Quantifying stochastic noise in cultured circadian reporter cells

Peter C. St. John¹ and Francis J. Doyle III^{1,*}

¹Department of Chemical Engineering, University of California Santa Barbara, Santa Barbara, California 93106-5080

*Email: doyle@engineering.ucsb.edu

February 18, 2015

Running head: Quantifying circadian stochastic noise

Keywords:

Systems Biology | Circadian Rhythms Gene Regulatory Network | Stochastic | Synchronization

Abstract

Introduction

Circadian rhythms in mammals are daily changes in gene expression and physiology that persist even in the absence of external environmental cues (6). Such rhythms are generated by a large network of interacting regulatory elements, in which time-delayed negative feedback gives rise to sustained oscillations (17). The functional roles of different species in circadian regulation have traditionally been studied using behavioral-level data and genetic knockout experiments (18). Bioluminescence-based cellular circadian reporters offer a more direct view of the gene regulatory network (2), and are amenable to high-throughput screens, allowing genome-wide exploration into factors which affect circadian rhythmicity (21). Additionally, cultured circadian reporter cells allow the change in transcriptional amplitude following a perturbation to be quantified. This additional parameter has proven useful in differentiating between perturbations with the same effect on period (15), and has lead to the search for small-molecule therapeutics which boost clock amplitude (4).

Transcription at the single-cell level is strongly affected by the low molecular counts of the mRNA and protein species involved. As a result, bioluminescence traces of individual cells are stochastic, with significant period-to-period variability (19). The collective behavior of thousands of cells results in more reliable oscillations at the tissue-level, especially in the suprachiasmatic nucleus (SCN) where cell-to-cell coupling keeps individual oscillators at a consistent phase (7). While communication between cells is common in many tissues, it is currently thought that coupling between circadian oscillations outside the SCN, such as in peripheral tissues or cultured reporter cells, is very weak, if present (5, 11). In populations which lack cell-to-cell coupling, stochastic noise at the single-cell level is manifested in damped oscillations at the population-level (19). Despite the averaging which occurs at the population-level, stochastic noise at the singlecell level plays an important role in determining the function of the circadian oscillator. A recent study showed that stochasticity is critical to the population-level response to a neuropeptide and forms the basis for how the SCN entrains to light-mediated cues (1). Additional studies have even argued that the basis of single-cell rhythmicity depends on stochastic noise, as models of deterministically damped oscillators - when simulated stochastically - better capture the noise characteristics seen in single-cell fibroblast data (20).

Despite the importance of single-cell stochasticity in circadian rhythms, measuring stochastic noise currently requires careful plating and recording of fibroblast cells and subsequent image processing (10). As a result, while circadian perturbations have been postulated to affect single-cell stochasticity (13), no study has experimentally quantified changes to single-cell noise as a result of a small molecule or genetic perturbation. In this study, we demonstrate single-cell stochasticity can be reliably inferred from the damping rate of population-level bioluminescence recordings. Additionally, we show that a small-molecule modulator is able to change circadian noise in a dose-dependent fashion. Finally, we calculate the genome-wide effects of siRNA knockdown on single-cell noise, and demonstrate that population-level damping rate is independent of other circadian parameters, such as period or amplitude. Our results should prove especially important in the future search for small molecule circadian therapeutics, as it allows the effect of candidate drugs on single-cell noise to be quantified in a high-throughput manner.

Materials and Methods

Fitting a damped sinusoid to experimental data

A damped sinusoid, specified by:

$$\hat{y}(t) = Ae^{-dt}\sin\left(\frac{2\pi t}{T} + \theta\right)$$

is fit to experimental data $x_i(t_i)$, $i \in \{0, \ldots, N-1\}$. The x_i data points are first detrended using Hodrick-Prescott filter with a smoothing parameter $\gamma = 0.05 \left(24 \, \mathrm{hrs}/s\right)^4$, in which s is the sampling rate (in hours) (12). The detrended data is then filtered using a low-pass filter to remove high-frequency noise (forward-backward Butterworth filter with n = 5, $w_c = 0.1$). We denote the detrended and filtered experimental data by $y_i(t_i)$. For numerical efficiency, the period, T, and damping rate, d, parameters are fit first using a matrix pencil method (9), reviewed in (22). Amplitude, A, and phase, θ , parameters are subsequently fit using a linear least-squares regression. Overall R^2 values for the regression were calculated from the residual error between the detrended data and fitted sinusoid:

