# Practicals in Quantitaive Genetic Analyses

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# Introduction

In these practicals we will be analysing quantitative traits observed in a mice population. The mouse data consist of phenotypes for traits related to growth and obesity (e.g. body weight, glucose levels in blood), pedigree information, and genetic marker data. The practicals will be a mix of theoretical and practical exercises in R that are used for illustrating/applying the theory presented in the lectures and corresponding notes.

- Practical 1: Use R for Analysing Quantitative Traits
- Practical 2: Basic Quantitative Genetics illustrated in the mouse data
- Practical 3: Estimation of Genetic Parameters for traits in the mouse data
- Practical 4: Estimation of Breeding Values for traits in the mouse data
- Practical 5: Estimation of Genomic Breeding Values for traits in the mouse data

# Mouse data

The M16 mouse was established as an outbred animal model of early onset polygenic obesity and diabesity. This was done by selection for 3- to 6-week weight gain for 27 generations from an outbred ICR base population. Breeding criterion was within-litter selection for the male and female with the largest weight gain from 3 to 6 weeks of age. An ICR control line was maintained in parallel, with random mating from generation to generation but maintaining a similar effective population size. Mice from the M16 line ar elarger at all ages and have increased body fat percentage, fat cell size, fat cell numbers, and organ weights when compared with ICR. Mice from the M16 line are larger at all ages and have increased body fat percentage, fat cell size, fat cell numbers, and organ weights when compared with ICR. These mice also exhibit hyperphagia, accompanied by moderate obesity, and are hyperglycemic, hyperinsulinemic, and hypercholesterolemic.

The **ICR** mouse is a strain of albino mice originating in SWISS and selected by Dr. Hauschka to create a fertile mouse line. Because mice of this strain have been sent to various places from the Institute of Cancer Research in the USA, the strain was named ICR after the initial letters of the institute. Mice of this strain are relatively large albinos with a gentle nature that grow well. The ICR mouse is a general-purpose model used for studies in a wide range of fields including toxicity, pharmacology, drug efficacy, and immunology.

A large **F2** population (n=1181) was established by crossing the M16 and ICR lines (for a recent description of relevant phenotypes in the parental lines, see https://onlinelibrary.wiley.com/doi/epdf/10. 1038/oby.2004.176). Twelve F1 families resulted from six pair matings of M16 males x ICR females and six pair matings of the reciprocal cross. A total of 55 F1 dams were mated to 11 F1 sires in sets of five F1 full sisters mated to the same F1 sire. These same specific matings were repeated in three consecutive replicates. Thus, the F2 population consisted of 55 full-sib families of up to 24 individuals each and 11 sire families families of up to 120 individuals each. Actual numbers of mice within families varied slightly due to a small number of failed pregnancies. All litters were standardized at birth to eight pups, with approximately equal representation of males and females.

More information about the mouse data can be found in the following publications:

https://onlinelibrary.wiley.com/doi/epdf/10.1038/oby.2004.176

https://www.ncbi.nlm.nih.gov/pmc/articles/PMC1449794/

# Practical 1: Use R for Analysing Quantitative Traits

## Time schedule of practical session 1:

Time	Activity
11:15	Questions to lecture and multiple-choice questions
11:25	Introduction to R-studio
11:45	Assignments to groups – work with exercises
12:00	Break
12:35	Prepare final words of exercises in each group
12:45	Present final words
12:55	Repeat multiple-choice questions
13:00	End of practical session 1

# **Introduction:**

In this practical we use R for explorative data analyses of two quantitative traits, body weight and blood glucose levels, observed in the F2 mouse population. These explorative data analyses includes computation of basic descriptive statistics such as mean, and variance used to describe each of these traits. Distribution plots (e.g., histogram) will be used to visualize whether the trait phenotypes follow a normal distribution. Boxplots will be used to spot potential effects of explanatory variables. Furthermore relationships between traits and variables will be characterized in terms of correlations and linear relationships.

# Let's get started to explore our mouse data

One of the first thing to do is to explore the data used in the analysis. The goal is to understand the variables, how many records the data set contains, how many missing values, what is the variable structure, what are the variable relationships and more. Several commands/functions will be used. To read more about a specific function (e.g., str) write ?str.

The mouse data set can be loaded using the following command:

```
mouse <- readRDS(url("https://github.com/psoerensen/bgcourse/raw/main/data/mouse.rds"))</pre>
```

Question 1: How many observations and which variables do we have in the data set? To get a fast overview of the data set you are working with you can use the str function:

```
str(mouse)
## 'data.frame': 1177 obs. of 6 variables:
```

```
## 'data.frame': 1177 obs. of 6 variables:
## $ sire: Factor w/ 11 levels "25","28","34",..: 6 6 6 6 6 6 6 6 6 6 ...
## $ dam : Factor w/ 55 levels "26","27","29",..: 8 8 8 8 8 8 8 8 8 8 8 ...
## $ sex : Factor w/ 2 levels "Female","Male": 1 1 1 1 2 2 2 2 1 1 ...
## $ reps: Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 2 2 ...
```

```
## $ Gl : num 187 136 115 125 112 190 169 159 111 89 ...
## $ BW : num 36.6 33.3 42.1 37.1 38.4 ...
```

The two quantitative traits we will be analysing are glucose levels in the blood (Gl) and body weight (BW) measured in the mice at 8 weeks of age. A more detailed view of the two quantitative traits in the data.frame is provided by the summary function:

```
summary(mouse[,5:6])
```

```
BW
##
          Gl
##
           : 65.0
                           :23.04
   Min.
                   Min.
   1st Qu.:121.0
                    1st Qu.:34.06
##
   Median :139.0
                    Median :38.32
   Mean
           :144.2
                    Mean
                           :38.72
##
   3rd Qu.:164.0
##
                    3rd Qu.:43.40
  Max.
           :292.0
                           :60.28
##
                    Max.
```

