

Dynamic programming approach (Bottom Up):

$$\text{distance}(7, 4) = 0$$

$$\text{distance}(4, 3) = \min \{c(4,7) + \text{distance}(7, 4)\} = 18$$

$$\text{distance}(5, 3) = \min \{c(5,7) + \text{distance}(7, 4)\} = 13$$

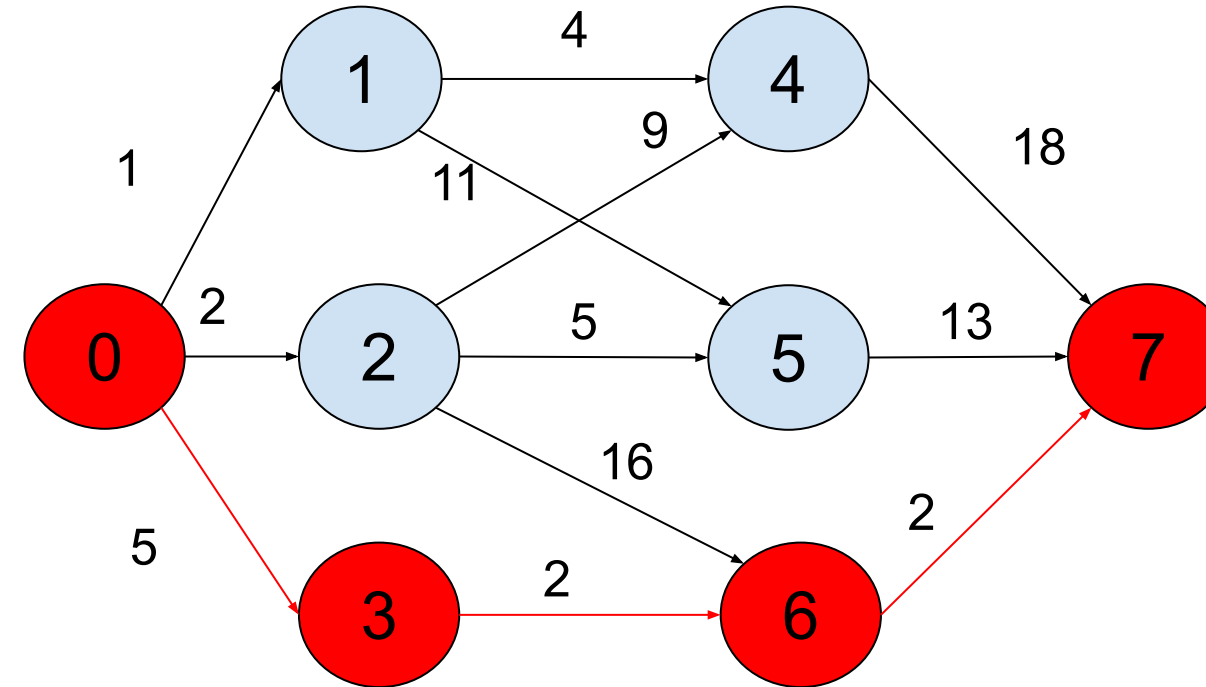
$$\text{distance}(6, 3) = \min \{c(6,7) + \text{distance}(7, 4)\} = 2$$

$$\text{distance}(1, 2) = \min \{4 + \text{distance}(4,3), 11 + \text{distance}(5,3)\} = 22$$

$$\text{distance}(2, 2) = \min \{9 + 18, 5 + 13, 16 + 2\} = 18$$

$$\text{distance}(3, 2) = \min \{2 + 2\} = 4$$

$$\begin{aligned} \text{distance}(0, 1) &= \min \{ \\ &\quad 1 + \text{distance}(1,2), \\ &\quad 2 + \text{distance}(2,2), \\ &\quad 5 + \text{distance}(3,2) \\ &\quad \} \\ &= \min \{ 1 + 22, 2 + 18, 5 + 4 \} \\ &= 9 \end{aligned}$$



Program's Solution: [9, 22, 18, 4, 18, 13, 2, 0]

Solution approach:

~~Greedy approach: we keep on selection minimum edges from outgoing edges of each stage til reach last node.~~

~~0-1, 1-4, 4-7 → 23 is this minimum between 0-7?~~

distance(node n, stage s) = distance from node n in stage s to the last node.

c(u,v) = cost of edge <u,v>

Stage 0,1,2,4

$$\text{distance}(0,1) = \min (\\ c(0,1) + \text{distance}(1,2), \\ c(0,2) + \text{distance}(2,2), \\ c(0,3) + \text{distance}(3,2) \\)$$

$$\text{distance}(1,1) = \min (\\ c(1,4) + \text{distance}(4,3), \\ c(1,5) + \text{distance}(5,3), \\)$$

$$\text{distance}(2,1) = \min (\\ c(2,4) + \text{distance}(4,3), \\ c(2,5) + \text{distance}(5,3), \\ c(2,6) + \text{distance}(6,3), \\) \dots\dots\dots$$

$$\text{distance}(7,4) = 0$$