$$R^{2} = 1 - \frac{\sum_{i=0}^{N-1} (y_{i}(t_{i}) - \hat{y}(t_{i}))^{2}}{\sum_{i=0}^{N-1} (y_{i}(t_{i}) - \bar{y}(t_{i}))^{2}}$$

Processing single-cell bioluminescence data

Single-cell bioluminescence data for 79 cells was obtained from Leise *et al.*, 2012 (10). As was done in the original study, a discrete wavelet transform (using PyWavelets, http://www.pybytes.com/pywavelets) was performed to detrend and remove noise.

Sorting cells by noise level

As in the original study, various parameters describing the average noise level of each cell were collected. Traces were denoised and detrended by keeping only the (8hr,258hr) wavelet components. From these smoothed trajectories, a Hilbert transform was used estimate points at which the phase crossed 0 to find period and amplitude coefficients of variation. An additional noise parameter, the standard deviation in the (1hr,8hr) wavelet components divided by the overall rhythm amplitude, was used to quantify the high-frequency noise of the system. From these three noise variables, a combined noise metric was constructed by projecting the variables along their first principle component (using scikit-learn, http://scikit-learn.org/). Cells were ranked according to this combined noise metric, and a high-noise group and low-noise group were constructed by taking the 39 highest-noise and lowest-noise cells, respectively. The raw bioluminescence profiles were not initially synchronized, so in order to simulate the gradual desynchronization of a group of oscillators the traces were offset to have the same starting phase. This was accomplished by starting each trace at the first phase zero-crossing, which were found using a Hilbert transform.

Bootstrap estimations of the damping rate difference

Averaged traces for low and high-noise group displayed a damped sinusoidal rhythm. The first 4 days of rhythms (s = 0.5, N = 192) were fit using a damped sinusoid. To ensure the difference in damping rate between groups was statistically significant, a bootstrap analysis was performed.

In each of 10,000 bootstrap trials, the cells were randomly assigned evenly to either the low-noise or the high-noise group. The absolute difference in damping rate between the two populations was recorded to yield a two-tailed test. The observed test statistic, $|d_h - d_l| = 6.65 \times 10^{-3}$, was found to be significant at the $\alpha = 0.05$ confidence threshold (p = 0.0264).

Quantifying dose-dependent effects of small molecule modulators

Bioluminescence traces (s = 1.67, N = 71) from the application of increasing concentrations of small molecule were fit using the method described in a previous section. Because the small molecules were toxic to the cells at very high concentrations, experiments were removed from further analysis when the R^2 of the sinusoidal regression fell below 0.80 (Figure S1).

In silico prediction of small molecule experiments

A previously published mathematical model of circadian rhythms was used to predict the effects on population damping rate from the dose-dependent small molecule experiments (8). The parameters used to capture the effects of each small molecule were the same as described previously (15). The model was converted to a stochastic biochemical system and subsequently simulated using StochKit2 (14). Population-level rhythms were found by taking the average of 1,000 noninteracting oscillators, starting at identical initial conditions. The only parameter left unspecified by the deterministic model was the cell volume Ω , which controlled the amount of noise in the system. For a given Ω , the population-level damping rate was found by finding the phase diffusivity parameter which gave the closest fit to the simulated population-level rhythms, as described in (16). An R^2 value was calculated for each fit, taking into account all eight state variables.

