*n*1/fs)
signalAxe = fig.add subplot(2.2.2)
signalRLn.signalILn = plt.plot([].[].'b-'.[].[].'r-')
signalAxe.grid(True)
signalAxe.set xlim(θ,N/fs)
```

```
signalAxe.set xlim(0.N/fs)
 signalAxe.set vlim(-1.1)
 signalFrec = 2
 signalData=[]
 #def signal(f.n):
 # return np.sin(2*np.pi*f*n*1/fs)+0.4j*np.sin(2*np.pi*f*n*1/fs)
 promAxe = fig.add subplot(2.2.3)
 promRLn, promILn, = plt.plot([],[],'q-o',[],[],'y-o')
 promAxe.grid(True)
 promake set xlim(-fs/2.fs/2)
promAxe.set vlim(-1.1)
 promData=np.zeros(N.dtype=complex)
                                                          = fig.add subplot(2,2,4)
 inversal, penk, p
 inversaAxe.grid(True)
 inversaAxe.set xlim(-1.1)
 inversaAxe.set vlim(-1.1)
 inversaData.penData= [1.[]
 tData=np.arange(0.N/fs.1/fs)
             return circleln.circlelg.signalRLn.signalILn.massLn.promRLn.promILn.inversaLn.penILn.penRLn.
 def undateF(n):
             global promData.fData.vectorData.frecIter.penData
             if aniT.repeat==True:
                          return inversaln.
             vectorData=[A]
                          vectorData.append(vectorData[-1]+circleInv(circleFrec[f],frecIter,promData[f]))
            inversal n. set data(np.imag(vectorData).np.real(vectorData))
```

Un conejo como entrada?

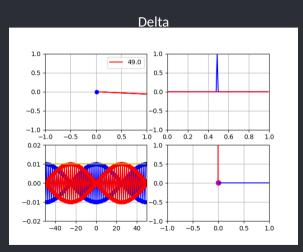


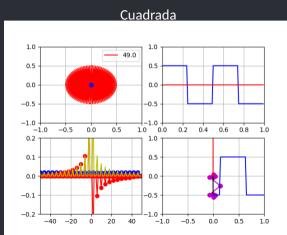
```
inversaLn.set data(np.imag(vectorData).np.real(vectorData))
   nenData_insert(0.vectorData[-11)
   traceData=penData[0:N//2]
   t=np.linspace(0.1.len(traceData))
   penRLn.set data(t.np.real(traceData))
   penII n. set_data(np.imag(traceData).t)
   nenin set data(nn.iman(nenData).nn.real(nenData))
   frecIter+=1
   if frecTter==N:
       frecIter=0
    return inversaLn, penLn, penILn, penRLn,
def undateT(nn):
   global circleData signalData promData frecIter circleFrec circleIn
   circleData = []
   signalData = []
       circleData.append(circle(circleFrec[frecIter].n)*signal(signalFrec.n))
       mass=np.average(circleData)
       signalData.append(signal(signalFrec,n))
       nromData[frecIter]=mass
   massLn.set data(np.real(mass).
                    np.imag(mass))
   circleLn.set data(np.real(circleData),
                     np.imag(circleData))
   signalRLn.set data(tData[:n+1].np.real(signalData))
   signalILn.set data(tData[:n+1].np.imag(signalData))
   promRLn.set data(circleFrec[:frecIter+1].np.real(promData[:frecIter+1]))
   promILn.set data(circleFrec[:frecIter+1].np.imag(promData[:frecIter+1]))
   circleLn.set label(circleFrec[frecIter])
   circleLa=circleAxe.legend()
   if frecTter == N-1:
        aniT.repeat=False
        frecIter+=1
   return circleLn,circleLq,signalRLn,signalILn,massLn,promRLn,promILn,
aniT=FuncAnimation(fig.updateT.N.init.interval=10 .blit=True.repeat=True)
aniF=FuncAnimation(fig.updateF.N.init.interval=30 .blit=True.repeat=True)
nlt.show()
```



DFT<>IDFT

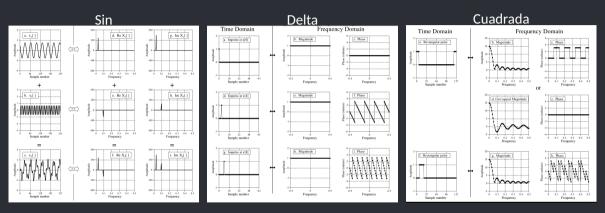
Transformadas relevantes





DFT<>IDFT

Transformadas relevantes



DFT<>IDFT

1.0

0.5

0.0

-0.5

-1.0

0.2 0.1

0.0

-0.1

-0.2

-1.0 -0.5 0.0 0.5 1.0 0.0 0.2 0.4 0.6 0.8

Transformadas relevantes



49.0

0.5

0.0

-0.5

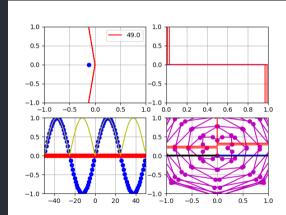
0.5

0.0

-0.5

-0.5 0.0 0.5

Congujado



-20

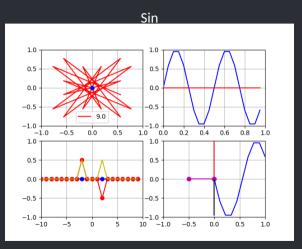
ò

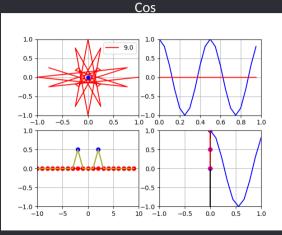
-40

20

1.0

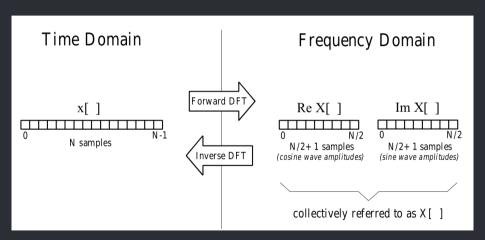
DFT para señales reales RDFT





DFT para señales reales RDFT





RDFT

Análisis en la CIAA



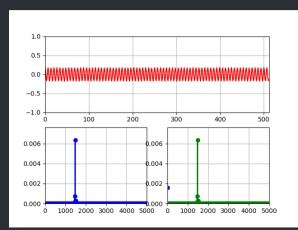
```
#include "sapi.h"
#include "arm math.h"
#define MAX FFT LENGTH 2848
                                    // maxima longitud para la fft v chunk de samples
#define BITS 18
