$$\frac{d\Omega(t)}{dt} = \mu N - \beta \Omega(t) \frac{S(t)}{N} - \mu \Omega(t)$$

$$\frac{dS(t)}{dt} = \beta \Omega(t) \frac{S(t)}{N} - (\mu + \chi)S(t)$$

$$\frac{dO(t)}{dt} = \chi S(t) - \mu \Omega(t)$$

$$\frac{dO(t)}{dt} = \chi S(t)$$

$$\frac{dO(t)}{dt}$$

$$\frac{dP(t)}{dt} = \mu N - \beta P(t) \frac{S(t)}{N} - \alpha P(t) \frac{L(t)}{N} - (\mu + \mu_t)P(t) + \delta Q(t)$$

$$\frac{dL(t)}{dt} = \alpha P(t) \frac{L(t)}{N} + \beta P(t) \frac{S(t)}{N} - (\mu + \mu_L + k + \frac{3}{2})L(t)$$

$$\frac{dS(t)}{dt} = \frac{1}{2}L(t) - (\mu + \mu_S + \frac{3}{2})S(t)$$

$$\frac{dS(t)}{dt} = \frac{1}{2}L(t) + \frac{1}{2}S(t) - (\mu + \mu_S + \frac{3}{2})Q(t)$$
Dividing by N:
$$\frac{dX(t)}{dt} = \mu - \beta X(t)Y(t) - \alpha X(t)L(t) - (\mu + \mu_P)X(t) + \delta Z(t)$$

$$\frac{dL(t)}{dt} = \alpha X(t)L(t) + \beta X(t)Y(t) - (\mu + \mu_L + k + \frac{3}{2})L(t)$$

$$\frac{dL(t)}{dt} = \kappa L(t) + \delta Y(t) - (\mu + \mu_S + \frac{3}{2})L(t)$$
where $L(t) = \frac{L(t)}{N}$