Fitting the volume parameter

We calculated an average experimental damping rate of d=0.0151 from the $0\mu M$ bioluminescence trajectories for both KL001 and longdaysin. In silico damping rates were calculated for logarithmically space values of $\Omega \in (100,500)$. Ten independent groups of 1,000 oscillators were simulated for each Ω , from which the means and standard errors were found. Simulations in which $R^2 < 0.90$ were removed from further analysis. A weighted least-squares regression (using statsmodels, http://statsmodels.sourceforge.net/) was performed for log d vs. log Ω , using the log SEM of each measurement as a regression weight (Figure S2). The best fit was found to be $\Omega = 226.3 \pm 9.0$.

Parameter knockdown experiments

We mathematically replicated the effects of the small molecules KL001 and longdaysin through the reductions of the vdcn and vac1p parameters, respectively. Simulations were performed with 20 values of each parameter, linearly spaced between 100% and 15% of their nominal value. Similar to the volume calibration simulations, 10 independent groups of 1,000 oscillators were simulated from an initially entrained state. Means and standard errors in period and damping rate were calculated from each trajectory. Simulations in which $R^2 < 0.90$ were removed from further analysis.

Fitting the genome-wide siRNA screen

We analyzed the supplemental annotations and data for the 111,743 wells (s=2, N=72) in the Zhang $et\ al.$, 2009 screen (21). Fits for which the $R^2<0.80$ were discarded. We rescaled amplitude values on a logarithmic basis, as these were more normally distributed. Plate to plate variation, as shown in Figure S3, was more severe than variation on a well-to-well basis, Figure S4. Parameters were therefore normalized on a plate-by-plate basis using a robust z-score, median \pm median absolute deviation (3). We chose the "control" wells to be those which contained no siRNA, as these proved to be more numerous than those containing reference siRNA perturbations and were clustered similarly to the highest-density regions of the perturbed fits.

Detecting outlier perturbations

To find which target genes confidently shifted the fitted parameters away from the control population, we performed a test similar to a two-sample t-test with equal variance. Because the control distribution (n=11,253) is much larger than that for any particular gene ID ($n\approx 4$), the outlier test is dependent almost entirely on the control distribution and the perturbed mean. We found the average perturbed response by grouping the perturbed dataset by target gene ID (using pandas, http://pandas.pydata.org/). To extend the t-test to two dimensions, we used a one-class support vector machine (SVM) with a radial basis function kernel ($\nu=0.1,\ \gamma=0.2$). The one-class SVM, after training with the control dataset, draws a decision boundary around 90% of the control points, flagging the remaining 10% (n=1124) as outliers. The decision boundary was then used to classify the averaged perturbed points, from which 43% (n=3139) were flagged as outliers.

Results and Discussion

Single-cell stochastic noise is manifested in damped population-level rhythms

We first sought to determine whether single-cell stochastic noise affects the population-level damping rate in cultured bioluminescence cells. To do this, we calculated noise characteristics from experimental data on individual PER2::LUC fibroblast cells (10). We sorted the cells into two groups, a low-noise group and a high-noise group, based on the relative high-frequency noise, period variability, and amplitude variability present in each trace. Example rhythms from cells in both groups are shown in Figure 1A. Because the cells were not synchronized at the start of the recording, we replicate this effect *in silico* by shifting each series in time to align their start phases. We next calculated expected population-level bioluminescence traces by averaging the cellular PER2::LUC signal in each group. Both populations displayed averaged rhythms which resembled a damped sinusoid, similar to those seen in bioluminescence recordings of entire cell cultures. Fitting the averaged expression of each group with a damped sinusoid revealed that the low-noise group also had a lower damping rate (Figure 1B). The significance of this difference was confirmed via a bootstrap analysis (Figure 1C), where in each bootstrap trial cells were randomly assigned to either the low-noise or the high-noise group.