Question 2: What is the mean and variance of body weight and blood glucose levels? Use the mean and var functions to compute the mean and variance two traits:

### Answer:

## [1] 1150.66

```
weight <- mouse[,"BW"]
glucose <- mouse[,"G1"]
mean(weight)

## [1] 38.72392

mean(glucose)

## [1] 144.2234

var(weight)

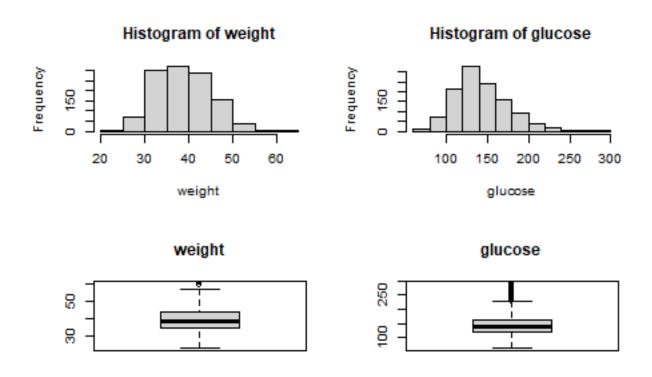
## [1] 37.84458

var(glucose)</pre>
```

Question 3: How are the phenotypes of weight and glucose distributed? Use the histogram and boxplot functions to visualize the distribution the two traits:

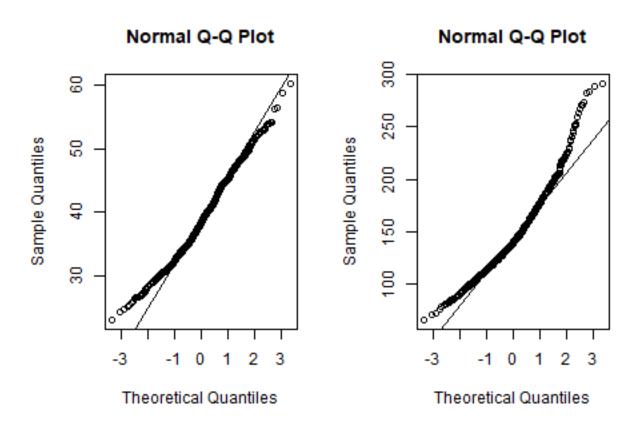
### Answer:

```
layout(matrix(1:4,ncol=2,byrow=TRUE))
hist(weight)
hist(glucose)
boxplot(weight, main="weight")
boxplot(glucose, main="glucose")
```



Question 4: Are the phenotypes of weight and glucose normally distributed? Use the qqnorm function to create a quantile-quantile (QQ) plot of the trait values. Use the qqline function to add a line to a "theoretical," by default normal, quantile-quantile plot:

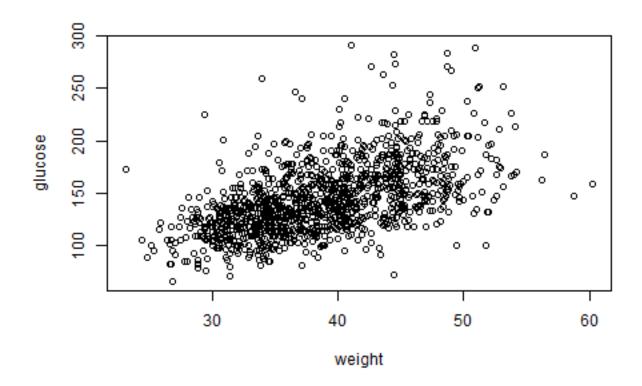
```
layout(matrix(1:2,ncol=2))
qqnorm(weight)
qqline(weight)
qqnorm(glucose)
qqline(glucose)
```



Question 5: Is there a relationship between the phenotypes of weight and glucose? Make a scatter plot of the 2 traits using the plot function. Compute the correlation using the cor function and perform a statistical test to assess the significance of correlation between values of weight and glucose using the cor.test function:

Answer:

plot(weight,glucose)



```
cor(weight,glucose)
```

## [1] 0.5440533

cor.test(weight,glucose)

```
##
## Pearson's product-moment correlation
##
## data: weight and glucose
## t = 22.227, df = 1175, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.5025357 0.5830674
## sample estimates:
## cor
## 0.5440533</pre>
```

Let us explore the family structure. Use the table function to determine the family size for sires and dams:

### table(mouse\$sire)

```
## ## 25 28 34 40 51 63 69 72 78 79 85 ## 115 114 107 95 110 103 103 119 119 118 74
```

### table(mouse\$dam)

```
## 26 27 29 30 31 32 33 35 36 37 38 39 41 42 43 44 45 46 47 48 49 50 52 53 54 55 ## 24 16 23 24 24 24 24 25 16 16 24 23 16 24 24 16 16 23 16 16 15 16 24 ## 56 57 58 59 60 61 62 64 65 66 67 68 70 71 73 74 75 76 77 80 81 82 83 84 86 87 ## 16 23 24 21 24 24 24 24 25 22 15 19 23 24 23 24 24 24 23 24 24 24 26 23 24 24 26 26 27 ## 88 89 90 ## 24 24 24 20
```

Question 6: What are the min and max family size? Use the table and min or max functions to determine the min/max family size for sires and dams:

#### Answer:

```
min(table(mouse$sire))

## [1] 74

max(table(mouse$sire))

## [1] 119

min(table(mouse$dam))

## [1] 15

max(table(mouse$dam))
```

Question 7: Does family influence the traits? Use the boxplot function to visualize the potential effect of family on the two traits:

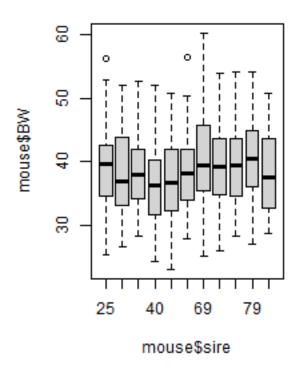
## Answer:

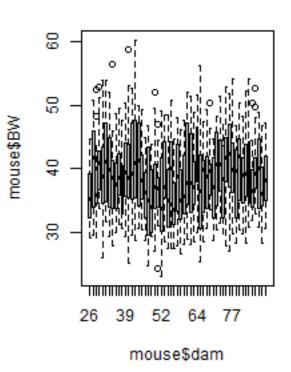
## [1] 24

```
layout(matrix(1:2,ncol=2))
boxplot(mouse$BW~mouse$sire, main="Paternal families")
boxplot(mouse$BW~mouse$dam, main="Maternal families")
```

# Paternal families

# **Maternal families**





Question 8: How many males and females?

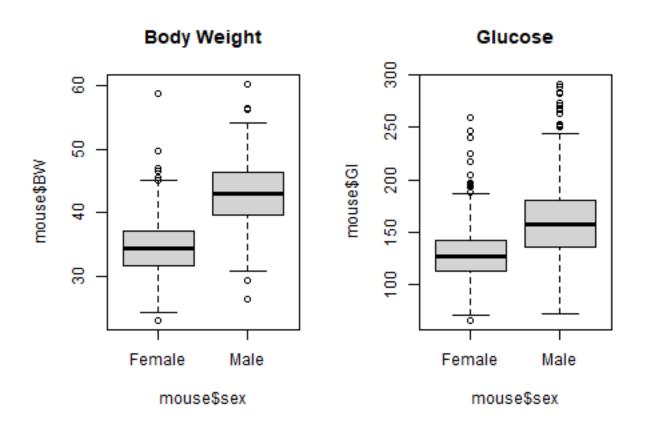
Answer:

# table(mouse\$sex)

```
## ## Female Male ## 589 588
```

Question 9: Does gender influence the traits? Use the boxplot function to visualize the potential effect of gender on the two traits:

```
layout(matrix(1:2,ncol=2))
boxplot(mouse$BW~mouse$sex, main="Body Weight")
boxplot(mouse$Gl~mouse$sex, main="Glucose")
```



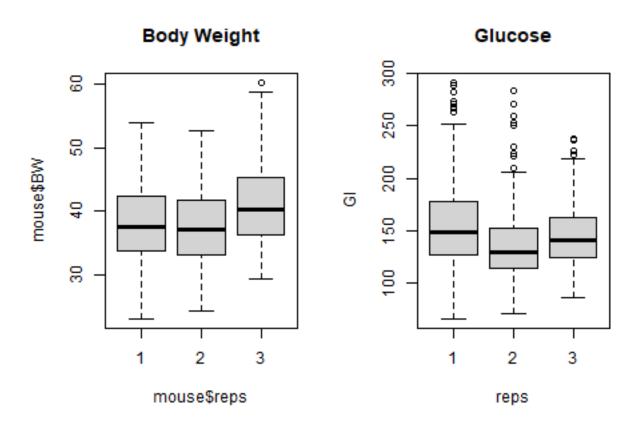
Question 10: How many observations in each replicate?

Answer:

## table(mouse\$reps)

Question 11: Does replicate influence the phenotype of weight and glucose? Use the boxplot function to visualize the potential effect of replicate on the two traits:

```
layout(matrix(1:2,ncol=2))
boxplot(mouse$BW~mouse$reps, main="Body Weight")
boxplot(Gl~reps, main="Glucose", data=mouse)
```



The exploratory data analysis is the process of analyzing and visualizing the data to get a better understanding of the data. It is not a formal statistical test.

Which factors should we include in the statistical model? To best answer these question we can fit a linear model that include these factors (sire, dam, sex, reps) in the model. This can be done using the 1m function:

```
fit <- lm(BW~sire+dam+sex+reps, data=mouse)</pre>
```

To test the effect of the variables in the model use the anova function on the fit object from the lm function:

```
anova(fit)
```

Question 12: Do genetic factors influence the traits? Look at the output of the anova function.

#### Answer:

# Some useful links explaining how to use R for basic concepts in statistics:

```
http://www.r-tutor.com/elementary-statistics/probability-distributions/normal-distribution http://www.r-tutor.com/elementary-statistics/numerical-measures http://www.r-tutor.com/elementary-statistics/numerical-measures/mean http://www.r-tutor.com/elementary-statistics/numerical-measures/variance http://www.r-tutor.com/elementary-statistics/numerical-measures/standard-deviation http://www.r-tutor.com/elementary-statistics/numerical-measures/covariance http://www.r-tutor.com/elementary-statistics/numerical-measures/correlation-coefficient http://www.r-tutor.com/elementary-statistics/numerical-measures/correlation-coefficient http://www.r-tutor.com/elementary-statistics/simple-linear-regression http://www.r-tutor.com/elementary-statistics/multiple-linear-regression http://www.r-tutor.com/elementary-statistics/analysis-variance https://antoinesoetewey.shinyapps.io/statistics-202/
```

# Practical 2: Basic Quantitative Genetics

# Time schedule of practical session 2:

11:15	Question to lectures, multiple-choice question and follow up on previous multiple choice questions
11:30	Today's exercise and assignment to groups
12:00	15 minutes break
12:30	Go through excercises using final word
12:50	Repeat multiple-choice questions
13:00	End of practical session 2

# **Introduction:**

In this practical we use R for explorative data analyses of two quantitative traits, body weight and blood glucose levels, observed in the F2 mouse population. We will be characterizing and investigating the potential effects of a single marker locus. This includes computation of allele and genotype frequencies, evaluating different genetic models, and estimation of the breeding values and genetic variances for the single marker locus.

