#### Metacommunities, assembly, $\alpha$ and $\gamma$

February 10, 2015

## Species distribution across multiple localities

#### Questions

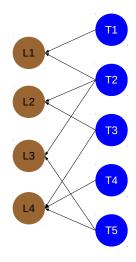
- ▶ How do mammal species traits effect co-occurrence patterns?
- What is the expected proportion of the mammal metacommunity pool present at a single locality?
- Have these relationships changed over the Cenozoic?

#### System

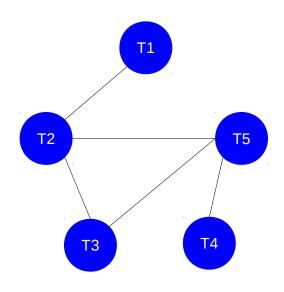
- Record
  - North American Cenozoic
  - 2 My bins
- Units
  - mammal species
  - 2x2 Lat-Long equal area grid cells
- Covariates
  - taxa: diet, locomotor, body size
  - localities: ??
- Hierarchical effects
  - spatial relation
  - phylogeny

- Relations to community assembly
- Covariate hypotheses
  - carnivore greatest diet co-occur
  - ground dwelling > scansorial > arboreal
  - ▶ body size: positive
- Hierarchical effect interpretations
  - spatial effect: structured vs random
  - phylogeny: attract vs repel

## Bipartite network



#### One-mode network



#### Modeling co-occurrence

#### Assumption and setup

 $y_i$ : # co-occurring species with species i per # of localities.

Any species is equally likely to co-occur with any other species.

Consequence, node degree follows Poisson distribution (Erdos-Renyi random graph).

## Modeling phylogenetic effect

#### Definition

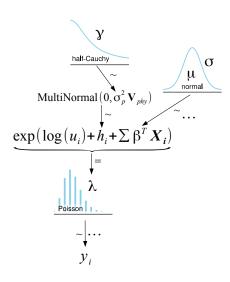
Assuming Brownian motion, effect drawn from multivariate normal distribution.

$$h \sim \mathcal{N}(0, \sigma_p^2 \mathbf{V_p})$$

- ▶ Covariance known up to constant,  $\sigma_p$ .
- $ightharpoonup V_p$  phylogenetic covariance matrix (shared branch lengths).

Follows Lynch 1991 Evolution, Housworth et al. 2004 Am. Nat.

### Species co-occurrence model



 $y_i \sim \text{Poisson}(\lambda)$   $h_i \sim \text{MultiNormal}(0, \Sigma_p)$   $\Sigma_p = \sigma_p^2 V_{phy}$   $\sigma_p \sim \text{half-Cauchy}(2.5)$  $\beta \sim \text{Normal}(0, 10)$ 

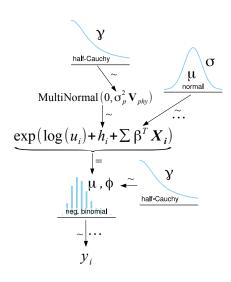
#### Modeling co-occurrence

#### Improvement

Poisson assumption  $\frac{Var[x]}{E[x]} = 1$ .

Relax assumption by modeling overdisperssion  $\phi$ .

### Species co-occurrence model redux



 $y_i \sim \text{NegBinom}(\mu, \phi)$   $\phi \sim \text{half-Cauchy}(2.5)$   $h_i \sim \text{MultiNormal}(0, \Sigma_p)$   $\Sigma_p = \sigma_p^2 V_{phy}$   $\sigma_p \sim \text{half-Cauchy}(2.5)$  $\beta \sim \text{Normal}(0, 10)$ 

## Modeling locality richness

#### Assumption and setup

 $y_i$ : # species at locality i per # of species.

 $y_i$  drawn from Poisson (or Negative Binomial) distribution.

Localities are from non-uniform lattice (areal units).

### Spatial effect

#### Definition

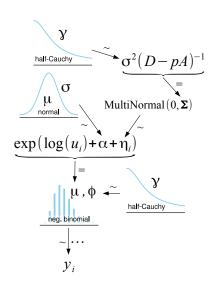
Autoregressive prior; spatial effect drawn from multivariate normal.

$$s \sim \mathcal{N}(0, \sigma_s^2 (D - pA)^{-1})$$

- $\sigma_s$  is variance of spatial effect (size).
- D is diagonal matrix of neighbor count.
- A is adjacency matrix of localities.
- p is "strength" of spatial effect.

Bunch of assorted problems regarding propriety. See Banerjee et al. 2004 book.

### Locality richness model



 $y_i \sim \text{NegBinom}(\mu, \phi)$   $\phi \sim \text{half-Cauchy}(2.5)$   $\alpha \sim \text{Normal}(0, 10)$   $\eta_i \quad \text{MultiNormal}(\vec{0}, \Sigma)$   $\Sigma = \sigma^2 (D - pA)^{-1}$  $\sigma \sim \text{half-Cauchy}(2.5)$ 

# Analysis framework