Clock perturbations can change single-cell stochastic noise

We next demonstrate that perturbations to the transcriptional oscillator are capable of altering single-cell level stochastic noise. The actions small-molecule circadian modulators KL001 and

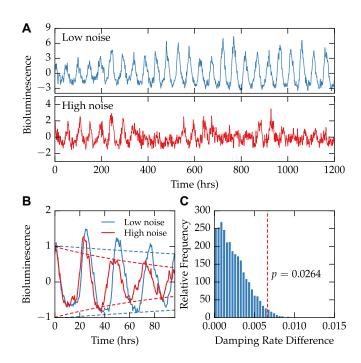


Figure 1: Single-cell bioluminescence recordings show that higher stochastic noise results in faster damping at the population-level. Data on the bioluminescence of single-cell fibroblasts was taken from Leise $et\ al.$, 2012 (10). (A) Cells were sorted into two groups depending on their degree of stochastic noise. An example trace from each of the two groups is shown, demonstrating different levels of noise present in the dataset. (B) After artificially synchronizing each cell, averaged bioluminescence rhythms of each group (solid lines) resemble damped recordings taken at cell culture level. A damped sinusoid fit to both both groups reveals a difference in damping rate, demonstrated by fitted envelope functions ($\pm A \exp -dt$, dashed lines). (C) The observed absolute difference in damping rate was shown to be significant (p = 0.0264) using 10,000 bootstrap trials.

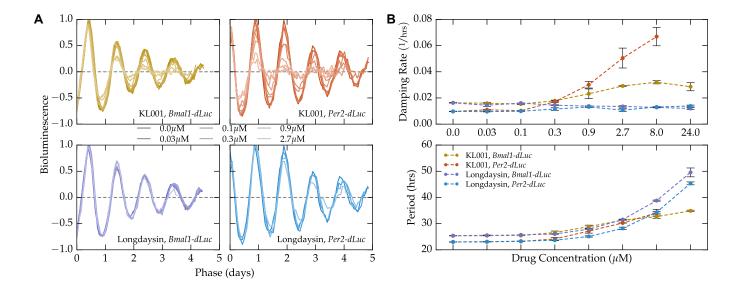


Figure 2: Small molecule modulator KL001 increases damping rate in a dose-dependent fashion. Experimental data on the dose-dependent effect of small molecules KL001 and Longdaysin on cultured circadian reporter cells was taken from Hirota *et al.*, 2012 (8). (**A**) Detrended bioluminescence signals from the two cells and two reporter systems, normalized by the fitted amplitude, period, and phase. The normalized bioluminescence highlights the dose-dependent change in damping rate seen with the KL001 application, but not with longdaysin. (**B**) Quantification of the dose-dependent change in damping rate caused by small molecule modulators. While both molecules lead to a dose-dependent increase in period, only KL001 shows a reliable change in damping rate.

longdaysin are well-characterized, and are known to affect circadian period and amplitude in a dose-dependent fashion (15). By fitting experimental data on the population-level responses to increasing dosages of each molecule with a damped sinusoid, we show that KL001, but not longdaysin, increases damping rate in a dose-dependent fashion (Figure 2). This change in damping rate is consistent across both reporter systems (*Bmal1-dLuc* and *Per2-dLuc*), indicating it is a fundamental property of the overall gene regulatory network.

To lend further support to the conclusion that the dose-dependent change in damping rate from KL001 is due to changes in single-cell noise characteristics, we employed a model of circadian rhythms previously used to explain the effects of both small molecule perturbations (15). In order to capture changes to noise characteristics, the model had to first be converted to a stochastic biochemical system. Population-level rhythms were therefore generated by averaging the rhythms of 1,000 individual, noninteracting oscillators. The only free parameter in converting the existing deterministic model to a stochastic one is the cell volume, which was determined by fitting the observed population-level damping rate to the experimental unperturbed controls (Figure S2).

The model was then used to predict the effects of KL001 and longdaysin administration on single-cell noise and population damping rates (Figure 3A). Reductions in parameters previously attributed to the activities of each small molecule caused dose dependent changes in period and damping rate at the population-level which closely matched experimental results (Figure 3B). As the model includes no cell to cell communication, this difference is manifested solely by changing