Furthermore you may also want to explore these shinyapps that could help understand some of the basic concepts of quantitative genetics:

```
https://neyhartj.shinyapps.io/qgshiny/
```

https://shiny.cnsgenomics.com/Falconer2/

# Let's continue explore our mouse data

The mouse data set can be loaded using the following command:

```
mouse <- readRDS(url("https://github.com/psoerensen/bgcourse/raw/main/data/mouseqtl.rds"))</pre>
```

Question 1: How many observations and which variables do we have in the data set? To get a fast overview of the data set you are working with you can use the str function:

### Answer:

### str(mouse)

```
## 'data.frame': 1177 obs. of 8 variables:
## $ sire : Factor w/ 11 levels "25","28","34",..: 6 6 6 6 6 6 6 6 6 6 ...
## $ dam : Factor w/ 55 levels "26","27","29",..: 8 8 8 8 8 8 8 8 8 8 8 ...
## $ sex : Factor w/ 2 levels "Female","Male": 1 1 1 1 1 2 2 2 2 1 1 ...
## $ reps : Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 1 2 2 ...
## $ Gl : num 187 136 115 125 112 190 169 159 111 89 ...
## $ BW : num 36.6 33.3 42.1 37.1 38.4 ...
## $ M227 : Factor w/ 3 levels "AA","AB","BB": 2 1 2 2 2 1 2 1 2 2 ...
## $ M1139: Factor w/ 3 levels "AA","AB","BB": 3 NA 1 1 1 2 3 3 2 2 ...
```

Question 2: How many observations do the two marker variables have in each genotype class? Use the table function to explore the two marker variables:

### Answer:

```
table(mouse$M227)
```

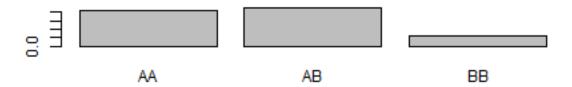
```
## ## AA AB BB
## 493 536 145
```

Question 2: What are the genotype and allele frequencies for M227? Include the allele and genotype frequencies for M227 in the following table:

Variable	M227
$f_{AA}$	
$f_{AB}$	
$f_{BB}$	
$f_A$	
$f_B$	

```
freq_genotypes <- table(mouse$M227)/sum(table(mouse$M227))
fA <- sum(table(mouse$M227)*c(2,1,0))/(sum(table(mouse$M227))*2)
fB <- sum(table(mouse$M227)*c(0,1,2))/(sum(table(mouse$M227))*2)
freq_alleles <- c(fA,fB)
names(freq_alleles) <- c("A","B")
layout(matrix(1:2,nrow=2))
barplot(freq_genotypes, main="Genotype Frequencies")
barplot(freq_alleles, main="Allele Frequencies")</pre>
```

# **Genotype Frequencies**



# **Allele Frequencies**



```
## ## AA AB BB
## 0.4199319 0.4565588 0.1235094

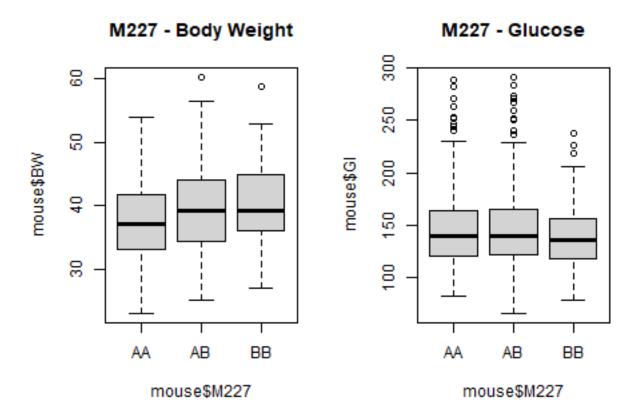
freq_alleles
## A B
```

Question 3: Does the marker variable M227 potentially influence body weight and glucose? Use the boxplot function to visualize the potential effect of the marker variable M227 on the two traits:

### Answer:

## 0.6482112 0.3517888

```
layout(matrix(1:2,ncol=2))
boxplot(mouse$BW~mouse$M227, main="M227 - Body Weight")
boxplot(mouse$G1~mouse$M227, main="M227 - Glucose")
```



To best answer these question we can fit a linear model that also include the effect of the marker variable in addition to sex and reps. This can be done using the lm function:

```
fit <- lm(BW~ sex + reps + M227, data=mouse)
```

To test the effect of the variables in the model use the anova function on the fit object from the lm function:

```
anova(fit)
```

```
## Analysis of Variance Table
##
## Response: BW
##
                  Sum Sq Mean Sq F value
                                               Pr(>F)
## sex
                1 20542.9 20542.9 1203.352 < 2.2e-16 ***
                                     64.315 < 2.2e-16 ***
## reps
                   2195.9
                           1097.9
## M227
                2
                   1660.3
                            830.1
                                    48.627 < 2.2e-16 ***
## Residuals 1168 19939.3
                             17.1
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Signif. codes:
```

Question 4: Based on the linear model results do marker variable M227 influence body weight?

