## Problem

A set function f from the set of subsets of a finite set N to the positive real numbers is called submodular if for any  $A \subseteq B \subseteq N$  and element u in N-B, we have

$$f(A \cup \{u\}) - f(A) \ge f(B \cup \{u\}) - f(B)$$

In many cases the greedy algorithm works well to optimize submodular objective functions. Find an example of a set N and submodular function f defined on N such that the greedy algorithm returns a subobptimal result when trying to maximize f.

## Solution