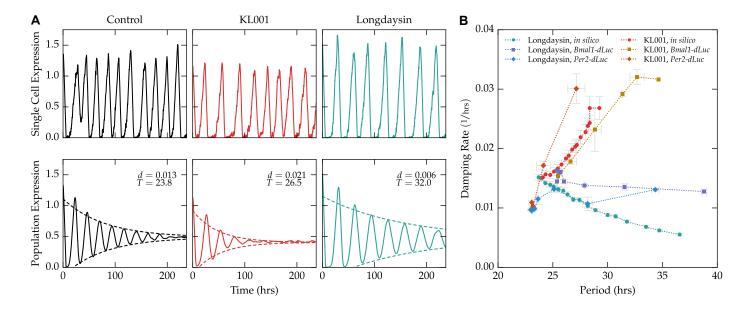


Figure 3: Mathematical model accurately predicts dose-dependent changes in damping rate. (A) Example single-cell trajectories (top) and population-averaged trajectories (mean of 1,000 cells, bottom) of cells under various treatments. Cells with the nominal parameter set (left, black) closely match the experimental damping rate for unperturbed cells. Cells with simulated KL001 action (red, center) are noisier at the single-cell level, and show faster damping at the population-level. Cells with simulated longdaysin action show slightly more accurate single-cell rhythms, with a corresponding dip in the population-level damping rate. (B) The model accurately predicts the general trend of period vs. damping rate for both KL001 and longdaysin perturbations. Experimental data points represent the mean of two replications at each concentration. Computational data points represent the mean of ten independent population simulations.

the noise characteristics of individual cells.

Genome-wide effects of siRNA knockdown on single-cell stochastic noise

Unlike with single-cell imaging of fibroblast rhythms, inferring stochastic noise from the desynchronization rate of population-level recordings can be applied to existing and future high-throughput circadian screens. We demonstrate the insights that can be gained from such an approach by analyzing the publicly available genome-wide siRNA screen from Zhang $et\ al.$, 2009 (21). The results of fitting a damped sinusoid to each of the 111,743 bioluminescence trajectories is shown in Figure 4, in which 86% of fits had an $R^2 > 0.80$ and were kept for further analysis. Additionally, of the fits with a high R^2 value, only a small minority had a negative damping rate (0.1%): lending further support to the assumption that intercellular synchronization is unlikely in cultured U2OS cells.

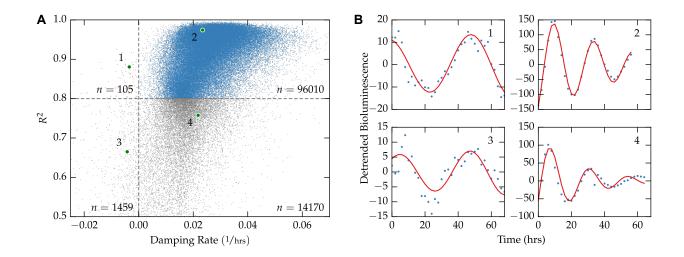


Figure 4: Figure Title. (A) Part A. (B) Part B.

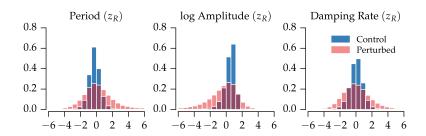


Figure 5: Figure Title. (A) Part A. (B) Part B.

	T		$\ln A$		d	
	C	P	C	P	C	P
μ	-0.234	0.187	0.443	-0.343	0.043	0.090
σ	0.774	1.820	0.778	1.753	0.878	1.688
Skew	0.153	0.367	-1.823	-0.580	-0.107	0.371
Kurt	3.772	0.591	8.329	0.476	2.423	0.373

Table 1: Fitted Parameters

	d	ln A	T	θ
d	1.000	0.285	-0.142	-0.269
ln A	0.285	1.000	-0.022	-0.112
T	-0.142	-0.022	1.000	-0.113
θ	-0.269	-0.112	-0.113	1.000

Table 2: Correlation matrix

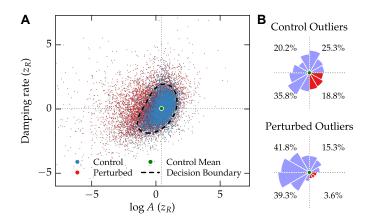


Figure 6: Figure Title. (A) Part A. (B) Part B.