The additive effect is modeled by a variable, add, with levels that is coded as -1, 0, and 1 (corresponding to -a, 0, a) for the genotypes AA, AB, and BB. The following lines of R code create a the add variable, fit the linear model and test the effects:

```
alleles <- c(-1,0,1)
names(alleles) <- c("AA","AB","BB")
mouse$add <- alleles[mouse$M227]
fit <- lm(BW~ sex + reps + add, data=mouse)
summary(fit)

##
## Call:</pre>
```

```
## lm(formula = BW ~ sex + reps + add, data = mouse)
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -15.9743 -2.6780 -0.0483
                                2.5625
                                        19.7455
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 34.3598
                            0.2396 143.399
                                             <2e-16 ***
## sexMale
                 8.4133
                            0.2415
                                    34.838
                                             <2e-16 ***
## reps2
                -0.3787
                            0.2852
                                    -1.328
                                              0.184
## reps3
                 2.8966
                            0.3043
                                     9.518
                                             <2e-16 ***
                                             <2e-16 ***
## add
                 1.7381
                            0.1790
                                     9.713
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 4.135 on 1169 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.5492, Adjusted R-squared: 0.5477
## F-statistic: 356.1 on 4 and 1169 DF, p-value: < 2.2e-16
```

The summary(fit) command produced

- parameter estimates (or Coefficients)  $\widehat{\mu}$  and  $\widehat{\beta}$ ,
- their standard errors (SE) (estimates for square root of the sampling variance of the parameter estimates),
- t-statistic (estimate/SE) and
- P-value under the null hypothesis that the parameter is 0 and errors are uncorrelated and have distribution  $N(0, \sigma^2)$ .

Under the assumptions of linear model, sampling distribution of t-statistic is t-distribution and hence q% confidence intervals are determined as  $\hat{\beta} \pm a \times SE$ , where a is the q/2% quantile of t-distribution with n-2 degrees of freedom. To get a confidence interval use the **confint** function:

```
confint(fit,parm="add")

## 2.5 % 97.5 %
## add 1.387014 2.089222
```

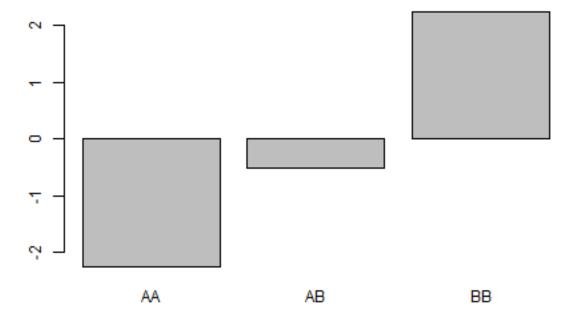
The regression coefficient for the variable add is 1.74. The coefficient corresponds to the allele substitution effect ( $\alpha$ ). Previously we have estimated allele and genotype frequencies for M227. The following table summarizes all genotypic values, all breeding values and the dominance deviations.

Genotyp	Genotypic value	Breeding Value	Dominance Deviation
$A_i A_j$	$GV_{ij}$	$BV_{ij}$	$D_{ij}$
$A_1A_1$	a	$2q\alpha$	$-2q^2d$
$A_1A_2$	d	$(q-p)\alpha$	2pqd
$A_2A_2$	-a	$-2p\alpha$	$-2p^2d$

# Question 5: What are the breeding values for body weight based on the M227 locus?

```
alpha <- -fit$coefficients["add"]
BV_AA <- 2*fA*alpha
BV_AB <- (fA-fB)*alpha
BV_BB <- -2*fA*alpha
BV <- c(BV_AA,BV_AB,BV_BB)
names(BV) <- c("AA","AB","BB")
barplot(BV, main="Breeding Values")</pre>
```

# **Breeding Values**



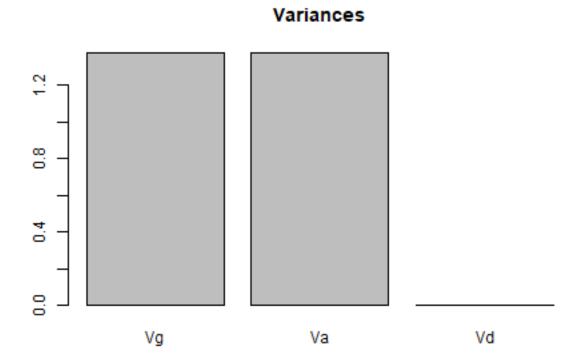
Now we want to compute the genetic variance associated with marker M227. The formula below shows that genetic variance for a single locus model  $\sigma_G^2$  consists of two components. The first component  $\sigma_A^2$  is called the **genetic additive variance** and the second component  $\sigma_D^2$  is termed **dominance variance**. Here  $\sigma_A^2$  corresponds to the variance of the breeding values. The variance of breeding values is also called the additive genetic variance, because as we have already seen the breeding values are additive in the number of favorable alleles. In populations where there is no additive genetic variance, individuals all have the same breeding value. Therefore, they will produce offspring with the same expected advantage (zero), and selection cannot generate any improvement over generations. Because  $\sigma_D^2$  corresponds to the variance of the dominance deviation effects it is called dominance variance.

$$\sigma_G^2 = 2pq\alpha^2 + (2pqd)^2$$
$$= \sigma_A^2 + \sigma_D^2$$

Question 6: What is the additive genetic variance associated with M227 for body weight?

```
alpha <- fit$coefficients["add"]
d <- 0
Va <- 2*fA*fB*alpha^2
Vd <- (2*fA*fB*d)^2</pre>
```

```
Vg <- Va + Vd
V <- c(Vg,Va,Vd)
names(V) <- c("Vg","Va","Vd")
barplot(V, main="Variances")</pre>
```



Question 7: Should you have considered other factors in the linear model specified above?