                                    // cantidad de hits usado para cuantizar
int16 t fftLength = 32:
int16 t adc [ MAX FET LENGTH 1:
                                    // quarda los samples
g15 t fftIn [ MAX FFT LENGTH 1:
                                    // guarda conja de samples en 015 como in para la fft la fft corromne
          los datos de la entrada!
q15 t fftOut[ MAX FFT LENGTH*2 ]; // salida de la fft
g15 t fftMag[ MAX FFT LENGTH/2+1 1: // magnitud de la FFT
uint32 t maxIndex = 0:
                                    // indexador de maxima energia por cada fft
g15 t maxValue = 0:
                                    // maximo valor de energia del bin por cada fft
arm rfft instance ol5 S:
uint16 t sample = 0:
                                    // contador para samples
int main ( void ) f
   boardConfig
   uartConfig
                      ( UART USB. 460800
   adcConfig
                      ( ADC ENABLE
   cyclesCounterInit ( EDU CIAA NXP CLOCK SPEED ):
      cvclesCounterReset():
                                                                                     // inicializa el
               conteo de ciclos de reloi
      uartWriteByteArray ( UART USB .(uint8 t* )&adc[sample]
                                                                .sizenf(adc[Al) ): // envia el sample
                ANTERTOR
      uartWriteByteArray ( UART USB .(uint8 t* )&fftOut[sample] .sizeof(fftOut[0])): // envia la fft del
               sample ANTERIO
      //TODO hay que mandar fftLength/2 "+1" y solo estoy mandando fftLength/2, revisar
                                                                                     // PTSA el sample que
      adc[sample] =(((int16 t )adcRead(CH1)-512)>>(10-BITS))<<(6+10-BITS);
                 se acaba de mandar con una nueva muestra
      fftIn[sample] = adc[sample]:
                                                                                     // copia del adc
               porque la fft corrompe el arreglo de entrada
                                                                                     // si es el ultimo
      if ( ++sample==fftLength ) {
```

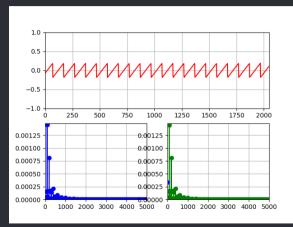
```
// arranca de nuevo
  sample = \theta:
  uartWriteByteArray ( UART USB .(uint8 t* )&maxValue .2):
  uartWriteByteArray ( UART USB , (uint8 t* )&maxIndex ,2);
  uartWriteByteArray ( UART USB , "header" ,6 );
                                                                               // manda el header
            que casualmente se llama "header" con lo que arranca una nueva trama
  uartWriteRyteArray ( HART HSR (uint8 t* )&fftLength .sizeof(fftLength)): // manda el largo de
            la fft que es variable
  arm rfft init q15 ( &S ,fftLength ,0 ,1 );
                                                                               // inicializa una
            estructira que usa la funcion fft para procesar los datos. Notar el /2 para el largo
                    ( &S .fftIn
  arm rfft d15
                                    .fftOut ):
                                                                               // por fin.. ejecuta
            la rfft REAL fft
  arm cmplx mag squared q15 ( fftOut ,fftMag ,fftLength/2+1 );
  arm max g15 ( fftMag .fftLength/2+1 .&maxValue .&maxIndex ):
  apioToggle( LEDR);
  if ( gpioRead(TEC1 )==0) {
     gpioToggle(LEDB):
     if((fftlength<<=1)>MAX_FFT_LENGTH)
         fftLength=32:
      while(gpioRead(TEC1)==0)
while(cyclesCounterRead()< 20400) //clk de 204000000 => 10k samples x seg.
```

RDFT

Análisis en la CIAA







Bibliografía

Libros, links y otro material

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