Problem

Moe's revolutionary "oreo design" hotel has become so successful that his VBA-powered MSFT Access CRS is having trouble handling the transaction volume coming at it when both of his room service / sales agents (Huey and Looey) take calls at the same time. The system doesn't have any logging and doesn't store enough info to count transactions, but Joe found a way to sample counts of transactions per hour throughout the day. Using his Colorado City HS AP Stats training, Joe estimated a polynomial regression model from the data and came up with the following model for the rate of incoming transactions per hour (in thousands) as a function of time over the period when Huey and Looey answer the phone (between 2 and 6 in the afternoon):

$$r(t) = -t^2 + 8t - 12$$

where t is measured in hours starting at t = 2 and ending at t = 6. How many total transactions should Moe expect to receive between 2 and 6?

Solution

$$\int_{2}^{6} -t^{2} + 8t - 12dt = \left[x^{3}/3 + 4x^{2} - 12x\right]_{2}^{6} = 32/3$$
 thousand transactions.