### Answer:

Now we will fit the full genetic model to locus M227 including both additive and dominance effects. The additive effect is modeled as previously shown by a variable add that is coded as -1, 0, and 1 (corresponding to -a, 0, a) for the genotypes AA, AB, and BB. The dominance effect is modeled by a variable dom that is coded as 0, 1, and 0 (corresponding to 0,d,0) for the genotypes AA, AB, and BB. The corresponding R code is shown below:

```
alleles <- c(-1,0,1)
names(alleles) <- c("AA","AB","BB")
mouse$add <- alleles[mouse$M227]
mouse$dom <- as.numeric(mouse$add==1)
fit <- lm(BW~sex + reps + add+dom, data=mouse)
summary(fit)</pre>
```

```
##
## Call:
## lm(formula = BW ~ sex + reps + add + dom, data = mouse)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
   -16.1773 -2.7642 -0.0437
                                 2.5549
                                         20.1121
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                34.5549
                            0.2666 129.635
                                             < 2e-16 ***
                 8.4130
                             0.2413
                                     34.863
                                             < 2e-16 ***
## sexMale
## reps2
                -0.3706
                             0.2850
                                     -1.300
                                              0.1937
## reps3
                 2.9062
                             0.3041
                                      9.555
                                            < 2e-16 ***
## add
                             0.2580
                                      7.937 4.82e-15 ***
                 2.0479
## dom
                -0.8811
                             0.5290
                                     -1.665
                                              0.0961 .
##
                   0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 4.132 on 1168 degrees of freedom
     (3 observations deleted due to missingness)
## Multiple R-squared: 0.5503, Adjusted R-squared: 0.5484
## F-statistic: 285.8 on 5 and 1168 DF, p-value: < 2.2e-16
confint(fit,parm="add")
##
          2.5 %
                  97.5 %
## add 1.541656 2.554078
confint(fit,parm="dom")
##
           2.5 %
                    97.5 %
## dom -1.919038 0.1569128
```

The results from the linear model analysis suggest that only the additive genetic effect, add, is significantly different from 0. However in the following exercise we will be using the both the additive effect (add) and dominance effect (dom) estimated for locus M227, and the frequency of the positive allele (p) to explore the effect of changes in allele frequency.

Use the following shinyapp, https://shiny.cnsgenomics.com/Falconer2/, to understand the relationship between allelic substitution effect  $(\alpha)$  and additive gene action (a), dominance gene action (d), and allele frequency (p).

Question 8: Use the estimated gene actions (Question 7) and the estimated allele frequency (Question 2) to obtain the predicted allelic substitution effect? Use rounded values if necessary.

Question 9: Does the value of $\alpha$ match the estimate of the (marginal) additive effect from Question 5?
Answer:
Question 10: How does $\alpha$ depend on a larger dominance gene action $d$ (e.g., maximum value, 10)?
Answer:
Question 11: How does $\alpha$ depend on a different allele frequency $p$ (e.g., 0.95)? Answer:
Question 12: Under that new value of $p$ , how does $\alpha$ depend on $d$ (e.g., from the initial value of $d$ to the maximum value)?
Answer:

# Practical 3: Estimation of Genetic Parameters

# Time schedule of practical session 3:

11:15	Question to lectures, multiple-choice question and follow up on previous multiple choice questions
11:30	Today's exercise and assignment to groups
12:00	15 minutes break
12:30	Go through excercises using final word
12:50	Repeat multiple-choice questions
13:00	End of practical session 3

# **Introduction:**

In this practical we will estimate genetic parameters (heritability) for quantitative traits observed in the F2 mouse population. We will be using the REML method. This method allow for estimation of genetic parameters using phenotypic information for individuals from a general pedigree. REML is based on linear mixed model methodology and uses a likelihood approach to estimate genetic parameters. The REML method also require us to calculate an genetic relationship matrix using a recursive algorithm. These methods and algorithms are implemented in the R package qgg.

This package provides an infrastructure for efficient processing of large-scale genetic and phenotypic data including core functions for:

- fitting linear mixed models
- constructing genetic relationship matrices
- estimating genetic parameters (heritability and correlation)
- performing genomic prediction and genetic risk profiling
- single or multi-marker association analyses

We will also be using the qgg package for the remaining practicals.

### Installation of the R package qgg:

You can install qgg from CRAN with:

```
install.packages("qgg")
```

You can install the latest version of qgg from github with:

```
#install.packages("devtools") # needed if devtools is not allready installed
library(devtools)
options(devtools.install.args=" --no-multiargs")
devtools::install_github("psoerensen/qgg")
```

### Load R packages that will be used in this practical

```
library(qgg) # R package used for REML analysis
#install.packages("corrplot")
library(corrplot)
```

# Explore mouse pedigree data

The mouse data set can be loaded using the following command:

```
mouse <- readRDS(url("https://github.com/psoerensen/bgcourse/raw/main/data/mouseqtl.rds"))</pre>
```

The mouse pedigree is loaded in a similar way using the following command:

```
pedigree <- readRDS(url("https://github.com/psoerensen/bgcourse/raw/main/data/pedigree.rds"))</pre>
```

Question 1: Which variables do we have in the pedigree? Use the str function to get a fast overview of the pedigree you are working.

#### Answer:

```
str(pedigree)
```

```
## 'data.frame': 1267 obs. of 6 variables:
## $ id : int 1 2 3 4 5 6 7 8 9 10 ...
## $ sire : int 0 0 0 0 0 0 0 0 0 0 ...
## $ dam : int 0 0 0 0 0 0 0 0 0 ...
## $ family : Factor w/ 68 levels "0/0","1/2","11/12",..: 1 1 1 1 1 1 1 1 1 1 1 1 ...
## $ sex : chr "Male" "Female" "Female" ...
## $ generation: chr "M6" "IC" "IC" "M6" ...
```

### Question 2: How many individuals do we have in the pedigree?

### Answer:

## [1] 1267

6

```
nrow(pedigree)

## [1] 1267

dim(pedigree)
```

Question 3: How many generations and number of mice in each generation do we have in the pedigree? Use the table function on the generation variable.