Conclusion

Acknowledgments

This work was supported by the National Institutes of Health/National Institute of General Medical Sciences under award number 1R01GM096873-01 and by the Institute for Collaborative Biotechnologies through grant W911NF-09-0001 from the U.S. Army Research Office.

References

- 1. An S, Harang R, Meeker K, Granados-Fuentes D, Tsai Ca, Mazuski C, Kim J, Doyle FJ, Petzold LR, Herzog ED (2013) A neuropeptide speeds circadian entrainment by reducing intercellular synchrony. *Proc Natl Acad Sci U S A* **110**: E4355–61
- 2. Balsalobre A, Damiola F, Schibler U (1998) A serum shock induces circadian gene expression in mammalian tissue culture cells. *Cell* **93**: 929–37
- 3. Birmingham A, Selfors LM, Forster T, Wrobel D, Kennedy CJ, Shanks E, Santoyo-Lopez J, Dunican DJ, Long A, Kelleher D, Smith Q, Beijersbergen RL, Ghazal P, Shamu CE (2009) Statistical methods for analysis of high-throughput RNA interference screens. *Nat Methods* **6**: 569–75
- 4. Chen Z, Yoo SH, Takahashi JS (2013) Small molecule modifiers of circadian clocks. *Cell Mol Life Sci* **70**: 2985–98
- 5. Guenthner CJ, Luitje ME, Pyle La, Molyneux PC, Yu JK, Li AS, Leise TL, Harrington ME (2014) Circadian rhythms of Per2::Luc in individual primary mouse hepatocytes and cultures. *PLoS One* **9**: e87573
- 6. Herzog ED (2007) Neurons and networks in daily rhythms. Nat Rev Neurosci 8: 790-802
- 7. Herzog ED, Aton SJ, Numano R, Sakaki Y, Tei H (2004) Temporal precision in the mammalian circadian system: a reliable clock from less reliable neurons. *J Biol Rhythms* **19**: 35–46

- 8. Hirota T, Lee JW, St. John PC, Sawa M, Iwaisako K, Noguchi T, Pongsawakul PY, Sonntag T, Welsh DK, Brenner DA, Doyle FJ, Schultz PG, Kay SA (2012) Identification of Small Molecule Activators of Cryptochrome. *Science* 337: 1094–1097
- 9. Hua Y, Sarkar T (1990) Matrix pencil method for estimating parameters of exponentially damped/undamped sinusoids in noise. *IEEE Trans Acoust* **38**: 814–824
- 10. Leise TL, Wang CW, Gitis PJ, Welsh DK (2012) Persistent cell-autonomous circadian oscillations in fibroblasts revealed by six-week single-cell imaging of PER2::LUC bioluminescence. *PLoS One* **7**: 1–10
- 11. Noguchi T, Wang LL, Welsh DK (2013) Fibroblast PER2 circadian rhythmicity depends on cell density. *J Biol Rhythms* **28**: 183–92
- 12. Ravn M, Uhlig H (2002) On adjusting the Hodrick-Prescott Filter for the frequency of observations 84
- 13. Rougemont J, Naef F (2007) Dynamical signatures of cellular fluctuations and oscillator stability in peripheral circadian clocks. *Mol Syst Biol* **3**: 93
- 14. Sanft KR, Wu S, Roh M, Fu J, Lim RK, Petzold LR (2011) StochKit2: software for discrete stochastic simulation of biochemical systems with events. *Bioinformatics* 27: 2457–8
- 15. St. John PC, Hirota T, Kay SA, Doyle FJ (2014) Spatiotemporal separation of PER and CRY posttranslational regulation in the mammalian circadian clock. *Proc Natl Acad Sci U S A* **111**: 2040–5
- 16. St. John PC, Taylor SR, Abel JH, Doyle FJ (2014) Amplitude Metrics for Cellular Circadian Bioluminescence Reporters. *Biophys J* **107**: 2712–2722
- 17. Ueda HR, Hayashi S, Chen W, Sano M, Machida M, Shigeyoshi Y, Iino M, Hashimoto S (2005) System-level identification of transcriptional circuits underlying mammalian circadian clocks. *Nat Genet* **37**: 187–92
- 18. Vitaterna MH, King DP, Chang aM, Kornhauser JM, Lowrey PL, McDonald JD, Dove WF, Pinto LH, Turek FW, Takahashi JS (1994) Mutagenesis and mapping of a mouse gene, Clock, essential for circadian behavior. *Science* **264**: 719–725
- 19. Welsh DK, Yoo SH, Liu AC, Takahashi JS, Kay SA (2004) Bioluminescence imaging of individual fibroblasts reveals persistent, independently phased circadian rhythms of clock gene expression. *Curr Biol* 14: 2289–95
- 20. Westermark PlO, Welsh DK, Okamura H, Herzel H (2009) Quantification of circadian rhythms in single cells. *PLoS Comput Biol* 5: e1000580
- 21. Zhang EE, Liu AC, Hirota T, Miraglia LJ, Welch G, Pongsawakul PY, Liu X, Atwood A, Huss JW, Janes J, Su AI, Hogenesch JB, Kay SA (2009) A genome-wide RNAi screen for modifiers of the circadian clock in human cells. *Cell* **139**: 199–210
- 22. ZieliÅĎski TP, Duda K (2011) Frequency and damping estimation methods An overview. *Metrol Meas Syst* **18**: 505–528