#### Answer:

### table(pedigree\$generation)

```
## ## F1 F2 IC M6
## 66 1177 12 12
```

# Computing genetic relationship matrix for the mouse pedigree:

The REML analysis require us to calculate the genetic relationship matrix A. This is done using information about the id, mother, and father which is avaliable in our pedigree data file.

To illustrate this step we will first calculate it for a small part of the mouse pedigree. We are given the following pedigree and we want to compute the matrix A.

```
family <- c(13,14,84,1244,1248)
pedigree[family,]
```

```
id sire dam family
##
                                 sex generation
## 13
          13
                    0
                          0/0
                0
                                Male
                                              IC
## 14
          14
                0
                    0
                          0/0 Female
                                             M6
## 84
          84
               13
                   14
                       13/14 Female
                                             F1
## 1244 1244
               78
                   84
                       78/84 Female
                                             F2
## 1248 1248
               78
                   84
                       78/84
                                Male
                                              F2
```

The additive genetic relationship  $(A_{ij})$  between the various sources (j) and the individual itself, i.e. the candidate to be evaluated (i), can be seen in the table below.

Relative	$A_{ij}$
Self	1.0
Unrelated	0
Mother	0.5
Father	0.5
Grandparent	0.25
Half-sib	0.25
Full-sib	0.5
Progeny	0.5

Next we will compute the genetic relationship matrix for the entire mouse pedigree. The matrix A can be computed using a recursive algorithm implemented in the function grm from the qgg package. Use the command below to compute the genetic relationship matrix for the mouse pedigree:

```
A <- grm(pedigree=pedigree)
```

# Question 4: What is the dimension of the genetic relationship matrix?

### Answer:

```
dim(A)
```

```
## [1] 1267 1267
```

The number of rows and columns should be equal to the number of individuals in the pedigree. Check the first 5 individuals in the matrix using the following command:

### A[1:5,1:5]

```
## 1 2 3 4 5
## 1 1 0 0 0 0
## 2 0 1 0 0 0
## 3 0 0 1 0 0
## 4 0 0 0 1 0
## 5 0 0 0 0 1
```

# Question 5: Are these individuals related?

#### Answer:

To further explore the genetic relationship we compute the mean of diagonal elements of A using the following command:

```
mean(diag(A))
```

```
## [1] 1
```

### Question 6: How should we interpret this value?

#### Answer:

Previously we have determined the genetic relationship matrix for a small part of the mouse pedigree. We can extract the corresponding elements from the A matrix for the entire mouse pedigree using the following command:

```
ids <- c(13,14,84,1244,1248)
A[ids,ids]
```

```
## 13 14 84 1244 1248

## 13 1.00 0.00 0.5 0.25 0.25

## 14 0.00 1.00 0.5 0.25 0.25

## 84 0.50 0.50 1.0 0.50 0.50

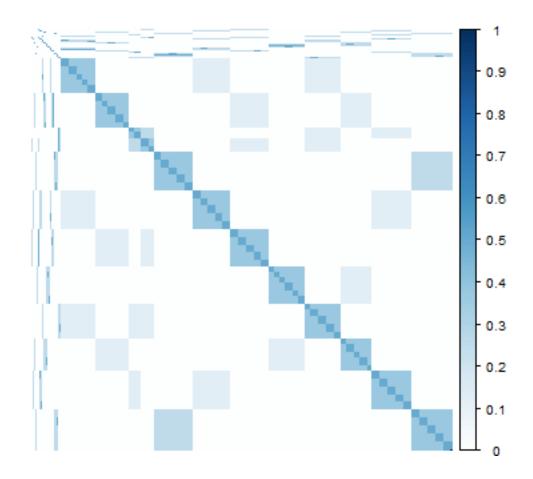
## 1244 0.25 0.25 0.5 1.00 0.50

## 1248 0.25 0.25 0.5 0.50 1.00
```

Question 6: Are the values in this part of the genetic relationship matrix the same as you have found using the "manual" approach?

#### Answer:

Make a plot of the genetic relationship matrix using the corrplot function from the corrplot R package:



Question 7: Describe the plot you just made of the genetic relationship?

### Answer:

# Specifying the linear mixed model for the mouse data:

The next step is to prepare the linear mixed model for the mouse data. Recall that the linear mixed model contains the observation vector for the trait(s) of interest (y), the fixed effects that explain systematic differences in y, and the random genetic effects a and random residual effects e.

A matrix formulation of a general model equation is:

$$y = Xb + a + e$$

where

y: is the vector of observed values of the trait,

b: is a vector of fixed effects,

a: is a vector of random genetic effects,

e: is a vector of random residual effects,

X: is a known design matrix that relates the elements of b to their corresponding element in y.

In the statistical model (specified above) the random effects (a and e) and the phenotypes (y) are considered to be random variables which follow a multivariate normal distribution: In general terms the expectations of these random variables are:

$$E(y) = Xb$$

$$E(a) = 0$$

$$E(e) = 0$$
(1)

and the variance-covariance matrices are:

$$Var(a) = A\sigma_a^2$$
  
 $Var(e) = I\sigma_e^2$   
 $Var(y) = A\sigma_a^2 + I\sigma_e^2$ 

where  $A\sigma_a^2$ , and  $I\sigma_e^2$  are square matrices of genetic and residual (co)variances among the individuals, respectively. In the previous section we have allready constructed the genetic relationship matrix A.

In order to perform the REML analysis we need to construct y and X from the mouse data. Let us just have a quick look at the mouse data again:

### str(mouse)

```
## 'data.frame': 1177 obs. of 8 variables:
## $ sire : Factor w/ 11 levels "25","28","34",..: 6 6 6 6 6 6 6 6 6 6 ...
## $ dam : Factor w/ 55 levels "26","27","29",..: 8 8 8 8 8 8 8 8 8 8 8 8 ...
## $ sex : Factor w/ 2 levels "Female", "Male": 1 1 1 1 2 2 2 2 1 1 ...
## $ reps : Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 1 2 2 ...
## $ Gl : num 187 136 115 125 112 190 169 159 111 89 ...
## $ BW : num 36.6 33.3 42.1 37.1 38.4 ...
## $ M227 : Factor w/ 3 levels "AA","AB","BB": 2 1 2 2 2 1 2 1 2 2 ...
## $ M1139: Factor w/ 3 levels "AA","AB","BB": 3 NA 1 1 1 2 3 3 2 2 ...
```

Here we will estimate the heritability for body weight. The vector of observed trait values for body weight can be extracted from the mouse data as follows:

```
y <- mouse[,"BW"]
```

Let us explore the trait values using the head, tail and summary functions:

```
head(y)
```

```
## [1] 36.65 33.29 42.07 37.15 38.39 39.82
```

```
tail(y)
```

## [1] 39.67 39.35 44.80 52.23 47.63 54.10

### summary(y)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 23.04 34.06 38.32 38.72 43.40 60.28
```

To make the X matrix we need to decide which variables we should include as fixed effects in the model. We have sex, reps, sire, dam, M227 and M1139 in the mouse data frame.

### Question 8: Which variables should we include as fixed effects in the model?

#### Answer:

The model.matrix function can be used to construct the X matrix in the linear mixed model specified above:

```
X <- model.matrix(BW ~ sex + reps, data=mouse)</pre>
```

We can use the head and tail functions to look at the X matrix:

### head(X)

##		(Intercept)	sexMale	reps2	reps3
##	91	1	0	0	0
##	92	1	0	0	0
##	93	1	0	0	0
##	94	1	0	0	0
##	95	1	1	0	0
##	96	1	1	0	0

### tail(X)

reps3	reps2	sexMale	(Intercept)		##
1	0	0	1	1262	##
1	0	0	1	1263	##
1	0	1	1	1264	##
1	0	1	1	1265	##
1	0	1	1	1266	##
1	0	1	1	1267	##

### Estimating genetic parameters on the mouse data using REML:

The goal of the REML analysis to estimate the parameters (i.e. variance components  $\sigma_a^2$  and  $\sigma_e^2$ ) in the linear mixed model specified above. In this analysis we find the set of parameters which maximizes the **likelihood** of the data, i.e., the probability of observations given the model and its parameter estimates:  $p(y|\hat{b}, \hat{\sigma}_a^2, \hat{\sigma}_e^2)$ .

The input required the vector of observed values of the trait (y), the deisgn matrix for the fixed effects (X), and the genetic relationship matrix (A). The A matrix calculated previously include genetic relationships for all individuals in the pedigree. However only a subset of the inviduals have phenotypes recorded for body weight. Therefore we need to subset the A matrix as shown in the R code below:

```
ids <- rownames(X)
A <- A[ids,ids]</pre>
```

The REML method is implemented in the greml function from the "qgg" package. The REML analysis is done using the following command:

```
fit <- greml(y=y,X=X, GRM=list(A=A))</pre>
```

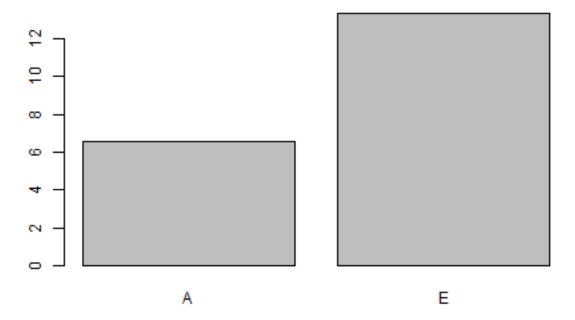
The fit object (i.e., output from the greml function) contains estimates of variance components, fixed and random effects, first and second derivatives of log-likelihood, and the asymptotic standard deviation of parameter estimates.

Our main interest is the variance components  $\sigma_a^2$  and  $\sigma_e^2$  which are in the fit\$theta slot of the fit. The following commands extract and makes a barplot of the estimates of the variance components:

### fit\$theta

```
## A E
## 6.569611 13.384147
```

### barplot(fit\$theta)



The first element in the theta vector is the estimate of the additive genetic variance  $(\hat{\sigma}_a^2)$  and the second element is the estimate of the residual variance  $(\hat{\sigma}_e^2)$ .

```
Va <- fit$theta[1]
Ve <- fit$theta[2]
Va</pre>
```

## A ## 6.569611

Vе

## E ## 13.38415

From the REML estimate of the variance components, the heritability can easily be computed by:

$$\hat{h}^2 = \hat{\sigma}_a^2 / (\hat{\sigma}_a^2 + \hat{\sigma}_e^2) \tag{2}$$

where the hat (^) refers to estimators.

# Question 9: What is the heritability for body weight?

Answer:

Va/(Va+Ve)

## A ## 0.3292418

In the experiment the mice were feed ad libitum. Now we want to perform a similar experiment where mice are reared under restricted feed intake, We will record phenotypes for body weight and blood glucose levels and use mice from the same F2 population.

Question 10: Should we re-estimate the heritability?

Answer:

Question 11: What is the heritability for glucose levels in the blood?

```
y <- mouse[,"G1"]
X <- model.matrix(G1 ~ sex + reps, data=mouse)
ids <- rownames(X)
A <- grm(pedigree=pedigree)
A <- A[ids,ids]
fit <- greml(y=y,X=X, GRM=list(A=A))
Va <- fit$theta[1]
Ve <- fit$theta[2]
Va/(Va+Ve)</pre>
```

## A ## 0.4058474