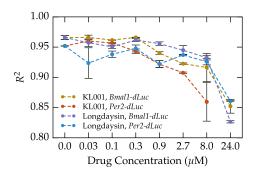


Figure S1: Figure Title. (A) Part A. (B) Part B.

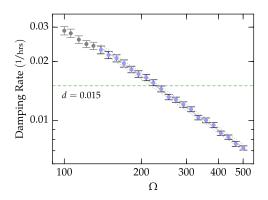


Figure S2: Figure Title. (A) Part A. (B) Part B.

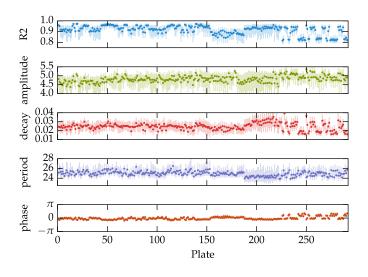


Figure S3: figure title. (a) part a. (b) part b.

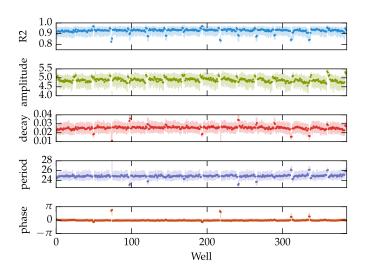


Figure S4: figure title. (a) part a. (b) part b.

Dep. Variable: Da		mping Rat	te R-s	R-squared:		0.169
Model:		OLS	Ad	Adj. R-squared:		0.169
Method:		ast Square	es F-s	F-statistic:		4782.
		, 11 Feb 20	015 Pr o	5 Prob (F-statistic)		0.00
Time:		16:26:22 L		Log-Likelihood:		-1.7248e + 05
No. Observations:		94053 AI		C:		3.450e + 05
Df Residuals:		94048	048 BI			3.450e + 05
	coef	std err	t	P> t	[95.0%	Conf. Int.]
const	-0.0370	0.014	-2.572	0.010	-0.0	65, -0.009
amplitude	0.2375	0.003	86.282	0.000	0.2	32, 0.243
period	-0.1521	0.003	56.798	0.000	-0.1	57, -0.147
phase	-0.2354	0.003	85.598	0.000	-0.2	41, -0.230
type	0.3197	0.015	20.664	0.000	0.2	89, 0.350
Omnibus:		9769.391	Durbin-Watson:		n:	1.876
Prob(O	0.000	Jarque-Bera (JB):		B): 18	3459.719	
Skew:	0.697	Prob(JB):			0.00	
Kurtosis:		4.664	Cond. No.			8.34

Table S1: OLS Regression Results